

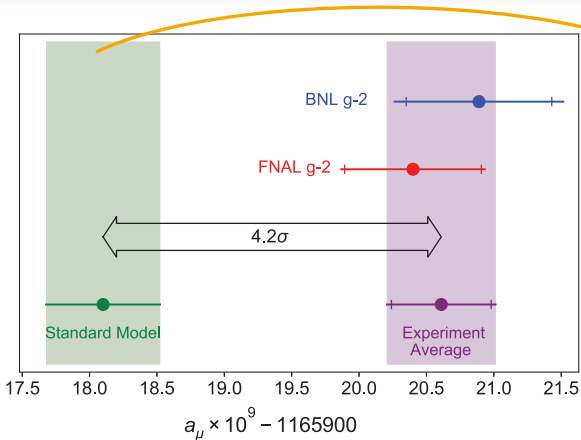
Experimental Inputs to HVP at the BESIII Experiment

Riccardo Aliberti

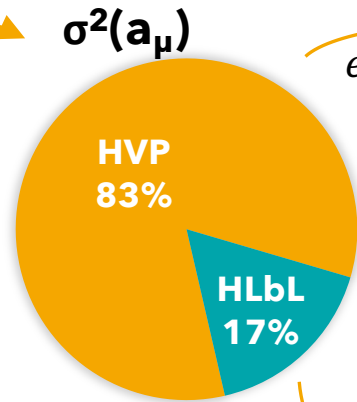
Muon $g-2$ Theory Initiative Workshop

Edinburgh, 5-9 September 2022

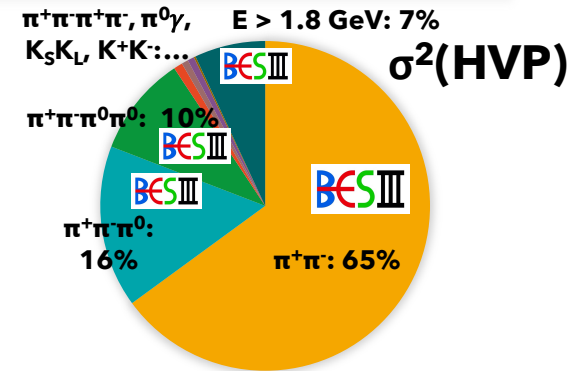
Muon ($g-2$): SM and Experiment



[Phys.Rev.Lett. 126 (2021) 141801]



$e^+e^- \rightarrow had$



[Data from: Phys.Rep 887 (2020) 1-166]

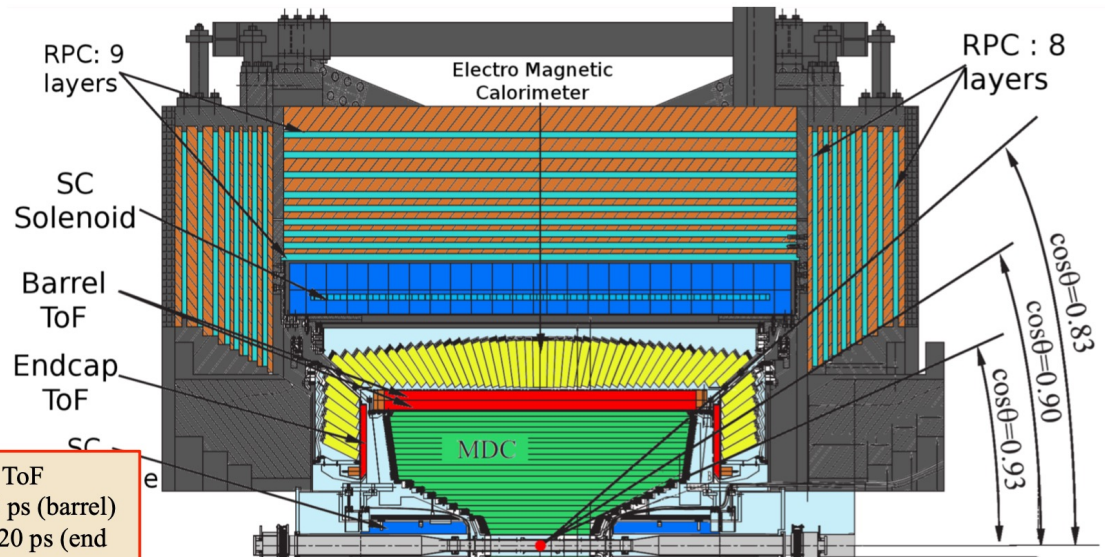
$\gamma^{(*)}\gamma^{(*)} \rightarrow hadrons$
BESIII

- New result from FNAL confirms tension with SM (4.2σ !)
- Improvement of SM prediction highly desirable
- Uncertainty dominated by HVP and HLbL
- BESIII can provide important inputs to reduce the uncertainty!

The BESIII Experiment (1)



[NIM A614 (2010) 345]



- Located at the BEPCII collider (Beijing, China)
- Symmetric e^+e^- beams
- ECM between 2-5 GeV
- Maximum luminosity: $1 \text{ nb}^{-1}/\text{s}$
- 93% coverage of the solid angle

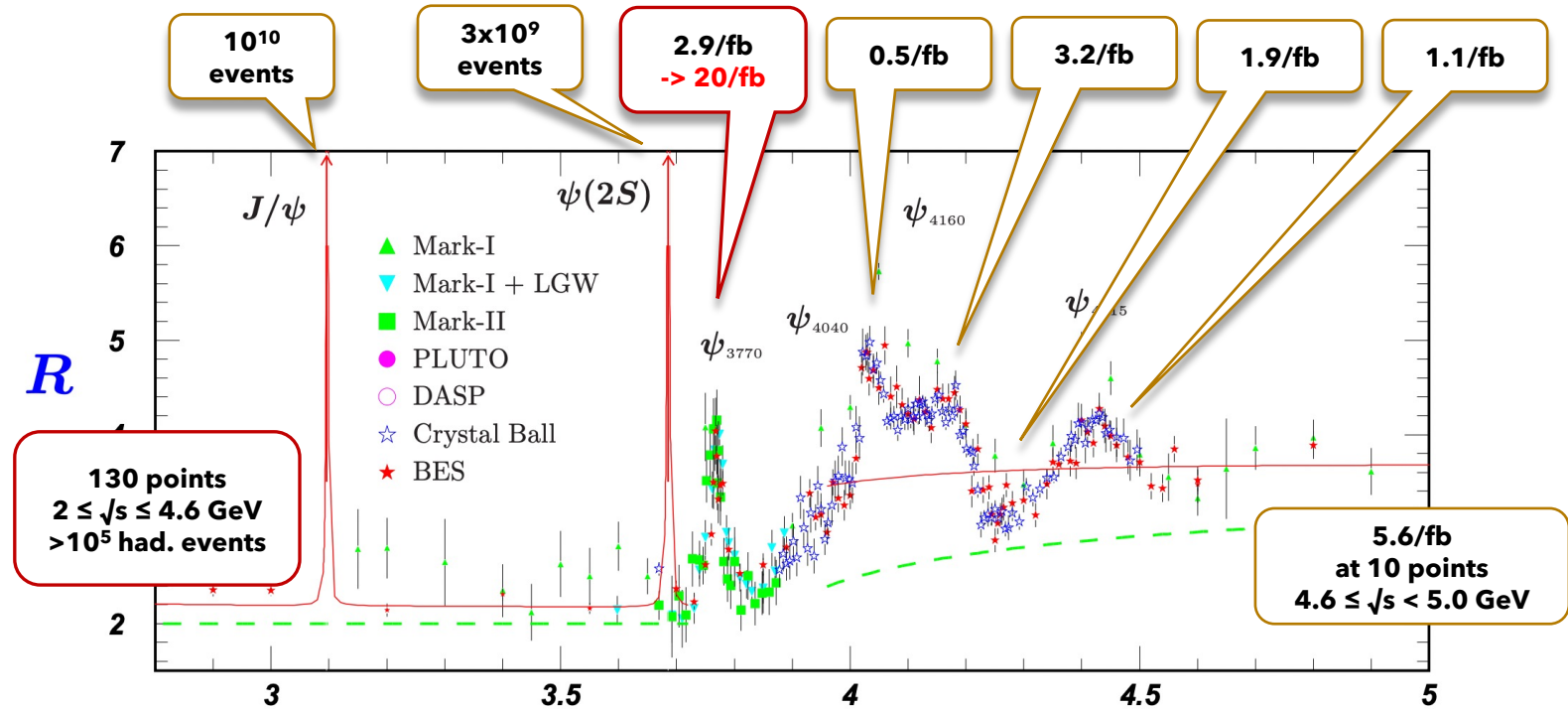
ToF
 $\sigma_t \sim 90 \text{ ps}$ (barrel)
 $\sigma_t \sim 120 \text{ ps}$ (end caps)

Drift Chamber
 $\sigma_{r\phi} \sim 130 \mu\text{m}$ (single wire)
 $\sigma_{p_t}/p_t \sim 0.5 \%$ @ 1 GeV

Electromagnetic CsI(Tl) Calorimeter
 $\sigma_E/E < 2.5\%$ @ 1 GeV (barrel)
 $\sigma_E/E < 5\%$ @ 1 GeV (end caps)
 $\sigma_{xy} \sim (6 \text{ mm})E^{1/2}$ @ 1 GeV

RPC Muon Detector
 $\Delta\Omega/4\pi = 93\%$

The BESIII Experiment (2)



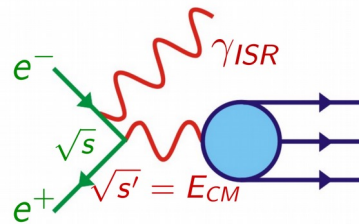
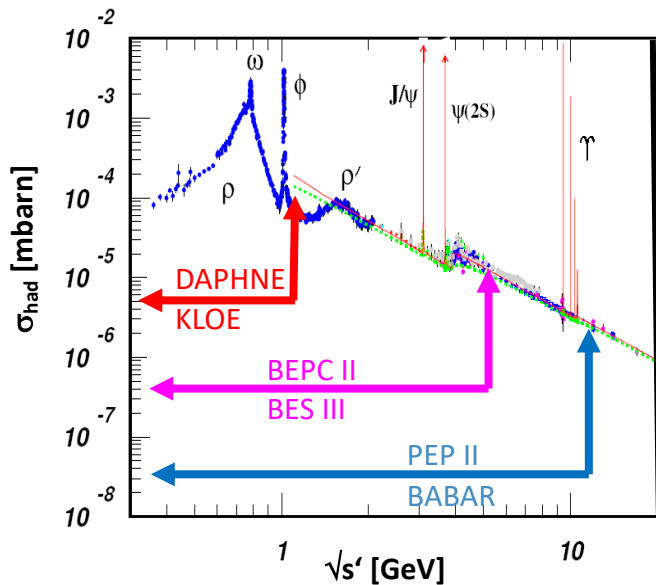
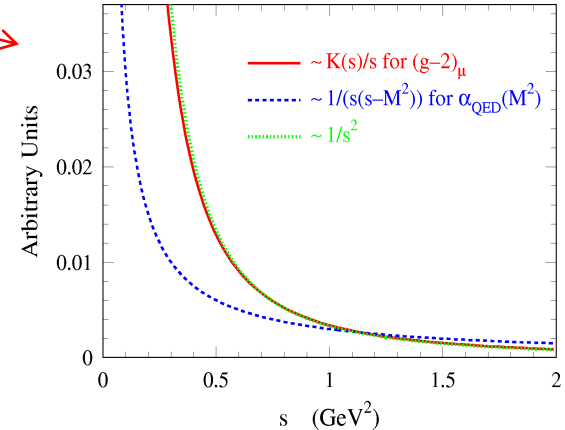
- World largest τ -charm dataset in e^+e^- annihilation
- Detailed studies in:
 - Charmonium spectroscopy and charm physics
 - Light hadron dynamics
 - τ -physics
 - R-scan

Initial State Radiation: Scan at Fixed Energy

[Brodsky, de Rafael, 1988]

$$\alpha_{\mu}^{HVP,LO} = \frac{1}{3} \left(\frac{\alpha}{\pi} \right)^2 \int_{m_{\pi}^2}^{\infty} ds \frac{K(s)}{s} R(s)$$

- Dominated by low energy region
- Not accessible in scan mode
- Initial State Radiation (ISR)



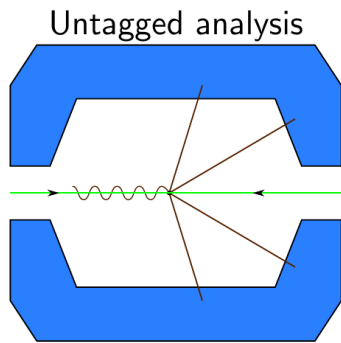
$$\sqrt{s'} = \sqrt{s - 2\sqrt{s}E_{\gamma}}$$

- Effectively reduces \sqrt{s}
- Emission suppressed by $\frac{\alpha}{\pi}$
- Radiator function relates ISR to non-radiative process

$$\frac{d\sigma_{ISR}(\sqrt{s'})}{d\sqrt{s'}} = \frac{2\sqrt{s'}}{s} W(s, E_{\gamma}, \theta_{\gamma}) \sigma(\sqrt{s'})$$

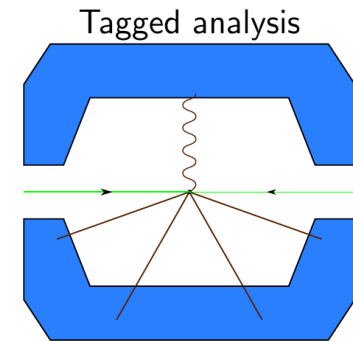
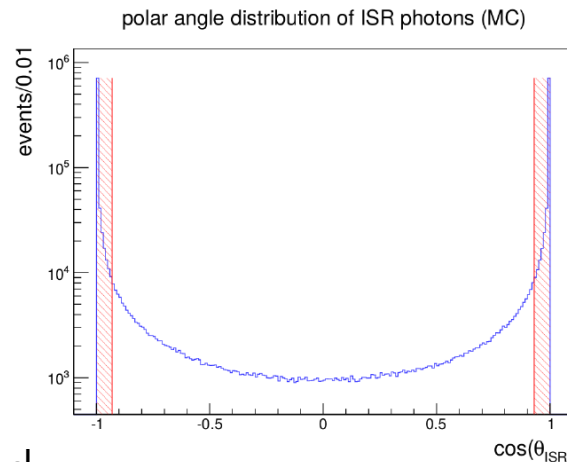
Initial State Radiation: Analysis Strategy

Detect full hadronic system



ISR photon undetected

- High statistics
- Only high masses accessible (>900 MeV)
- Small background

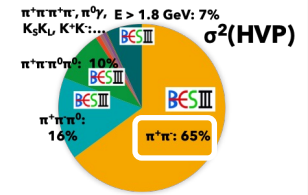


ISR photon detected

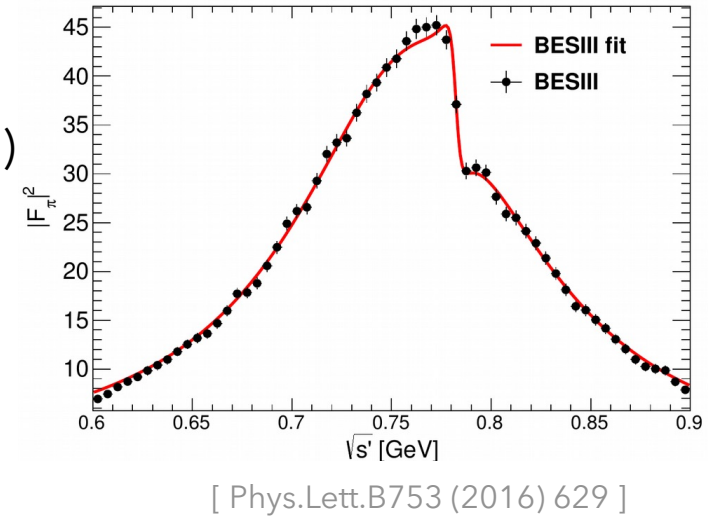
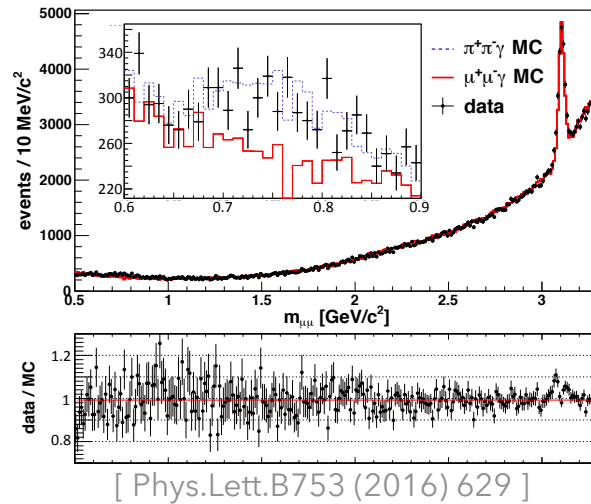
- Access to had. threshold region
- Large background at high masses

In the following results from 2.93 fb^{-1} at 3.773 GeV

The Golden Channel: $e^+e^- \rightarrow \pi^+\pi^-$

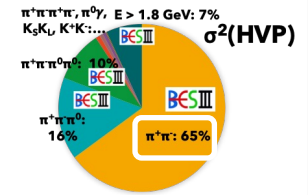


- Tagged analysis
- Background only from $\mu\mu(\gamma)$ events
- π/μ separation based on neural network (ANN)



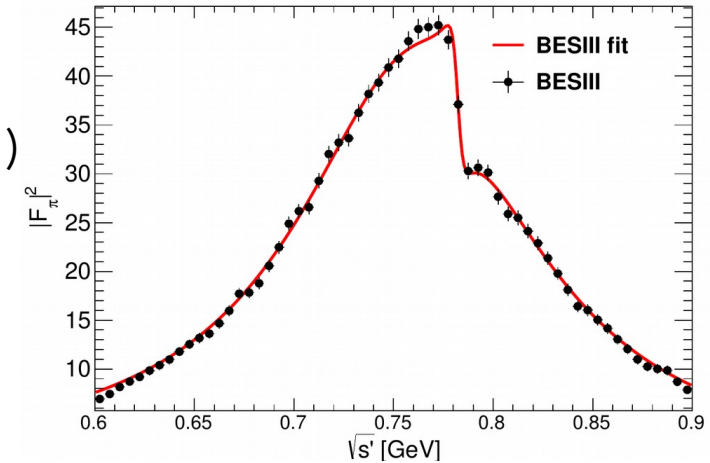
- Selecting muons using ANN
- Perfect agreement with QED prediction
- Measurement of J/ψ electronic width

The Golden Channel: $e^+e^- \rightarrow \pi^+\pi^-$



- Tagged analysis
- Background only from $\mu\mu(\gamma)$ events
- π/μ separation based on neural network (ANN)
- Careful evaluation of systematics

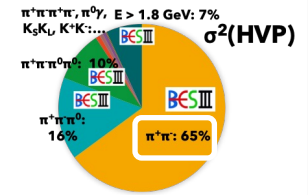
Source	Uncertainty (%)
Photon efficiency	0.2
Tracking efficiency	0.3
Pion ANN efficiency	0.2
Pion e-PID efficiency	0.2
Angular acceptance	0.1
Background subtraction	0.1
Unfolding	0.2
FSR correction δ_{FSR}	0.2
Vacuum polarization correction δ_{vac}	0.2
Radiator function	0.5
Luminosity \mathcal{L}	0.5
Sum	0.9



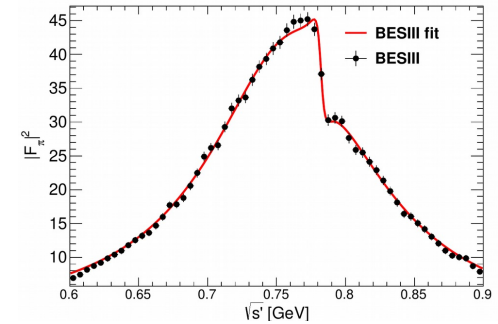
[Phys.Lett.B753 (2016) 629]

- Form factor evaluation for $0.6 \leq m_{\pi\pi} \leq 0.9$ GeV
 - 70% of total 2π contribution
 - 50% of a_μ^{HVP} contribution
 - Fit with Gounaris-Sakurai parameterization

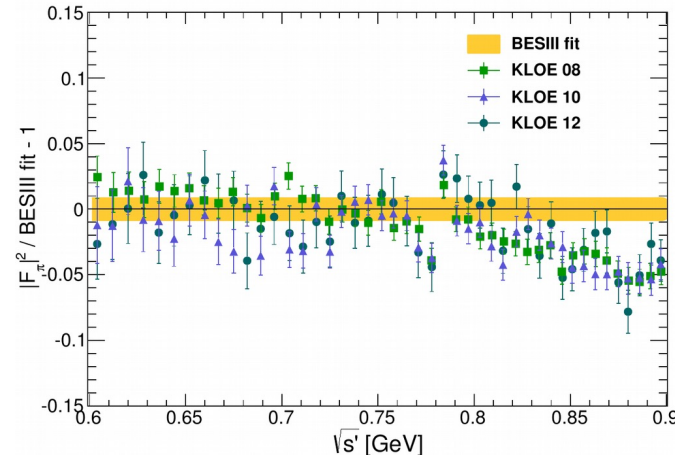
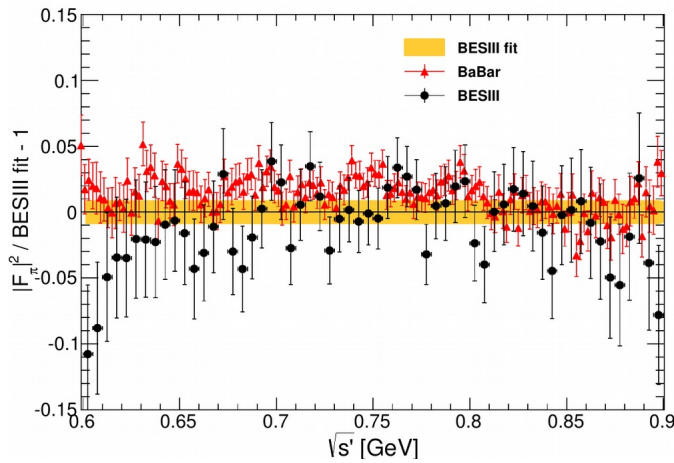
The golden channel: $e^+e^- \rightarrow \pi^+\pi^-$



- Tagged analysis
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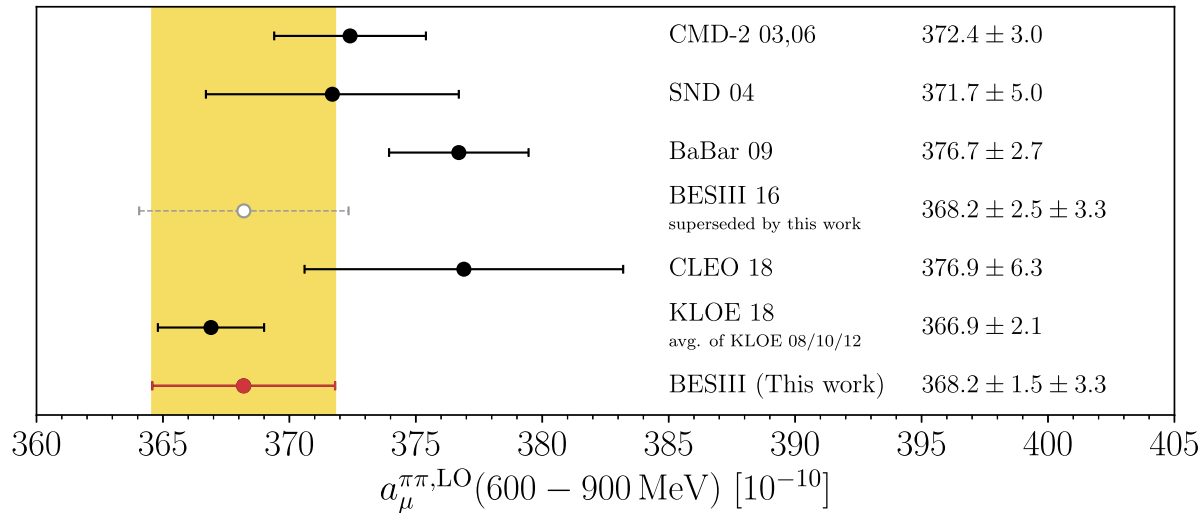
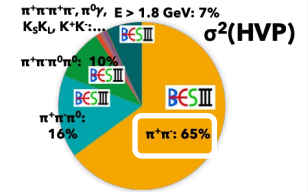


[Phys.Lett.B753 (2016) 629]



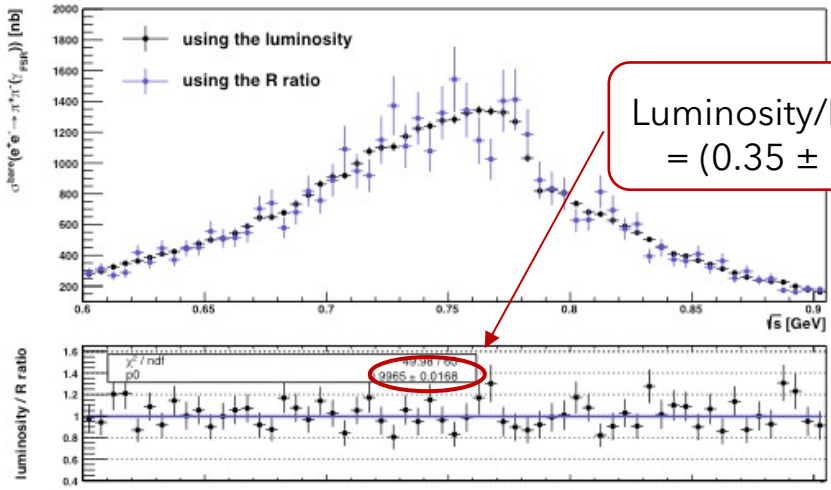
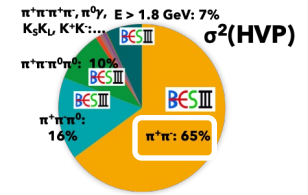
- Systematic shifts wrt previous (best) measurements
 - Below ρ/ω interference wrt BaBar
 - Above ρ/ω interference wrt KLOE

The Golden Channel: $e^+e^- \rightarrow \pi^+\pi^-$



- Precision competitive with current best results:
 - BESIII: 1.0%
 - BaBar: 0.7%
 - KLOE: 0.6%
- Evaluation of covariance matrix corrected [Phys.Lett.B812 (2021) 135982]
 - Lower statistical uncertainty
- Work on going to resolve the “KLOE-BaBar puzzle”

The golden channel: $e^+e^- \rightarrow \pi^+\pi^-$



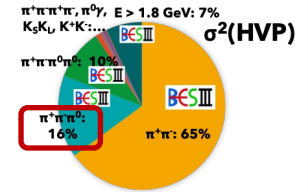
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FSR correction δ_{FSR}	0.2
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Radiator function	0.5
Luminosity \mathcal{L}	0.5
Sum	0.9 0.5

Aim to reach 0.5% precision with new analysis:

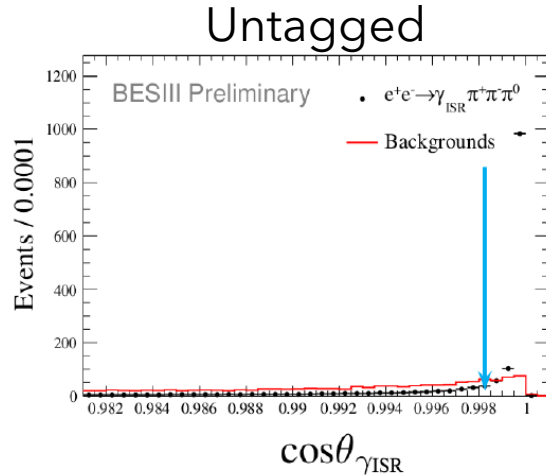
- **20 fb⁻¹ of data at 3.773 GeV** (before only 2.9 fb⁻¹)
- **Normalization to $\mu\mu$ (γ) events**
- Improved $\pi/\mu/e$ separation
- 2 independent analyses (Tagged and Untagged)
- Full $m_{\pi\pi}$ coverage up to 3 GeV
- Successful DFG funding request

$$R = \frac{N_{2\pi\gamma}}{N_{2\mu\gamma}} \cdot \frac{\epsilon^{2\mu\gamma} \cdot \left(1 + \delta_{FSR}^{2\mu}\right)}{\epsilon^{2\pi\gamma} \cdot \left(1 + \delta_{FSR}^{2\pi}\right)}$$

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0 \quad [\text{arXiv:1912.11208}]$$

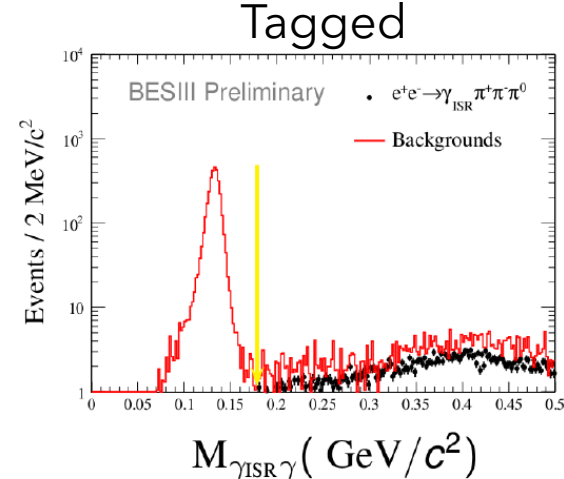


- Reconstructing events with $\pi^+\pi^- 2\gamma + \gamma_{\text{ISR}}$
- Kinematic Fit + constrain $m_{\gamma\gamma} = m_{\pi^0}$
- Both tagged and untagged configurations considered



γ_{ISR} polar angle

- Strong reduction of background

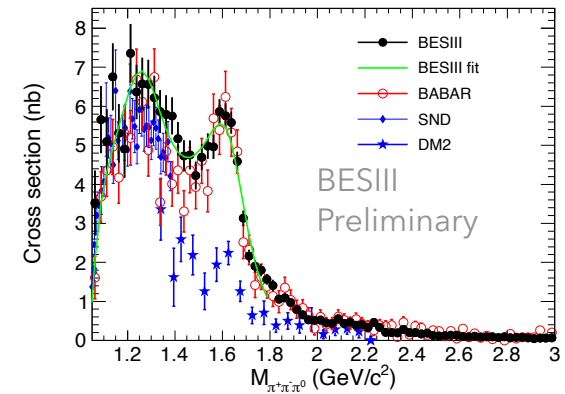
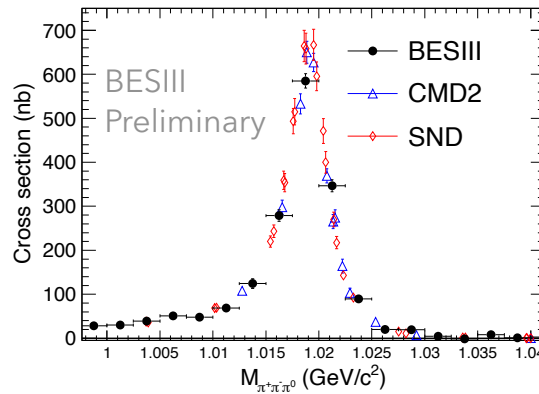
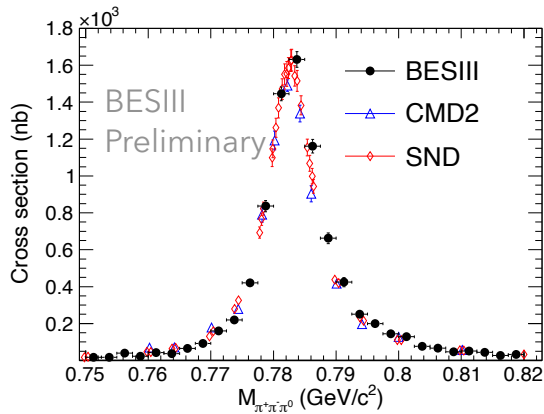
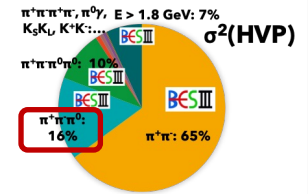


π^0 veto

- Check combination of γ_{ISR} with any other photon

- Measure $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$ to correct background description

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0 \quad [\text{arXiv:1912.11208}]$$



$$a_\mu^{3\pi} (0.7 - 3.0 \text{ GeV}) = (49.15 \pm 0.56 \pm 0.58) \times 10^{-10}$$

$$a_\mu^{3\pi} (E < 1.8 \text{ GeV}) = (46.63 \pm 0.94 / 46.21 \pm 1.45) \times 10^{-10}$$

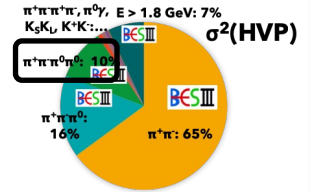
BESIII Preliminary

KNT19, DHMZ19

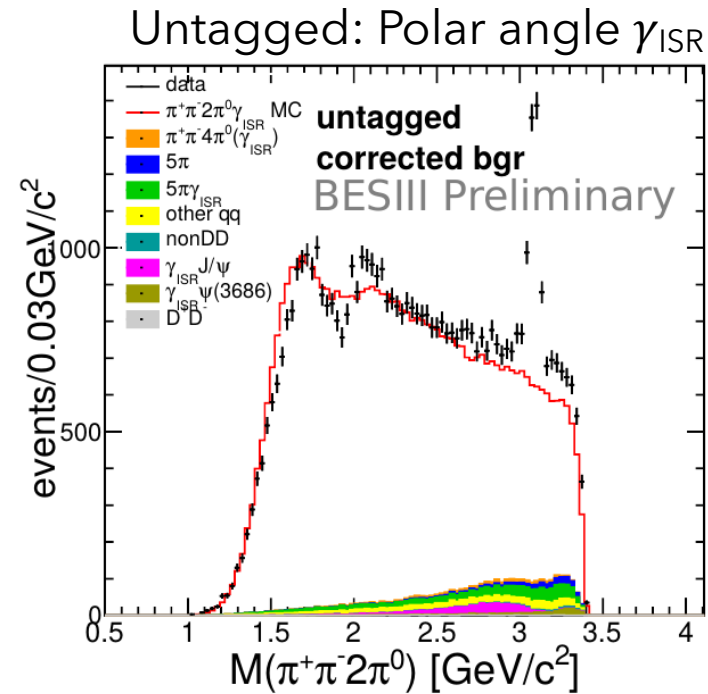
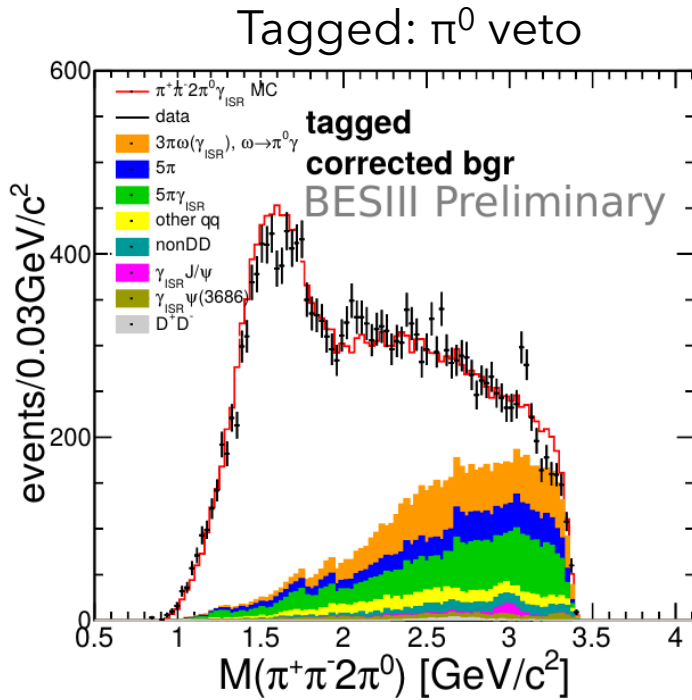
[Phys.Rep 887 (2020) 1-166]

- Extraction of 3π contribution to a_μ in 0.7 to 3 GeV:
 - Precision comparable to latest calculations
 - Paper under journal review
 - Statistics limited
 - Improvement foreseen with the upcoming dataset at 3.773 GeV!

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$

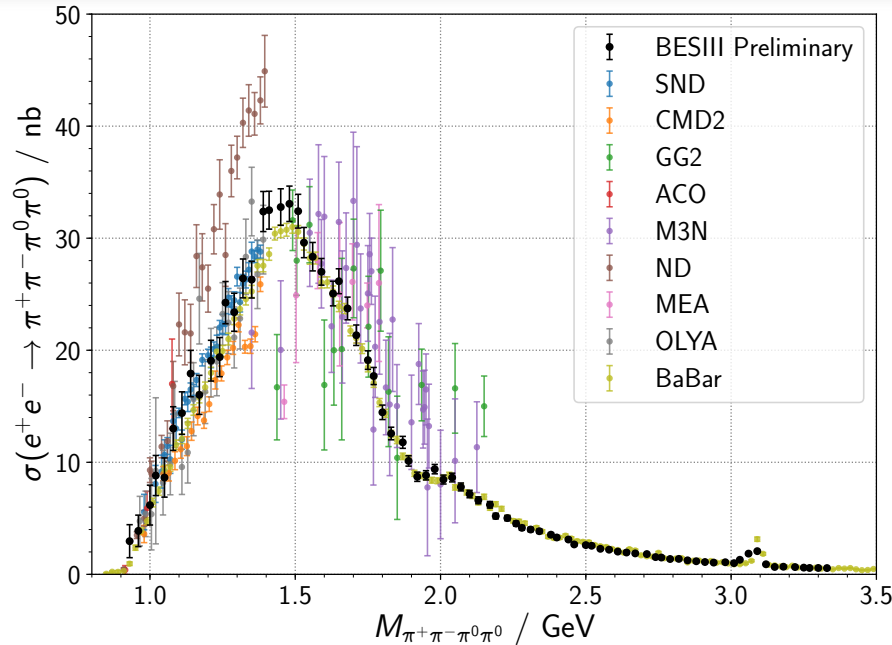
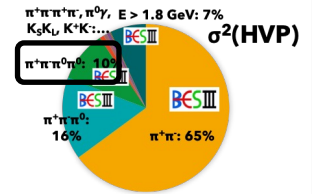


- Selection similar to $e^+e^- \rightarrow \pi^+\pi^-\pi^0$
 - Events with $\pi^+\pi^- 4\gamma + \gamma_{\text{ISR}}$
 - Kinematic Fit + constrain $m_{\gamma\gamma} = m_{\pi^0}$



➤ Measure $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$ to correct background description

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$



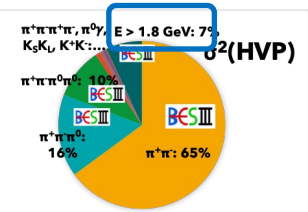
- Result from error weighted mean of tagged and untagged
- Strong improvement in precision
- a_μ compatible with BaBar result
- Room for improvement!

$$a_\mu^{\pi^+\pi^-\pi^0, \text{LO}} = \frac{1}{4\pi^3} \int_{(4m_\pi)^2}^{(1.8 \text{ GeV})^2} ds K(s) \sigma_{\pi^+\pi^-\pi^0}(s)$$

	$a_\mu^{\pi^+\pi^-\pi^0, \text{LO}} / 10^{-10}$
BESIII (preliminary)	$18.63 \pm 0.27 \pm 0.57$
BABAR	$17.9 \pm 0.1 \pm 0.6$

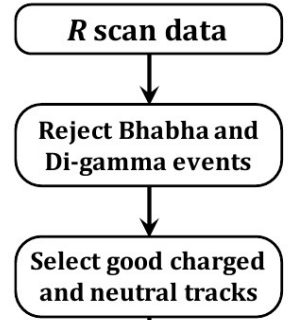
R Measurement

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)}$$

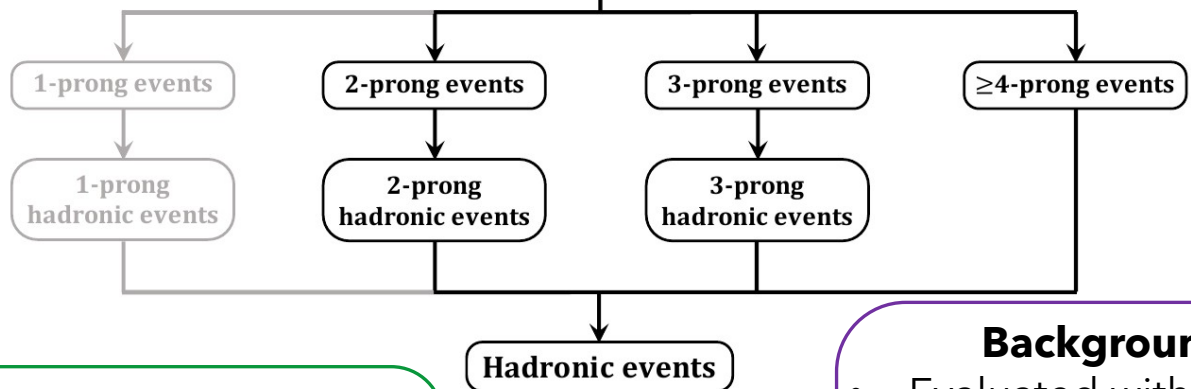


$$R = \frac{1}{\sigma_{\mu\mu}} \cdot \mathcal{L} \cdot \epsilon_{\text{had}} \cdot (1 + \delta) \cdot \frac{N_{\text{had}} - N_{\text{bkg}}}{N_{\text{had}} - N_{\text{bkg}}}$$

[Phys. Rev. Lett. 128 (2022) 062004]



14 points
 $2.2 \leq \sqrt{s} \leq 3.7 \text{ GeV}$
 $> 10^5$ had. events



Luminosity
 Large angle Bhabha

Radiative corrections

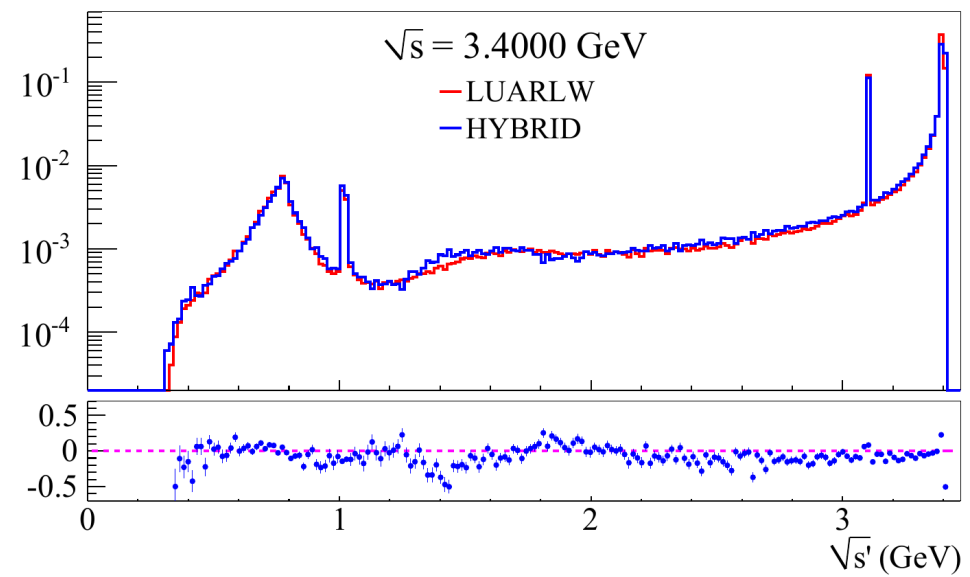
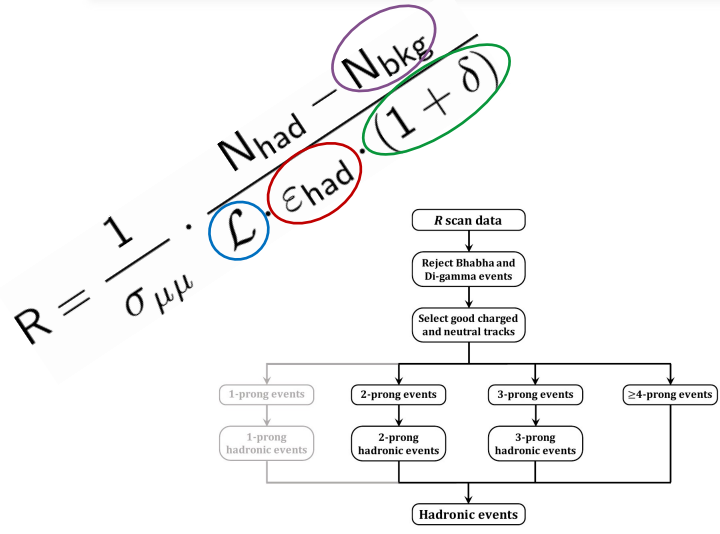
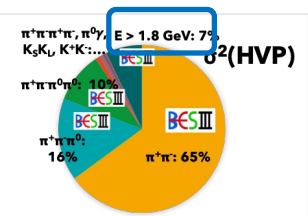
- Two schemes tested
 - Feynman diagram
 - Structure functions
- Agreement within 1.2%

Background contributions

- Evaluated with MC:
 - Babayaga, Phokhara, KKMC ($ee, \mu\mu, gg, tt$)
 - BdkRC, Diag36, Galuga, Ekharra ($ee \rightarrow ee + X$)
- Beam related background

R Measurement

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)}$$



Efficiency

Ratio of generated and reconstructed events

Fully inclusive generator

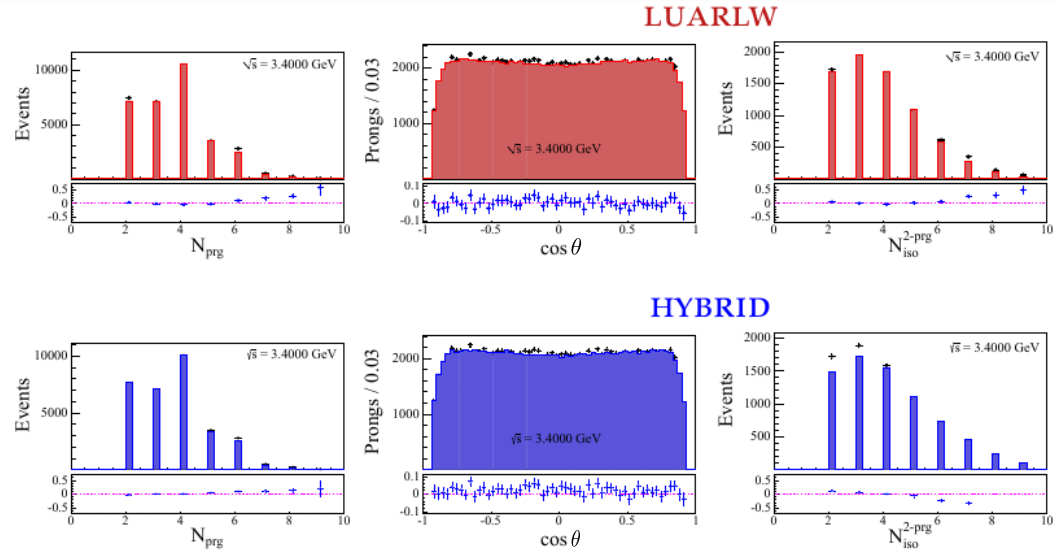
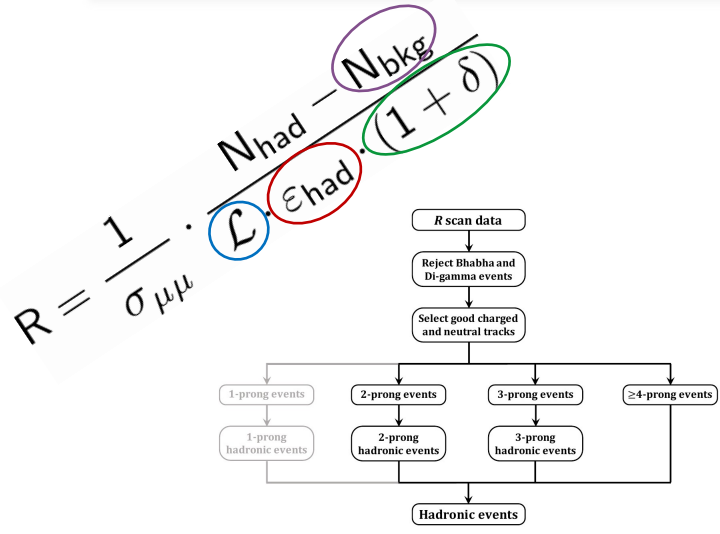
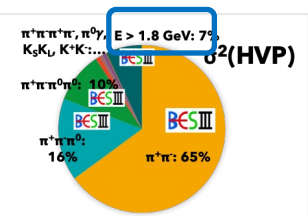
- Lund Area Law
- Low energy hadronization
- Continuum, ISR, $J^{PC}=1^{--}$ resonances
- Tuned to data

Hybrid generator

- Phokhara (10 excl. processes)
- ConExc (60 excl. proc. measured)
- Lund Area Law (unknown)

R Measurement

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)}$$



Efficiency

Ratio of generated and reconstructed events

Fully inclusive generator

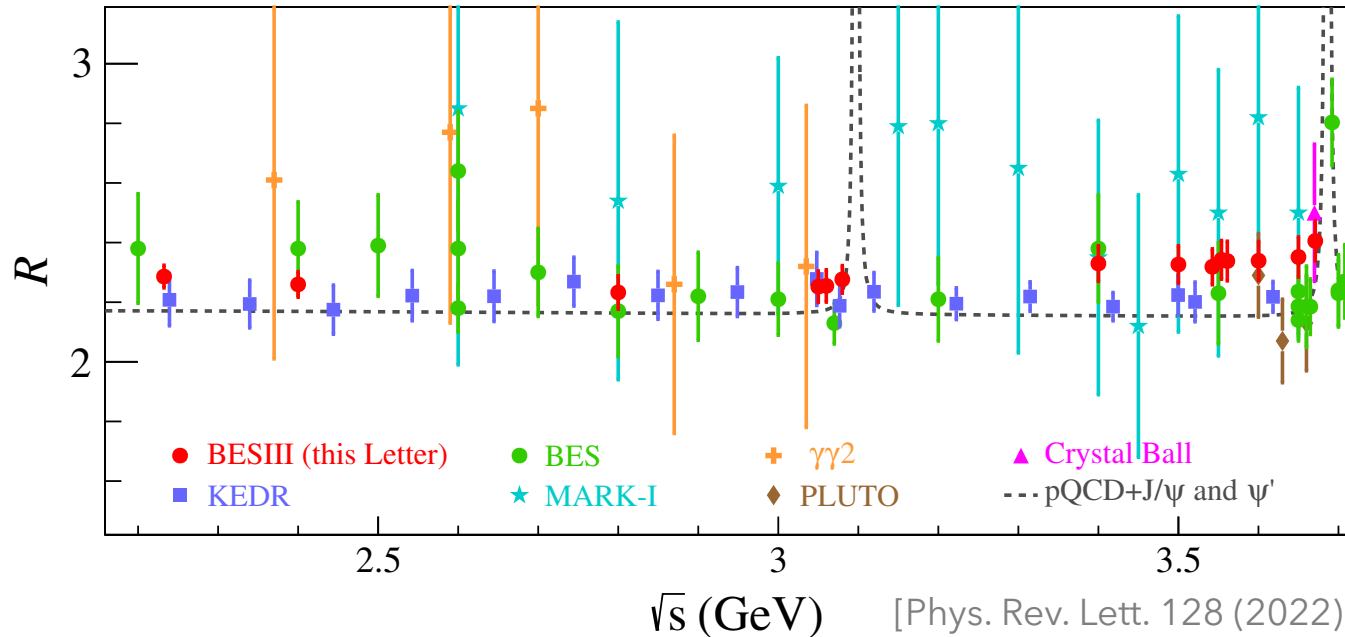
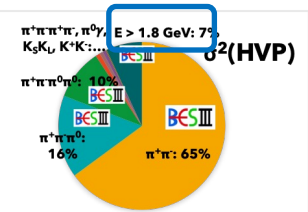
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R Measurement

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)}$$



- **Accuracy better than 2.6%** below 3.1 GeV and better than 3% above
- Exceeding pQCD predictions by 2.7σ above 3.4 GeV
- More to come in near future:
 - Result with **just 14 energy points out 130**
 - Feasibility studies for **low energy (<2 GeV) measurement via ISR**

Conclusion

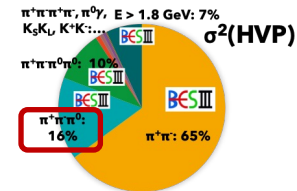
- SM uncertainty of a_μ dominated by hadronic processes
- BESIII plays an important role in the most important channels:
 - $e^+e^- \rightarrow \pi^+\pi^-$
 - Measurement with 1% uncertainty [Phys.Lett. B753 (2016) 629, B812 (2021) 135982]
 - Funding for new measurement granted
 - Aim to reach 0.5% precision \rightarrow Resolution of the KLOE-BaBar puzzle!
 - $e^+e^- \rightarrow \pi^+\pi^-\pi^0$
 - Evaluation of a_μ with O(1%) precision achieved [arXiv:1912.11208]
 - Paper under journal review
 - $e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$
 - Preliminary results with O(3%) precision in final review stage
 - **R measurement:** [Phys. Rev. Lett. 128 (2022) 062004]
 - Measurement with better than 2.6% accuracy below 3 GeV
 - More results to come: result based on 14 out of 130 energy points!

Great boost with upcoming 20fb^{-1} of data at 3.773 GeV

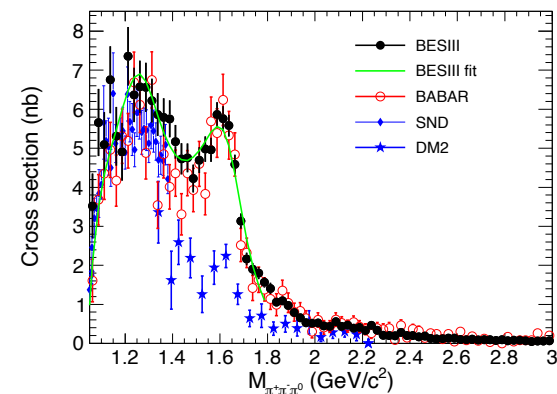
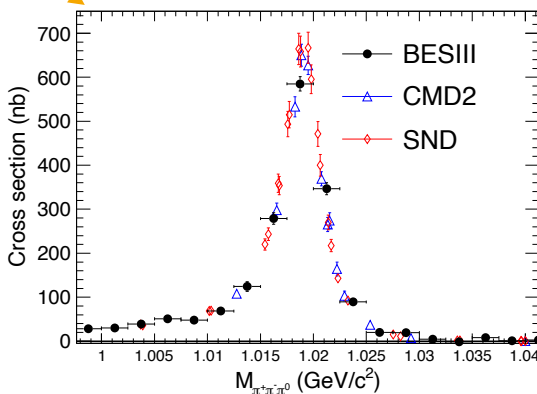
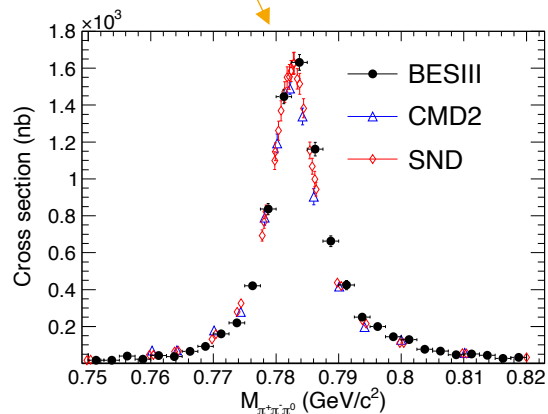
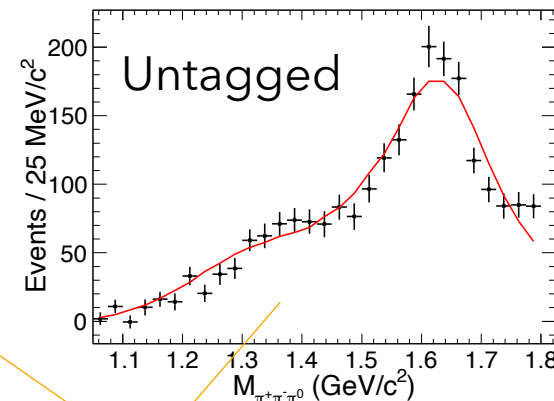
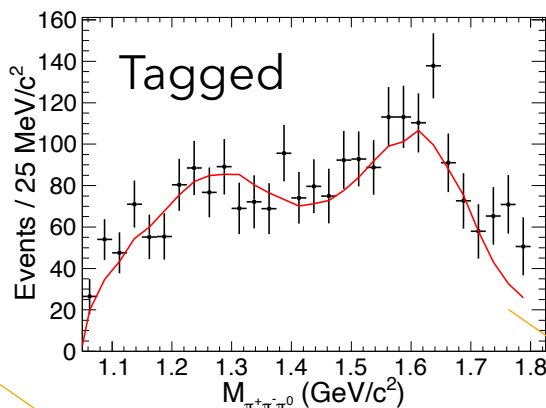
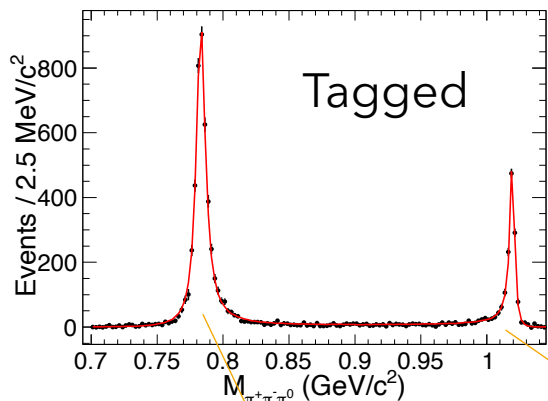


Backup

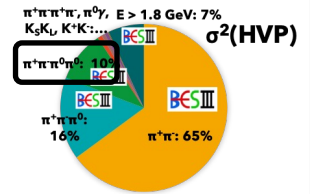
$e^+e^- \rightarrow \pi^+\pi^-\pi^0$ [arXiv:1912.11208]



$$\sigma(m) = \frac{12\pi}{m^3} F_{\rho\pi}(m) \left| \sum_{V=\omega, \phi, \omega', \omega''} \frac{\Gamma_V m^3 \sqrt{\Gamma_V^{ee} \mathcal{B}(V \rightarrow 3\pi)}}{D_V(m)} \frac{e^{i\varphi_V}}{\sqrt{F_{\rho\pi}(m_V)}} \right|^2 \quad [\text{Phys. Rev. D68 (2003) 052006}]$$



$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0$$



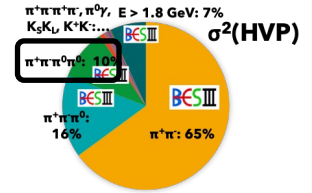
Systematic Uncertainties

Region	Mass range [GeV]
R1	$0.5 < M(4\pi) < 1.5$
R2	$1.5 < M(4\pi) < 2.0$
R3	$2.0 < M(4\pi) < 3.0$
R4	$3.0 < M(4\pi) < 3.8$

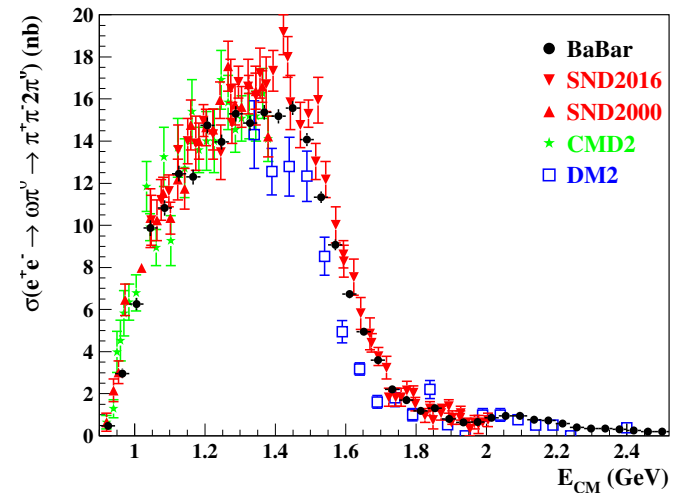
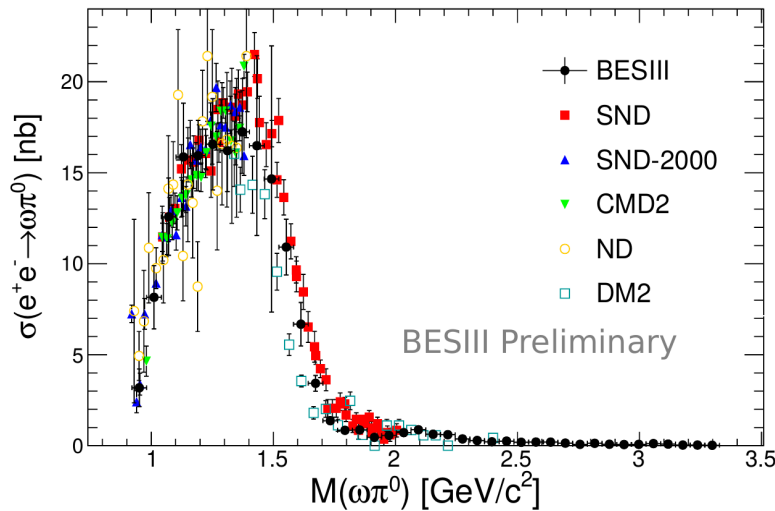
Source	Tagged [%]				Untagged [%]			
	R1	R2	R3	R4	R1	R2	R3	R4
Luminosity		0.50				0.50		
Tracking		0.60				0.60		
VP correction		0.05				0.05		
FSR correction		0.20				0.20		
Radiator Function		0.50				0.50		
ISR Photon Eff.		0.30				-		
π^0 Eff.		2.57				2.52		
Signal Eff.		0.58				0.61		
Kin. fit		0.42				0.45		
Event selection	0.60		1.46			0.64		
Bgr. Subrt. 5π	0.01	0.13	2.47	3.23	0.00	0.01	0.08	0.15
Bgr. Subrt. $5\pi\gamma_{ISR}$	0.48	0.47	7.77	10.27	0.59	0.25	0.65	0.71
Bgr. Subrt. $q\bar{q}$	0.50	0.98	12.68	21.05	0.58	0.22	0.82	0.76
Bgr. Subrt. other	0.05	0.14	2.31	5.34	0.01	0.02	0.30	0.32
ω fits (only for $\omega\pi^0$)		2.26				2.26		
$\pi^+\pi^-\pi^0$ Total	2.97	3.09	15.58	24.45	2.95	2.85	3.04	3.04
$\omega\pi^0$ Total	3.80	4.84	7.71	3.73	3.91	3.70	4.48	3.68

→ Limited by statistics! This can be reduced.

$$e^+e^- \rightarrow \pi^+\pi^-\pi^0\pi^0 \text{ as } e^+e^- \rightarrow \omega\pi^0$$



[Phys.Rev. D96 (2017) 092009]



- Fit the ω signal in every $m_{\pi^+\pi^-\pi^0\pi^0}$ bin
- Good agreement with previous results
- Extended measurement range wrt BaBar