# $B_{d,s} \rightarrow \mu^{+} \mu^{-} \gamma$ phenomenology

### - overview -

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- With Run 3 (  $\Box$  hopefully comparable e and  $\mu$  efficiencies),  $B_s \rightarrow \mu \mu \gamma / B_s \rightarrow ee \gamma$  no more science fiction

$$B_s \rightarrow \mu \mu \gamma$$
 from  $B_s \rightarrow \mu \mu$ 

[Dettori, DG, Reboud, 2017]

### **Basic Idea**

Extract  $B_s \rightarrow \mu\mu \gamma$  from  $B_s \rightarrow \mu\mu$  event sample, by enlarging  $m_{\mu\mu}$  below  $B_s$  peak

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Approach merges the advantages of both decays:

- Exploits rich and ever increasing  $B_s \rightarrow \mu\mu$  dataset
- $\cdots$  to access  $B_s \rightarrow \mu\mu\gamma$ , that probes flavour anomalies more thoroughly



[thanks F. Dettori]

- No need to reconstruct the  $\gamma$  (factor-of-20 loss in efficiency)
- Probes the high- $q^2$  region, where even a good  $\gamma$  detector is challenged
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- Trigger efficiency and reco somewhat below  $B_s \to \,\mu\mu$  But better than full  $\gamma$  reco
- Mass resolution, O(50 MeV), crucial: could be more challenging at ATLAS / CMS
- Calibration not trivial no "analogous" channel







# Backgrounds

[thanks F. Dettori]



4.....



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[LHCb-PAPER-2021-007] [LHCb-PAPER-2021-008





## The elephant in the room (f.f.'s)

## Radiative leptonic f. f.'s in LQCD

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### [RM123, '15] [1<sup>st</sup> application (K<sub>t2</sub>), RM123, '17]

Novel method to define an IR-safe LQCD correlator











## Radiative leptonic f. f.'s in LQCD

### Large $E_{\gamma}$

 The required correlator (weak & e.m. current insertion between a B and the vac) has always the desired large-Euclidean-t behavior
 [Kane, Lehner, Meinel, Soni, '19]

Note that this is non-trivial - e.g. it doesn't seem to hold if there are hadronic final states along with the  $\gamma$ 

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• However, the low-q<sup>2</sup> spectrum of  $B_s \rightarrow \mu \mu \gamma$  is dominated by resonant contributions (~98% of the BR), that LQCD is unable to capture

## f.f.'s at low $q^2$

## within factorization



[Beneke-Bobeth-Wang, '20]

For low q<sup>2</sup> ≤ (6 GeV)<sup>2</sup>, B<sub>s</sub> → χ<sup>\*</sup> f.f.'s can be calculated in a systematic expansion in 1/m<sub>b</sub>, 1/E<sub>γ</sub>

## $B_s \rightarrow \mu \mu \ \gamma$ with energetic $\gamma$

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- In particular
  - LP (  $\triangleleft$  expressible in terms of the B-meson LCDA) +  $O(\alpha_s)$  corr's

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  - LP ( sepressible in terms of the B-meson LCDA)
    + O(α<sub>s</sub>) corr's
  - local NLP






Amplitude structure [Beneke-Bobeth-Wang, '20] Take the weak operators as  $O_i \equiv J_i^{(1)} J_i^{(q)}$ • and i = 9,10 for definiteness (and simplicity)  $\overline{A} \propto \epsilon_{\mu}^{*} \left\{ \sum_{i} C_{i} \left[ T_{i}^{\mu\nu} \left\langle \ell \bar{\ell} \right| J_{i\nu}^{(l)}(0) \left| 0 \right\rangle \right. \right.$  $T_{i}^{\mu\nu} \propto \mathrm{FT}_{x} \langle 0 | T\{J_{\mathrm{em}}^{\mu}(x), J_{i}^{(q)\nu}(0)\} | B \rangle$ 





















[Beneke-Bobeth-Wang, '20]

#### Three sources

- coupling of  $\gamma$  to b quark
- power corr's to SCET, correlator at tree level
- annihilation-type insertions of 4q operators 📫 local



[Beneke-Bobeth-Wang, '20]

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- Two soft f.f.'s
  - $\xi(E_{\gamma})$ : computable as in  $B_u \rightarrow \ell \vee \gamma$  [Beneke-Rohrwild, '11]
  - For B-type contributions:  $\tilde{\xi}(E_{\gamma})$ Its Im develops resonances, thus escaping a factorization description

#### Resonances

......

[Beneke-Bobeth-Wang, '20]

- $T_{7B}^{\mu\nu}$  leads to  $\overline{A}_{res}$ 
  - standard spectral repr. (à la BW)
  - formally power-suppressed

hence inclusion won't lead to double counting of some short-distance contributions



[Beneke-Bobeth-Wang, '20]

- Dominant parametric error,  $^{+70\%}_{-30\%}$ , from  $\lambda_B$  (as expected)
- Also continuum contribution gives large error (± 35-45%)

## Concluding comments

[Beneke-Bobeth-Wang, '20]

- Dominant parametric error,  $^{+70\%}_{-30\%}$ , from  $\lambda_B$  (as expected)
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- Large NLP + little phase space available + large  $\lambda_B$  dependence challenge a precise  $B_s \rightarrow \mu \mu \gamma$  prediction at low  $q^2$

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- Prediction

 $\langle \mathcal{B} \rangle_{[4m_{\mu}^{2}, 6.0]} = (12.51^{+3.83}_{-1.93}) \cdot 10^{-9}, \quad \langle \mathcal{B} \rangle_{[2.0, 6.0]} = (0.30^{+0.25}_{-0.14}) \cdot 10^{-9}$ 

i.e.  $\phi$  region gives 97.6% of the BR



[Janowski, Pullin, Zwicky, '21] see also [Pullin, Zwicky, '21; Albrecht *et al.*, 19]

• Calculation includes: NLO at twist 1&2; LO at twist 3; partial twist 4





# Some specific observables

#### Guidelines

- focus on high q<sup>2</sup>
- *minimise dependence on LD physics*





 $B_{\xi} \rightarrow \mu\mu\gamma$  spectrum

Then main focus on large-q<sup>2</sup> region, above narrow charmonium.
 Broad-charmonium pollution estimated with similar resonant ansatz



D. Guadagnoli, QED in Weak Decays, Edinburgh, 22-24 June, 2022



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.....  $B_s \rightarrow \mu\mu\gamma$  effective lifetime de Bruyn et al., *'12* Natural exp observable: untagged rate  $\langle \Gamma(B_s(t) \to f) \rangle \equiv \Gamma(B_s^0(t) \to f) + \Gamma(\bar{B}_s^0(t) \to f)$ ..... Recalling the time dependence of the respective |amplitudes|<sup>2</sup>  $|\overset{_{\frown}}{\mathcal{A}}_{f}(t)|^{2} = \frac{e^{-\Gamma_{s}t}}{2} \Big[ \Big( |\mathcal{A}_{f}|^{2} + |q/p|^{2} |\bar{\mathcal{A}}_{f}|^{2} \Big) \cosh(\Delta\Gamma_{s}t/2) \pm \Big( |\mathcal{A}_{f}|^{2} - |q/p|^{2} |\bar{\mathcal{A}}_{f}|^{2} \Big) \cos(\Delta M_{s}t) \Big] + \frac{1}{2} \left[ \frac{1}{2} \left[ \frac{1}{2} + \frac{1}{2} \frac{1}$  $- 2\operatorname{Re}\left(q/p\,\bar{\mathcal{A}}_{f}\mathcal{A}_{f}^{*}\right)\sinh(\Delta\Gamma_{s}\,t/2) \mp 2\operatorname{Im}\left(q/p\,\bar{\mathcal{A}}_{f}\mathcal{A}_{f}^{*}\right)\sin(\Delta M_{s}\,t)$ 

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ight)}$  $A_{\Delta\Gamma}$  can be extracted from (an accurate measurement of)

the effective lifetime



[Carvunis et al., '21]

•  $A_{\Delta\Gamma}$  looks like a natural "ratio-of-amplitudes-squared" observable

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Motivation

- ... while ratio will still (partly) cancel hadr. matrix elem. dependence
- NP with non-standard CPV less constrained than NP with CKM CPV

(For NP with non-standard CPV, also constraints on Re(WCs) get looser)



 Identify NP scenarios (within WET) accounting for the anomalies & with large CPV on top

(Wealth of  $b \rightarrow s$  data still under-constraining for WC shifts w/ large non-CKM weak phases.)

Scenario	$O \parallel C_7^{\mathrm{NP}}$	$C_9^{ m NP}$	$C_{10}^{ m NP}$
$C_7$	0.02 - 0.13i	0	0
$C_9$	0	-1.0-0.9i	0
$C_{10}$	0	0	1.0 + 1.4i
$C_{LL}$	0	-0.7 - 1.4i	0.7 + 1.4i

£2.....



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- Survey  $A_{\Delta\Gamma}$  sensitivity to these scenarios
  - for both low and high q<sup>2</sup>
  - taking into account f.f. & resonance-modelling errors


Impact of broad cc Carvunis et al., '21 Parameterize the effect most generally (e.g. discussion in [Lyon, Zwicky, '14])  $C_9 \rightarrow C_9 - \frac{9\pi}{\alpha^2} \bar{C} \sum_V |\eta_V| e^{i\delta_V} \frac{\hat{m}_V \mathcal{B}(V \rightarrow \mu^+ \mu^-) \hat{\Gamma}_{\text{tot}}^V}{\hat{q}^2 - \hat{m}_V^2 + i\hat{m}_V \hat{\Gamma}_{\text{tot}}^V}$ .....  $|\eta_V| \in [1, 3] \& \delta_V \in [0, 2\pi)$  (uniformly and independently for the 5 resonances)  $S_{\psi(2S), \psi(3770), \psi(4040), \psi(4160), \psi(4415)} = \{0.47, 0.49, 0.57, 0.61, 0.68\}$ for  $S_{min} \in [0.5, 0.7] \ m_{Bs}^2$ for all TH scenarios









[Carvunis et al., '21]

• Bottom line: broad  $c\bar{c}$  has surprisingly small impact on  $A_{\Delta\Gamma}$ 

But broad-cc shift to  $C_9$  typically O(5%) – and with random phase



Far from obvious why such a small impact on  $A_{\Delta\Gamma}$ 

- Closer look (App. D for an analytic understanding)
  Cancellation is a conspiracy between
  - Complete dominance of contributions quadratic in C<sub>9</sub> and C<sub>10</sub>
  - Multiplying f.f.'s  $F_V, F_A \in \mathbb{R}$
  - Broad  $c\bar{c}$  can be treated as small modif. of (numerically large)  $C_9$

Ease cancellations between num & den in  $A_{\Delta\Gamma}$ 





- Broad  $c\bar{c}$  only shifts  $C_9$
- efficient cancellations possible
- f.f.'s enter in different ways (all numerically relevant) for the different WC combinations
- In short
  - f.f. error still too important to resolve between TH scenarios
  - Yet, dominance of jointly  $C_9 \& C_{10}$  implies high sensitivity to  $C_{LL}$ could be resolvable with ~ half the current f.f. error

- Low impact of broad  $c\overline{c}$  encouraging, given that this systematics inherently escapes a rigorous description
- f.f. uncertainty, even if still large, in principle "reducible"
- Maybe worthwhile to look for more observables with such properties



## Im shifts to WCs: how large?

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		Pre-Moriond 2021			Post-Moriond 2021		
Scenario		Best-fit	Pull	<i>p</i> -value	Best-fit	Pull	<i>p</i> -value
$C_7$	${\rm I\!R}$	-0.0079	$0.58\sigma$	0.11%	-0.0079	$0.57\sigma$	0.12%
	C	-0.0045 - 0.056i	$0.61\sigma$	0.11%	-0.0044 - 0.056i	$0.61\sigma$	0.11%
$C_9$	$\mathbb{R}$	-0.97	$6.4\sigma$	10.0%	-0.93	$6.7\sigma$	12.0%
	C	-0.98 - 0.22i	$6.1\sigma$	9.4%	-0.93 - 0.25i	$6.4\sigma$	12.0%
$C_{10}$	$\mathbb{R}$	0.72	$5.8\sigma$	6.1%	0.68	$6.0\sigma$	5.7%
	C	0.80 + 0.74i	$5.6\sigma$	6.0%	0.76 + 0.75i	$5.8\sigma$	5.6%
$C_{LL}$	$\mathbb{R}$	-1.1	$6.9\sigma$	18.0%	-0.96	$7.0\sigma$	16.0%
	C	-1.2-1.5i	$6.7\sigma$	18.0%	-1.1 - 1.4i	$6.8\sigma$	16.0%
$C_{LR}$	$\mathbb{R}$	0.34	$1.2\sigma$	0.13%	0.28	$1.1\sigma$	0.09%
	C	0.34 + 0.032i	$0.74\sigma$	0.11%	0.28 + 0.017i	$0.59\sigma$	0.08%
$C'_7$	${\rm I\!R}$	0.004	$0.28\sigma$	0.12%	0.005	$0.29\sigma$	0.07%
	C	0.004 - 0.001i	$0.05\sigma$	0.10%	0.005 - 0.0003i	$0.05\sigma$	0.06%
$C'_9$	${\rm I\!R}$	0.14	$0.74\sigma$	0.13%	0.0044	$0.06\sigma$	0.09%
	C	0.13+0.24i	$0.54\sigma$	0.12%	0.0012 + 0.2i	$0.24\sigma$	0.08%
$C_{10}^{\prime}$	${\rm I\!R}$	-0.18	$1.7\sigma$	0.14%	-0.09	$0.81\sigma$	0.08%
	C	-0.20 - 0.14i	$1.3\sigma$	0.13%	-0.063 - 0.11i	$0.45\sigma$	0.07%
$C_{RL}$	$\mathbb{R}$	0.22	$1.5\sigma$	0.17%	0.088	$0.23\sigma$	0.07%
	C	0.24+0.40i	$1.3\sigma$	0.16%	0.085 + 0.32i	$0.40\sigma$	0.07%
$C_{RR}$	$\mathbb{R}$	-0.37	$1.4\sigma$	0.17%	-0.28	$1.1\sigma$	0.09%
	C	-0.37 - 0.003i	$0.93\sigma$	0.15%	-0.28 - 0.004i	$0.65\sigma$	0.08%