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Dealing with QED at B Factories: Caveats and Lessons

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Florian Bernlochner QED in Weak Decays Workshop - Edinburgh 2022-

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Talk Outline



Talk Outline



FSR & Bremsstrahlung



FSR & Bremsstrahlung



Example material Budget of a detector (here *BaBar*):

		material	thickness l (mm)	density ρ (g/cm^3)	$\begin{array}{l} \mathrm{mean \ path} < l > \\ (mm) \end{array}$	radiation length X_0 (mm)	$< l > /X_0$	plasma frequency k_p (Gev)
3eam-pipe	PEP II tube	$ \begin{array}{c} \mathrm{Au} \\ \mathrm{Be} \\ \mathrm{H}_2 0 \\ \mathrm{Be} \\ total \end{array} $	$0.004 \\ 0.830 \\ 1.48 \\ 0.530$	$19.3 \\ 1.85 \\ 0.998 \\ 1.85$	0.005 1.064 1.896 0.679	3.347 346.416 370 [17] 346.416	0.00153 0.00307 0.00513 0.00196	$\begin{array}{c} 8.0168 \cdot 10^{-8} \\ 2.6113 \cdot 10^{-8} \\ 2.1476 \cdot 10^{-8} \\ 2.6113 \cdot 10^{-8} \end{array}$
) Detector E	SVT 1-3 SST SVT 4	Si Cu Kapton Kevlar (C) Si Cu Kapton	0.300 0.0089 0.0254 - 0.300 0.0089 0.0254	2.33 8.96 1.42 2.27 2.33 8.96 1.42	0.404 0.0119 0.0342 0.0911 0.387 0.0115 0.0328	93.344 14.350 324.948 188.109 93.344 14.350 324.948	0.00433 0.00084 0.00011 0.00048 0.00415 0.00080 0.00010	$\begin{array}{r} 3.1099 \cdot 10^{-8} \\ 5.8267 \cdot 10^{-8} \\ 2.3311 \cdot 10^{-8} \\ 3.0677 \cdot 10^{-8} \\ 3.1099 \cdot 10^{-8} \\ 5.8267 \cdot 10^{-8} \\ 2.3311 \cdot 10^{-8} \end{array}$
Trackinç	SST SVT 5 SST	Kevlar (C) Si Cu Kapton Kevlar (C) <i>total</i>	- 0.300 0.0089 0.0254 -	2.27 2.33 8.96 1.42 2.27	0.0911 0.386 0.0115 0.0327 0.0911	188.109 93.344 14.350 324.948 188.109	0.00048 0.00414 0.00080 0.00010 0.00048 0.03331	$3.0677 \cdot 10^{-8} 3.1099 \cdot 10^{-8} 5.8267 \cdot 10^{-8} 2.3311 \cdot 10^{-8} 3.0677 \cdot 10^{-8}$
chamber	ST DCH	Kevlar (C) Be He : C_4H_{10} + wires total overall total	0.97 1.00 573.0	2.27 1.85 0.000624	1.25 1.28 734.2	249 [14] 346.416 340000 [14]	0.005 [13] 0.00370 0.00216 0.00586 0.05086	$\frac{3.0677 \cdot 10^{-8}}{2.6113 \cdot 10^{-8}} \\ 5.0067 \cdot 10^{-10}$

Simulated **energy loss**:





Monochromatic

initial Energy

Drift chamber

Track fitting

See e.g. Comput.Phys.Commun. 259 (2021) 107610 or



Track fitting

See e.g. Comput.Phys.Commun. 259 (2021) 107610 or



Bremrecovery

Can try to identify and recover Bremsstrahlung & FSR emissions

Requires lower energy cut ~ **10 MeV** to identify photon in ECL

Once **identified**, can correct track momentum with identified photons:





Belle method: use a search cone or wedge around the initial direction to define a search region in the ECL





Extrapolate from **all major material** layers plus the transition region

Optimize Acceptance region to maximize finding efficiency & minimize fake rate



Finding Efficiency for Brem photons



LHCb faces similar challenges:

If emission happens before the magnet impacts momentum measurement

Identify Brem photon and **correct track momentum**

Done by **extrapolating** the upstream e^{\pm} to ECAL

 π^{\pm}





Reversing Bremsstrahlung Effects

Can use detailed **MC simulations** to **separate Brem & FSR effects** from each other on a statistical basis

Use detailed **Geant4** simulation of material effects of detector

Treat Brem effects as migration problem:

$$\widehat{S}_i = \sum_j \mathscr{P}(\text{in reco bin } i \mid \text{in true bin } j) S_j$$

Example: measured $B \to X_c \ell \bar{\nu}_\ell$ spectrum from BaBar



Reversing Brem + FSR Effects

To compare with theory, often also **FSR effects** need to be removed

Method very similar: use PHOTOS and MC simulations to assess migrations between **"bare"** and "**dressed**" leptons

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Typically correct for resolution, Bremsstrahlung, FSR effects in **one go:**



Uncertainties of FSR Effects in measurements

No **consensus** amongst experimentalists how such should be evaluated

Approaches:

* Ignore

on dedicated control samples. The uncertainty arising from radiative corrections is studied by comparing the results using PHOTOS [30] to simulate final state radiation (default case) with those obtained with PHOTOS turned off. We take 25 % of the difference as an error. The un-

- * Produce samples w/o FSR (PHOTOS), assign X% difference to nominal result as error (X = 20-30%)
- * Compare to Ginsberg calculation; derive uncertainty from difference



Talk Outline



D. Atwood and W. J. Marciano, Phys. Rev. D41, 1736 (1990). G. P. Lepage, Phys. Rev. D42, 3251 (1990). N. Byers and E. Eichten, Phys. Rev. D 42, 3885 (1990). R. Kaiser, A. V. Manohar, and T. Mehen, Phys. Rev. Lett. 90, 142001 (2003), arXiv:hep-ph/0208194. M. B. Voloshin, Phys. Atom. Nucl. 68, 771 (2005), arXiv:hep-ph/0402171

Long-standing problem...



Important observable to measure branching fractions:

$$R^{\pm 0} = \frac{\Gamma(\Upsilon(4S) \to B^+ B^-)}{\Gamma(\Upsilon(4S) \to B^0 \overline{B}{}^0)} ,$$

A "simple" QED problem

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Restricted phase-space results in small velocities, enhancing EM effects

Expect a phase-space & naive Coulomb enhancement of

Decay Mode	$\frac{p_{\pm}^3}{p_0^3}$	$\frac{2\pi\lambda(1+\lambda^2)}{1-\exp(-2\pi\lambda)}$	$R_0^{\pm 0}$
$\Upsilon(4S) \to B\overline{B}$	1.048	1.20	1.26

$$R_0^{\pm 0} = \frac{p_{\pm}^3}{p_0^3} \frac{2\pi\lambda(1+\lambda^2)}{1-\exp(-2\pi\lambda)},$$

 $\lambda = \alpha/(2v_+)$ Velocity $v_{\pm} = (1 - 4m_{R^{\pm}}^2/m_{\Upsilon})^2$

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$\Upsilon(4S) \to B\overline{B}$	1.048	1.20	1.26

Experimentally: R^2

$$b^{\pm 0} = 1.062 \pm 0.021$$

FB, M. Jung, G. Landsberg, Z. Ligeti, to appear

 $R_0^{\pm 0} = \frac{p_{\pm}^3}{p_0^3} \frac{2\pi\lambda(1+\lambda^2)}{1-\exp(-2\pi\lambda)},$

 $\lambda = \alpha/(2v_+)$ Velocity $v_{\pm} = (1 - 4m_{B^{\pm}}^2/m_{\Upsilon})^2$

QED effects **suppressed**?

Talk Outline





Corrections on $|V_{ub}| \& |V_{cb}|$





SIRLIN, A. : Large m(W), m(Z) Behavior of the O(alpha) Corrections to Semileptonic Processes Mediated by W. In: *Nucl. Phys.* B196 (1982), S. 83. http://dx.doi.org/10. 1016/0550-3213(82)90303-0. - DOI 10.1016/0550-3213(82)90303-0

Corrections on $|V_{ub}| \& |V_{cb}|$



Also don't correct for Coulomb enhancement



SIRLIN, A. : Large m(W), m(Z) Behavior of the O(alpha) Corrections to Semileptonic Processes Mediated by W. In: *Nucl. Phys.* B196 (1982), S. 83. http://dx.doi.org/10. 1016/0550-3213(82)90303-0. - DOI 10.1016/0550-3213(82)90303-0

RAPID COMMUNICATIONS

PHYSICAL REVIEW D

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1 MARCH 1990

Radiative corrections and semileptonic *B* decays

David Atwood and William J. Marciano Physics Department, Brookhaven National Laboratory, Upton, New York 11973 (Received 8 December 1989)

A prescription for approximating electroweak radiative corrections to weak decays is given. The method is illustrated for $\tau \rightarrow ev\bar{v}$ and a simplified (structureless) model of $B \rightarrow Me\bar{v}$, M = Dor π , where the complete $O(\alpha)$ corrections are known. Our procedure is shown to provide a proper description of radiation damping near the electron's end-point energy and a reasonable estimate of radiative corrections for much of the spectrum as well as the integrated rate. As a practical application, it is applied to the semileptonic decays $B \rightarrow Xe\bar{v}$, where an exact $O(\alpha)$ treatment of radiative corrections is very difficult, but an estimate of their effect is important for the extraction of V_{ub} and leptonic branching ratios. We also discuss an 18% enhancement of $\Upsilon(4S) \rightarrow B^+B^$ relative to $B^0\bar{B}^0$ due to large Coulomb corrections near threshold.

As our next example, we consider the decays $B \rightarrow Me\bar{v}$, where M is either a π or D meson. Since this exercise is meant only to test our prescription, we study a somewhat tions is to multiply (13) by the correction factors in (3) (with $m_Y = m_B$) and (5). In addition, for $\eta \approx 1$ our condition on c gives $c \approx \frac{2}{3}$, so we have¹⁷

$$\frac{d\Gamma(B \to Me\bar{v})}{dx} = \frac{G_{\mu}^2 m_B^5}{32\pi^3} |V_{ib}|^2 |f_{\pm}^M|^2 \eta^5 \frac{x^2(1-x)^2}{1-\eta x} \left(1 + \frac{2\alpha}{\pi} \ln \frac{m_Z}{m_B}\right) \left(\frac{1}{1-\eta x}\right)^2 \left(1 + \frac{2\alpha}{\pi} \ln \frac{m_Z}{m_B}\right) \left(1 + \frac{2\alpha}{\pi}$$

for charged *B* decays, while for neutral *B* decays, an additional $1 + \pi \alpha$ correction factor should be appended.¹¹ For comparison, we can use a complete $O(\alpha)$ calculation of radiative corrections for this simple model by Ginsberg.¹⁵ Such a comparison is illustrated in Fig. 4 where Ginsberg's result has been (arbitrarily) normalized to agree with (14) at x = 0.6. One formula does quite well in correctly describing the high-energy electron spectrum shape. Because of strong-interaction uncertainties we do

$$\left(1 + \frac{2\alpha}{\pi} \ln[\frac{m_Z}{m_b}]\right)(1 + \alpha\pi) = 1.0375 \quad \rightarrow$$

 $+\frac{2\alpha}{\pi}\ln\frac{m_Z}{m_B}\left[\left(\frac{1-x}{2x/3}\right)^{(2\alpha/\pi)\left[\ln(m_B x/m_e)-1\right]}\right]$ (14)

not worry about the low-x regime.

Having used two examples to illustrate and test our scheme, we now tackle a practical problem, radiative corrections to inclusive semileptonic decays $B \rightarrow X_c e \bar{v}$ and $B \rightarrow X_u e \bar{v}$, where X_q represents an inclusive hadron state containing q. A precise knowledge of the electron spectrum shape, particularly near the end point, is important for extracting V_{ub}/V_{cb} and measuring semileptonic branching ratios. In our approach, the radiative corrections are approximated by the same correction factors as

Would lead to a reduction of $|V_{cb}|$ of ~1.1% from B^0 decays, but does not correspond to a fully consistent treatment at $\mathcal{O}(\alpha)$

Corrections on $|V_{ub}| \& |V_{cb}|$



Measurement used to constrain theory corrected for **QED effects**

Also don't correct for Coulomb enhancement

So bit of a "mess", although at least we are throughout consistent of course

- Theory usually assumes QED does not exist
- Measurements correct for FSR using PHOTOS; unfold into observables w/o QED effects With current precision a priori ok; but unclear if with future datasets of O(50/ab) this is still a good choice

FB, M. Schönherr arXiv:1010.5997 [hep-ph]

Used scalar QED to study semileptonic $B \to P \ell \bar{\nu}_{\ell}$ decays

$$\mathcal{L}_{\text{int,QED}} = -eQ_{\ell} \bar{\psi}_{\ell} \gamma^{\mu} \psi_{\ell} A_{\mu} - ieQ_{\phi} A_{\mu} (\phi^{+} \partial^{\mu} \phi^{-} - \phi^{-} \partial^{\mu} \phi^{+}) + e^{2}Q_{\phi}^{2} A_{\mu} A^{\mu} \phi^{+} \phi^{-}$$
$$+ ie\sqrt{2}G_{\text{F}} V_{xy} f_{\pm} (Q_{B} \pm Q_{X}) \phi_{B} \phi_{X} A_{\mu} \bar{\psi}_{\nu} P_{R} \gamma^{\mu} \psi_{\ell} + \text{h.c.} ,$$



- Several ad-hoc assumptions, e.g. incorporate FF dynamics ad-hoc for offshell states
- * Compare to **PHOTOS** and **PHOTONS++** YFS resummation improved prediction from Sherpa

We were young and did not know better...

The "backdrop"



The "backdrop"



The "backdrop"



	Electron sample						Muon sample						
item	$ ho_D^2$	$ ho_{D^*}^2$	$\mathcal{B}(D\ell\overline{\nu})$	$\mathcal{B}(D^*\ell\overline{\nu})$	$\mathcal{G}(1) V_{cb} $	$\mathcal{F}(1) V_{cb} $	ρ_D^2	$ ho_{D^*}^2$	$\mathcal{B}(D\ell\overline{\nu})$	$\mathcal{B}(D^*\ell\overline{\nu})$	$\mathcal{G}(1) V_{cb} $	$\mathcal{F}(1) V_{cb} $	
R'_1	0.44	2.74	0.71	-0.38	0.60	0.71	0.50	2.67	0.74	-0.40	0.63	0.70	
R'_2	-0.40	1.02	-0.18	0.30	-0.32	0.49	-0.45	0.96	-0.19	0.30	-0.33	0.48	
D^{**} slope	-1.42	-2.52	-0.07	-0.09	-0.82	-0.87	-1.42	-2.58	-0.10	-0.10	-0.77	-0.92	
D^{**} FF approximation	-0.87	0.33	-0.12	0.19	-0.54	0.20	-0.99	0.59	-0.12	0.21	-0.59	0.30	
$\mathcal{B}(B^- \to D^{(*)}\pi\ell\overline{\nu})$	0.28	-0.27	-0.22	-0.80	0.04	-0.49	0.59	-0.32	-0.13	-0.86	0.24	-0.54	
$f_{D_{2}^{*}/D_{1}}$	-0.39	0.16	-0.38	0.16	-0.41	0.13	-0.50	0.17	-0.41	0.18	-0.47	0.15	
$f_{D_0^*D\pi/D_1D_2^*}$	-2.30	1.12	-1.53	0.97	-2.07	0.85	-3.13	1.23	-1.53	1.02	-2.41	0.93	
$f_{D'_1D^*\pi/D_1D_2^*}$	1.82	-1.14	1.30	-0.65	1.65	-0.70	2.44	-1.15	1.35	-0.72	1.91	-0.75	
$f_{D\pi/D_0^*}$	-0.88	-1.28	0.36	0.17	-0.31	-0.34	-0.83	-1.23	0.31	0.18	-0.27	-0.33	
$f_{D^*\pi/D'_1}$	-0.21	-0.05	-0.13	0.21	-0.18	0.09	-0.30	-0.04	-0.15	0.23	-0.23	0.10	
NR D^*/D ratio	0.58	-0.16	0.11	-0.09	0.38	-0.04	0.66	-0.16	0.11	-0.09	0.40	-0.03	
$\mathcal{B}(B^- \to D^{(*)}\pi\pi\ell\overline{\nu})$	1.19	-1.97	0.25	-1.28	0.78	-1.28	1.98	-1.71	0.40	-1.20	1.20	-1.18	
X^*/X and Y^*/Y ratio	0.61	-1.15	0.09	-0.27	0.39	-0.52	0.74	-1.02	0.08	-0.24	0.42	-0.47	
X/Y and X^*/Y^* ratio	0.76	-0.83	0.21	-0.65	0.52	-0.60	1.09	-0.76	0.25	-0.63	0.68	-0.57	
$D_1 \rightarrow D\pi\pi$	2.22	-1.54	0.74	-1.08	1.63	-1.05	2.74	-1.48	0.76	-1.06	1.81	-1.03	
$f_{D_{2}^{*}}$	-0.14	-0.01	-0.10	0.07	-0.12	0.03	-0.16	-0.01	-0.10	0.07	-0.13	0.03	
$\mathcal{B}(\hat{D}^{*+} \to D^0 \pi^+)$	0.73	-0.01	0.43	-0.34	0.62	-0.17	0.80	-0.00	0.41	-0.33	0.61	-0.17	
$\mathcal{B}(D^0 \to K^- \pi^+)$	0.69	0.02	-0.21	-1.63	0.29	-0.80	0.92	0.12	-0.27	-1.68	0.35	-0.80	
$\mathcal{B}(D^+ \to K^- \pi^+ \pi^+)$	-1.46	-0.42	-2.17	0.30	-1.89	0.01	-1.43	-0.42	-2.10	0.28	-1.77	-0.01	
$ au_{B^-}/ au_{B^0}$	0.26	0.16	0.63	0.27	0.46	0.19	0.22	0.16	0.58	0.28	0.41	0.19	
f_{+-}/f_{00}	0.88	0.43	0.66	-0.53	0.82	-0.12	0.91	0.48	0.57	-0.52	0.75	-0.10	
Number of $B\overline{B}$ events	0.00	-0.00	-1.11	-1.11	-0.55	-0.55	0.00	-0.00	-1.11	-1.11	-0.55	-0.55	
Off-peak Luminosity	0.05	0.01	-0.02	-0.00	0.02	0.00	0.07	0.00	-0.02	-0.00	0.02	-0.00	
B momentum distrib.	-0.96	0.63	1.29	-0.54	-1.15	0.48	1.30	-0.10	1.27	-0.64	1.31	-0.35	
Lepton PID eff	0.52	0.16	1.21	0.82	0.90	0.46	3.30	0.06	5.11	5.83	1.99	2.90	
Lepton mis-ID	0.03	0.01	-0.01	-0.01	0.01	-0.00	2.65	0.70	-0.59	-0.50	1.06	-0.01	
Kaon PID	0.07	0.80	0.28	0.23	0.18	0.38	1.02	0.71	0.35	0.29	0.70	0.39	
Tracking eff	-1.02	-0.43	-3.35	-2.00	-2.25	-1.15	-0.63	-0.28	-3.37	-2.09	-2.02	-1.14	
Radiative corrections	-3.13	-1.04	-2.87	-0.74	-3.02	-0.71	-0.76	-0.61	-0.82	-0.25	-0.79	-0.33	
Bremsstrahlung	0.07	0.00	-0.13	-0.28	-0.04	-0.14	0.00	0.00	0.00	0.00	0.00	0.00	
Vertexing	0.83	-0.64	0.63	0.60	0.78	0.09	1.79	-0.76	0.97	0.54	1.41	0.01	
Background total	1.39	1.12	0.64	0.34	1.07	0.51	1.58	1.09	0.67	0.38	1.16	0.49	
Total	6.25	5.66	6.01	4.03	5.99	3.20	8.12	5.47	7.35	7.07	6.06	4.23	

Memory lane:

- I was a bit annoyed, that a QED effect should be one of the largest systematics.
 "Can't we just calculate this somehow? Why 20%? Why not 10% or 30%?"
- Teamed up with Marek Schönherr to develop a "NLO" model & benchmark against PHOTOS
- Heavily influenced what was done for Kaons by Troy Andre

• arXiv:hep-ph/0406006, AnnalsPhys.322:2518-2544,2007

- It builds on several assumptions: (some of them likely not entirely great or even justified for B mesons nor fully rigorous!)
 - First, we assumed we can split long-distance and short-distance physics



Matching on scale , $\Lambda \sim m_D$; used to regularize any UV divergencies in LD part

Short-distance parts: Sirlin

LARGE m_W , m_Z BEHAVIOUR OF THE O(α) CORRECTIONS TO SEMILEPTONIC PROCESSES MEDIATED BY W

A. SIRLIN¹

Department of Physics, New York University, 4 Washington Place, New York, NY 10003, USA

Received 17 August 1981

Using the current algebra formulation of radiative corrections and working in the framework of the $SU(2)_{L} \times U(1) \times SU(3)_{c}$ theory, we derive a theorem that governs the large m_{W} , m_{Z} behaviour of the $O(\alpha)$ corrections to general semileptonic processes mediated by W. The leading asymptotic dependence is logarithmic with a universal coefficient not affected by the strong interactions. As a byproduct, we obtain the leading asymptotic effect induced perturbatively by the strong interactions, which is of $O(\ln \ln (m_{W}/A))$.

The aim of this paper is to analyze the large m_W , m_Z behaviour of the O(α) corrections to semileptonic processes mediated by the W meson, in the framework of the SU(2)_L×U(1)×SU(3)_c theory.

Our main results are summarized in the following theorem:

(a) In the simplest version of the theory in which $\cos \theta_W = m_W/m_Z$ at the tree level, the leading asymptotic behaviour in m_Z of the O(α) corrections to an arbitrary semileptonic process mediated by W is given by

$$\frac{M}{M^0} = 1 + \frac{3\alpha}{4\pi} (1 + 2\bar{Q}) \ln \frac{m_2}{\mu} + \cdots, \qquad (1)$$

where M is the amplitude up to terms of $O(\alpha)$, M^0 is the zeroth-order amplitude but expressed in terms of the conventionally defined^{*} muon decay coupling constant G_{μ} , μ is an unspecified mass scale characteristic of the process, and \bar{Q} is the average charge of the quarks in a SU(2)_L isodoublet. Henceforth . . . indicates non-leading contributions as m_W^2 or $m_Z^2 \rightarrow \infty$. For the usual charge assignments, $\bar{Q} = \frac{1}{6}$. It is also





$$\mathcal{M}_{0,\mathrm{sd}}^1 = \frac{\alpha_{\mathrm{em}}}{\pi} \ln \frac{m_Z}{\Lambda} \mathcal{M}_0^0 + \dots$$

- [115] SIRLIN, A. : Current Algebra Formulation of Radiative Corrections in Gauge Theories and the Universality of the Weak Interactions. In: *Rev. Mod. Phys.* 50 (1978), S. 573. http://dx.doi.org/10.1103/RevModPhys.50.573. - DOI 10.1103/RevModPhys.50.573
- [116] SIRLIN, A. : Large m(W), m(Z) Behavior of the O(alpha) Corrections to Semileptonic Processes Mediated by W. In: Nucl. Phys. B196 (1982), S. 83. http://dx.doi.org/10. 1016/0550-3213(82)90303-0. - DOI 10.1016/0550-3213(82)90303-0

Long-Distance

Long-distance part: Scalar QED with some ad-hoc QCD evolution

$$\mathcal{L}_{W} = \frac{G_{F}}{\sqrt{2}} V_{cb} \left[(f_{+} + f_{-}) \phi' \partial^{\mu} \phi + (f_{+} - f_{-}) \phi \partial^{\mu} \phi' \right] \bar{\psi}_{\nu} P_{R} \gamma_{\mu} \psi_{\ell} + h.c.,$$



Long-distance part: Scalar QED with some ad-hoc QCD evolution

$$\mathcal{L}_{\mathrm{W}} = \frac{G_{\mathrm{F}}}{\sqrt{2}} V_{\mathrm{cb}} \left[(f_{+} + f_{-}) \phi' \partial^{\mu} \phi + (f_{+} - f_{-}) \phi \partial^{\mu} \phi' \right] \bar{\psi}_{\nu} P_{\mathrm{R}} \gamma_{\mu} \psi_{\ell} + \mathrm{h.c.},$$

• Assumed that the off-shell hadronic current can be modeled using the on-shell current; in particular that the form factors depend on $\mathbf{t} = \mathbf{q}^2$ only

$$\begin{split} \langle D(p') | \widehat{V}_{\mu} - \widehat{A}_{\mu} | B(p-k) \rangle &= \widehat{f}_{+}(t',r',s') (p-k+p')_{\mu} + \widehat{f}_{-}(t',r',s') (p-k-p')_{\mu}, \\ t' &= (p-p'-k)^{2} \\ r', s': \text{ other lorentz scalars} \\ \\ H'_{\mu}(t') &= \langle D(p') | \widehat{V}_{\mu} - \widehat{A}_{\mu} | B(p-k) \rangle &= f_{+}(t') (p-k+p')_{\mu} + f_{-}(t') (p-k-p')_{\mu}, \end{split}$$

• More formal: coupling an electromagnetic current to LO decay results in

$$\begin{aligned} & \text{lepton leg coupling} \quad \text{hadronic coupling} \\ & i \, e \, \frac{G_{\rm F}}{\sqrt{2}} \, V_{\rm cb} \, \bar{u}_{\nu} \, \gamma^{\mu} \, P_{\rm L} \, \left(-\frac{H_{\mu}}{2p_{\ell} \cdot k} \left(\gamma_{\nu} \not{k} + 2(p_{\ell})_{\nu} \right) + V_{\mu\nu} - A_{\mu\nu} \right) \, v_{l} \,, \end{aligned} \qquad \begin{array}{l} \text{hadronic current} \\ & H_{\mu}(t) \quad = \quad \langle D(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B(p) \rangle \\ \end{array} \end{aligned}$$

with a non-local operator describing the B-y and D-y coupling

$$V_{\mu\nu} - A_{\mu\nu} = \int \mathrm{d}^4 x \, e^{ik \cdot x} \langle D | \mathcal{T}\{h_\mu(0) \, J_\nu^{\mathrm{em}}(x)\} | B \rangle \,,$$

which can be expanded around first few resonant states

$$V_{\mu\nu} - A_{\mu\nu} = \frac{\langle D(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B(p-k) \rangle \langle B(p-k) | J_{\nu}^{\text{em}} | B(p) \rangle}{m_B^2 - (p-k)^2} + \frac{\langle D(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B^*(p-k) \rangle \langle B^*(p-k) | J_{\nu}^{\text{em}} | B(p) \rangle}{m_{B^*}^2 - (p-k)^2} + \frac{\langle D(p'-k) | J_{\nu}^{\text{em}} | D^*(p') \rangle \langle D^*(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B(p) \rangle}{m_{D^*}^2 - (p'-k)^2} + \dots,$$

See also D. Becirevic, N. Kosnik arXiv:0910.5031 [hep-ph]

Ward identities

$$\begin{array}{rcl}
k^{\nu} V_{\mu\nu} &=& H_{\mu} ,\\
k^{\nu} A_{\mu\nu} &=& 0 ,
\end{array}$$

• More formal: coupling an electromagnetic current to LO decay results in

$$\begin{array}{ll} \begin{array}{c} \text{lepton leg coupling} & \text{hadronic coupling} \\ \hline i \, e \, \frac{G_{\rm F}}{\sqrt{2}} \, V_{\rm cb} \, \bar{u}_{\nu} \, \gamma^{\mu} \, P_{\rm L} \, \left(-\frac{H_{\mu}}{2p_{\ell} \cdot k} \left(\gamma_{\nu} \not k + 2(p_{\ell})_{\nu} \right) + V_{\mu\nu} - A_{\mu\nu} \right) \, v_{l} \,, \end{array} \qquad \begin{array}{l} \begin{array}{c} \text{hadronic current} \\ H_{\mu}(t) & = & \langle D(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B(p) \rangle \end{array}$$

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Ward identities

$$k^{\nu} V_{\mu\nu} = H_{\mu}, k^{\nu} A_{\mu\nu} = 0,$$

which can be expanded around first few resonant states

$$V_{\mu\nu} - A_{\mu\nu} = \frac{\langle D(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B(p-k) \rangle \langle B(p-k) | J_{\nu}^{\text{em}} | B(p) \rangle}{m_{B}^{2} - (p-k)^{2}} \longrightarrow \boxed{k^{\nu} V_{\mu\nu} = H_{\mu}'(t') \frac{k \cdot (2p-k)}{2p \cdot k} + \dots} + \frac{\langle D(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B^{*}(p-k) \rangle \langle B^{*}(p-k) | J_{\nu}^{\text{em}} | B(p) \rangle}{m_{B^{*}}^{2} - (p-k)^{2}} \xrightarrow{\langle B(p-k) | J_{\nu}^{\text{em}} | B(p) \rangle} = \underbrace{(2p-k)_{\nu}}_{m_{D^{*}}} F_{\text{em}}, + \frac{\langle D(p'-k) | J_{\nu}^{\text{em}} | D^{*}(p') \rangle \langle D^{*}(p') | \hat{V}_{\mu} - \hat{A}_{\mu} | B(p) \rangle}{m_{D^{*}}^{2} - (p'-k)^{2}} + \dots, \qquad F_{\text{em}} \approx 1$$
in soft photon limit

$$k^{\nu} V_{\mu\nu} = H'_{\mu}(t') \frac{k \cdot (2p-k)}{2p \cdot k} + \dots$$

• For the hadronic current: Taylor expand

$$k^{\nu} V_{\mu\nu} = H_{\mu}(t) + k' \frac{\mathrm{d}H'_{\mu}}{\mathrm{d}t'}\Big|_{k'=0} + k'^2 \frac{\mathrm{d}^2 H'_{\mu}}{\mathrm{d}t'^2}\Big|_{k'=0} + \dots,$$

and neglect all higher order terms, plus introduce seagull terms to make sure matrix element fulfills the Ward identity / is gauge invariant:

- 1. The non-local operator Eq. (3.4) was expanded in a number of matrix elements which correspond to intermediate resonances allowed in the soft photon part of phase-space.
- 2. The off-shell hadronic current was approximated by the on-shell hadronic current.
- 3. The higher order terms of Eq. (3.13) which are ambiguous and depend on the parametrization of the on-shell matrix element were neglected.
- 4. No intermediate excited resonances were considered.
- Certainly not a bad set of approximations in the soft-photon limit, unclear how well this describes nature if one really wants achieve precision

More problems:

- Form factors enter into all of the calculations
 - All of them are measured by "factoring out QED"
 - E.g. tagged measurements simply use q² as calculated from hadronic systems

$$q^{2} = \left(p_{B} - p_{D}\right)^{2} = \left(p_{\ell} + p_{\nu} + \sum_{i} k_{i}\right)^{2}$$

 Even untagged measurements factorize QED effects out, i.e. change the shape of the templates are calculated using "true" q² values as defined w/o QED corrections

Shape differences due to inadequate QED modelling are just absorbed into form factor parameters.

Thus any theory based prediction you make on how fundamental parameters change based on kinematic changes, will likely not be valid.

• We regularized the UV poles using Pauli-Villars, made it easy to match to Sirlin's quark-level calculation

$$\mathcal{L}_{\mathrm{PV}} = \left[\frac{1}{4} \tilde{F}^2 + \Lambda^2 \tilde{A}^2 , \xrightarrow{\text{e.g.}} B_0(m_\ell^2, m_\ell^2, \lambda^2) \rightarrow B_0(m_\ell^2; m_\ell^2, \lambda^2) - B_0(m_l^2; m_\ell^2, \Lambda^2) , \\ \dot{B}_i(m_\ell^2, m_\ell^2, \lambda^2) \rightarrow \dot{B}_i(m_\ell^2, m_\ell^2, \lambda^2) - \dot{B}_i(m_\ell^2, m_\ell^2, \Lambda^2) , \\ \text{plus sign instead of } - \right]$$

• After that we also determined the total rate via

 And we produced NLO events using the corresponding matrix elements and mixed them according to these integrals We also calculated corrections to Sirlin's correction using

Sirlin's correction

revised EW correction

$$\Gamma_0^0 + \Gamma_0^1 + \Gamma_1^1 = (1 + \delta_{\rm sd} + \delta_{\rm ld}) \,\Gamma_0^0 = \eta_{\rm EW}^2 \,\Gamma_0^0 \,,$$

My new long-distance correction

$$\begin{split} B^0 &\to D^- \, e^+ \, \bar{\nu}_e(\gamma) & B^+ \to \bar{D}^0 \, e^+ \, \bar{\nu}_e(\gamma) \\ \eta^2_{\rm EW} &= 1.0235 \pm 0.0002_{\rm stat} \pm 0.0023_{\rm theo} \,, \qquad \eta^2_{\rm EW} &= 1.0147 \pm 0.0001_{\rm stat} \pm 0.0045_{\rm theo} \,, \\ B^0 &\to D^- \, \mu^+ \, \bar{\nu}_\mu(\gamma) & B^+ \to \bar{D}^0 \, \mu^+ \, \bar{\nu}_\mu(\gamma) \\ \eta^2_{\rm EW} &= 1.0237 \pm 0.0001_{\rm stat} \pm 0.0020_{\rm theo} \,, \qquad \eta^2_{\rm EW} &= 1.0150 \pm 0.0001_{\rm stat} \pm 0.0045_{\rm theo} \,, \end{split}$$

Sirlin's correction: $\eta_{EW}^2 = 1.014$

• Theory errors: Variation of the matching scale

Example: $B^0 \rightarrow D^- e^+ \nu_e$



Example: $B^0 \rightarrow D^- e^+ \nu_e$



- * Fair agreement between PHOTOS & NLO; YFS enhanced simulation radiates more high-energy photons
- * If truncated at $\mathcal{O}(\alpha)$ or $\mathcal{O}(\alpha^2)$ good agreement

Revised Systematics:

	ρ_D^2	$\rho_{D^*}^2$	$\mathcal{B}(D^0 l \nu_l)$	$\mathcal{B}(D^{*0} l \nu_l)$				Elec	tron samp	ole	
$B'_{1}(1)$	$\frac{7D}{1248}$	3 046	0.841	-0.253	item	$ ho_D^2$	$ ho_{D^*}^2$	$\mathcal{B}(D\ell\overline{\nu})$	$\mathcal{B}(D^*\ell\overline{\nu})$	$\mathcal{G}(1) V_{cb} $	$\mathcal{F}(1) V_{cb} $
$B'_{2}(1)$	1.210 1.351	-1.343	0.550	-0.481	R'_1	0.44	2.74	0.71	-0.38	0.60	0.71
$f_{\rm D}$ (D	-0.206	0.051	-0.153	0.101	R'_2	-0.40	1.02	-0.18	0.30	-0.32	0.49
JD_2/D_1	-0.637	-0.641	0.165	0.031	D^{**} slope	-1.42	-2.52	-0.07	-0.09	-0.82	-0.87
$J \mathcal{A}_1 / D_0$ f	0.001	0.041	0.100	0.071	D^{**} FF approximation	-0.87	0.33	-0.12	0.19	-0.54	0.20
$J_{\mathcal{A}_2/D'_1}$	-0.224	-0.103	-0.134	0.240	$\mathcal{B}(B^- \to D^{(*)}\pi\ell\overline{\nu})$	0.28	-0.27	-0.22	-0.80	0.04	-0.49
$\int D_0 \mathcal{A}_1 / D_1 D_2$	-1.199	0.430	-0.370	0.527	$f_{D_{2}^{*}/D_{1}}$	-0.39	0.16	-0.38	0.16	-0.41	0.13
$JD_1'\mathcal{A}_2/D_1D_2$	0.372	-0.284	0.335	-0.109	$f_{D_{2}^{*}D\pi/D_{1}D_{2}^{*}}$	-2.30	1.12	-1.53	0.97	-2.07	0.85
$f_{\pm 0}$	1.334	0.444	0.786	-0.529	$f_{D',D^*\pi/D_1D^*}$	1.82	-1.14	1.30	-0.65	1.65	-0.70
$ au_{+0}$	0.253	0.108	0.438	0.176	$f_{D\pi/D^*}$	-0.88	-1.28	0.36	0.17	-0.31	-0.34
f_{D_2}	-0.089	-0.004	-0.048	0.027	$f_{D^*\pi/D'}$	-0.21	-0.05	-0.13	0.21	-0.18	0.09
$\mathcal{B}(B^+ \to D^{(*)} \pi l \nu_l)$	0.490	-0.350	-0.130	-0.736	NR D^*/D ratio	0.58	-0.16	0.11	-0.09	0.38	-0.04
$\mathcal{B}(D^0 \to K^+ \pi^-)$	1.032	0.026	-0.138	-1.612	$\mathcal{B}(B^- \to D^{(*)}\pi\pi\ell\overline{\mu})$	1 19	-1.97	0.11	-1.28	0.58	-1.28
$\mathcal{B}(D^+ \to K^+ \pi^- \pi^+)$	-1.932	-0.361	-1.966	0.253	X^*/X and Y^*/Y ratio	0.61	-1.57	0.20	-0.27	0.10	-0.52
$\mathcal{B}(D^{*+} \to D^0 \pi^+)'$	1.116	-0.019	0.464	-0.314	X/Y and X^*/Y^* ratio	0.01	-0.83	0.05	-0.65	0.55 0.52	-0.60
$\mathcal{B}(D^{*+} \to D^+ \pi^0)'$	0.508	-0.008	0.212	-0.143	$D_1 \rightarrow D\pi\pi$	2.22	-1.54	0.21 0.74	-1.08	1 63	-1.05
Tracking	-0.371	-0.157	-1.000	-0.732	f_{D^*}	-0.14	-0.01	-0.10	0.07	-0.12	0.03
Vertexing				0.698	$\mathcal{B}(D^{*+} \rightarrow D^0 \pi^+)$	0.73	-0.01	0.10	-0.34	0.12	-0.17
Lepton mis-ID	∣ ⊢r	om a	Iπeren	Ce 0.010	$\mathcal{B}(D^0 \to K^- \pi^+)$	0.10	0.01	-0.40	-1.63	0.02	-0.80
Lepton PID		of DI		1.469	$\mathcal{B}(D^+ \rightarrow K^- \pi^+ \pi^+)$	-1.46	-0.02	-2.17	0.30	-1.80	0.00
Kaon PID	_		10103	0.065	$\mathcal{D}(\mathcal{D} \to \mathcal{H} \times \mathcal{H})$	0.26	0.42	0.63	0.30 0.27	0.46	0.01
Bremsstrahlung	- 2 ()ur C	alculat	bion 0.290	f_{B} / f_{B0}	0.20	0.10	0.05	-0.53	0.40	-0.12
D^{**} Slope				0.189	Number of $B\overline{B}$ events	0.00	-0.00	_1 11	_1 11	-0.55	-0.55
D^{**} FF approximation	0.920	-0.511	0.145	-0.195	Off-peak Luminosity	0.00	0.00	-0.02	-0.00	0.00	0.00
Number of $B\bar{B}$ events	-0.123	-0.100	-0.670	-0.669	B momentum distrib	-0.00	0.01	1 29	-0.54	-1.15	0.00
Off-resonance luminosity	0.059	0.003	-0.019	-0.003	Lepton PID eff	0.50 0.52	0.00	1.25	0.81	0.90	0.10
Radiative corrections for $B \to D l \nu_l$	-0.126	-0.056	−0.289	0.045	Lepton mis-ID	0.02	0.10	-0.01	-0.01	0.00	-0.00
Radiative corrections for $B \to D^* l \nu_l$	1.657	0.056	0.574	1.187	Kaon PID	0.07	0.80	0.28	0.23	0.18	0.38
Radiative corrections for $B \to D^{**} l \nu_l$	-0.023	0.072	0.111	0.298	Tracking eff	-1.02	-0.43	-3.35	-2.00	-2.25	-1.15
Correction to off-resonance	-1.057	0.155	-0.236	0.064	Radiative corrections	-3.13	-1.04	-2.87	-0.74	-3.02	-0.71
$D^{**}(2S) \rightarrow D^{(*)}\pi$ contributions	-0.463	-0.998	-0.184	-0.374	Bremsstrahlung	0.07	0.00	-0.13	-0.28	-0.04	-0.14
$B \rightarrow D^{(*)} \pi \pi l \nu_l$ contributions	0.876	0.364	0.245	0.445	Vertexing	0.83	-0.64	0.63	0.60	0.78	0.09
Further background	0.595	0.699	0.354	0.099	Background total	1.39	1.12	0.64	0.34	1.07	0.51
Total	4.856	4.515	3.318	3.124	Total	6.25	5.66	6.01	4.03	5.99	3.20

Talk Outline



Another slow moving system



But there is one final state, for which this is not true: τ has $\beta \approx 0.5 - 0.75$

Coulomb Correction scales as

$$\Omega_{\rm C} = \frac{2\pi\alpha}{\beta_{D\ell}} \frac{1}{1 - e^{-\frac{2\pi\alpha}{\beta_{D\ell}}}},$$
$$\beta_{D\ell} = \left[1 - \frac{4m_D^2 m_\ell^2}{(s_{D\ell} - m_D^2 - m_\ell^2)^2}\right]^{1/2}$$

Changes kinematic distributions, breaks isospin

Second concern: τ and ℓ radiate differently





018)

018)

Let's be more precise:

Of course experiments simulate this with PHOTOS (and there are additional FSR photons from the τ decay)

Problems could arise if real QED effects would differ between PHOTOS and e.g. full NLO rate

You can make this fairly dramatic looking by defining a cut-off $E_{\rm max}$, which defines the maximal value of the photon energy that we would identify $B \to D\ell \bar{\nu}_{\ell} \gamma$ still as signal





Very interesting point; but in measurements variables like E_{max} are not so well defined

One variable that is **similar** is E_{extra} : **Unassigned neutral energy** in ECL



In fact so similar, that it's impossible to separate both processes with $E_{\rm extra}$

Why similar? 1) more FSR when τ decays

2) Brem, Beam Backgrounds, not reconstructed π^0 or photons in the event

Ok, back to the first concern

Typical extraction variables for $R(D^{(*)})$: $q^2 = (p_B - p_{D^*})^2$; $M_{\text{miss}}^2 = (p_B - p_{D^*} - p_{\ell})^2$; E_u



Coulomb correction factor:





One can also put both effects together:



As the paper writes, this is somehow a worst case scenario, not a realistic assessment what the actual bias could be (as it is the difference to PHOTOS that drives any efficiency differences) **Experimental effects** broaden the experimental equivalent of $E_{\rm max}$ considerably

Reduction from [0,50 MeV] wildly different





Summary

Florian Bernlochner QED in Weak Decays Workshop - Edinburgh 2022-

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Summary

I am personally excited about the renewed attention that QED effects are getting!

We are stepping into an exciting era with

- Precision measurements of $B_{s,d} \rightarrow \mu \mu(\gamma)$ at the LHC
- Exciting prospects of $B \to \ell \nu \gamma$ and $B \to \ell \nu \gamma^* [\to \ell \ell]$ at Belle II & LHCb
- Belle II will discover $B \rightarrow \mu \nu$, how to deal with $B \rightarrow \mu \nu \gamma$ interesting question

- QED effects for $H_b\to H_{u,c}\ell\bar\nu_\ell(\gamma)$ will become more and more for $\|V_{qb}\|$ determinations

Many thanks to Roman and all the organizers for bringing us all together here!



