

The Coldness of Cold Dark Matter with the IGM

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OUTLINE

Introduction: small-scale crisis of cold dark matter

Warm Dark Matter implications for the Large Scale Structure

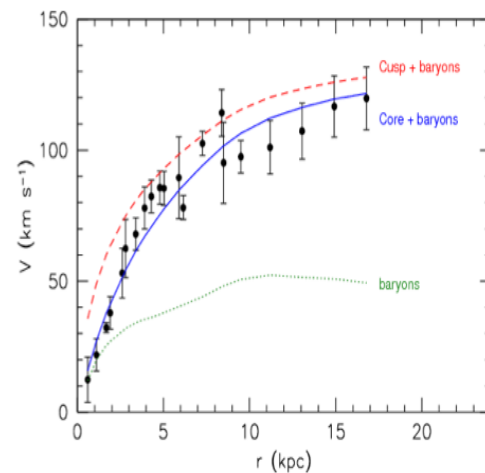
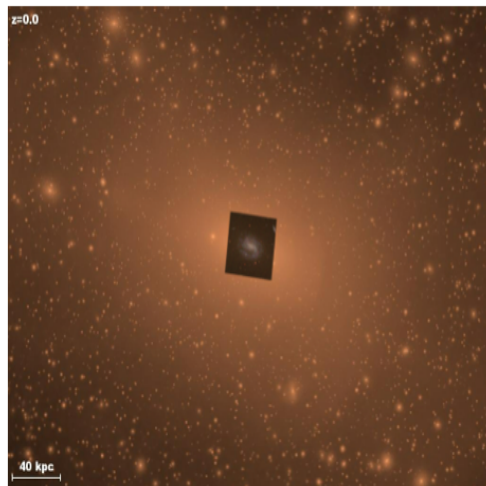
Constraints from the Lyman- α forest

THE SMALL-SCALE CRISIS OF Λ CDM

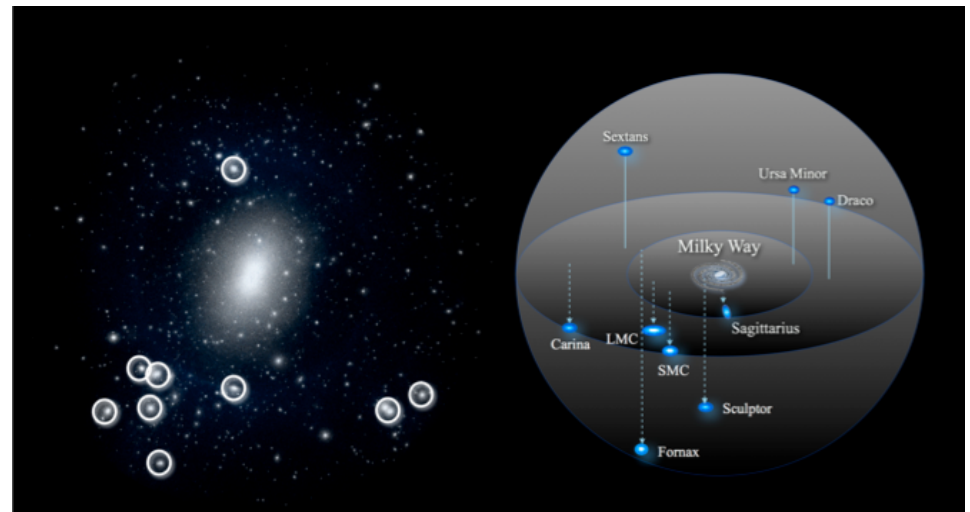
-Bode, Ostriker & Turok 01: number of satellites
 profiles
 clustering properties of dwarf galaxies

-Many more recent works on Λ CDM small-scale crisis

cuspid/core

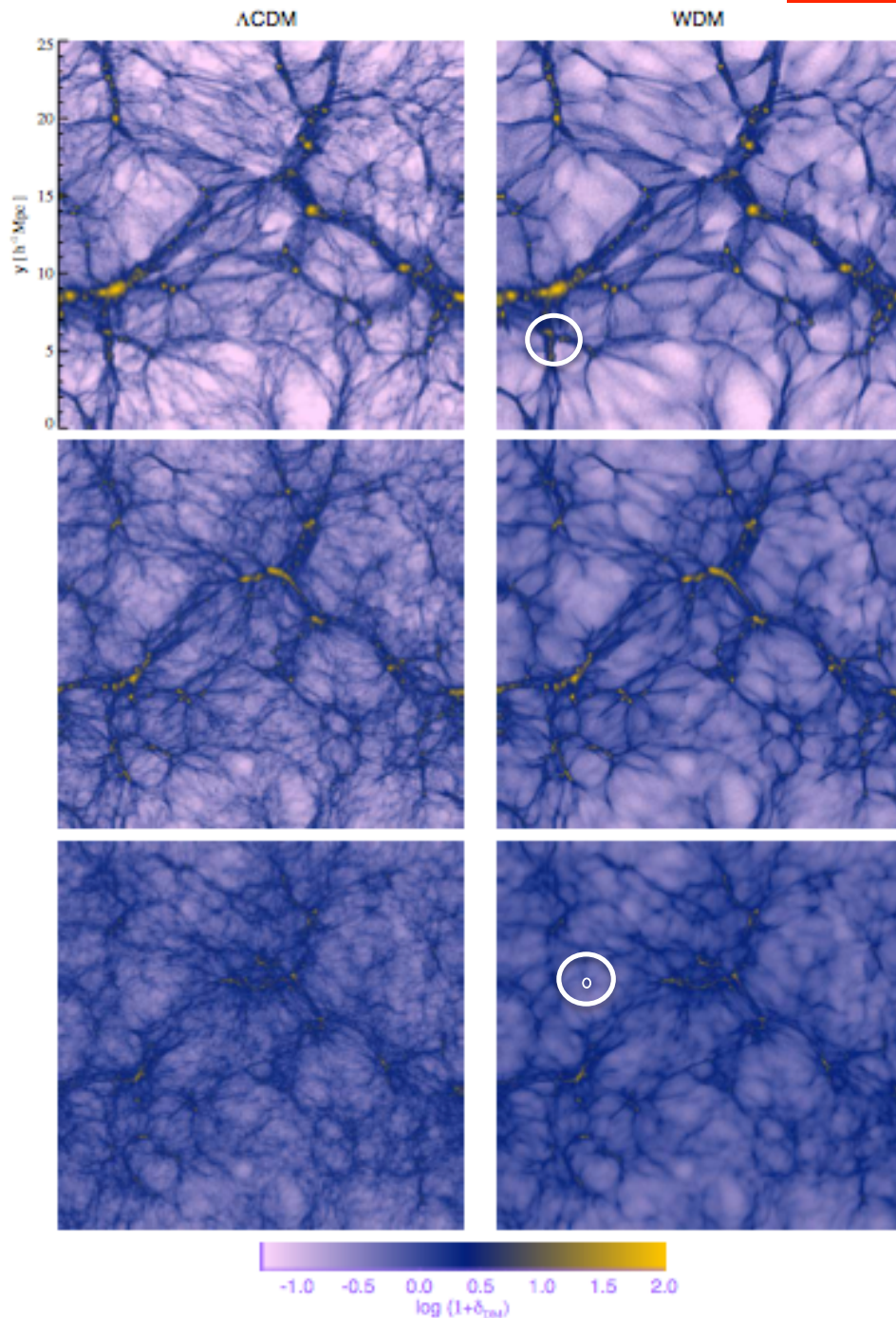


“too big to fail” problem (missing satellite)



See recent Weinberg et al. [arXiv:1306.0913](https://arxiv.org/abs/1306.0913)

THE COSMIC WEB



$$z=0 \quad \frac{T_x}{T_\nu} = \left(\frac{10.75}{g_*(T_D)} \right)^{1/3} < 1$$

$$k_{\text{FS}} = \frac{2\pi}{\lambda_{\text{FS}}} \sim 5 \text{ Mpc}^{-1} \left(\frac{m_x}{1 \text{ keV}} \right) \left(\frac{T_\nu}{T_x} \right)$$

$$\omega_x = \Omega_x h^2 = \beta \left(\frac{m_x}{94 \text{ eV}} \right)$$

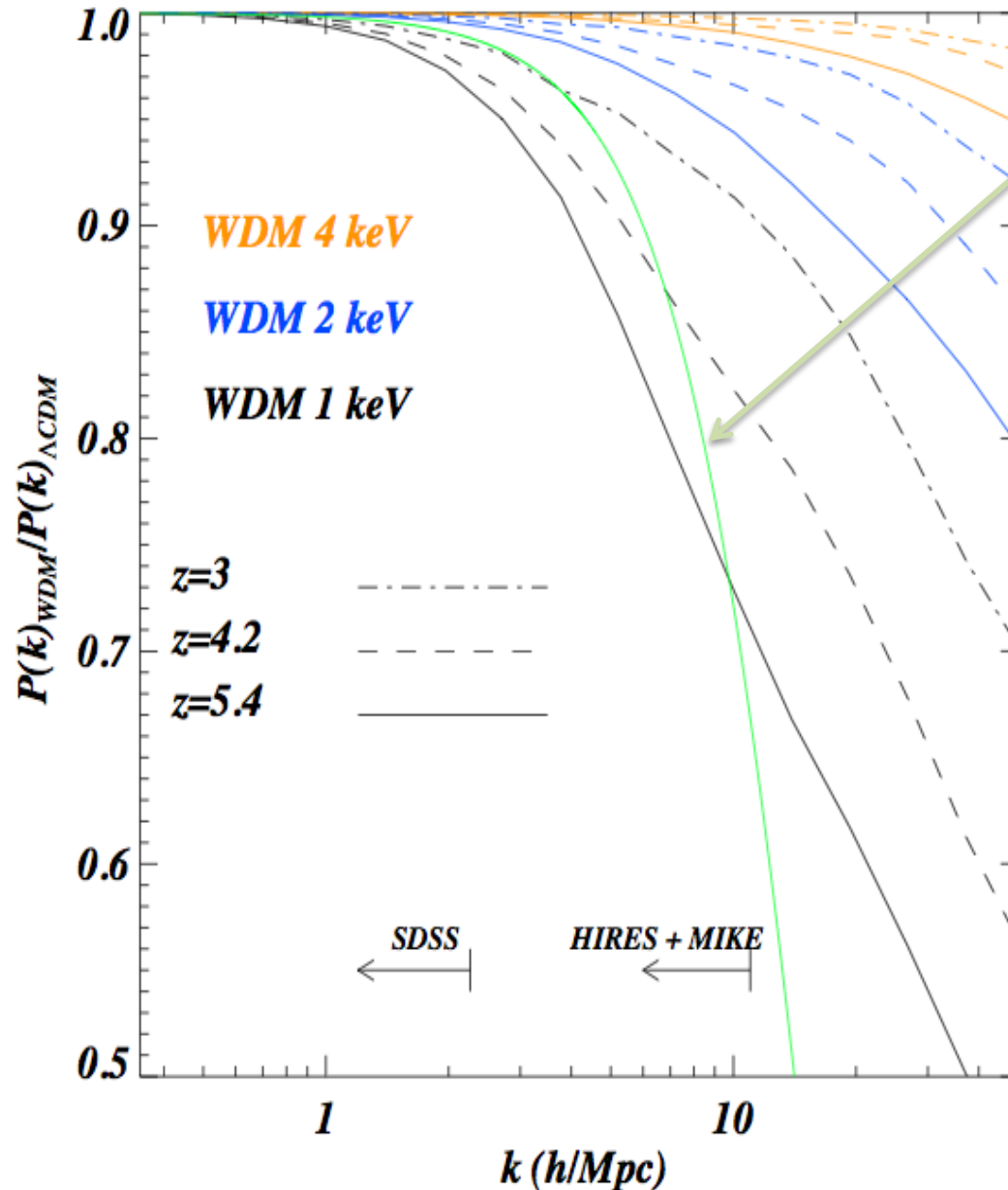
$$\beta = (T_x/T_\nu)^3$$

$$z=2$$

$$k_{\text{FS}} \sim 15.6 \frac{h}{\text{Mpc}} \left(\frac{m_{\text{WDM}}}{1 \text{ keV}} \right)^{4/3} \left(\frac{0.12}{\Omega_{\text{DM}} h^2} \right)^{1/3}$$

$$z=5$$

THE WARM DARK MATTER CUTOFF IN THE MATTER DISTRIBUTION



Linear cutoff for WDM 2 keV

Linear cutoff is redshift independent

Fit to the non-linear cut-off

$$T_{\text{nl}}^2(k) \equiv P_{\text{WDM}}(k)/P_{\Lambda\text{CDM}}(k) = (1 + (\alpha k)^{\nu l})^{-s/\nu},$$

$$\alpha(m_{\text{WDM}}, z) = 0.0476 \left(\frac{1\text{keV}}{m_{\text{WDM}}} \right)^{1.85} \left(\frac{1+z}{2} \right)^{1.3},$$

$\nu = 3, l = 0.6$ and $s = 0.4$.

Viel, Markovic, Baldi & Weller 2013

IMPLICATIONS FOR STRUCTURE FORMATION

- Strong and weak lensing	Markovic et al. 13/Faadely & Keeton 12
- Galaxy formation	Menci et al 13, Kang et al. 13
- Reionization/First Stars	Gao & Theuns 07
- Dark Matter Haloes (mass functions)	Pacucci et al. 13
- Luminous matter properties	Polisensky & Ricotti 11, Lovell et al. 09
- Gamma-Ray Bursts	De Souza et al. 13
- HI in the local Universe	Zavala et al. 09
- Phase space density constraints	Shi et al. 13
- Radiative decays in the high-z universe	Boyarsky et al. 13

QUESTION

Is the Lyman- α forest compatible with a cutoff in the matter power spectrum?



WHY LYMAN- α ???

1) ONE DIMENSIONAL

$$\langle \tilde{F}_k^2 \rangle = \frac{1}{(2\pi)^2} \int dk_x \int dk_y P(k_x, k_y, k) = \frac{1}{2\pi} \int_k^\infty P(y) y dy$$

e.g. Kaiser & Peacock 91

2) HIGH REDSHIFT

Where linear WDM cut-off is more prominent

HISTORY OF WDM LYMAN- α BOUNDS

Narayanan et al. 00 : $m > 0.75 \text{ keV}$

Nbody sims + 8 Keck spectra
Marginalization over nuisance not done

Viel et al. 05 : $m > 0.55 \text{ keV} (2\sigma)$

Hydro sims + 30 UVES/VLT spectra
Effective bias method of Croft et al. 02

Seljak et al. 06 : $m > 2.5 \text{ keV} (2\sigma)$

Hydro Particle Mesh method + SDSS
grid of simulation for likelihood

Viel et al. 06 : $m > 2 \text{ keV} (2\sigma)$

Fully hydro+SDSS
Not full grid of sims. but Taylor expans.

Viel et al. 08 : $m > 4.5 \text{ keV} (2\sigma)$

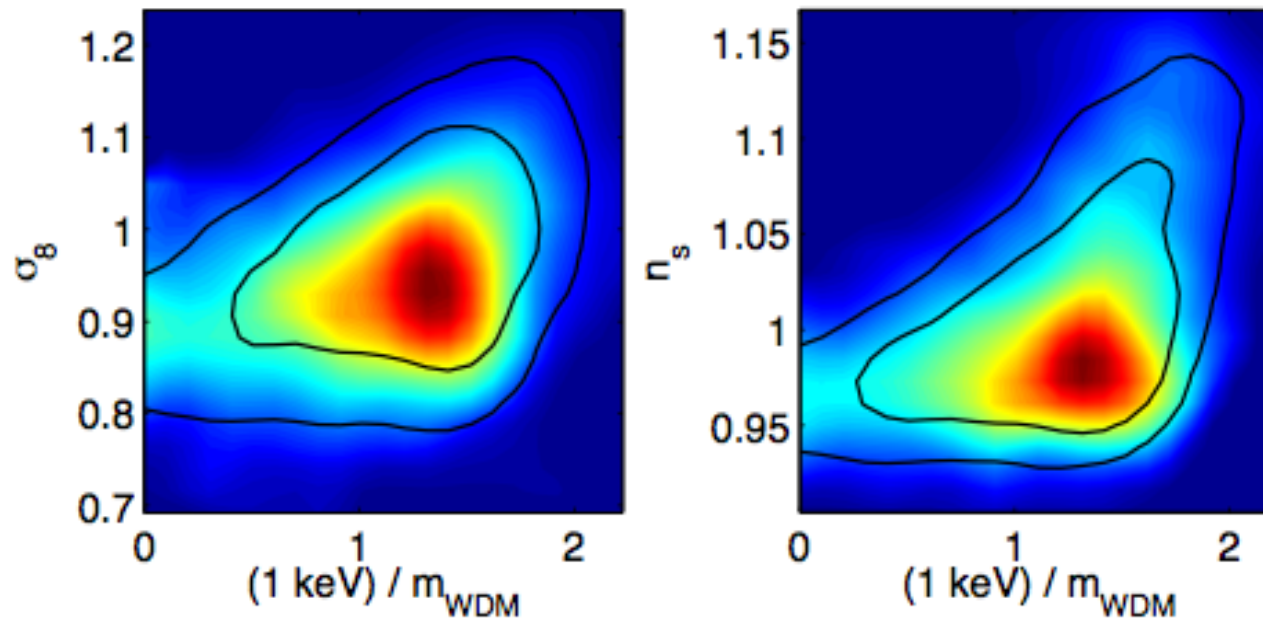
SDSS+HIRES (55 QSOs spectra)
Full hydro sims (Taylor expansion of the flux)

Boyarsky et al. 09 : $m > 2.2 \text{ keV} (2\sigma)$

SDSS (frequentist+bayesian analysis)
emphasis on mixed ColdWarmDM models

CONSTRAINTS FROM UVES/VLT SPECTRA

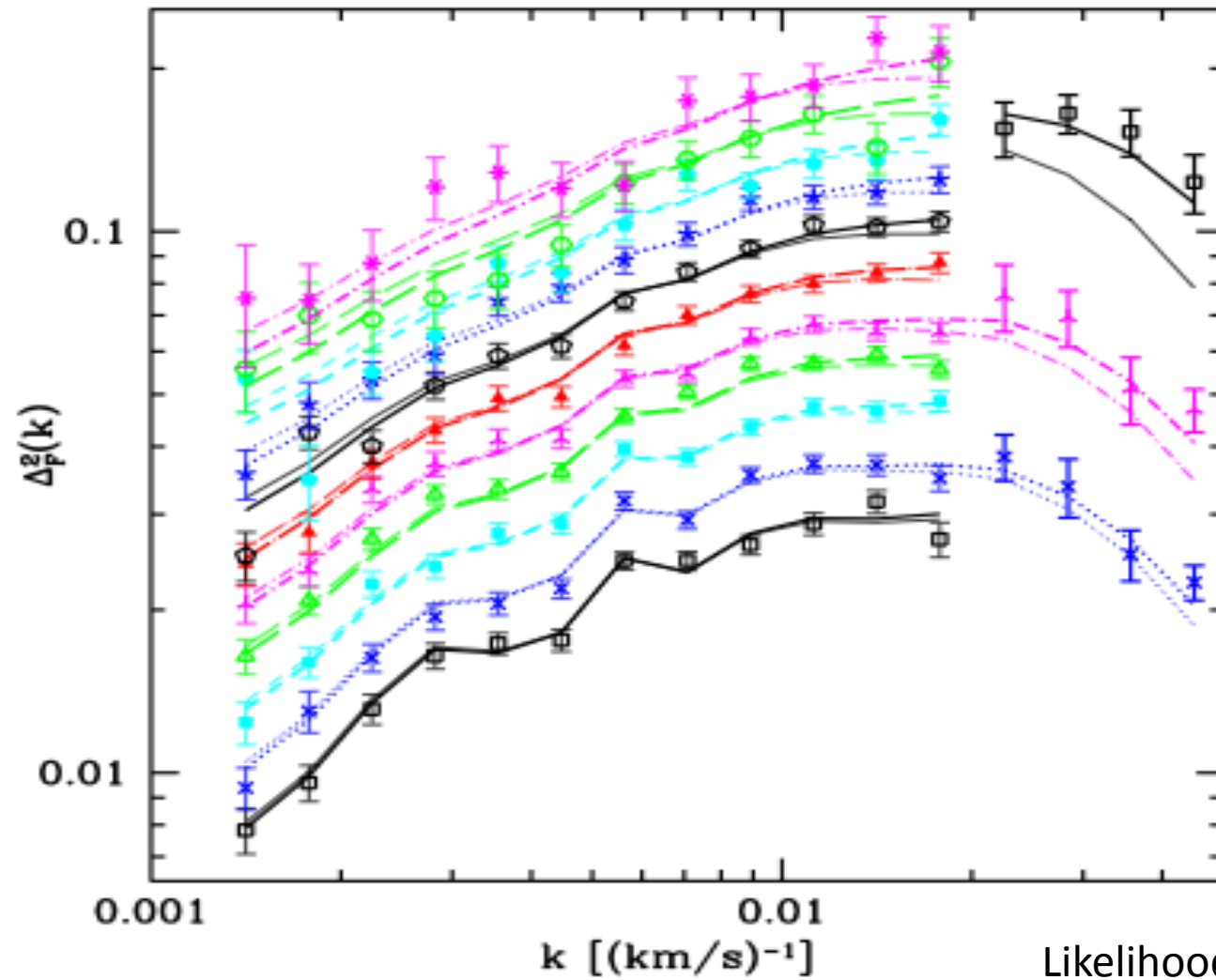
3D flux power spectrum $P_F(k) = b_{\text{eff}}(k,z)^2 P(k)$



Degeneracies are present, $z=2.12$ and $z=2.7$
data analysed with the effective bias model
of Croft et al. 02

MV + 2005, PRD, 71, 063534

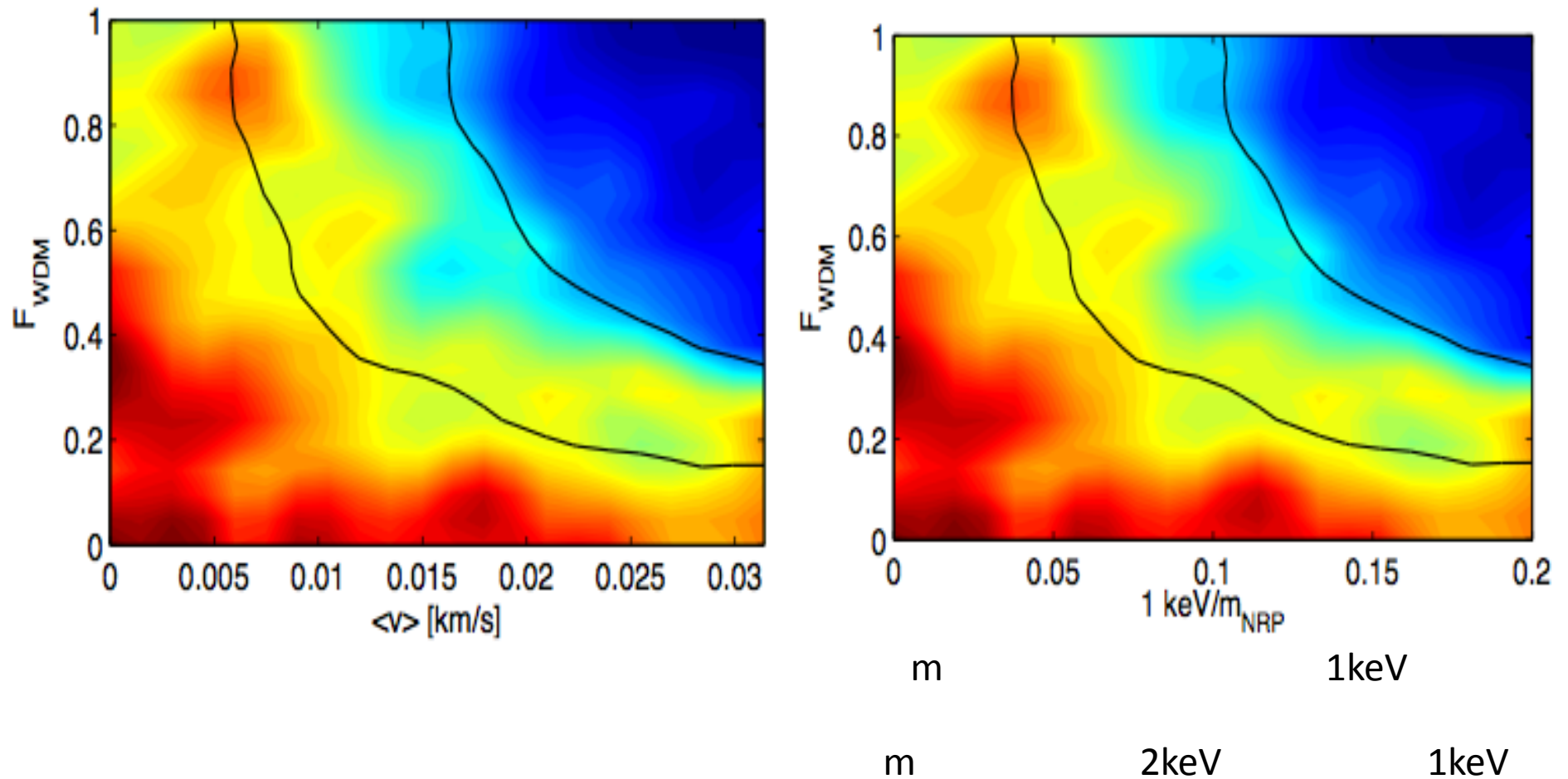
CONSTRAINTS FROM SDSS SPECTRA



Likelihood sampling with HPM sims.

Seljak et al. 2006

CONSTRAINTS FROM SDSS vs UVES SPECTRA



Boyarsky, Ruchayasky, Lesguorgues, Viel, 2009, JCAP, 05, 012

“Warm Dark Matter as a solution to the small scale crisis: new constraints from high redshift Lyman- α forest data”

MV, Becker, Bolton, Haehnelt 2013, arXiv:1306.2314

DATA: 25 high resolution QSO spectra at $4.48 < z_{\text{em}} < 6.42$
from MIKE and HIRES spectrographs
Becker, Bolton, Haenelt, Sargent (2011)

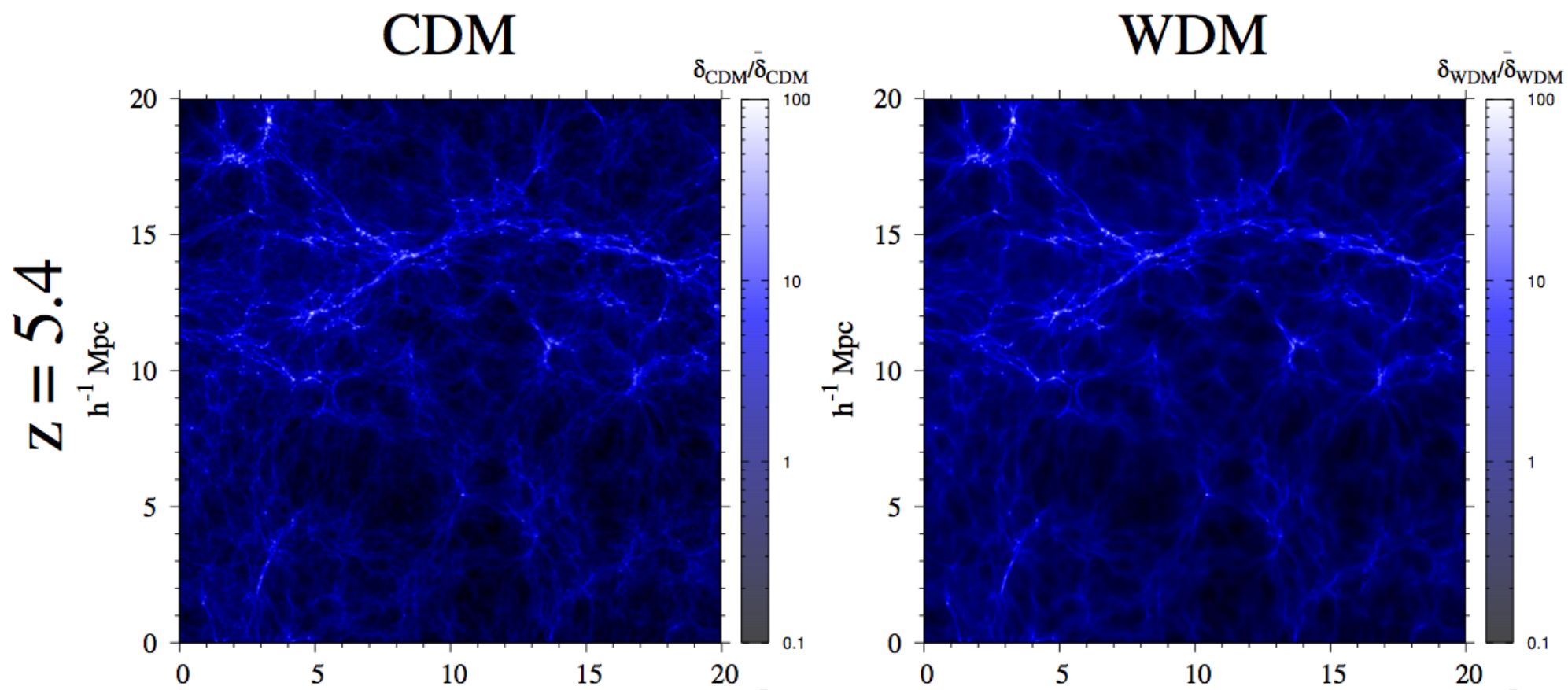
SIMULATIONS: Gadget-III
runs: 20 and 60 Mpc/h and $(512^3, 786^3, 896^3)$
Cosmology parameters: $\sigma_8, n_s, \Omega_m, H_0, m_{\text{WDM}}$
Astrophysical parameters: $z_{\text{reio}}, \text{UV fluctuations}, T_0, \gamma, \langle F \rangle$
Nuisance: resolution, S/N, metals

METHOD: Monte Carlo Markov Chains likelihood estimator
+ **very conservative assumptions** for the continuum
fitting and error bars on the data

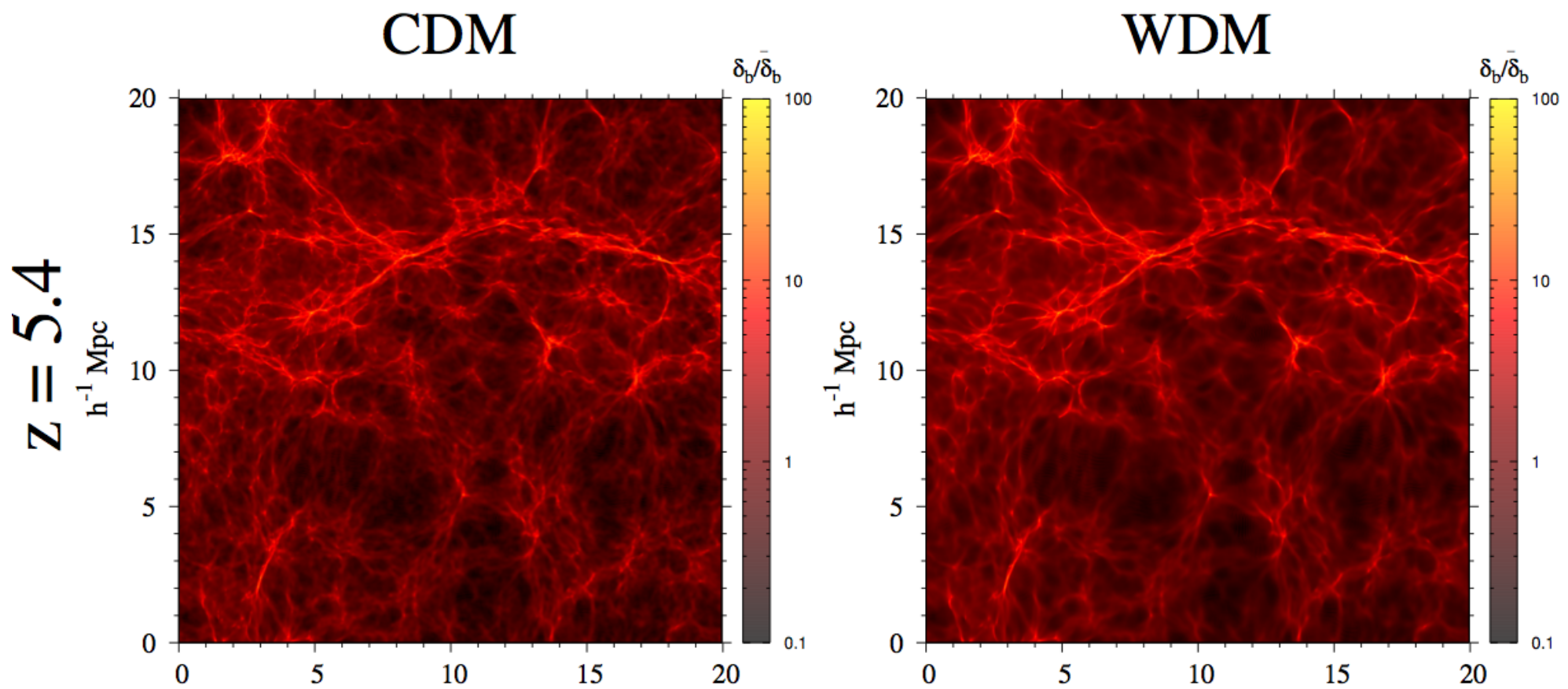
Parameter space: $m_{\text{WDM}}, T_0, \gamma, \langle F \rangle$ explored fully
Parameter space: $\sigma_8, n_s, \Omega_m, H_0, \text{UV}$ explored with second order
Taylor expansion of the flux power

$$P_F(k, z; \mathbf{p}) = P_F(k, z; \mathbf{p}^0) + \sum_i^N \left. \frac{\partial P_F(k, z; \mathbf{p}_i)}{\partial p_i} \right|_{\mathbf{p}=\mathbf{p}^0} (p_i - p_i^0) + \text{second order}$$

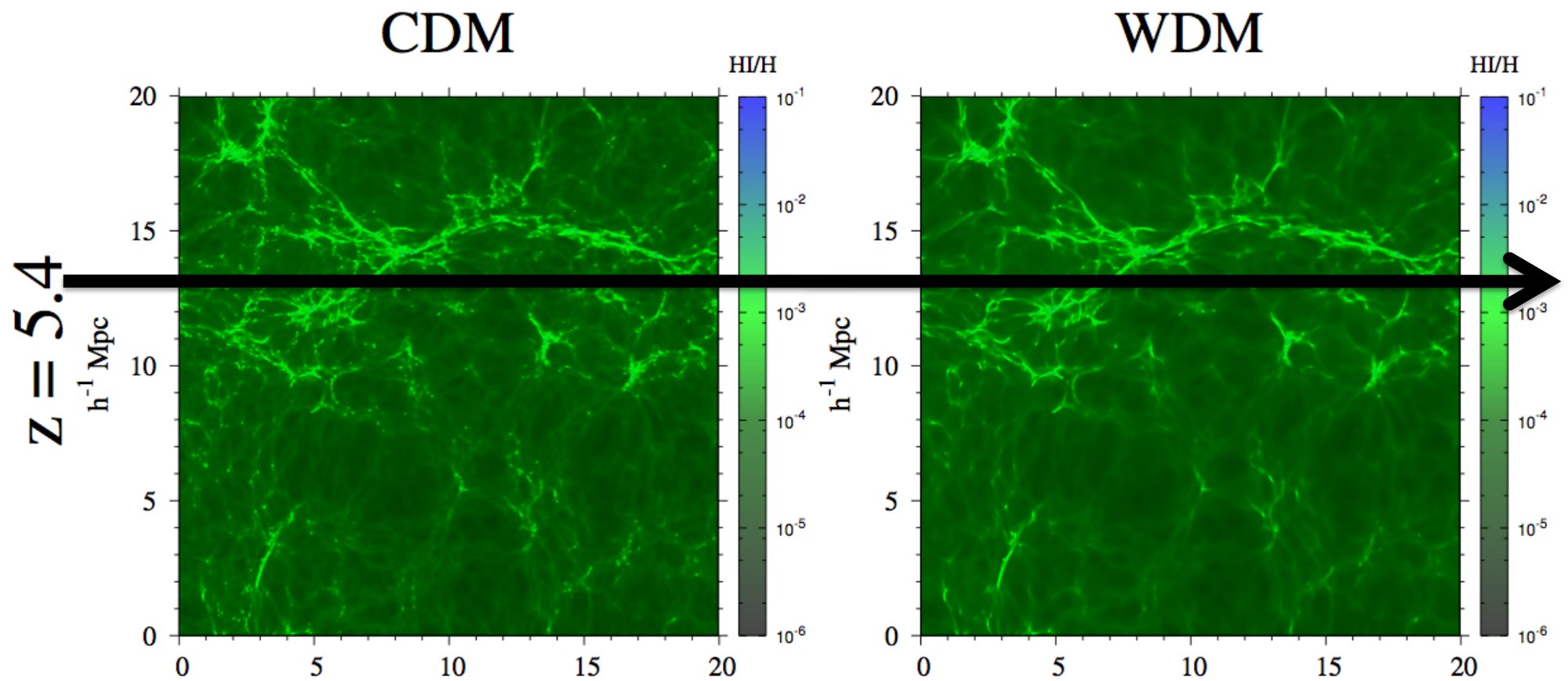
DARK MATTER DISTRIBUTION

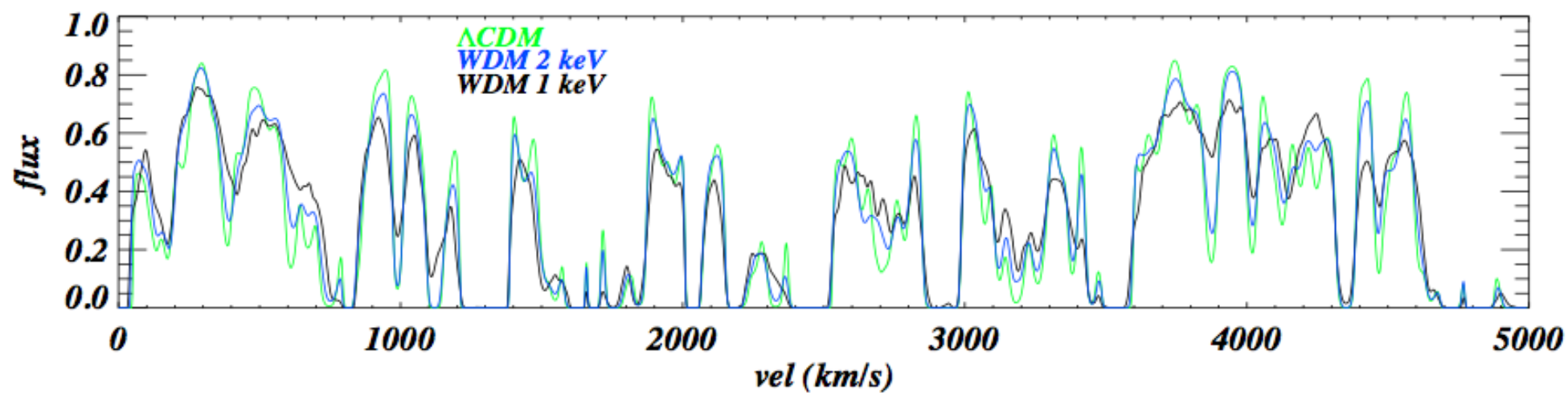


GAS DISTRIBUTION



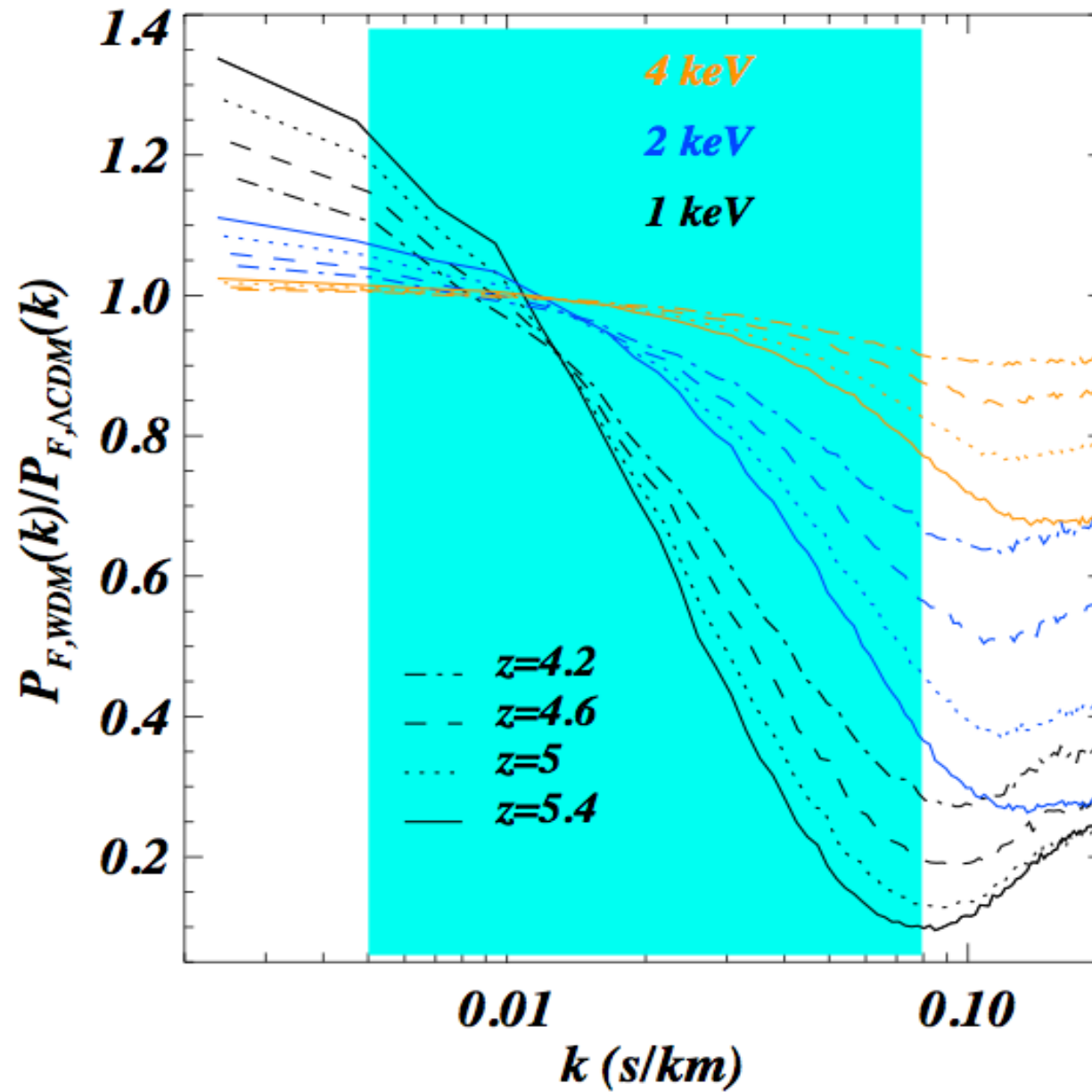
HI DISTRIBUTION





THE HIGH REDSHIFT WDM CUTOFF

$$\delta_F = F/\langle F \rangle - 1$$

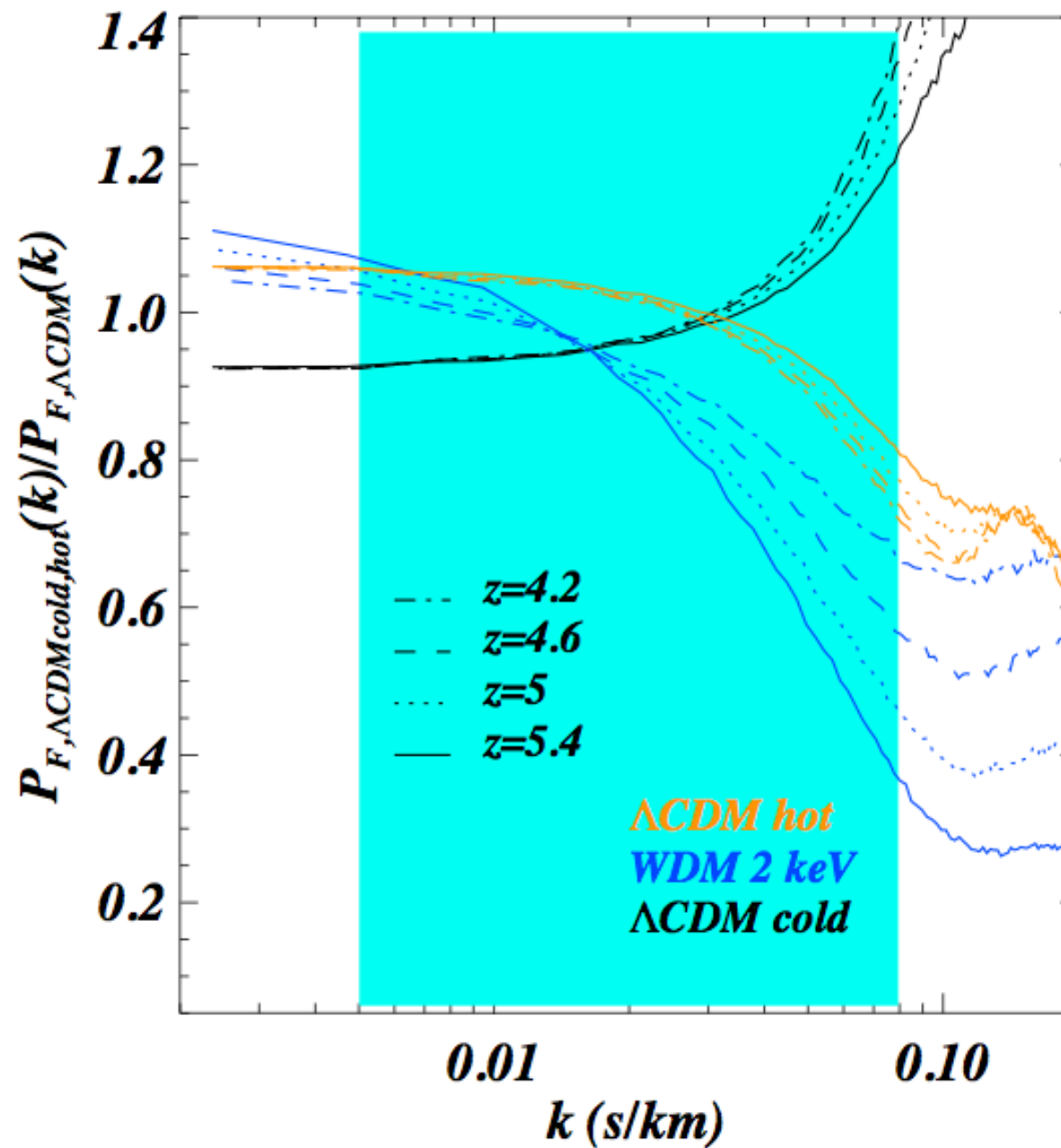


THE TEMPERATURE: T_0

$$T = T_0(1 + \delta)^{\gamma-1}$$

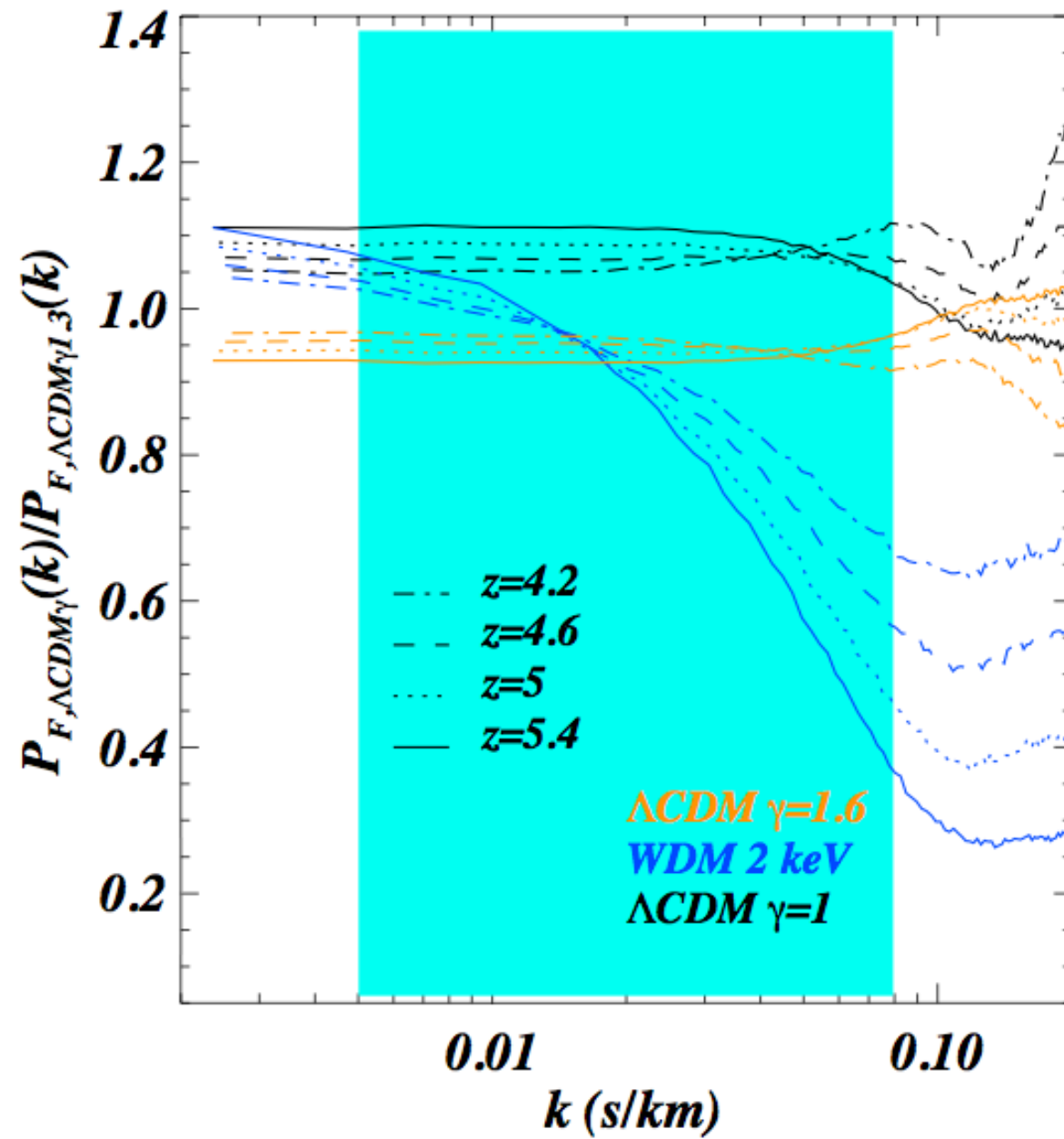
Hot + 3000 K
Cold – 3000 K

REF has 8300 K
at $z=4.6$

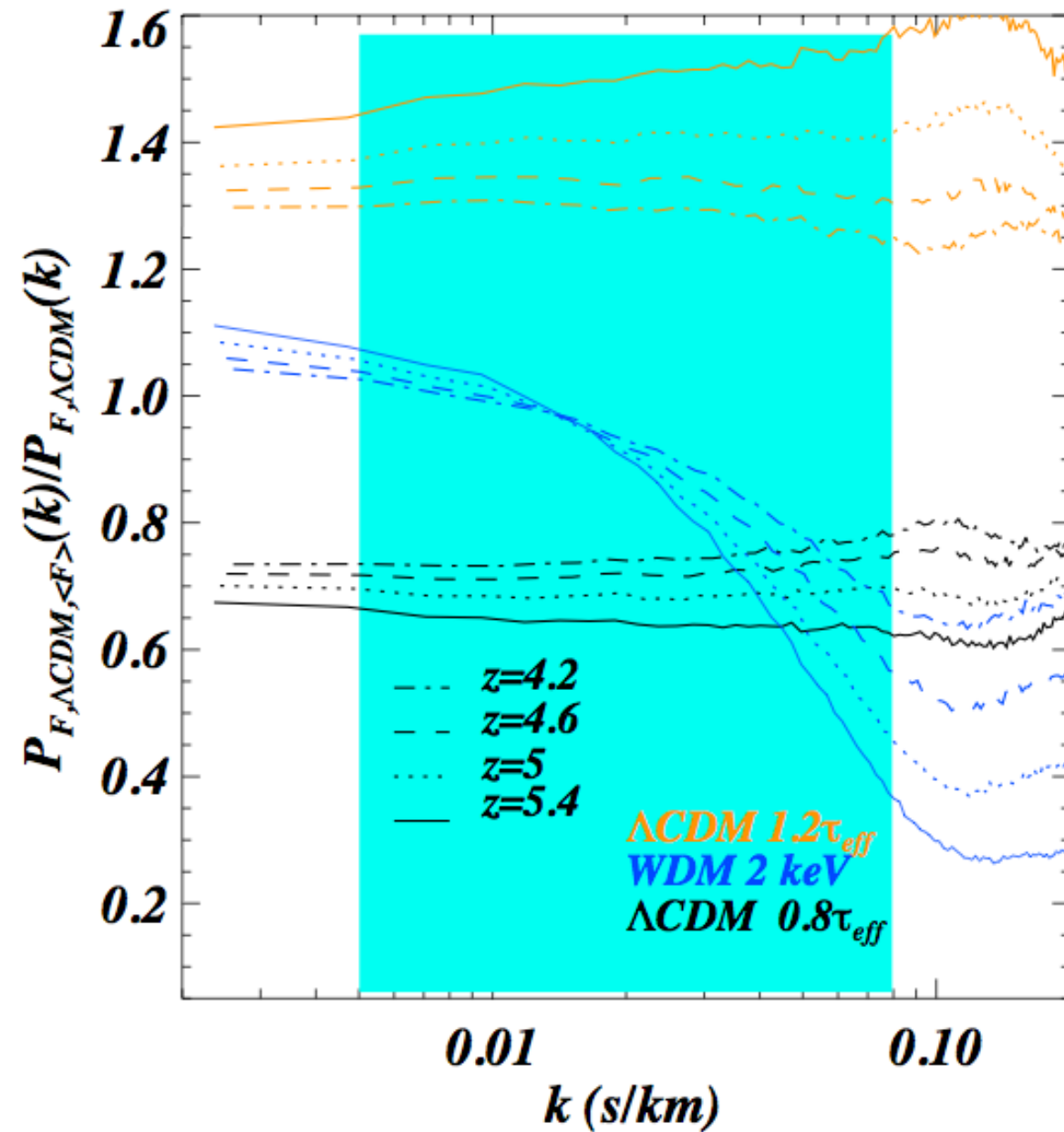


THE TEMPERATURE: γ

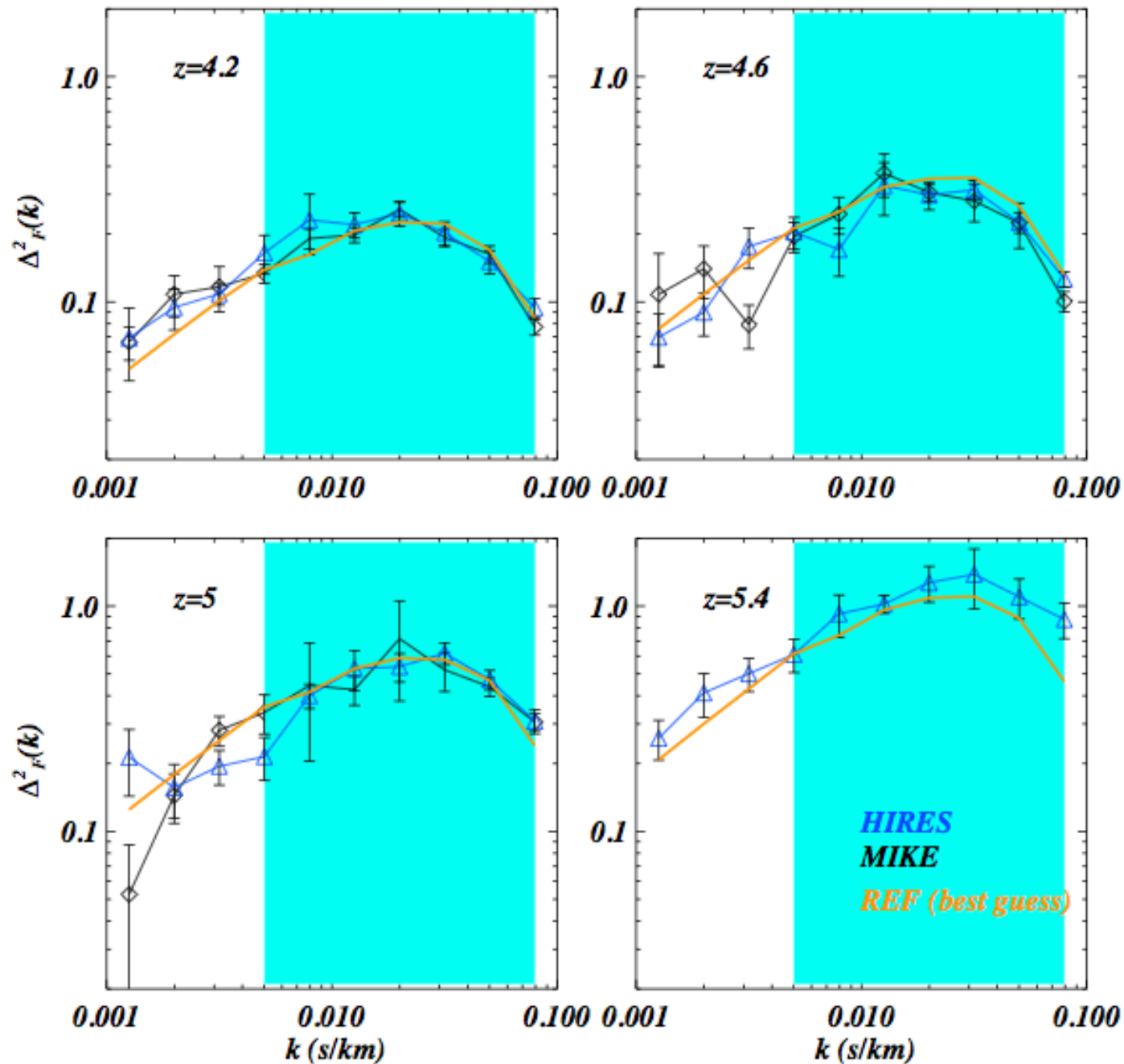
$$T=T_0(1+\delta)^{\gamma-1}$$



THE MEAN FLUX LEVEL

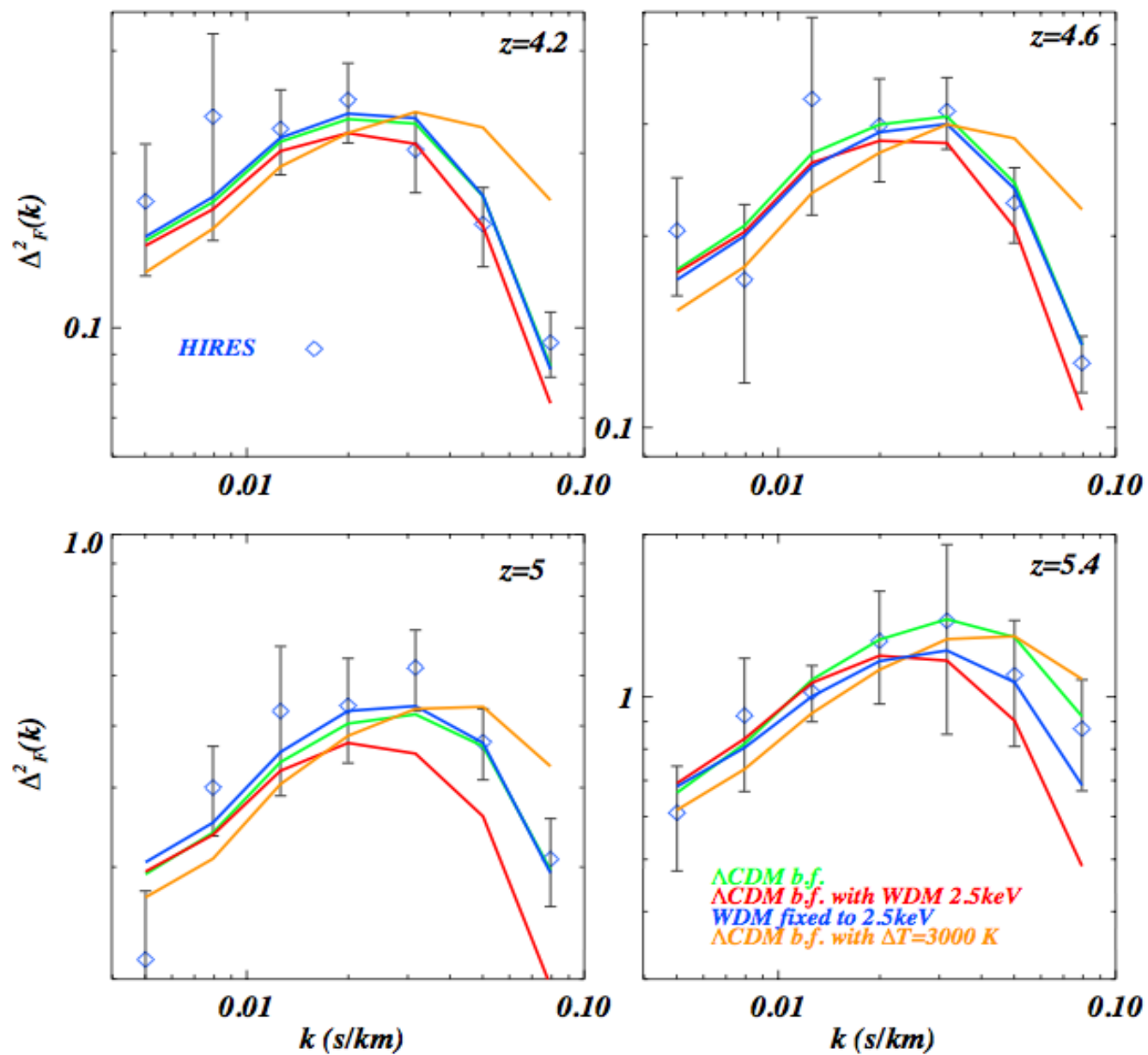


THE BEST GUESS MODEL

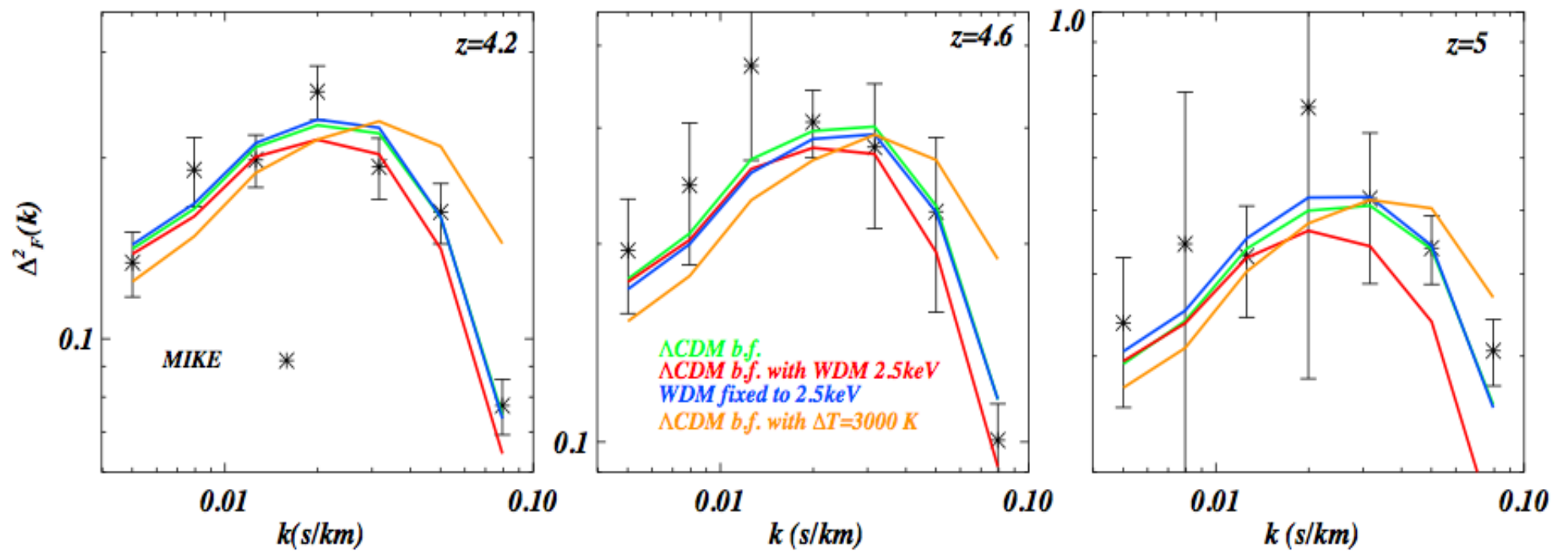


This is the starting point of the MCMC likelihood estimation cosmology close to Planck values

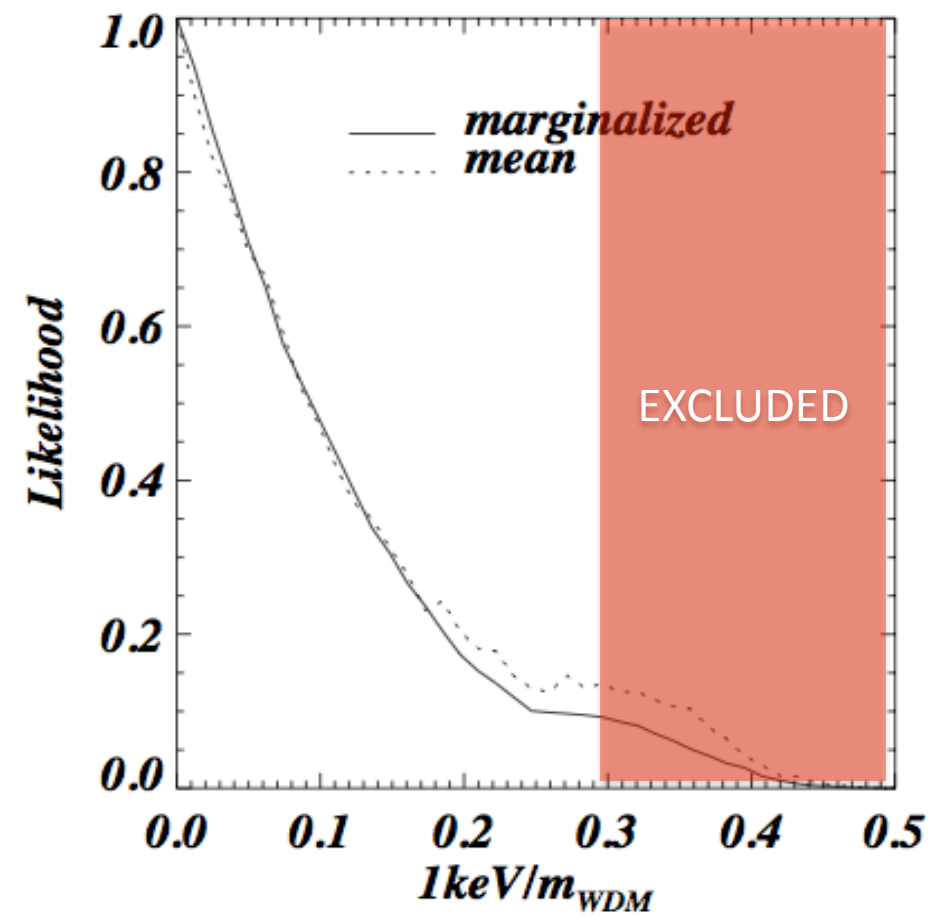
THE BEST FIT MODEL for HIRES



THE BEST FIT MODEL for MIKE



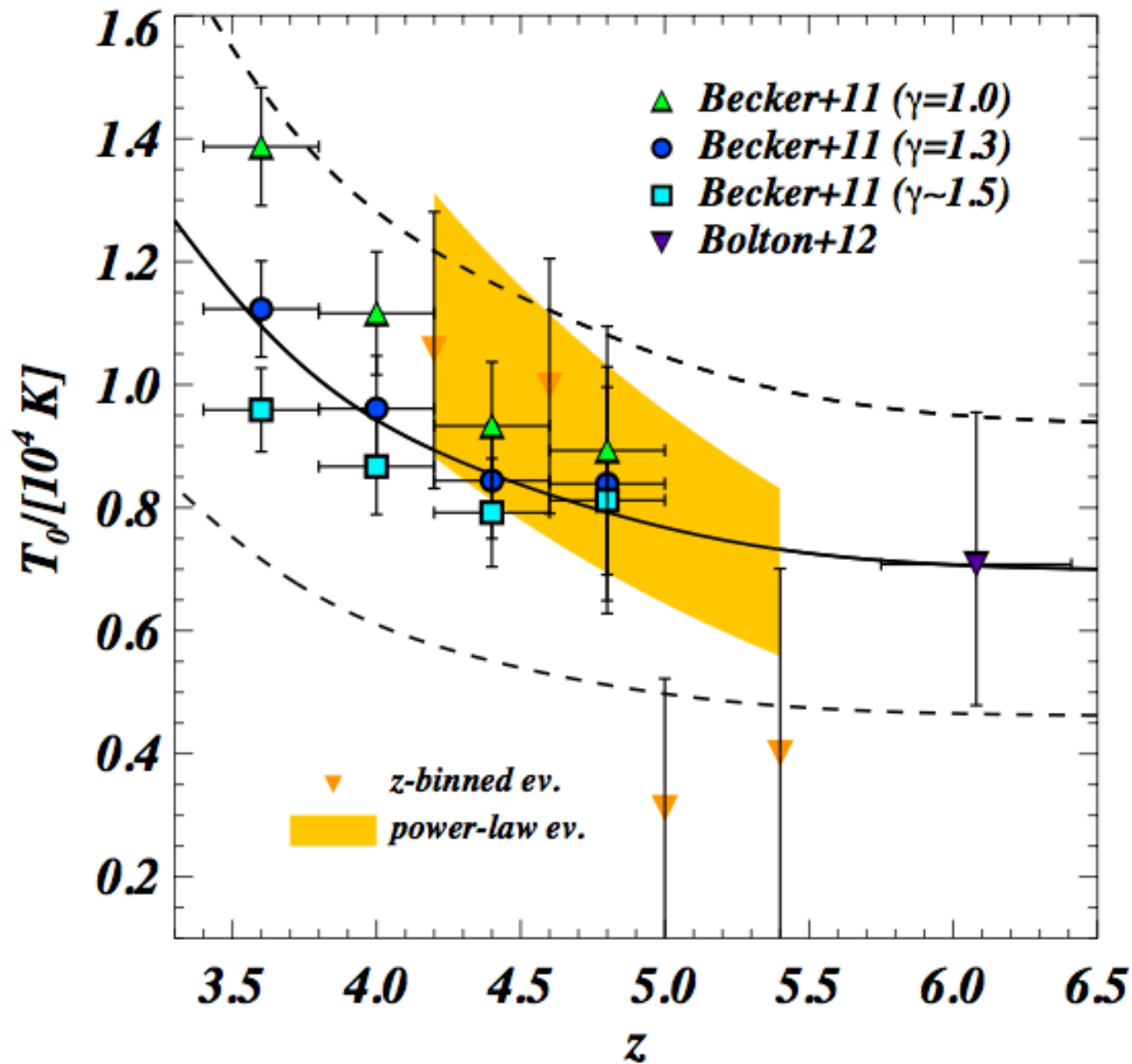
RESULTS FOR WDM MASS



$m > 3.3 \text{ keV} (2\sigma)$

RESULTS FOR TEMPERATURE

$$\gamma^A(z) = \gamma^A[(1+z)/5.5]^{\gamma_A^S} \quad T_0^A(z) = T_0^A[(1+z)/5.5]^{T_0^S}$$



SUMMARY OF RESULTS

$$\gamma^A(z) = \gamma^A[(1+z)/5.5)]\gamma_A^S \quad T_0^A(z) = T_0^A[(1+z)/5.5)]T_0^S$$

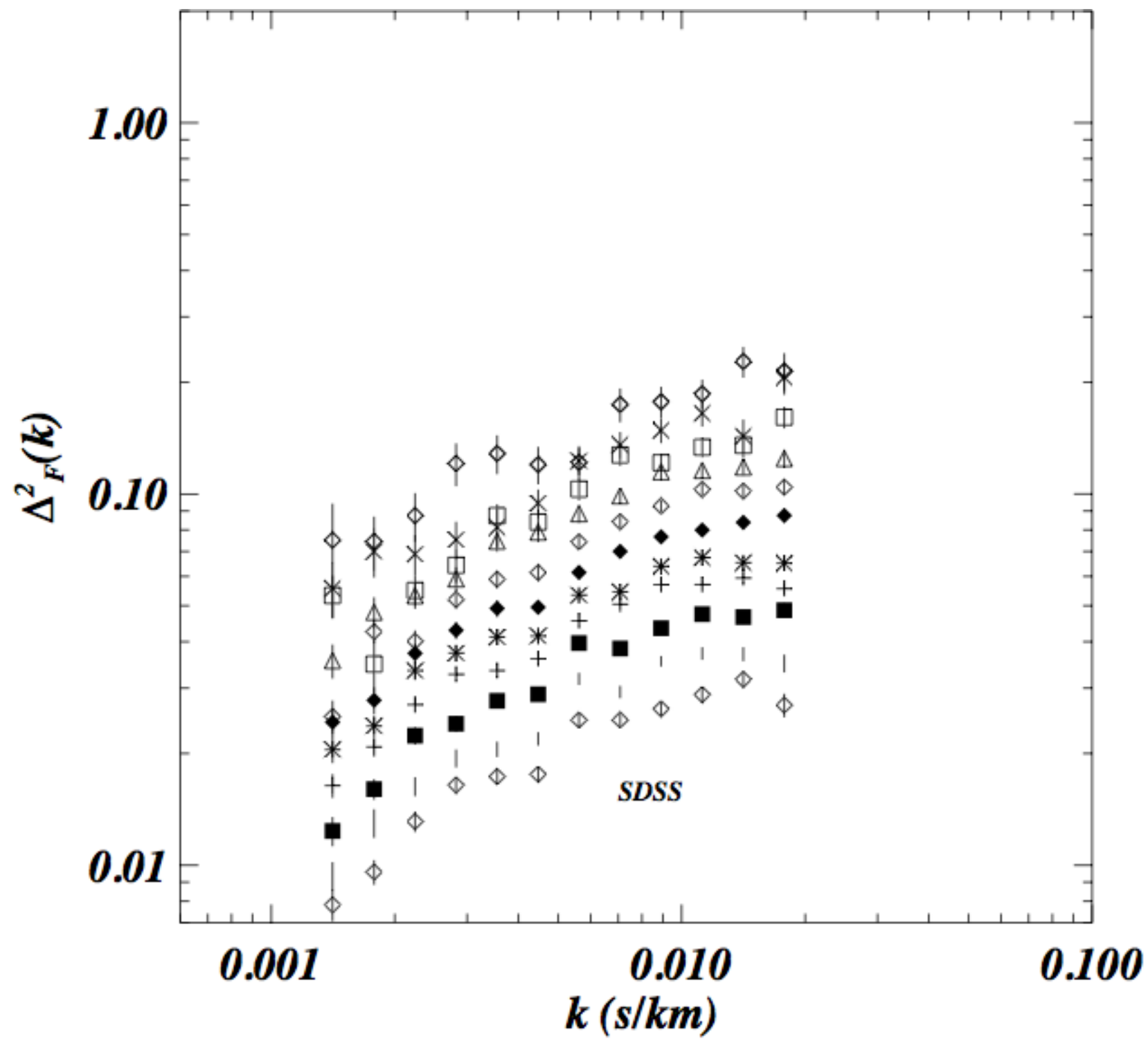
parameter	(1 σ)	(2 σ)	best fit
n_s	[0.942, 0.97]	[0.928, 0.984]	0.957
σ_8	[0.806, 0.856]	[0.781, 0.881]	0.822
Ω_m	[0.265, 0.331]	[0.234, 0.362]	0.298
$\tau_{\text{eff}}^A(z = 4.2)$	[1.04, 1.16]	[0.98, 1.22]	1.16
$\tau_{\text{eff}}^A(z = 4.6)$	[1.19, 1.33]	[1.12, 1.4]	1.32
$\tau_{\text{eff}}^A(z = 5)$	[1.76, 1.96]	[1.66, 2.05]	1.91
$\tau_{\text{eff}}^A(z = 5.4)$	[2.72, 3.06]	[2.55, 3.21]	3.09
$\gamma^A(z = 4.5)$	[1.38, 1.54]	[1.09, 1.65]	1.64
$\gamma^S(z = 4.5)$	[-0.76, 1.1]	[-2, 2.3]	-0.15
$T_0^A(z = 4.5)(10^3) \text{ K}$	[9.1, 10.4]	[7.8, 11.6]	9.2
$T_0^S(z = 4.5)(10^3) \text{ K}$	[-3, -2.05]	[-3, -1.1]	-2.5
f_{UV}	[0 - 1]	[0 - 1]	0.18
z_{reio}	[5 - 11]	[5 - 16.4]	11.2
1 keV/ m_{WDM}	[0 - 0.12]	[0 - 0.3]	0.03

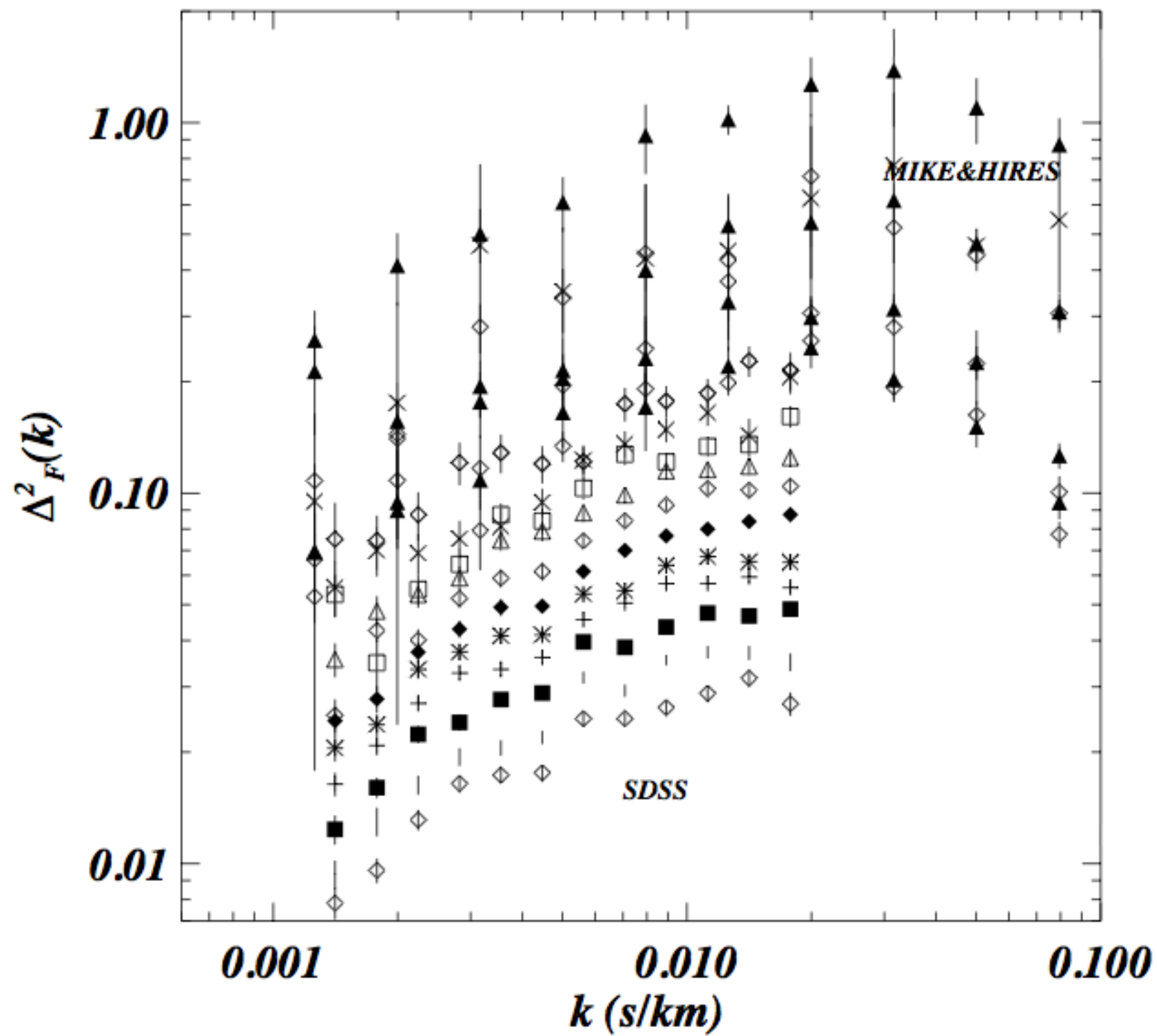
model	(1 σ)	(2 σ)	best fit	$\chi^2/\text{d.o.f.}$
REF.	> 8.3 keV	> 3.3 keV	33 keV	34/37
REF. w/o 30%	> 11.1 keV	> 4.5 keV	100 keV	48/37
REF. w/o covmat	> 7.7 keV	> 3.1 keV	14.3 keV	33.2/37
REF. + SDSS	> 7.2 keV	> 3.3 keV	42 keV	183.3/170

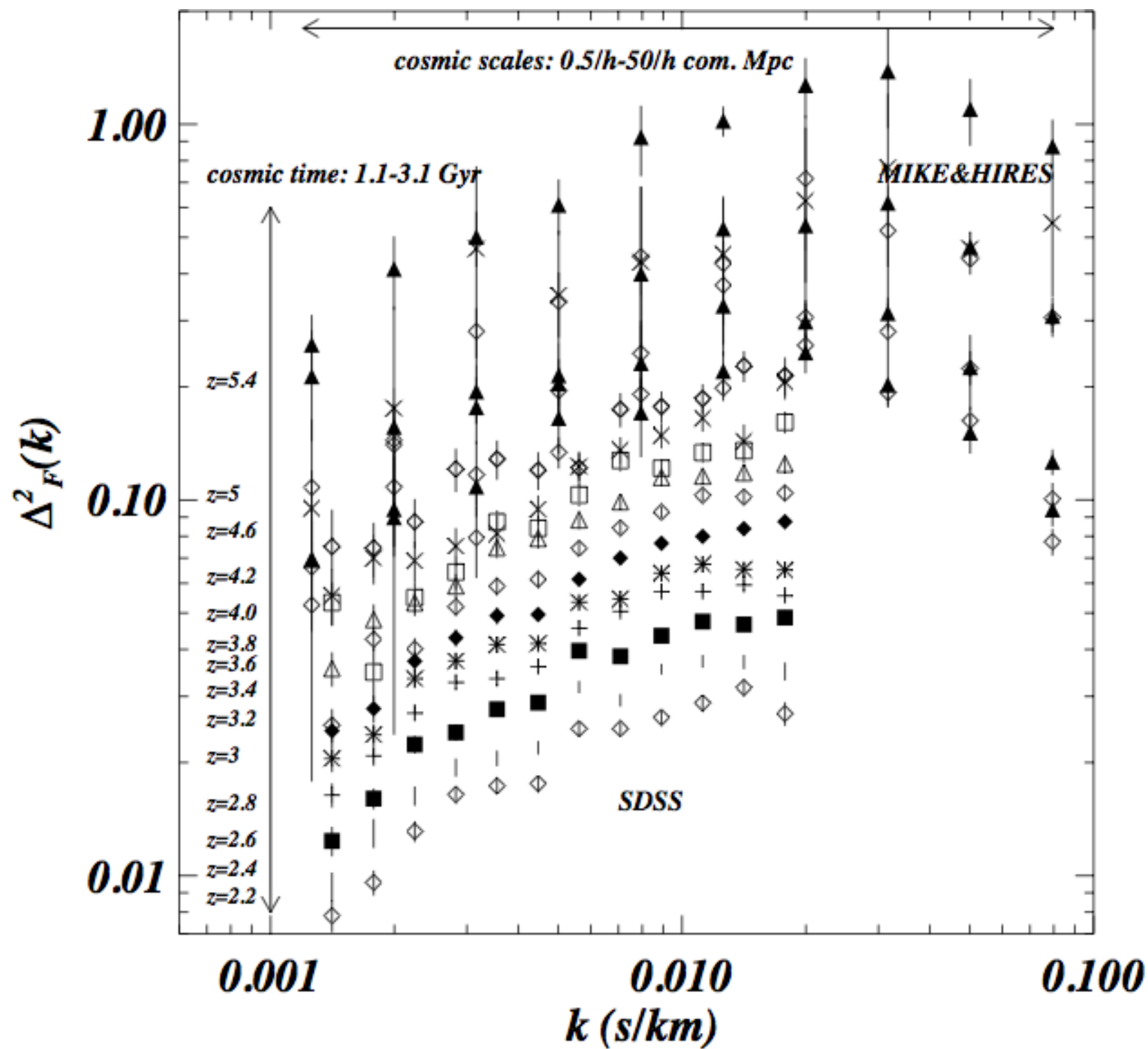
SDSS + MIKE + HIRES CONSTRAINTS

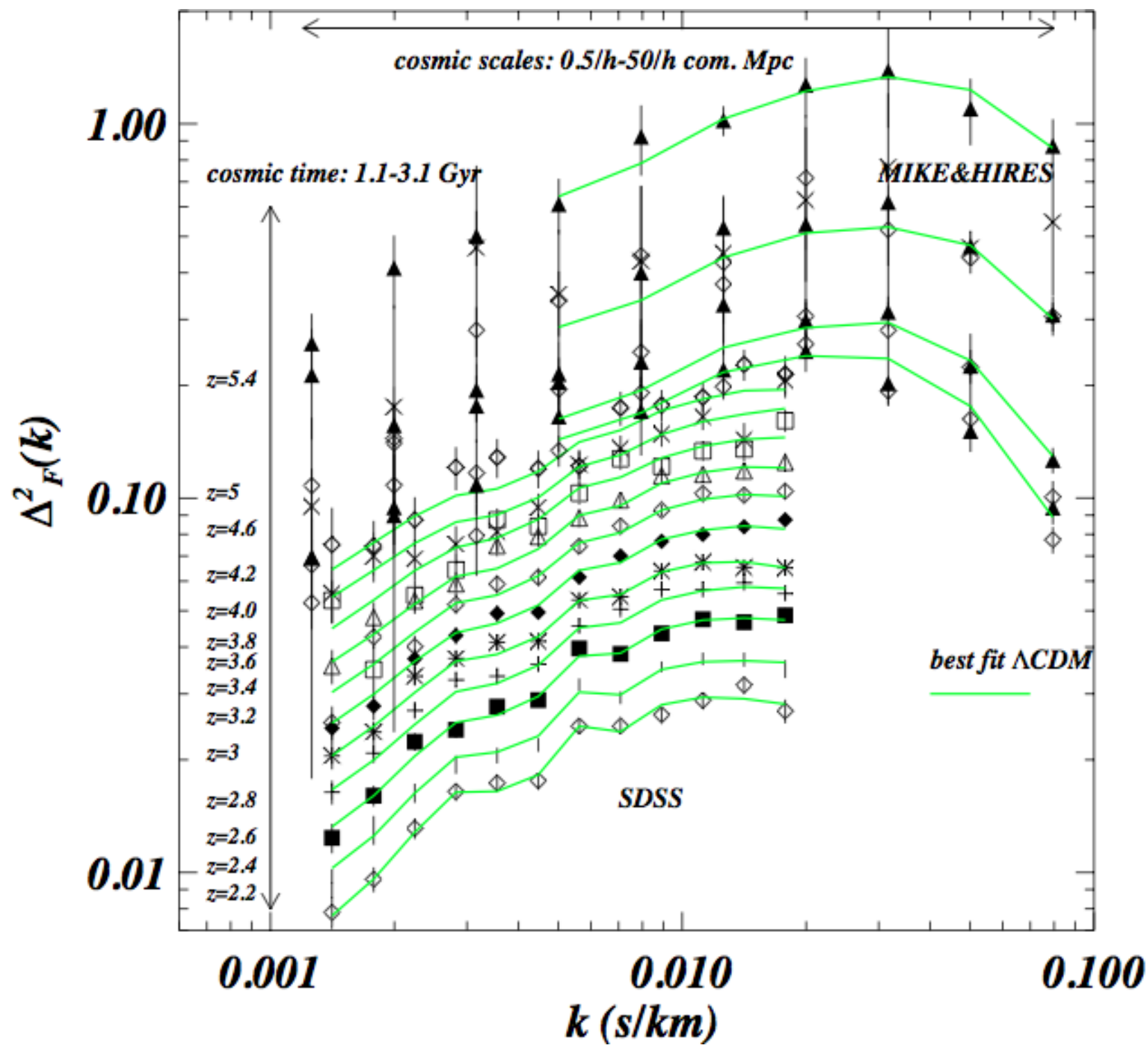
Joint likelihood analysis

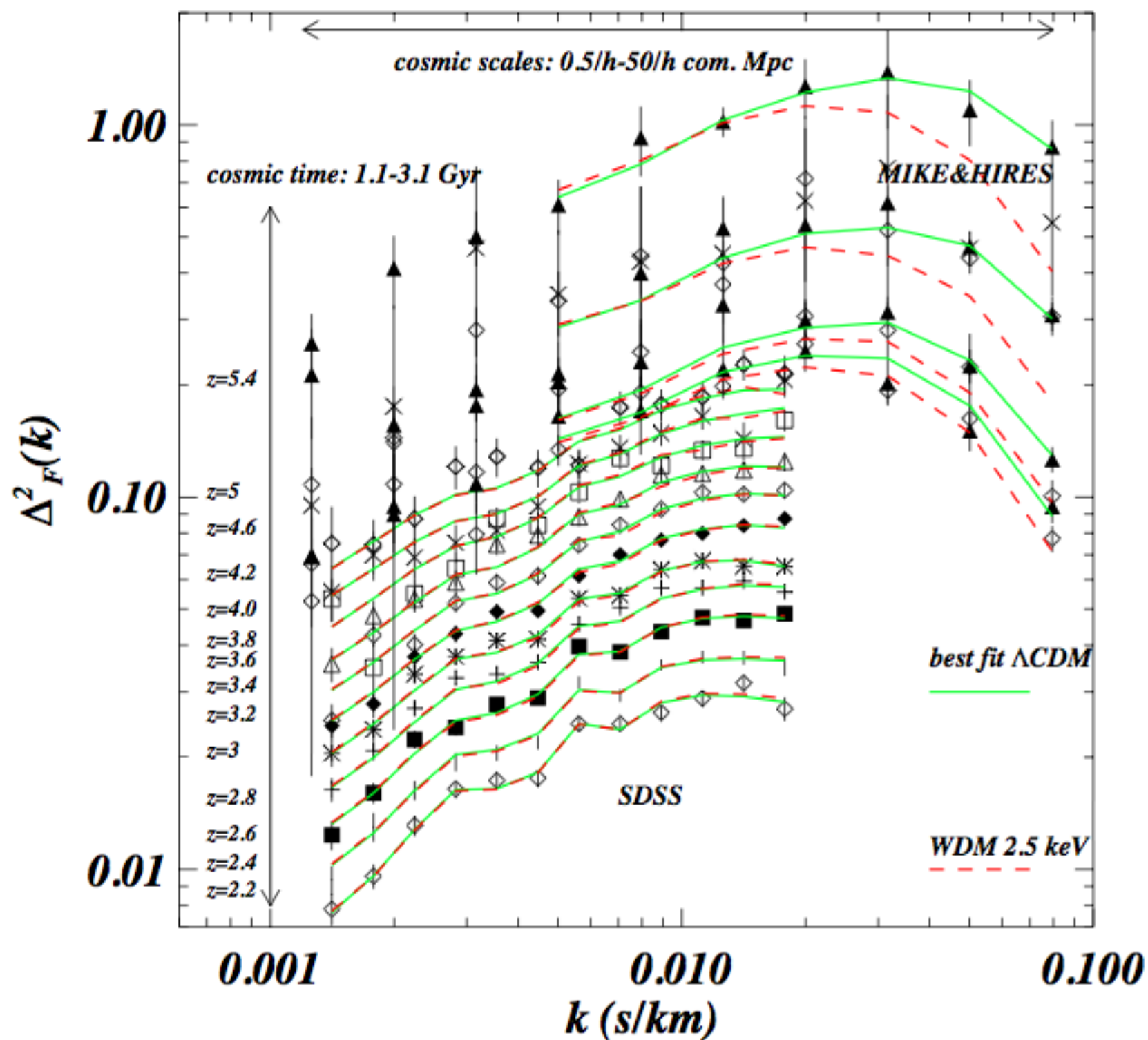
SDSS data from McDonald05,06 not BOSS



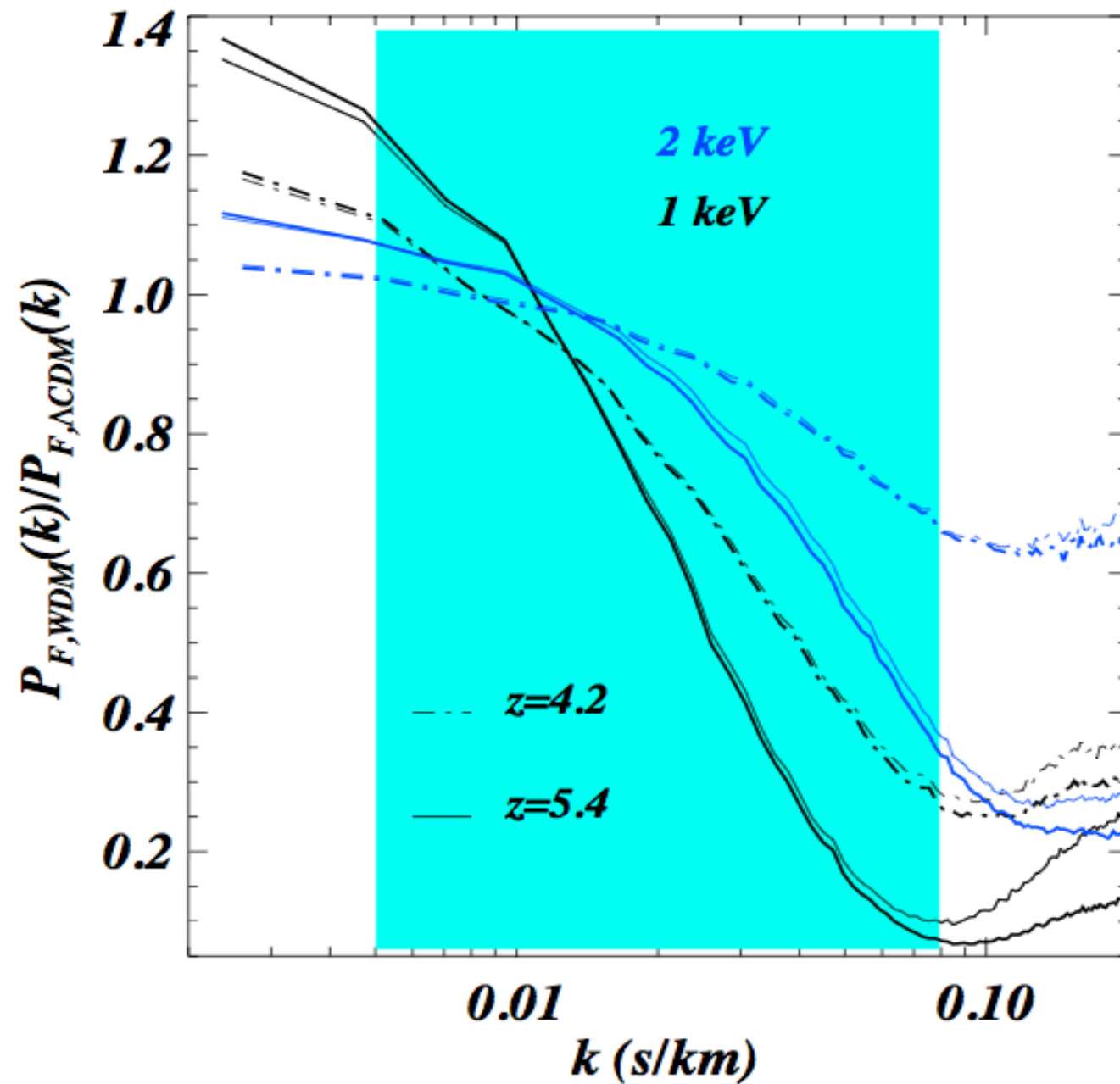








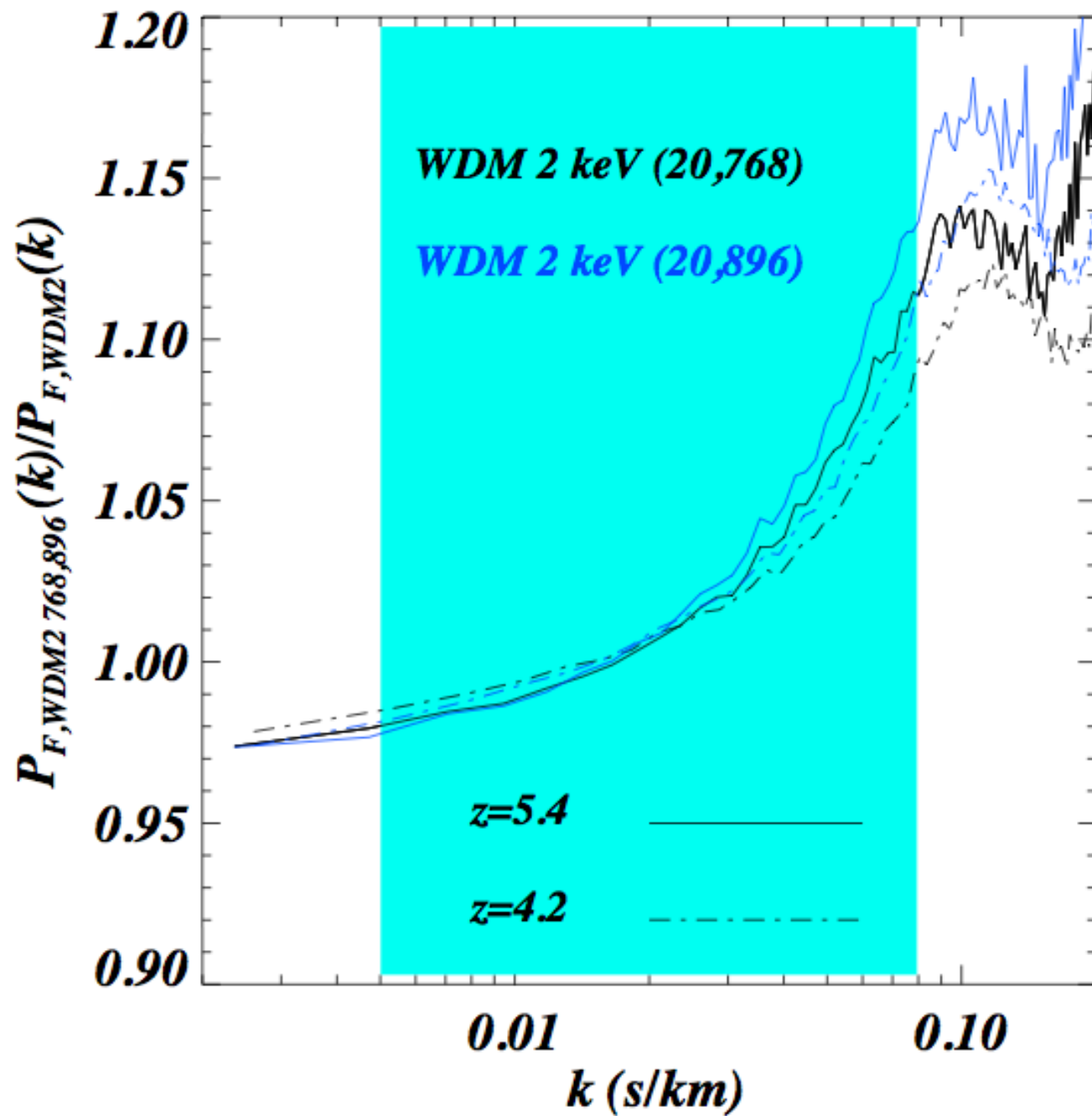
SYSTEMATICS: NUMERICAL CONVERGENCE – I



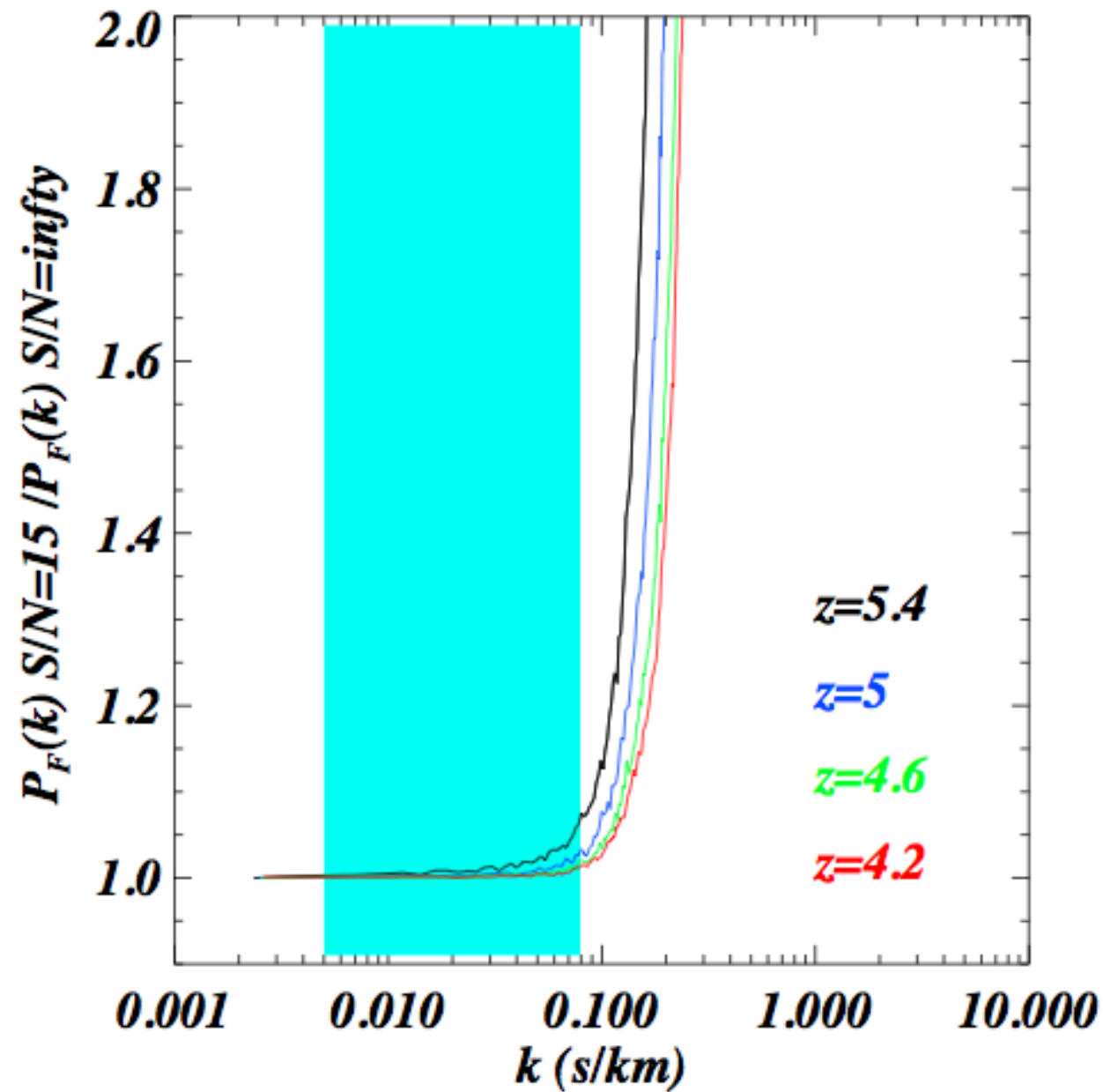
20 Mpc/h, 512³

20 Mpc/h, 768³

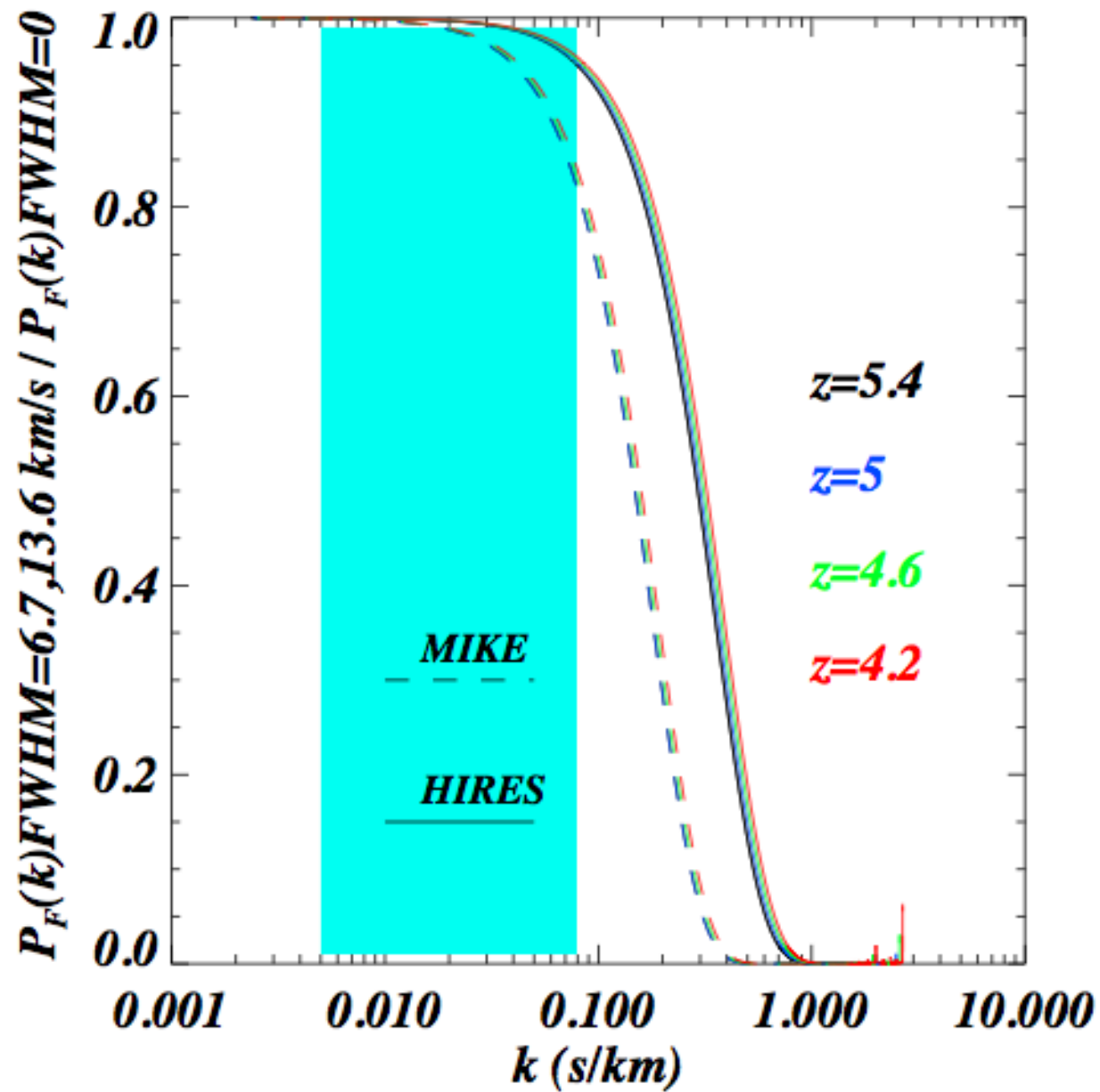
SYSTEMATICS: NUMERICAL CONVERGENCE – II



SYSTEMATICS: SIGNAL-TO-NOISE RATIO

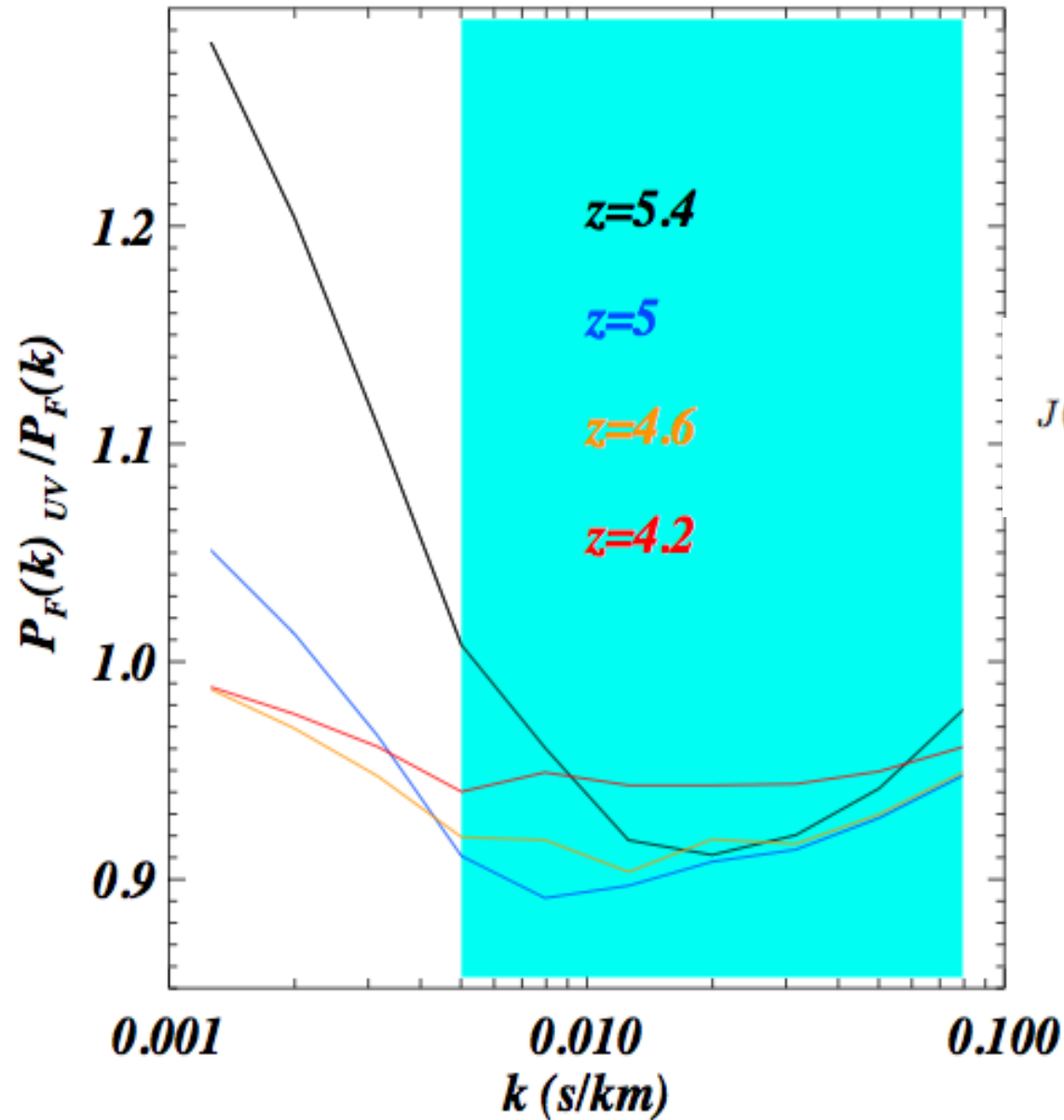


SYSTEMATICS: INSTRUMENTAL RESOLUTION



SYSTEMATICS: UV FLUCTUATIONS

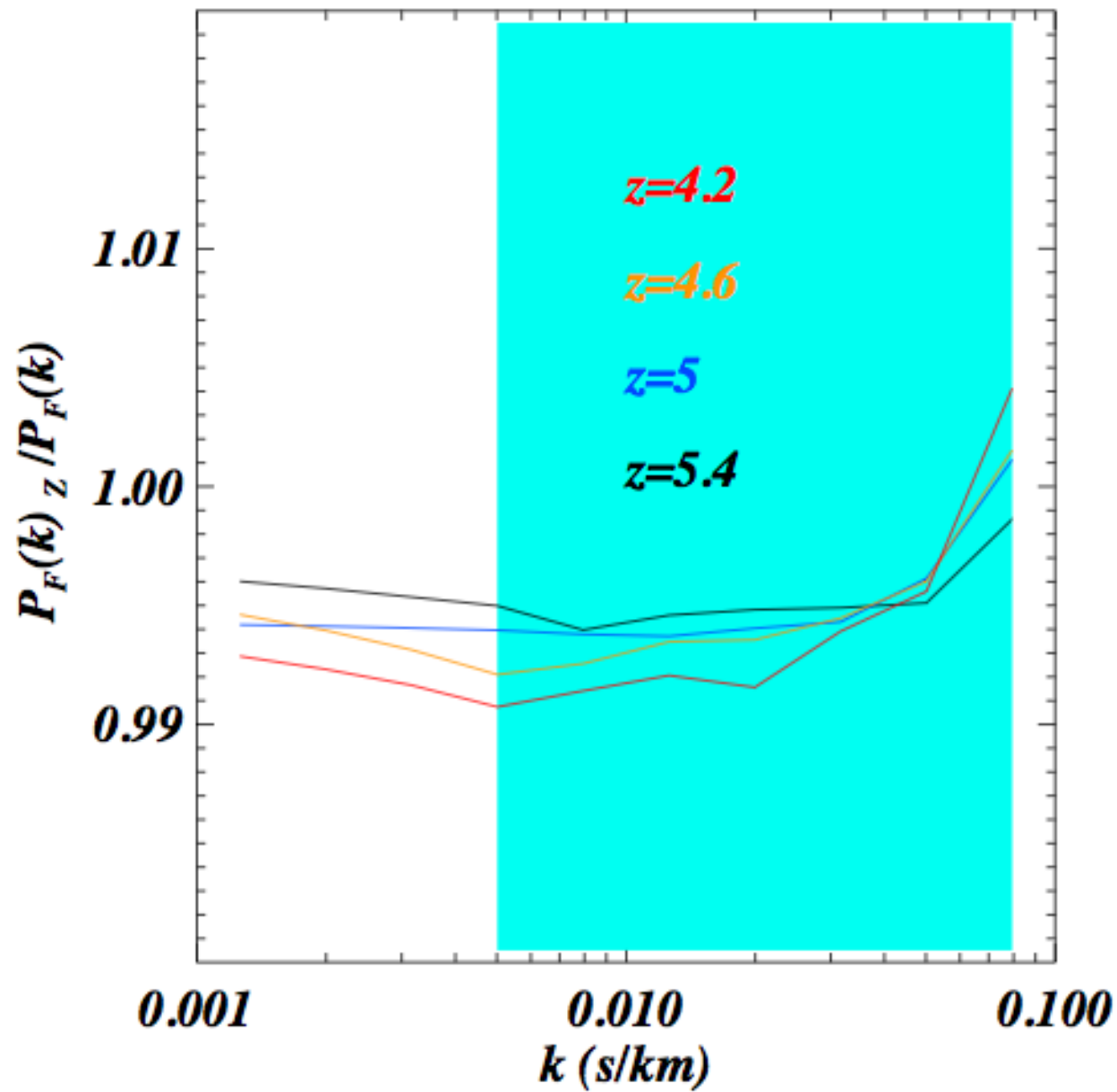
as in Bolton, J. S., & Viel, M. Mon. Not. Roy. Astron. Soc., 414, 241 (2011)



$$J(\mathbf{r}, \nu) = \frac{1}{4\pi} \sum_{i=1}^N \frac{L_i(\mathbf{r}_i, \nu)}{4\pi |\mathbf{r}_i - \mathbf{r}|^2} e^{-\frac{|\mathbf{r}_i - \mathbf{r}|}{\lambda_{\text{HI}}}} \left(\frac{\nu}{\nu_{\text{HI}}} \right)^{-3(\beta-1)}$$

Produced by QSOs with $M_B < -22$

SYSTEMATICS: METAL CONTAMINATIONS



CIV
MgII
SiIV
at lower redshift

SUMMARY OF SYSTEMATIC EFFECTS

syst. eff.	$\sigma(P_F)/P_F$	Notes
data res.	$< 5 - 15\%$	corrected
data S/N	$< 3\%$	corrected
num. res.	$< 5\%$	corrected
metals	$< 1\%$	neglected
mean flux	$\sim 30\%$	marginalized
thermal history	$\sim 30\%$	marginalized
UV	$< 10\%$	marginalized

Continuum: unimportant at the scales considered

Astrophysics (e.g. feedback from Galactic winds): unimportant at the redshifts considered

CONCLUSIONS

High redshift Lyman- α disfavours thermal relic models with masses that are typically chosen to solve the small-scale crisis of Λ CDM

Models with 1 keV are ruled out at 9σ

2 keV are ruled out at 4σ

2.5 keV are ruled out at 3σ

3.3 keV are ruled out at 2σ



1) free-streaming scale is $2 \times 10^8 M_{\odot}/h$

2) at scales $k=10 h/\text{Mpc}$ you cannot suppress more than 10% compared to Λ CDM

Of course they remain viable candidate for the Dark Matter (especially sterile neutrinos) but there are OBSERVATIONAL challenges

The one-dimensional Ly α forest power spectrum from BOSS

