Gravitational Waves, Numerical Relativity, and measuring Black Holes

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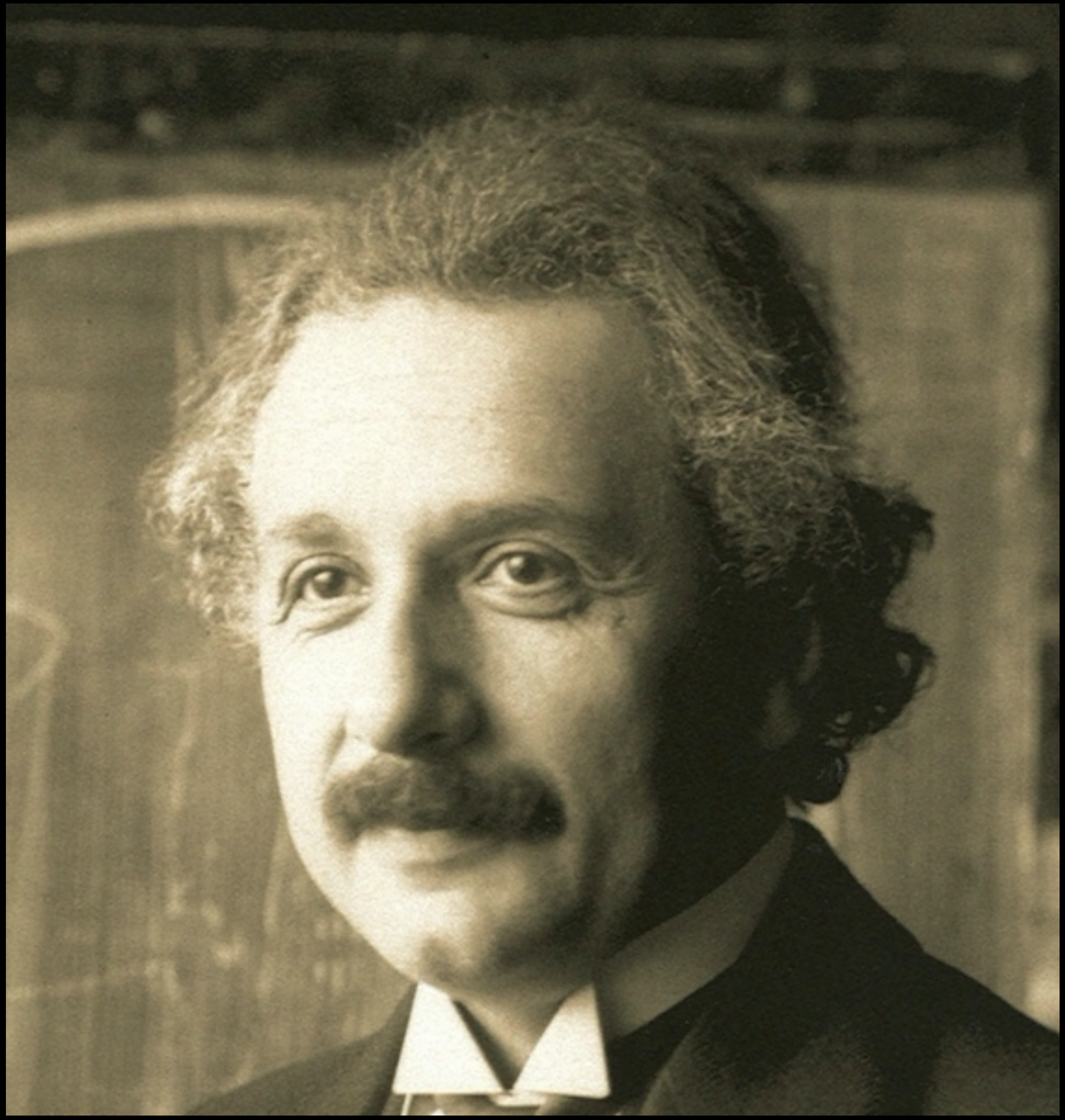
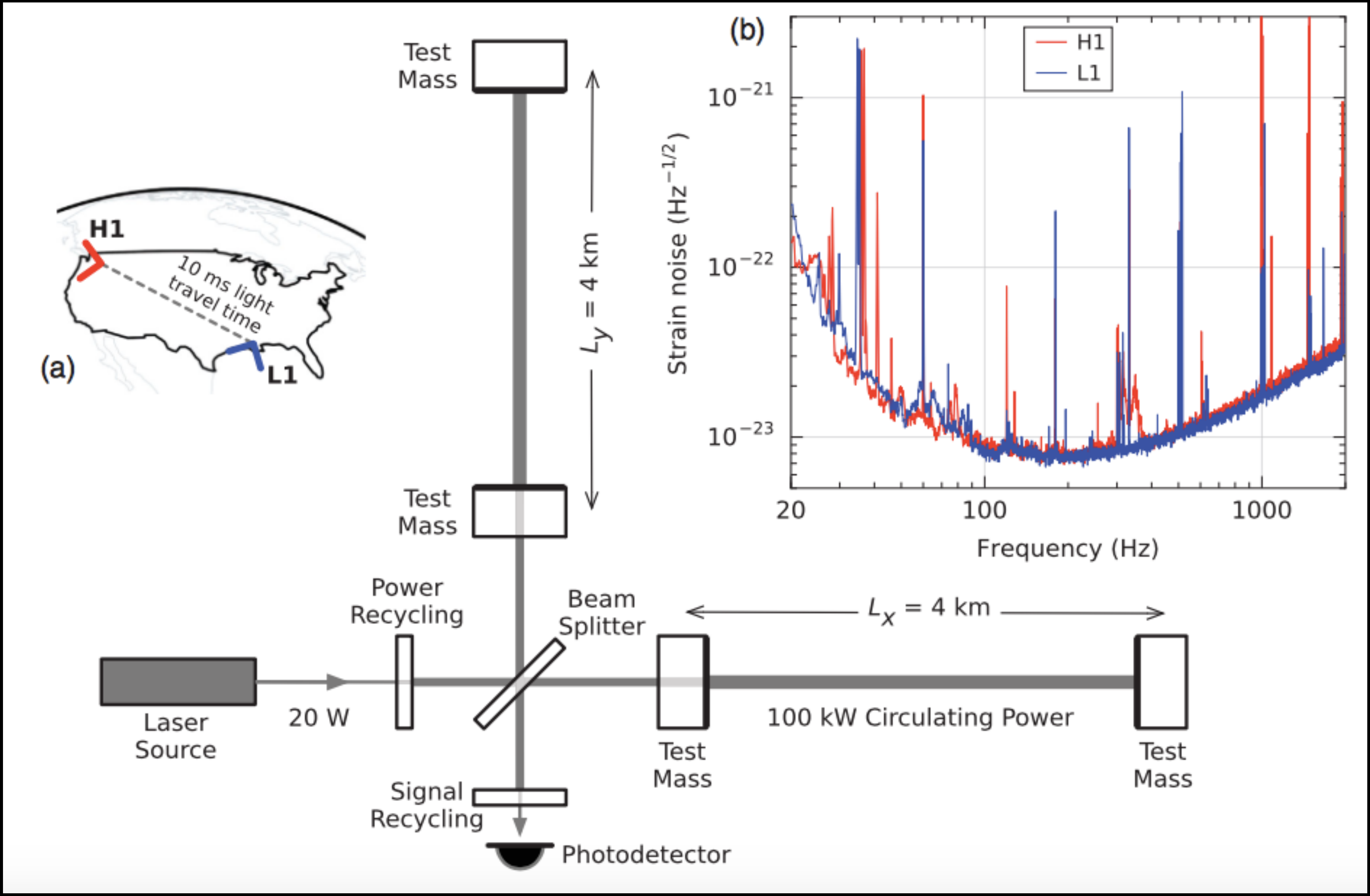
Cardiff University

DiRAC Day
Edinburgh, September 8, 2016

February 11, 2016



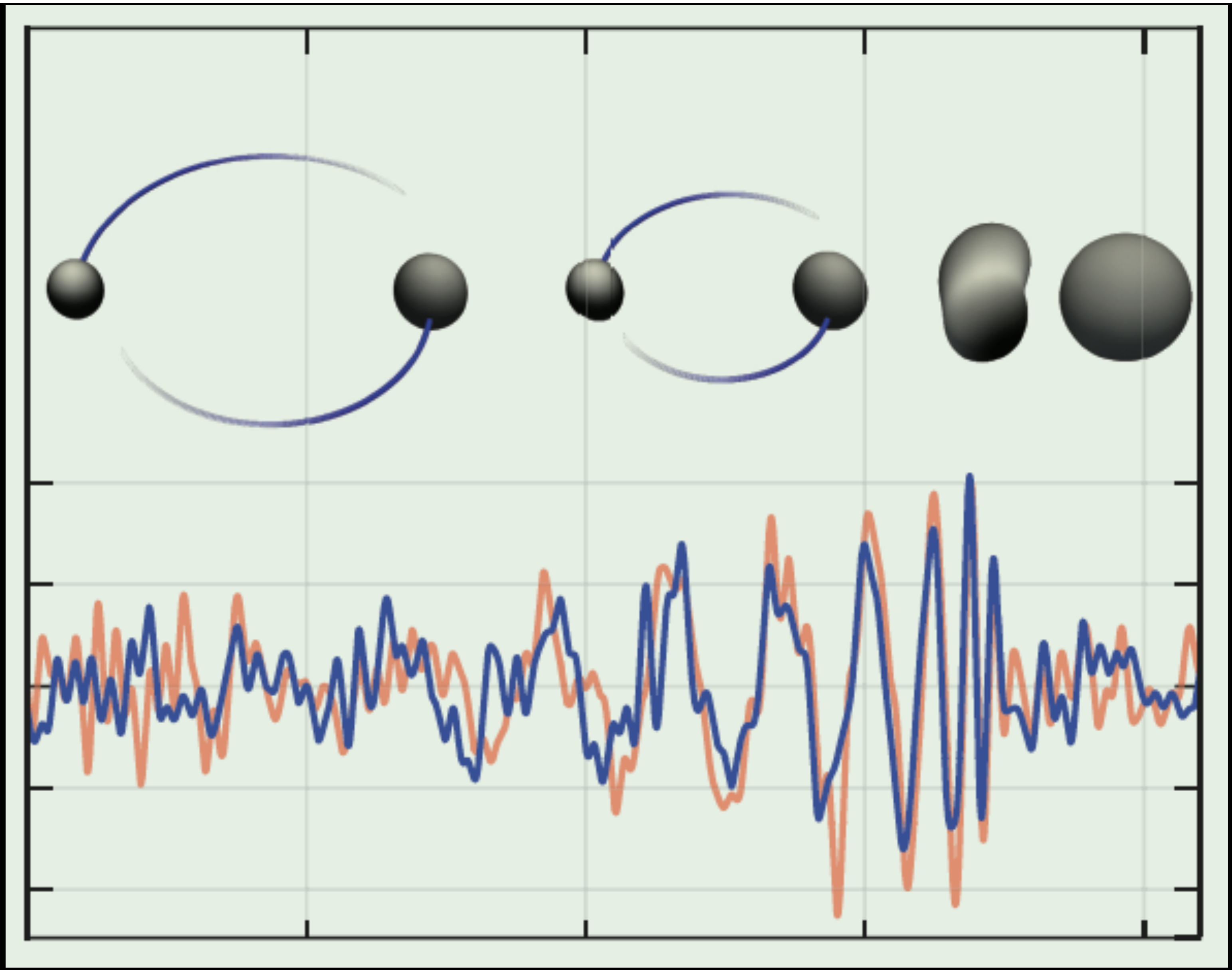


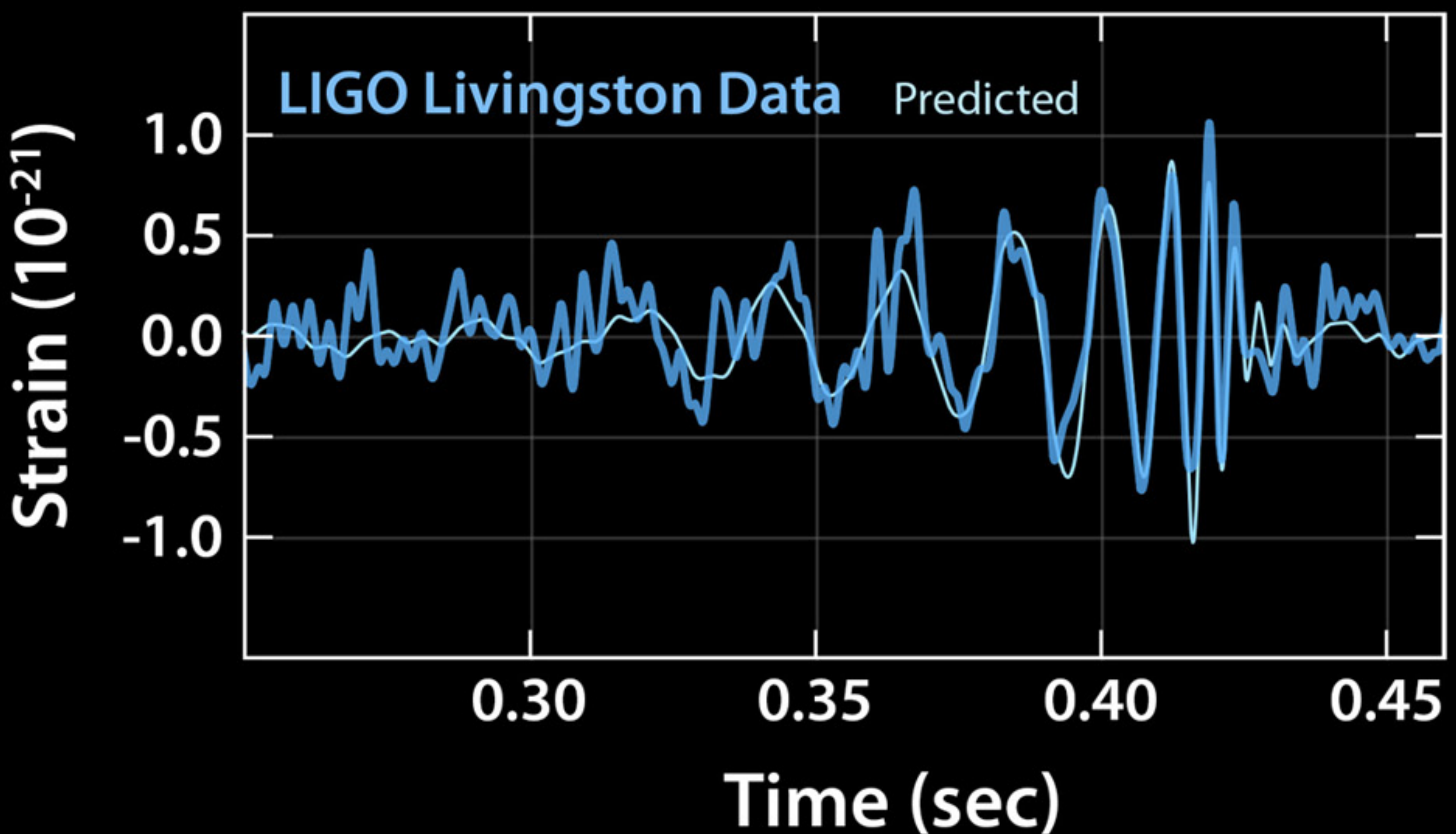
(a)
H1
L1
10 ms light travel time
(b)
H1
L1
Strain noise (Hz$^{-1/2}$)
10^{-21}
10^{-22}
10^{-23}
20
100
1000
Frequency (Hz)
Test Mass
Test Mass
L_y = 4 km
Laser Source
20 W
Power Recycling
Beam Splitter
L_x = 4 km
Test Mass
Test Mass
100 kW Circulating Power
Signal Recycling
Photodetector

Selected for a Viewpoint in *Physics*
PRL **116,** 061102 (2016) PHYSICAL REVIEW LETTERS week ending 12 FEBRUARY 2016

Observation of Gravitational Waves from a Binary Black Hole Merger

B. P. Abbott *et al.*[*]
(LIGO Scientific Collaboration and Virgo Collaboration)
(Received 21 January 2016; published 11 February 2016)



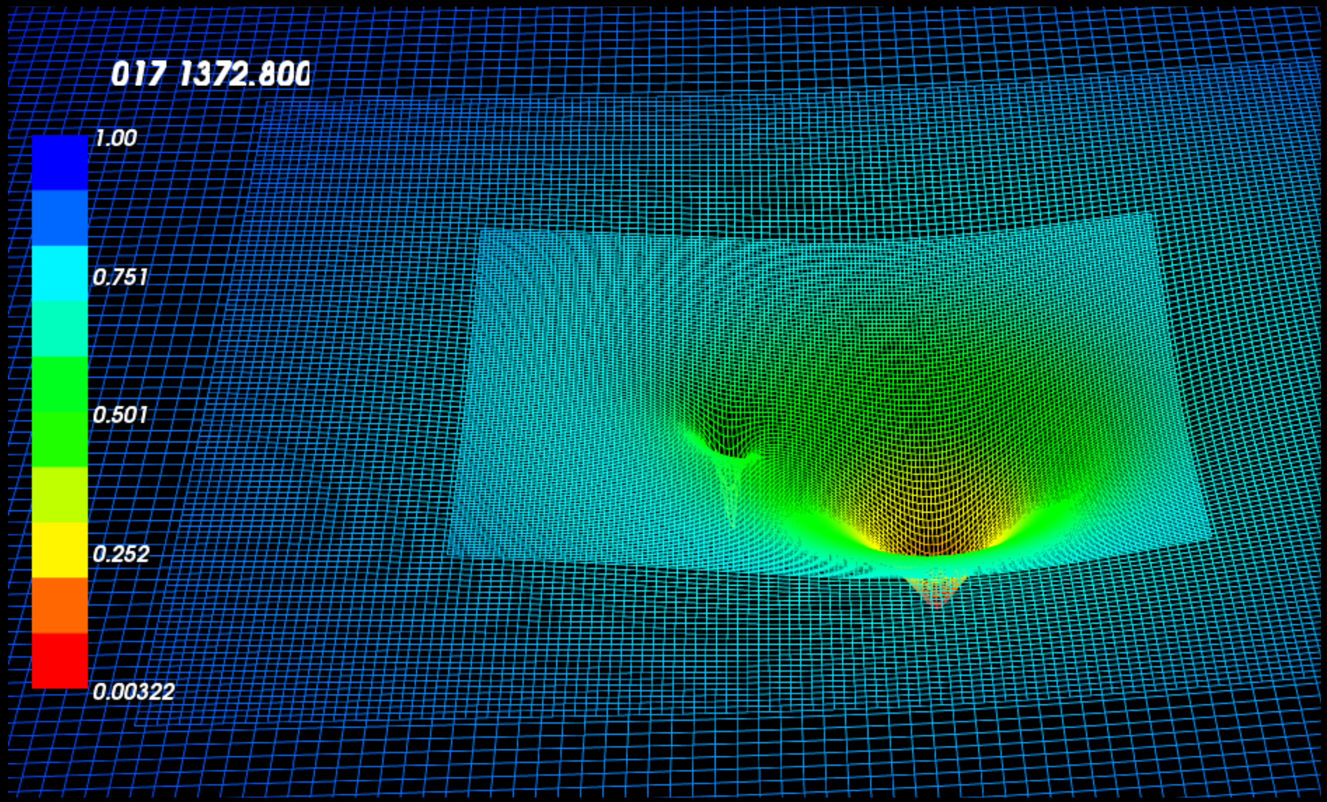


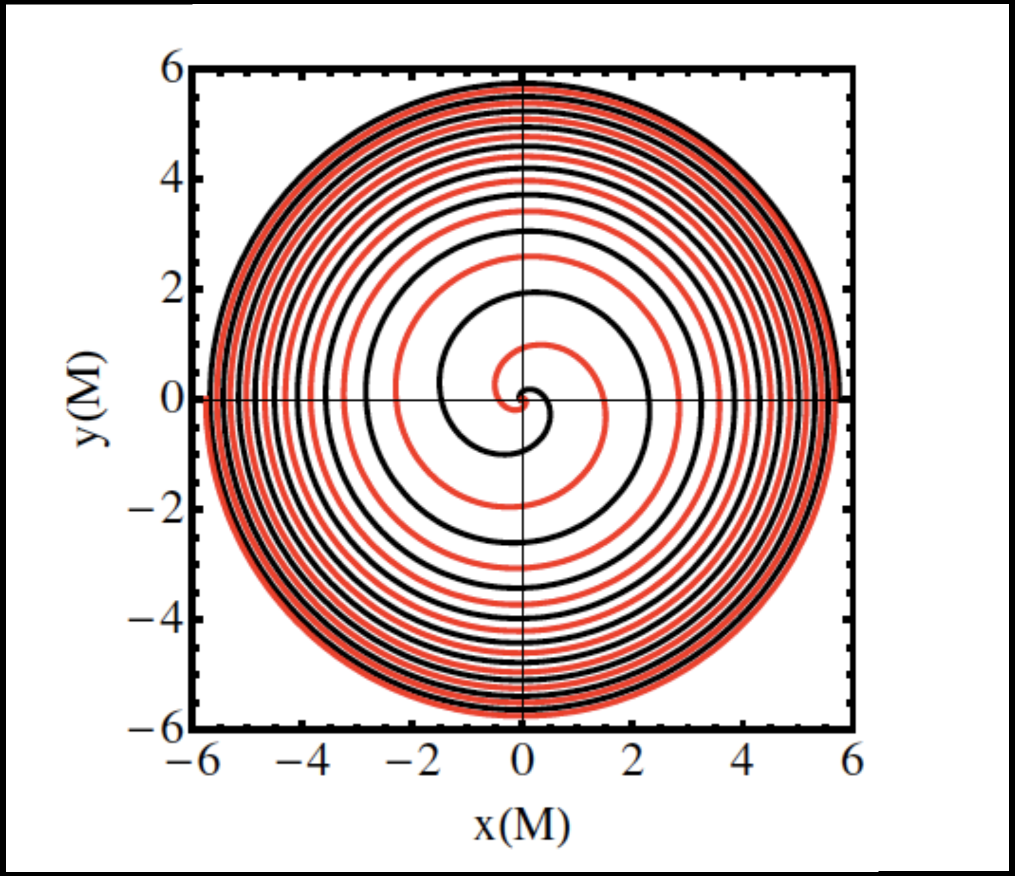
LIGO Livingston Data
Predicted
Strain (10-21)
1.0
0.5
0.0
-0.5
-1.0
0.30
0.35
0.40
0.45
Time (sec)

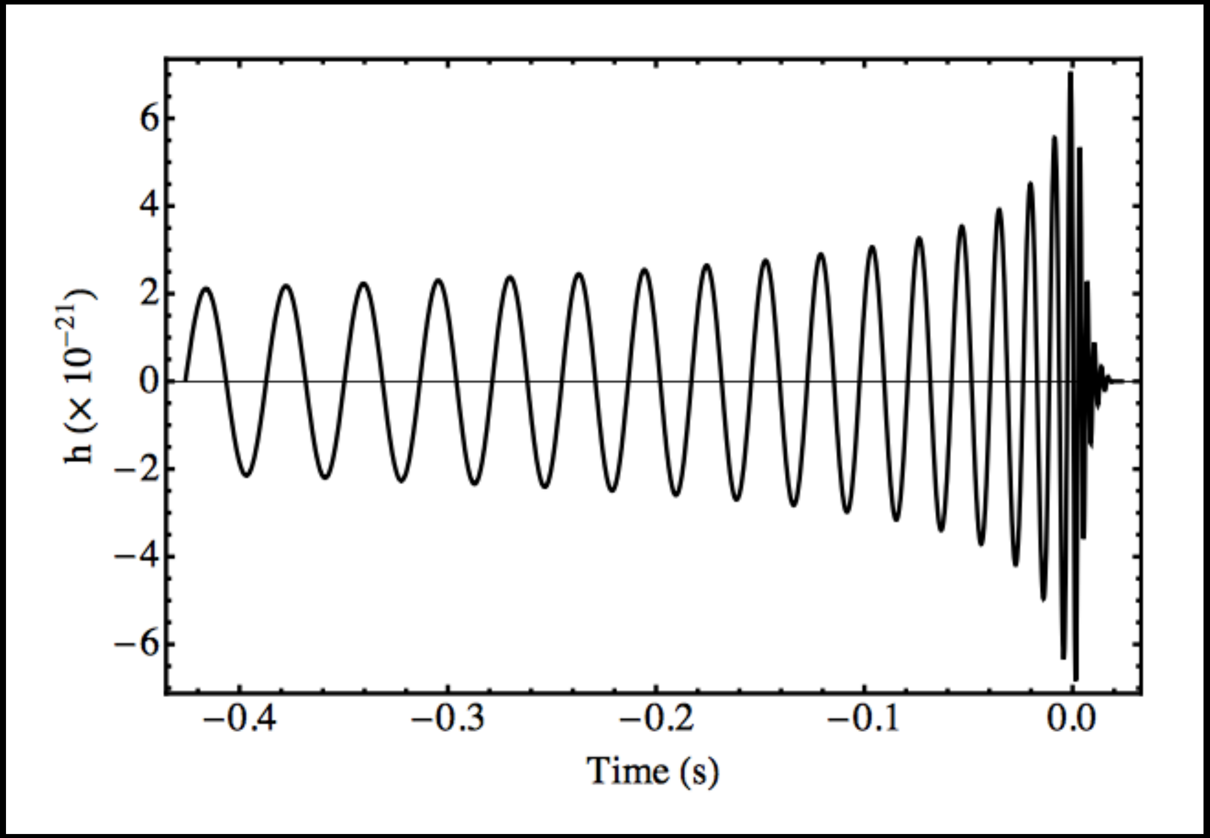
Numerical relativity

numerically solve
full Einstein equations
on 3D (mesh-refined) grids

Requires weeks to months
on 100s of cores.







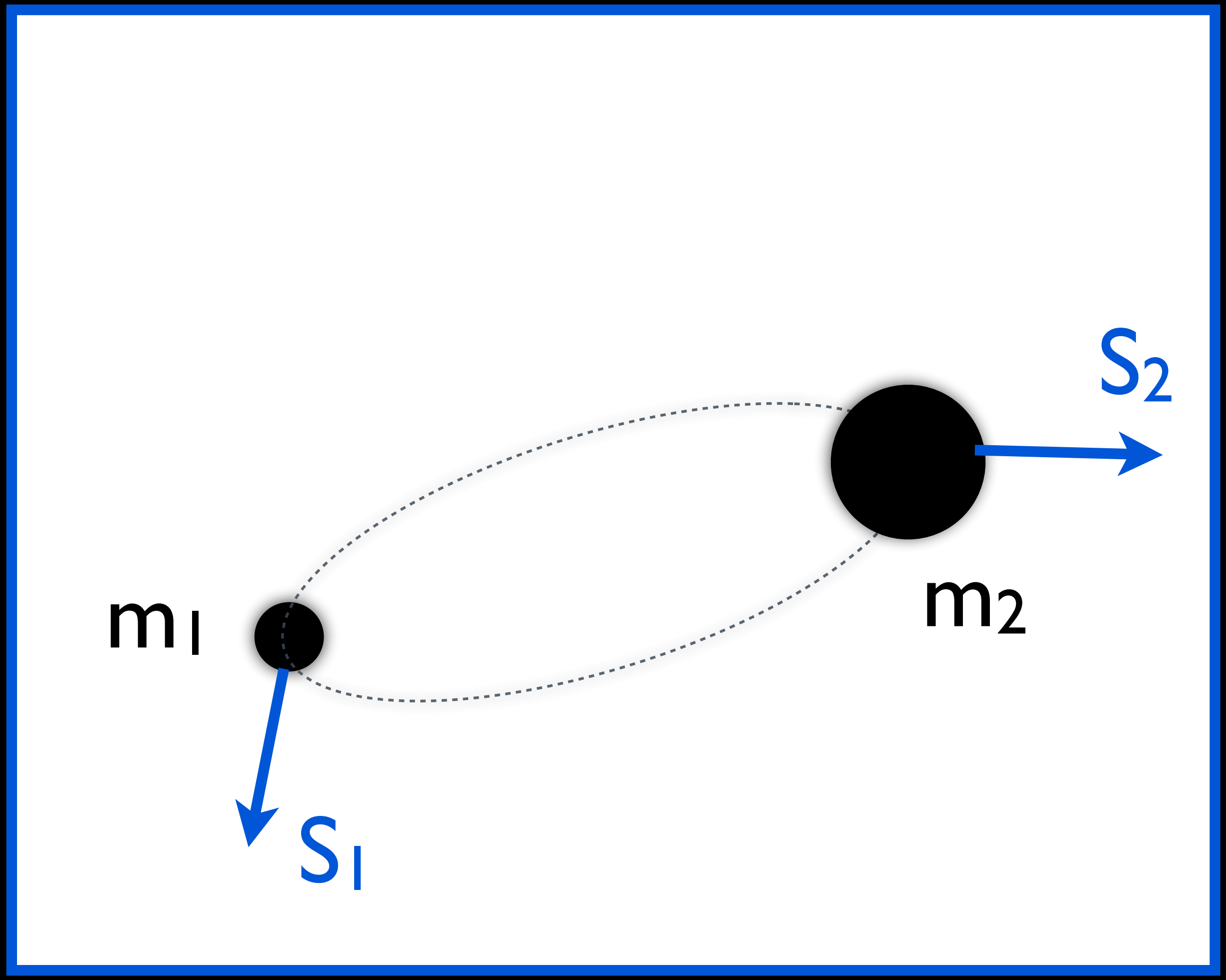
Masses: m_1, m_2

Spins: $\mathbf{S}_1, \mathbf{S}_2$

(8 parameters)

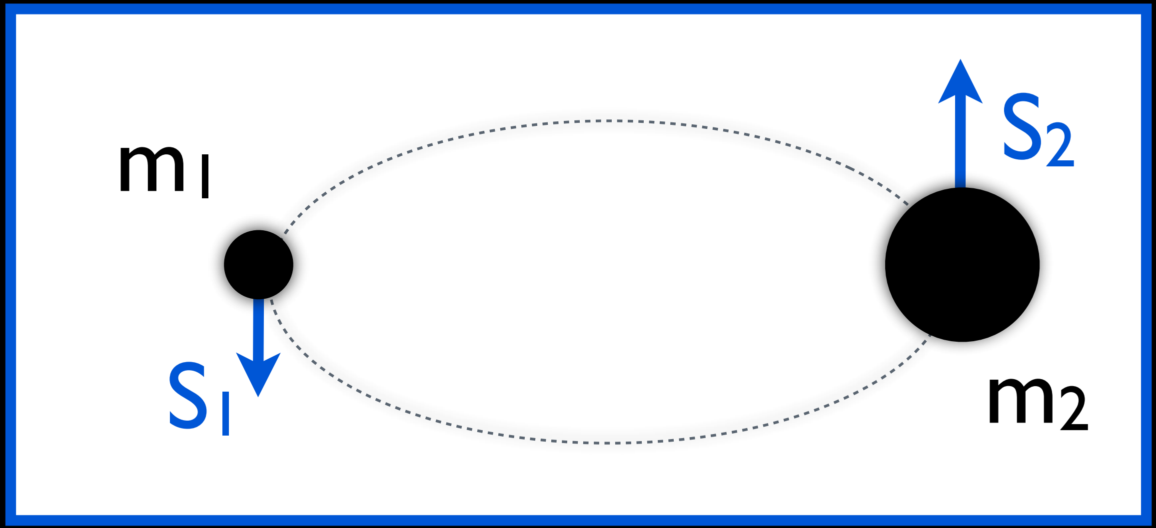
useful combinations:

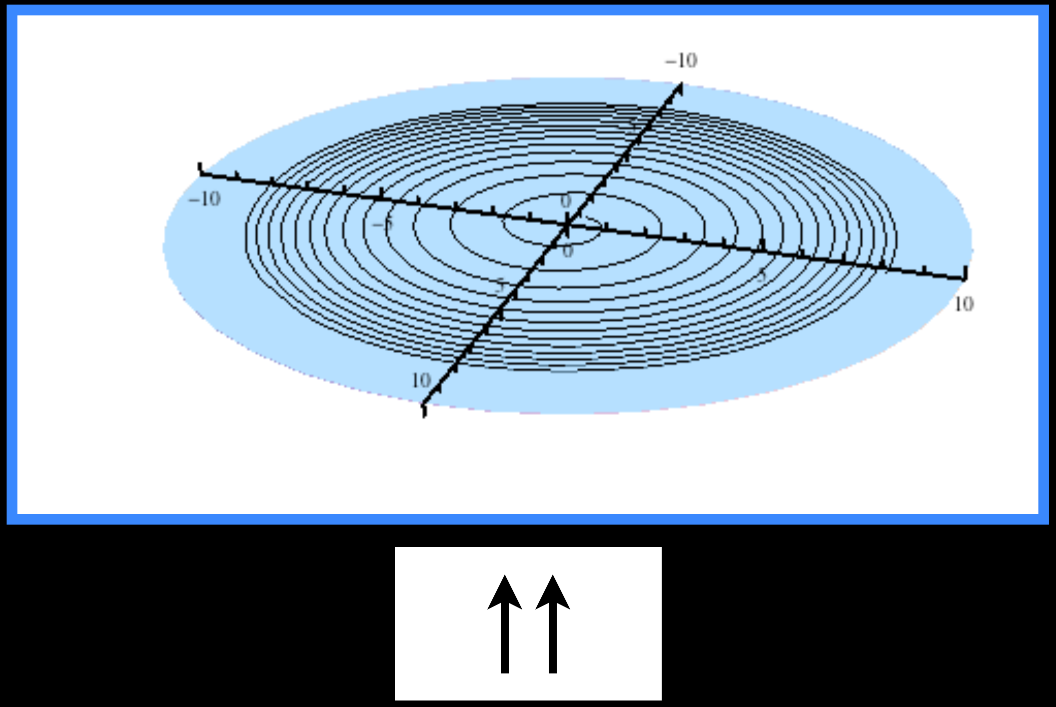
$$M = m_1 + m_2$$
$$q = m_2 / m_1$$
$$\eta = m_1 m_2 / M^2$$
$$\chi = S/m^2$$

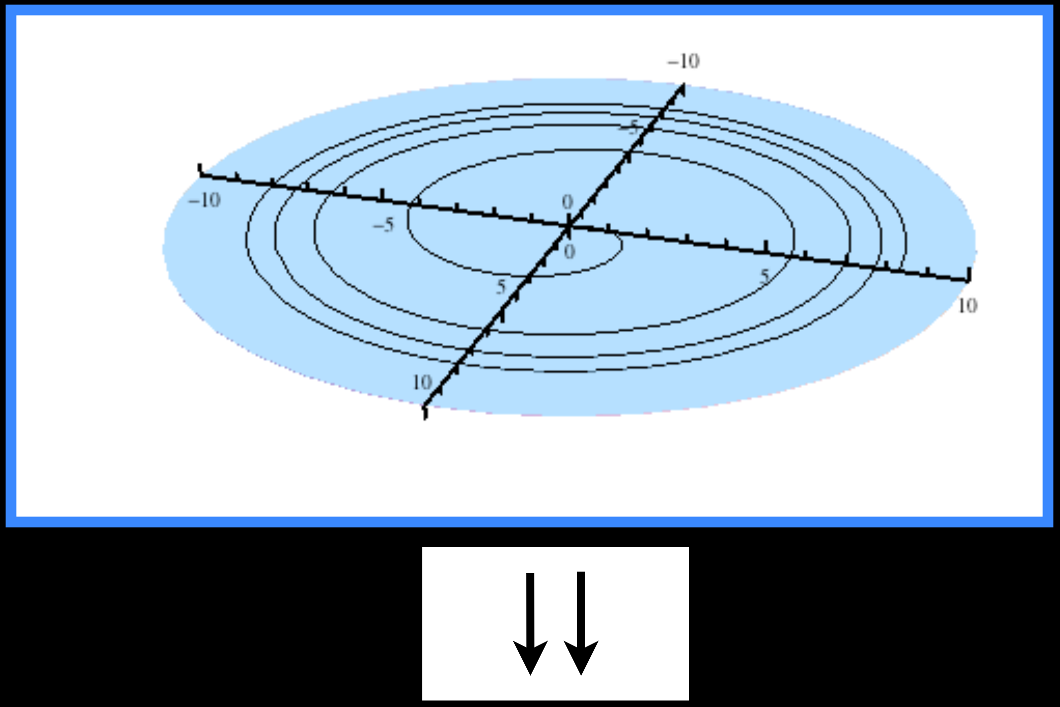


Plus: distance, sky location, orientation, polarisation

Aligned spins

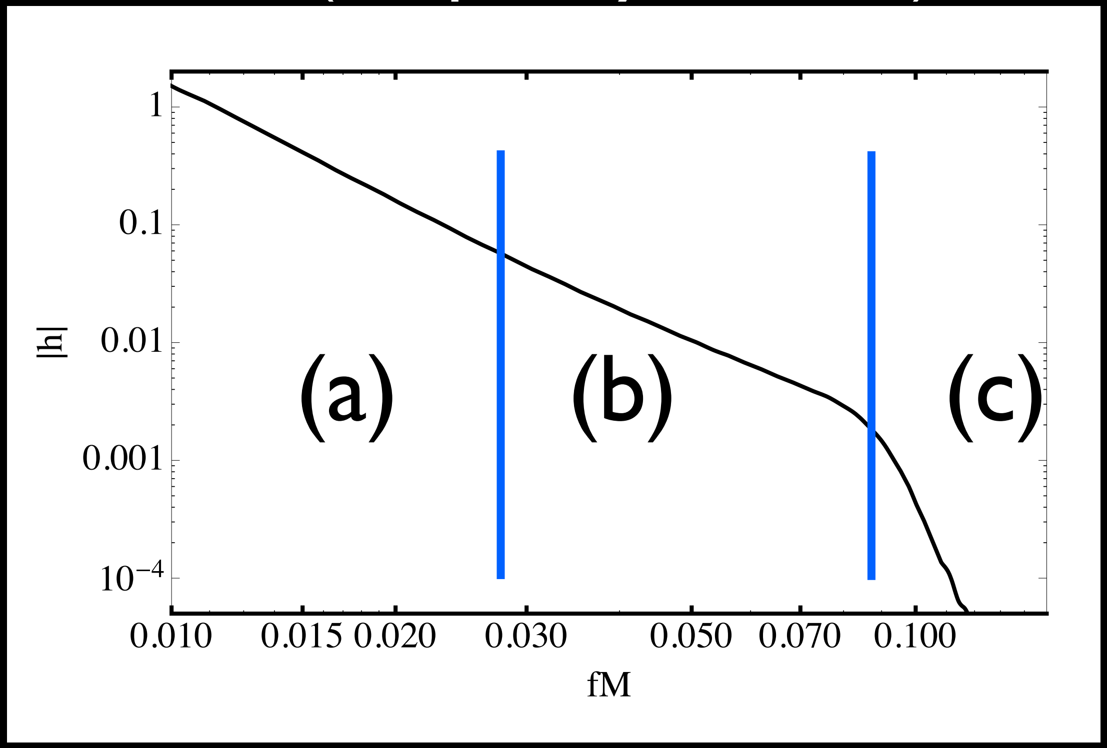






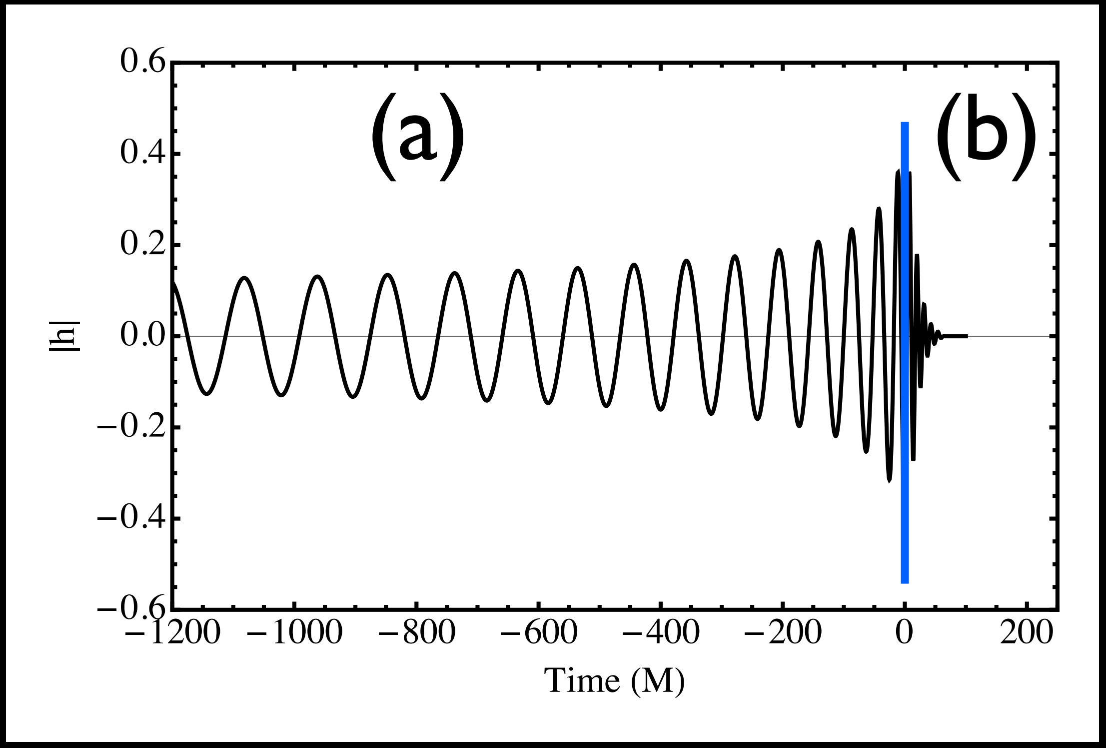
(Dominant spin effect is a weighted sum of the spins)

IMRPhenom
(frequency domain)



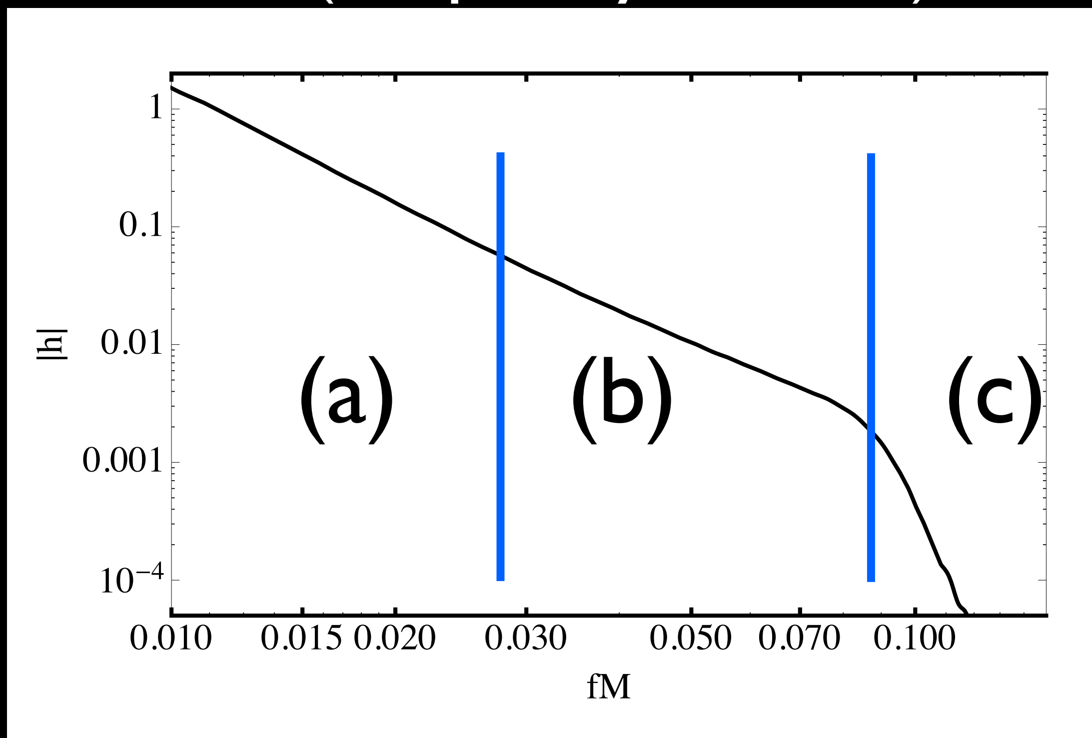
- (a) PN-based ansatz
- (b) phenomenological fit (based on NR behaviour)
- (c) FFT of ringdown waveform (Lorentzian)
- Analytic: fast

EOBNR
(time domain)

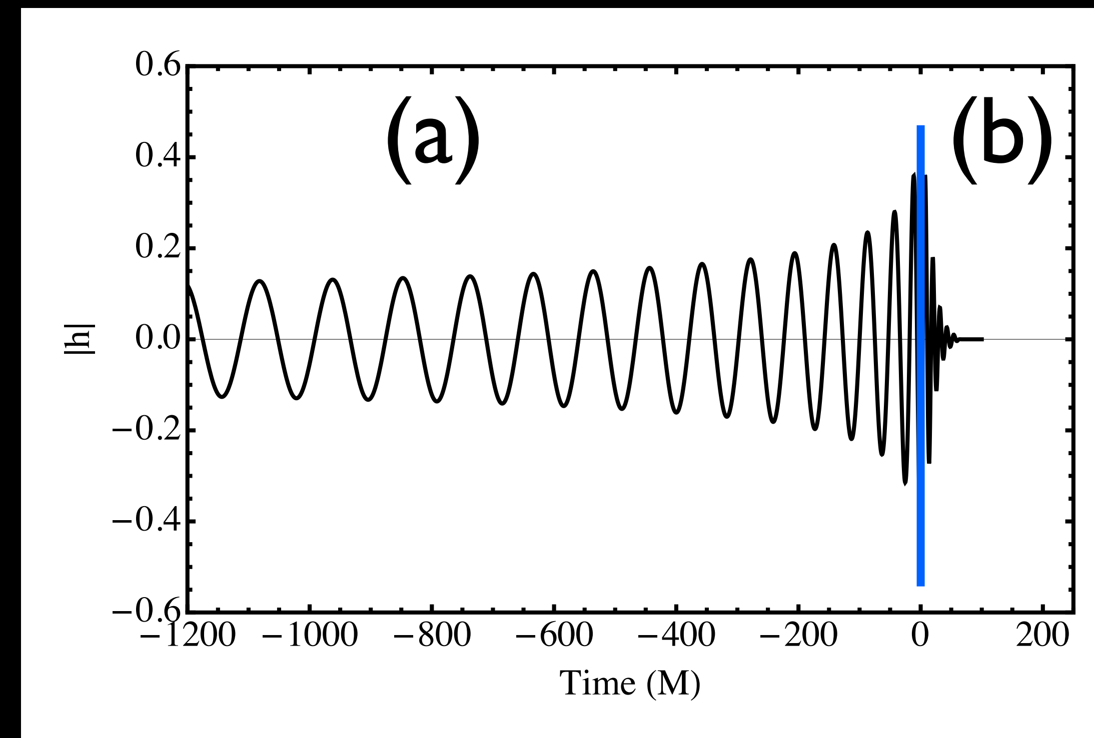


- (a) EOB + terms tuned to NR waveforms
- (b) Smooth transition to ringdown
- Includes both spins
- Numerically solve ODEs: slow
- Speed-up: Reduced-order models

Phenom
(frequency domain)



EOB-NR
(time domain)



- (a) PN-based ansatz
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DiRAC PRACE

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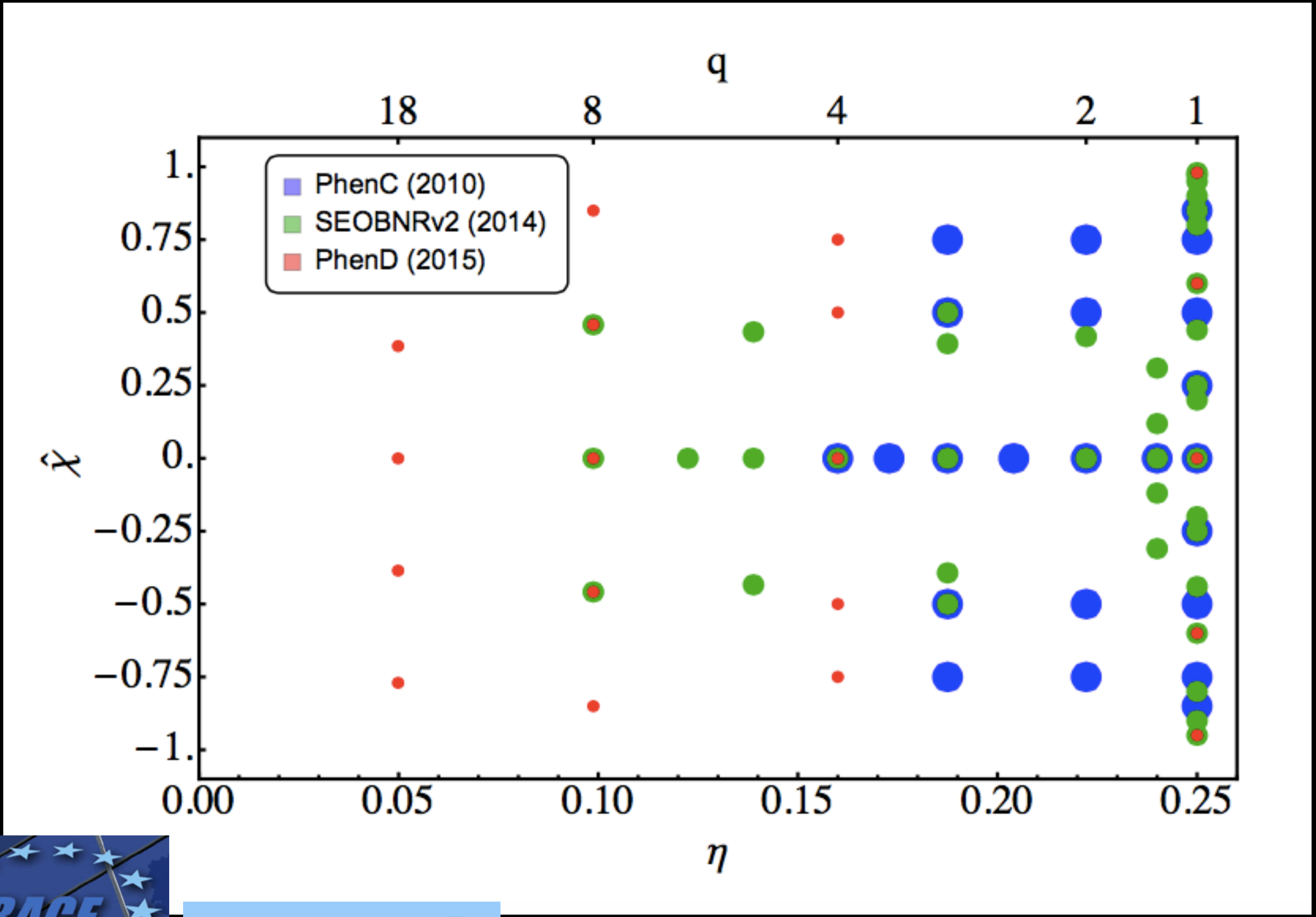
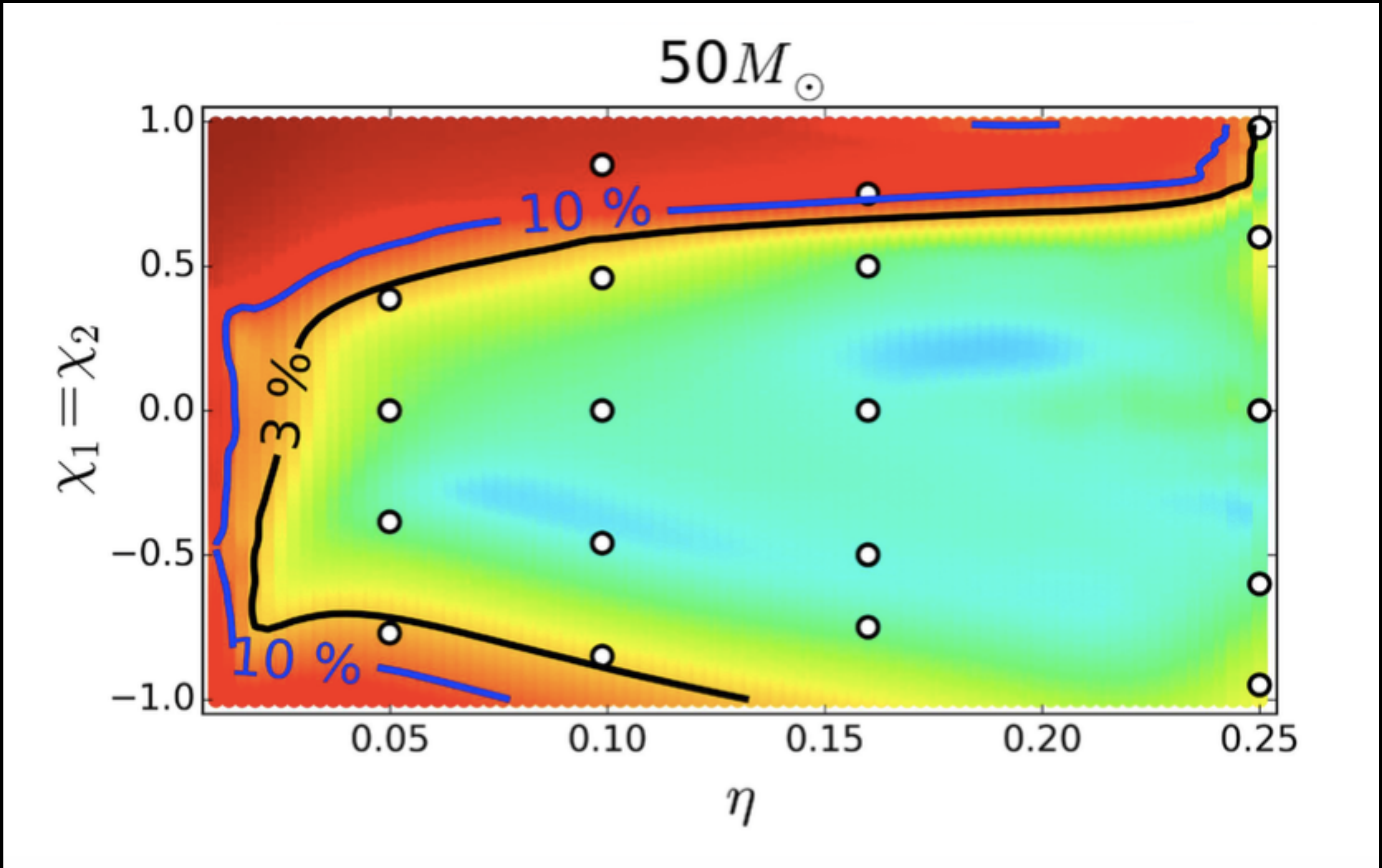
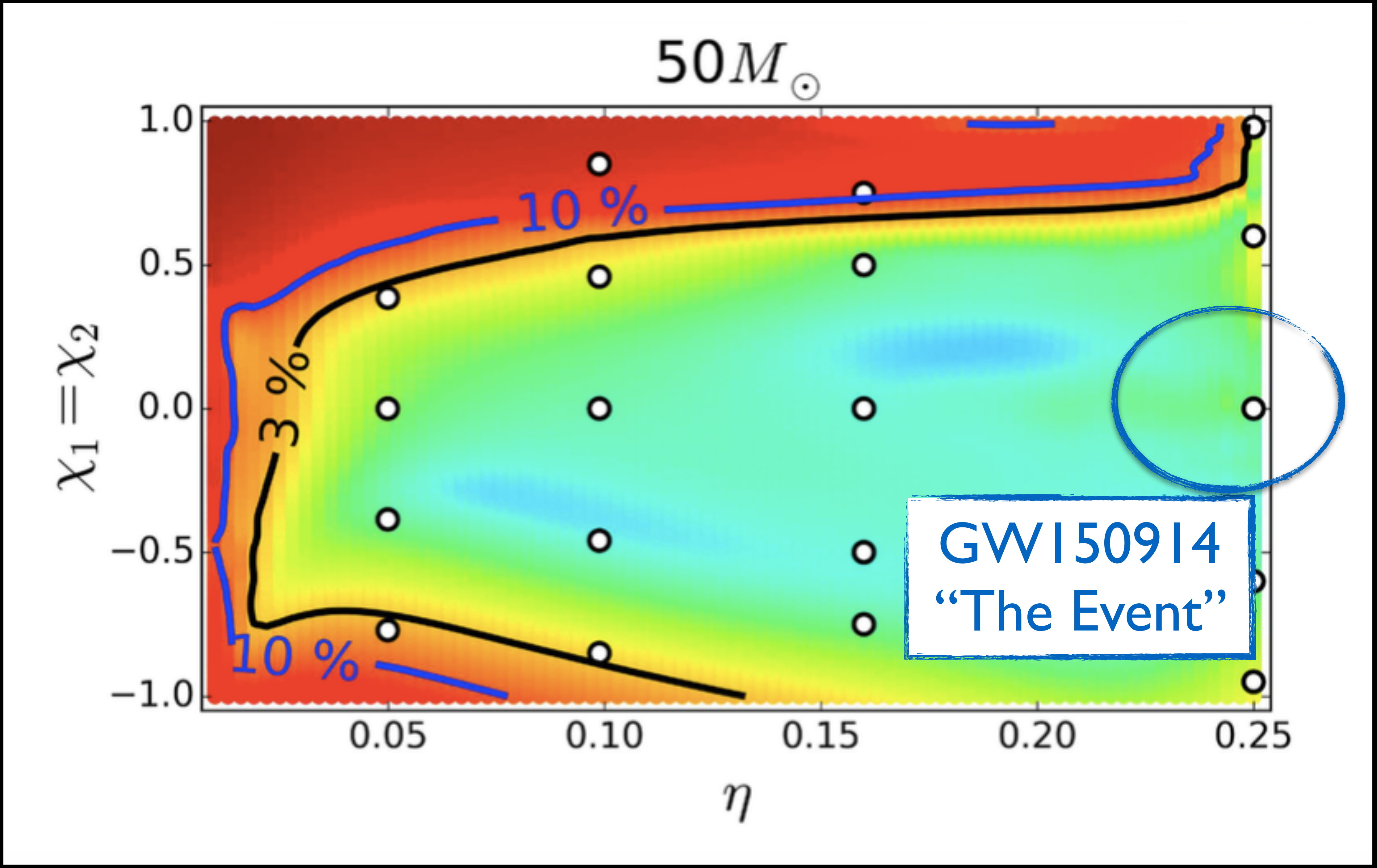


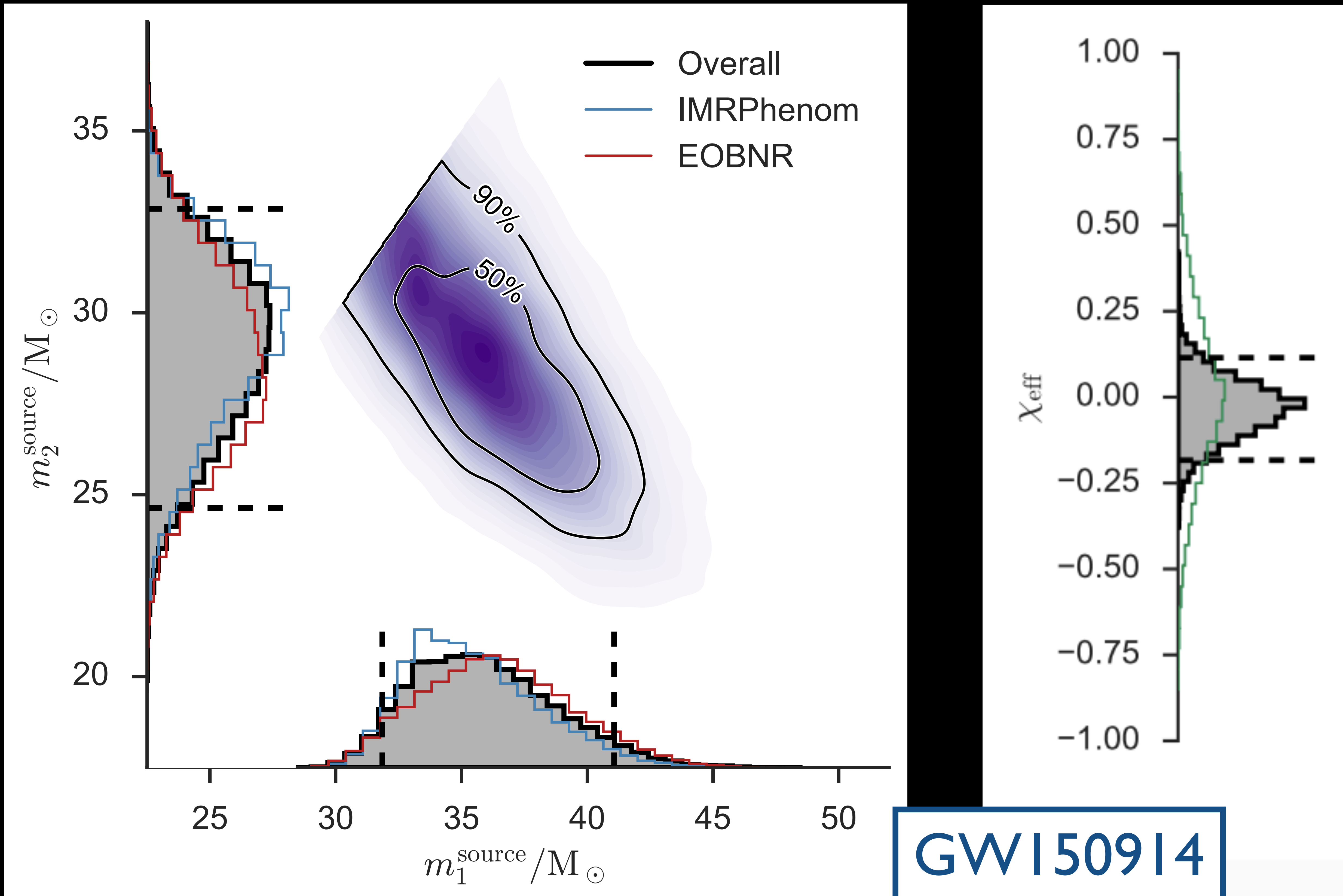
[Khan, *et. al* (2016)]



[Khan, *et. al* (2016)]



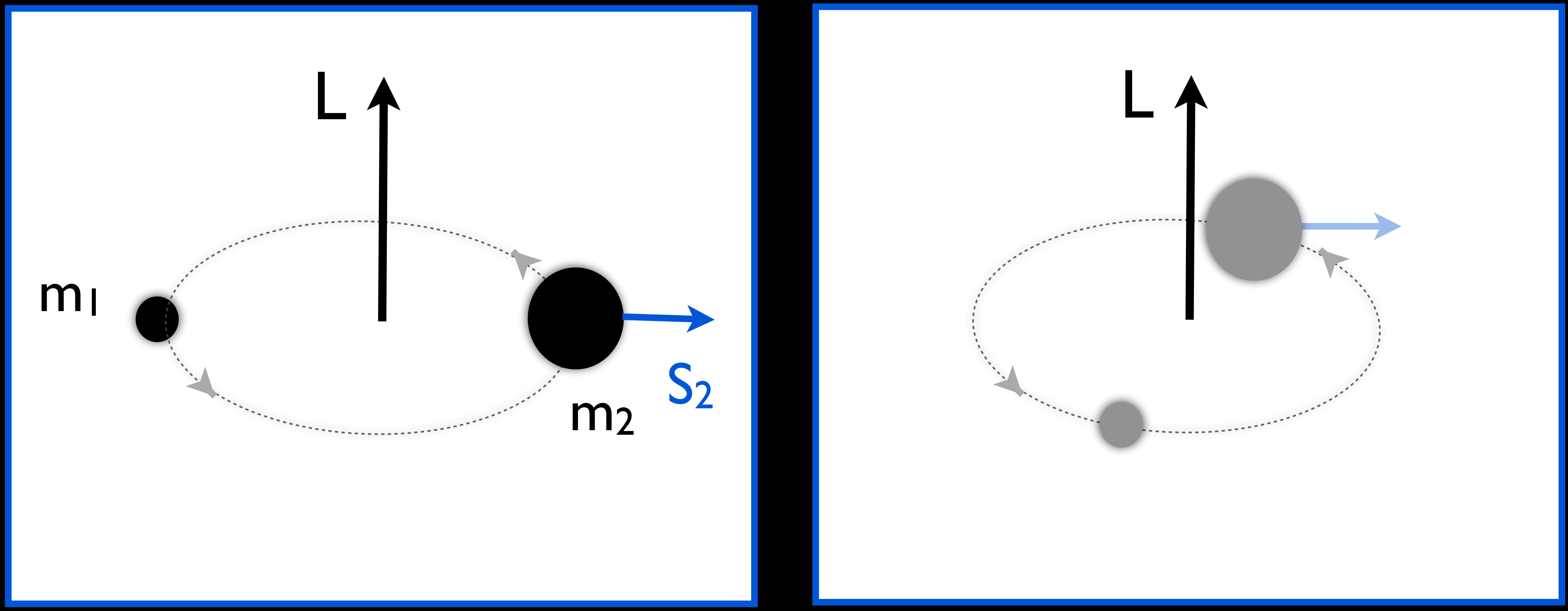
$50M_\odot$
1.0
0.5
0.0
−0.5
−1.0
$\chi_1 = \chi_2$
0.05
0.10
0.15
0.20
0.25
η
10 %
3 %
10 %
GW150914
“The Event”



GW150914
“The Event”

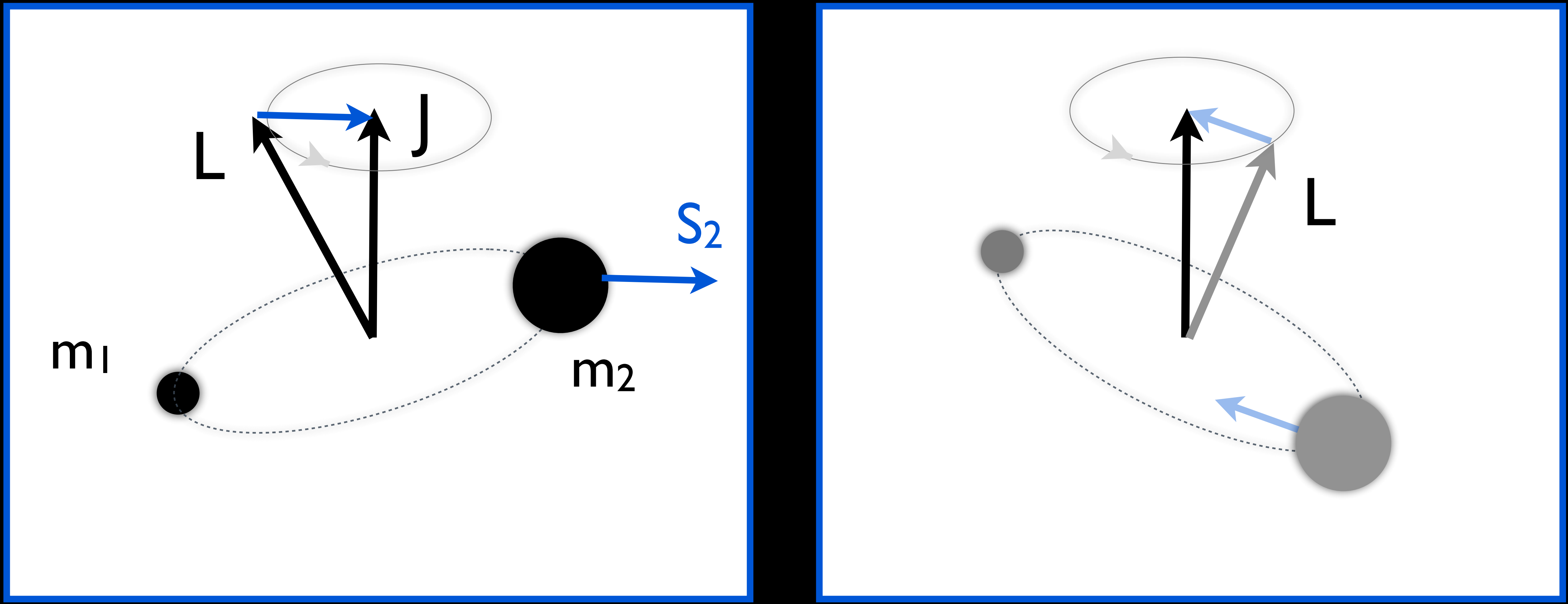
[LVC (2016)]

Orbital precession



Newtonian gravity:
L, S_1, S_2 remain fixed

Orbital precession



General relativity
(L, S_1, S_2) precess around J

Orientation dependence

q=3, $|S_2|$ = 0.75 (in plane)

Observer aligned with *J*

Orientation dependence

q=3, $|S_2|$ = 0.75 (in plane)

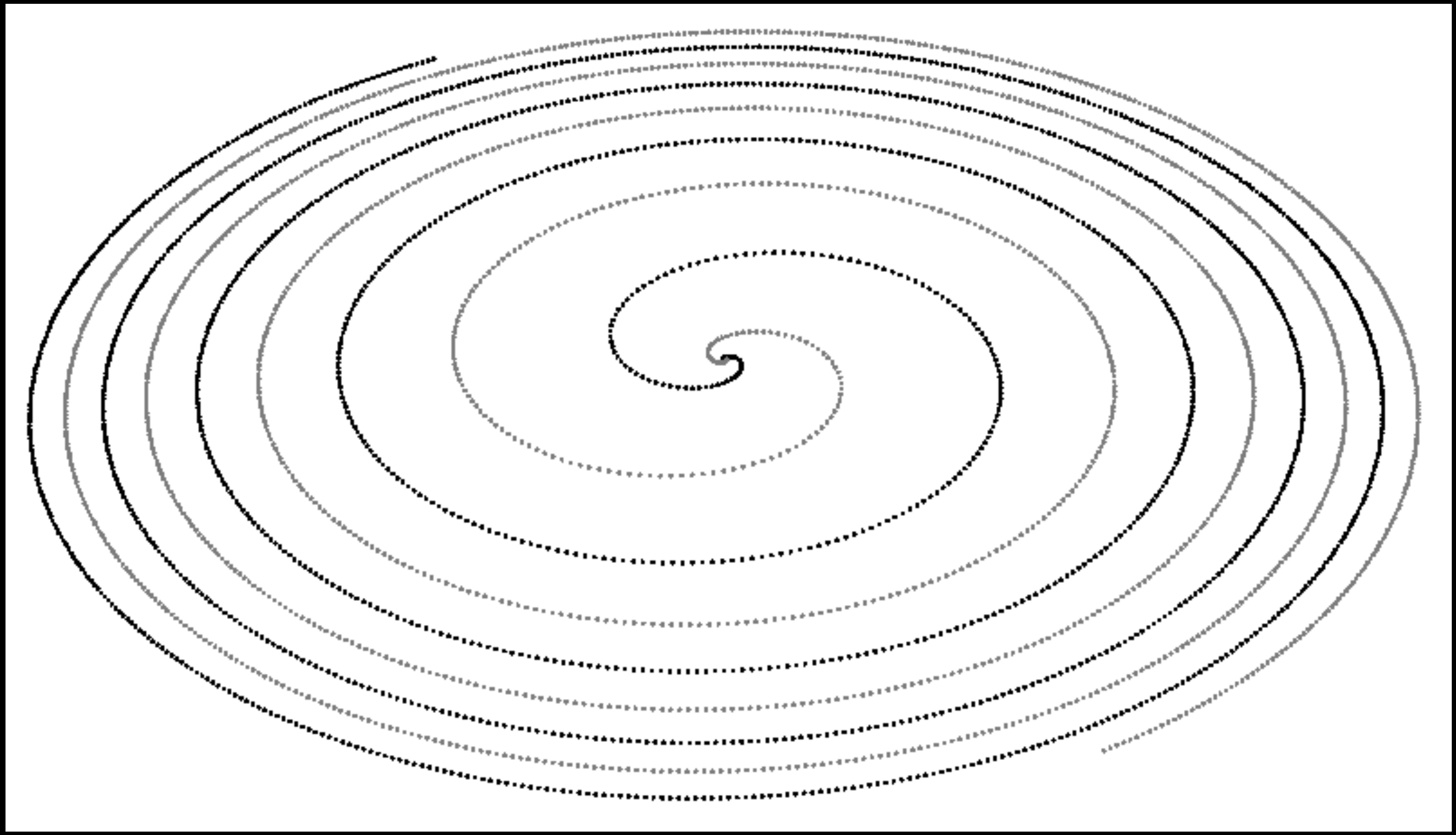
Observer aligned with J

Observer inclined $\pi/6$ to J

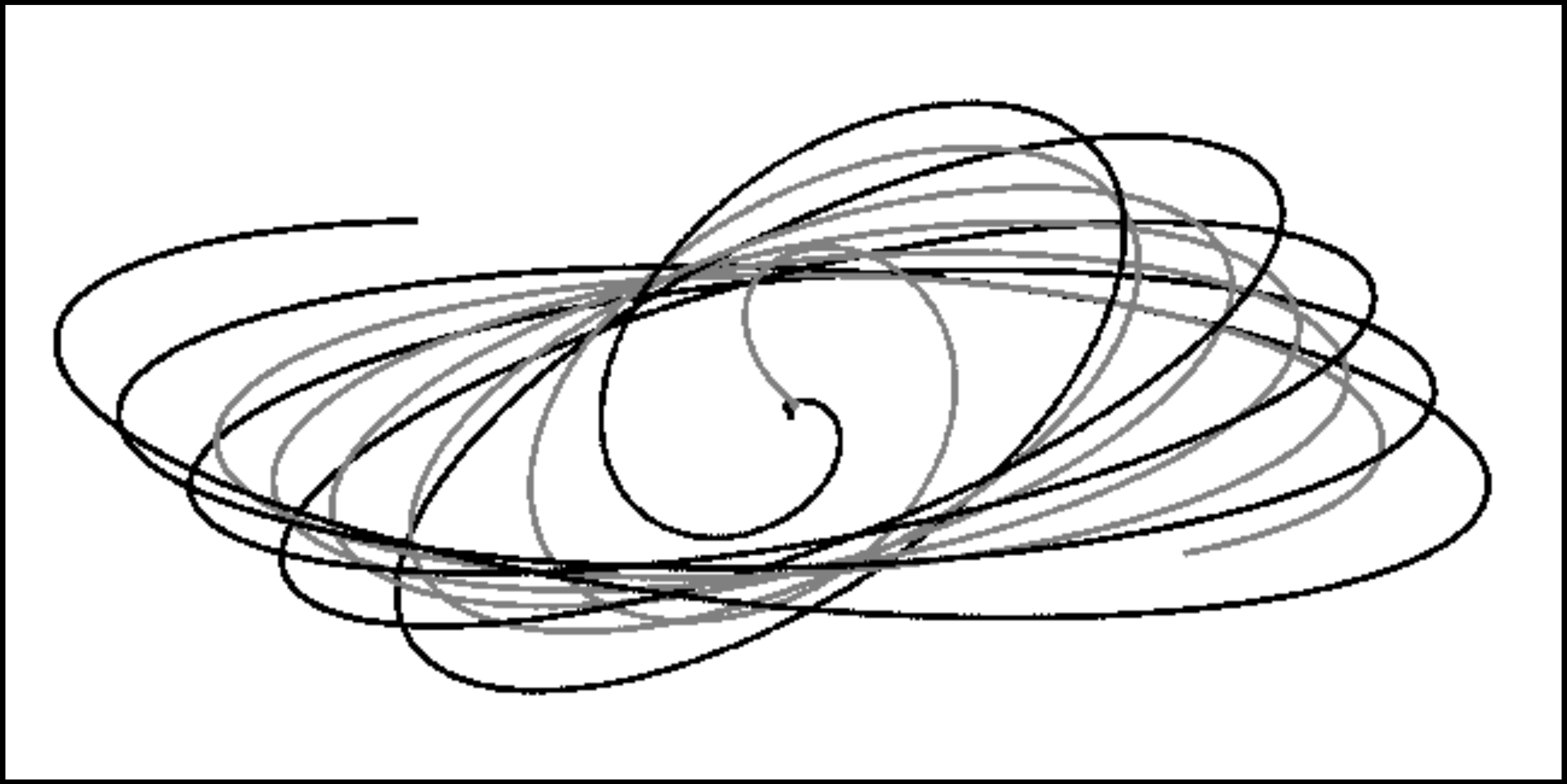
Observer inclined $\pi/3$ to J

Observer inclined $\pi/2$ to J

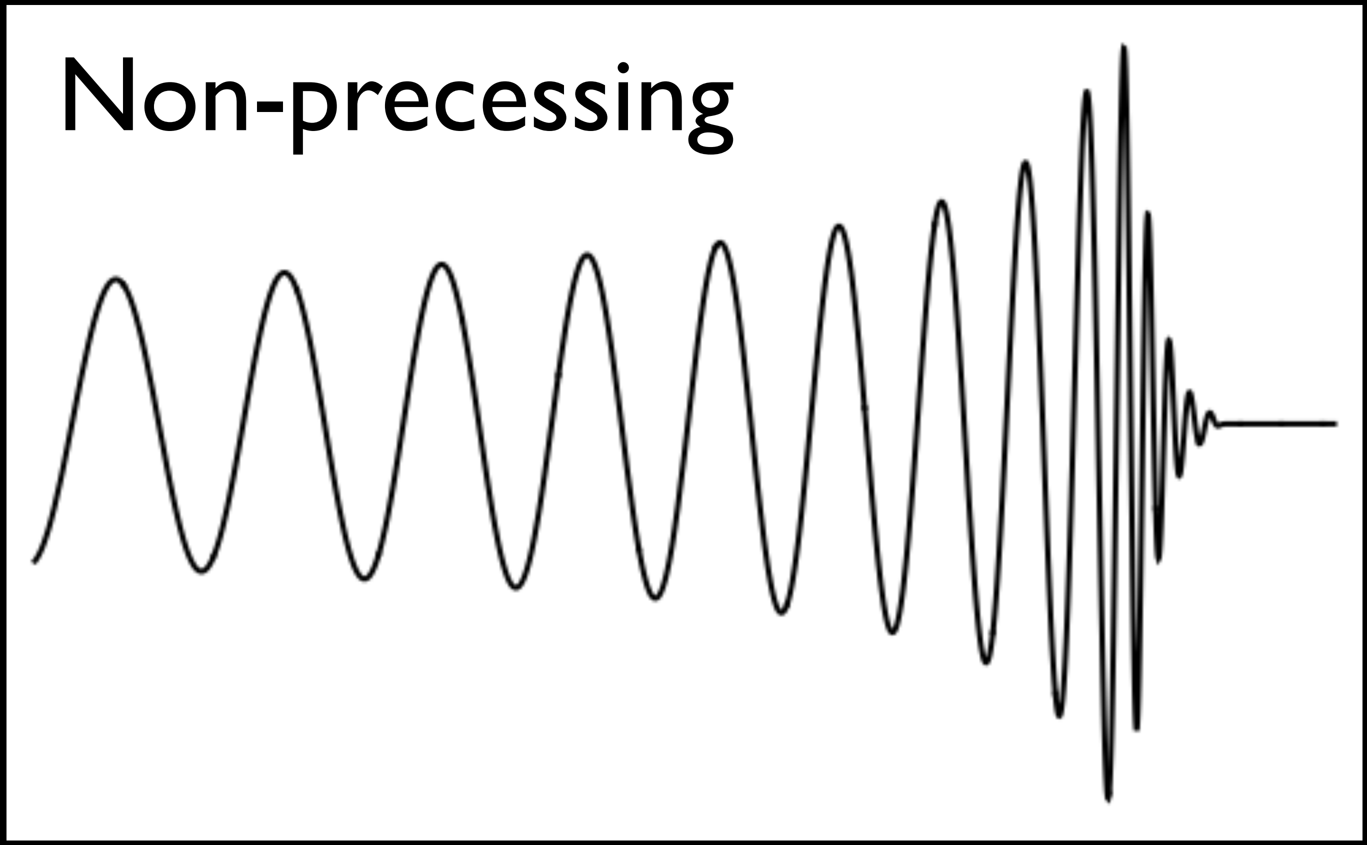
Equal-mass nonspinning BBH consistent with GW150914

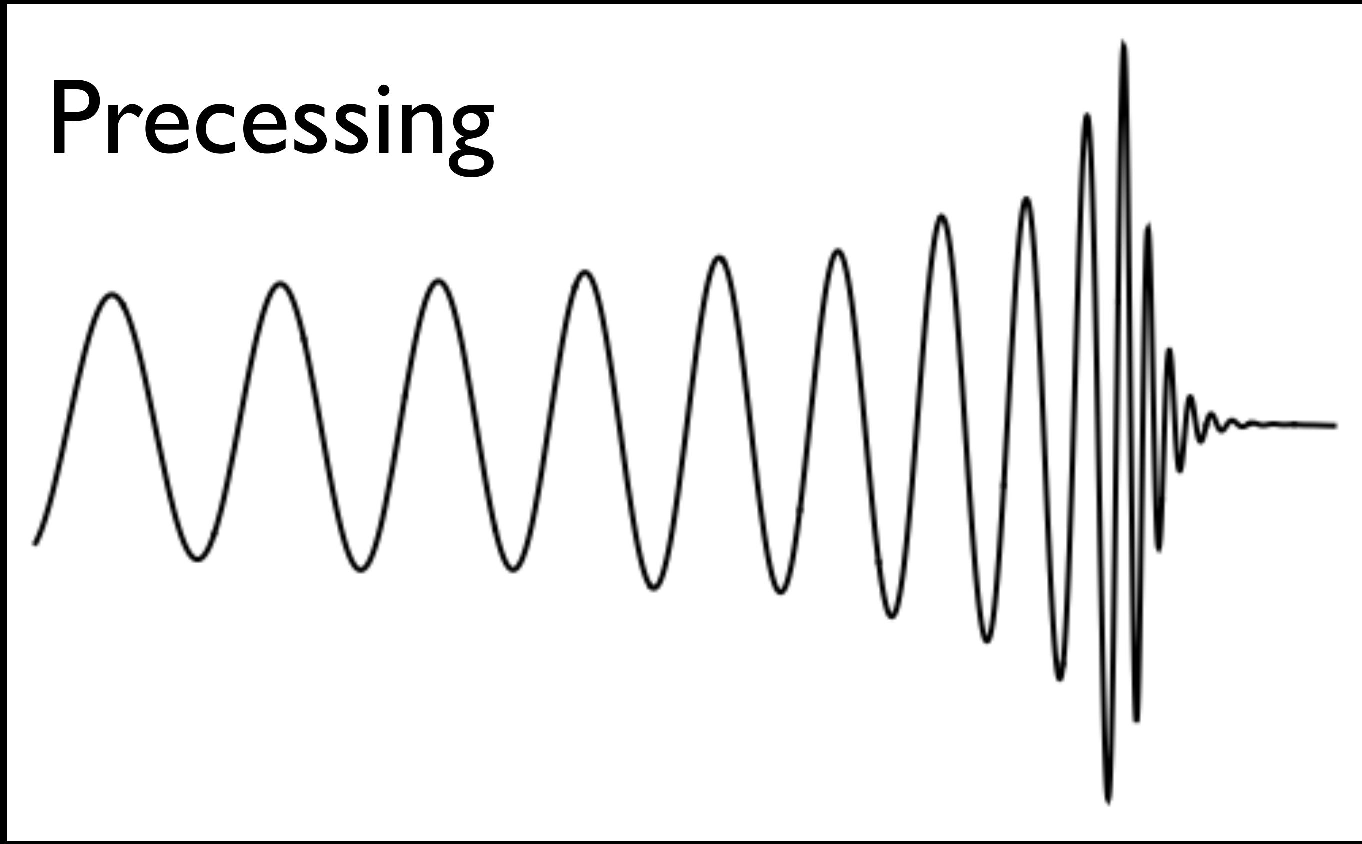


Unequal-mass precessing BBH consistent with GW150914

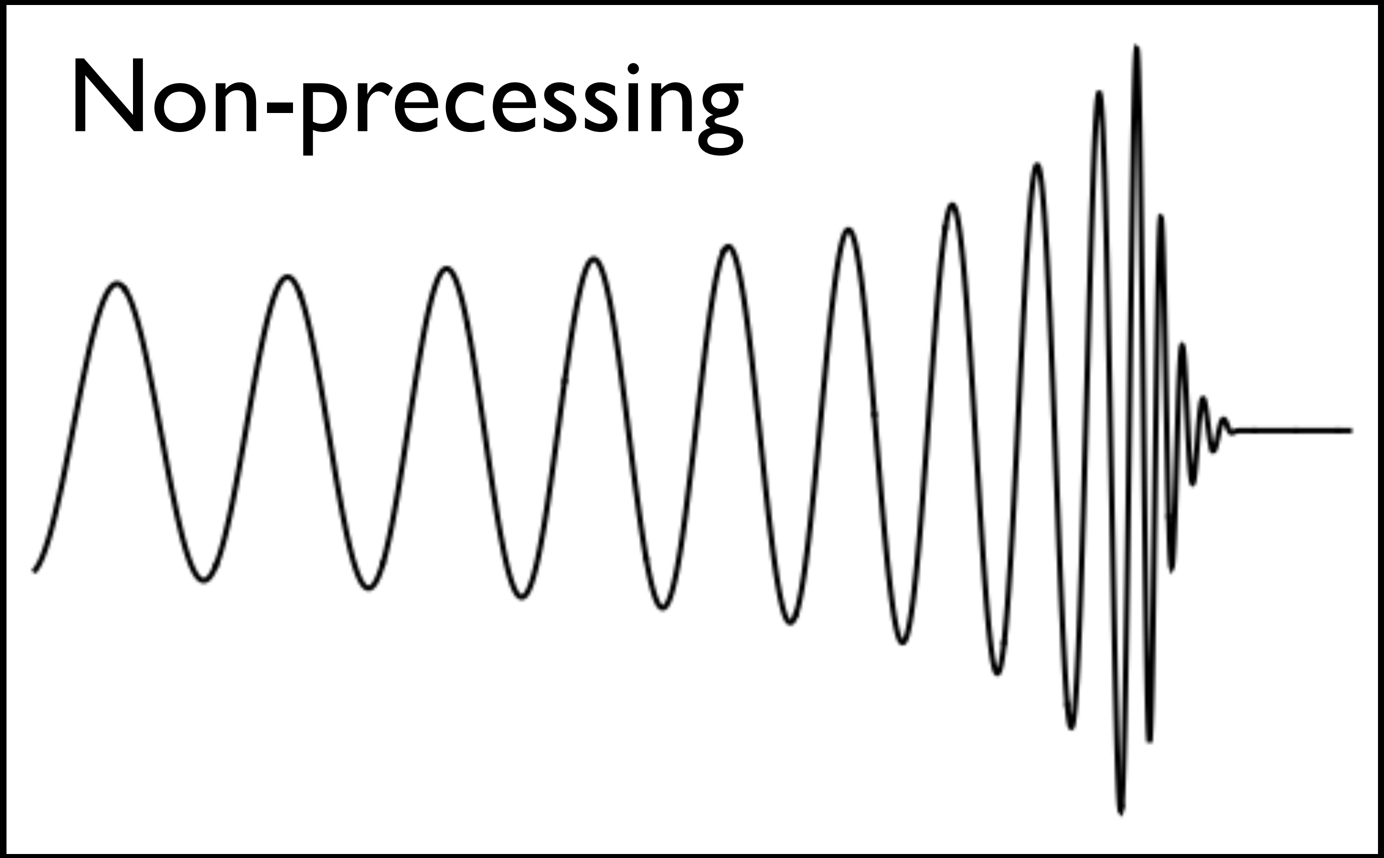


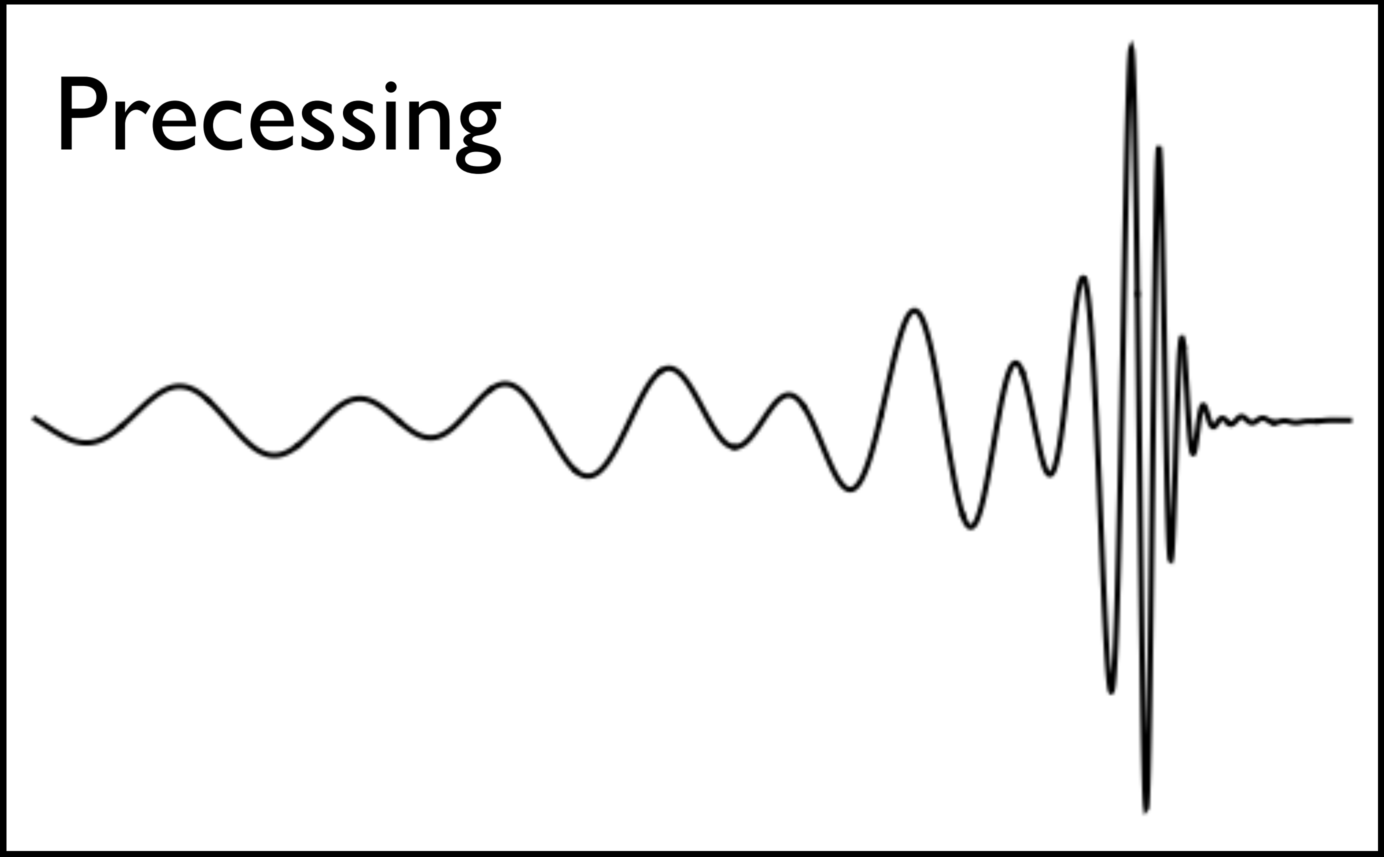
“Face-on” to the source

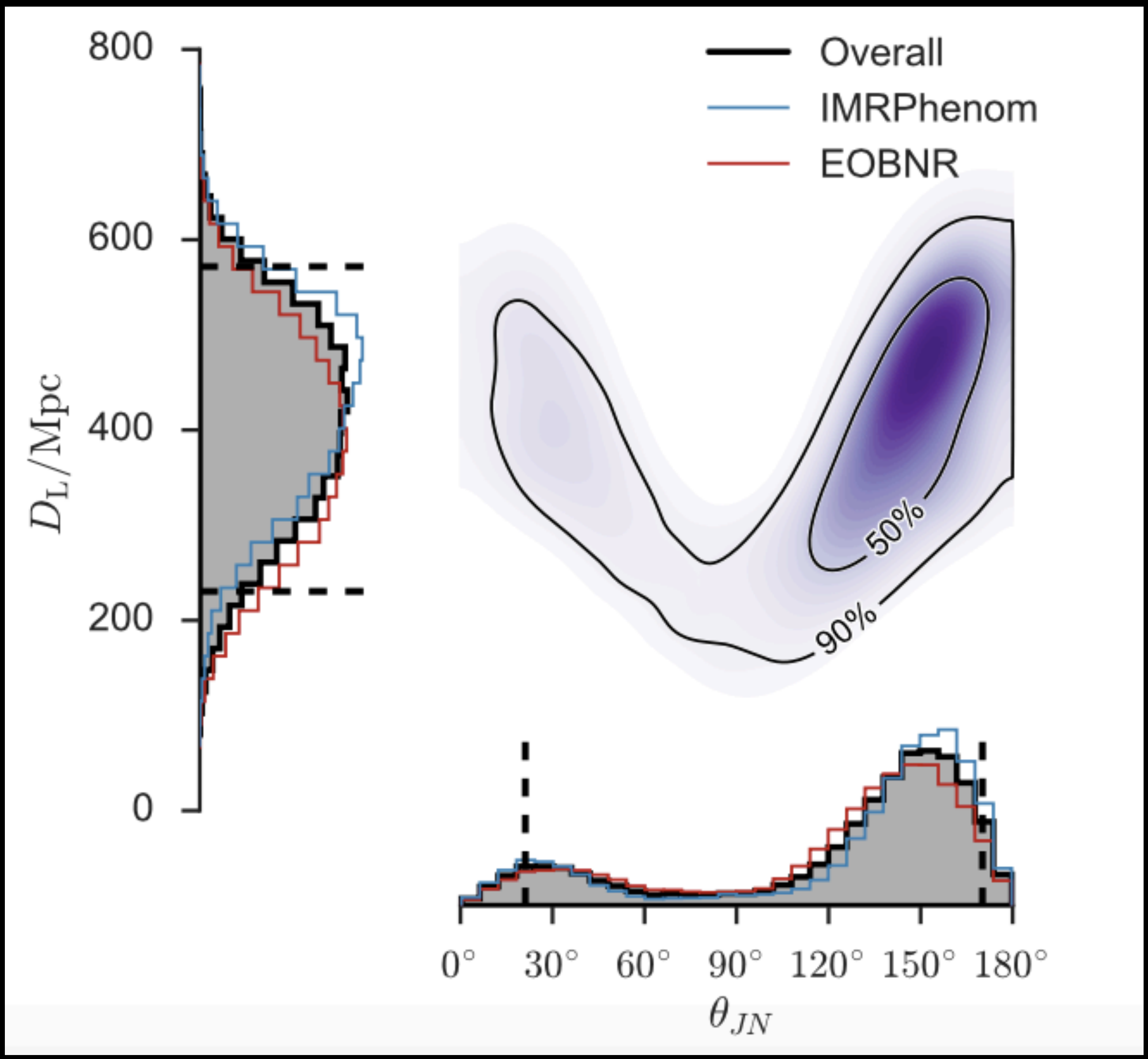




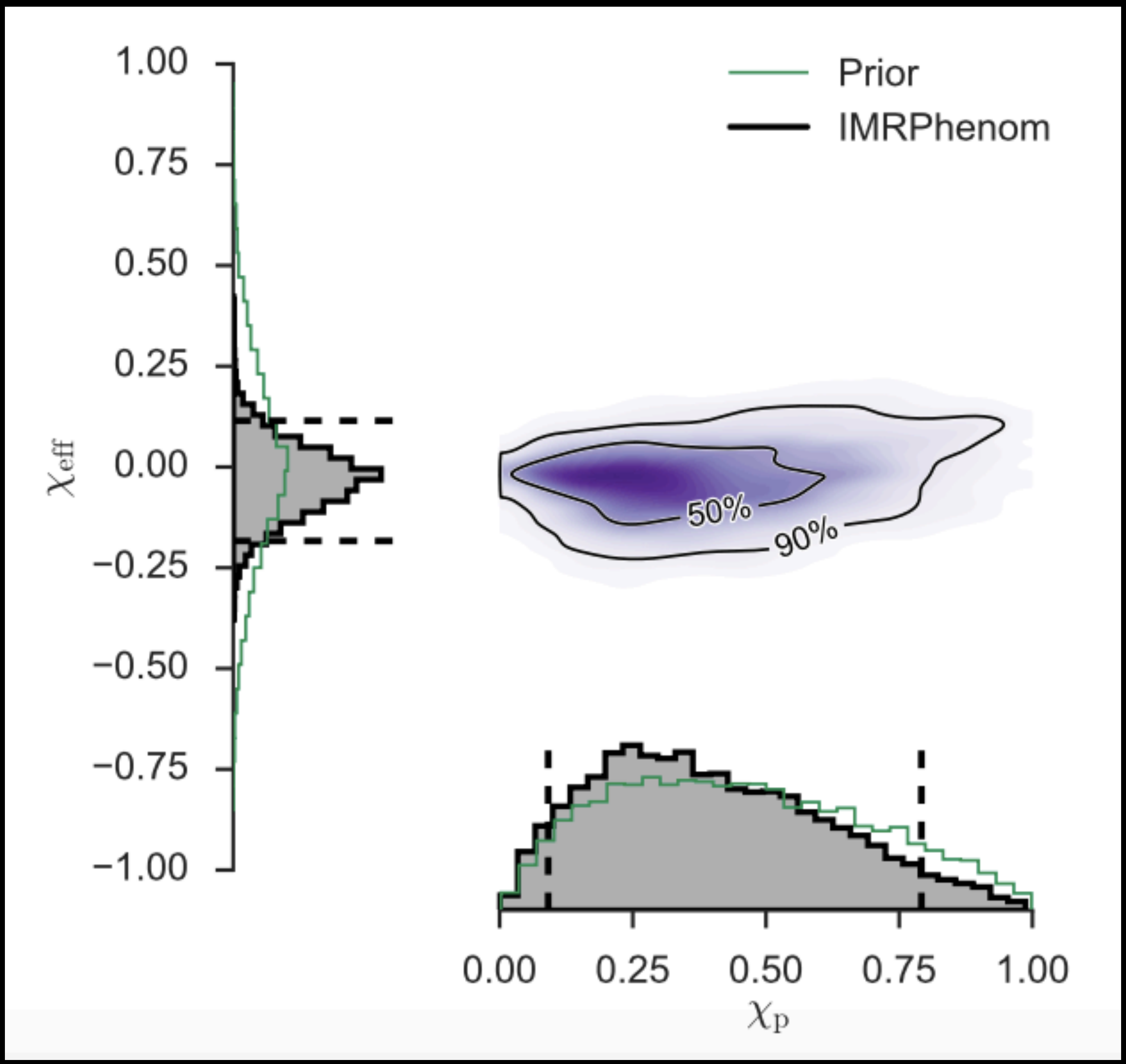
“Edge-on” to the source







Overall
IMRPhenom
EOBNR
D_L/Mpc
800
600
400
200
0
50%
90%
0° 30° 60° 90° 120° 150° 180°
θ_{JN}



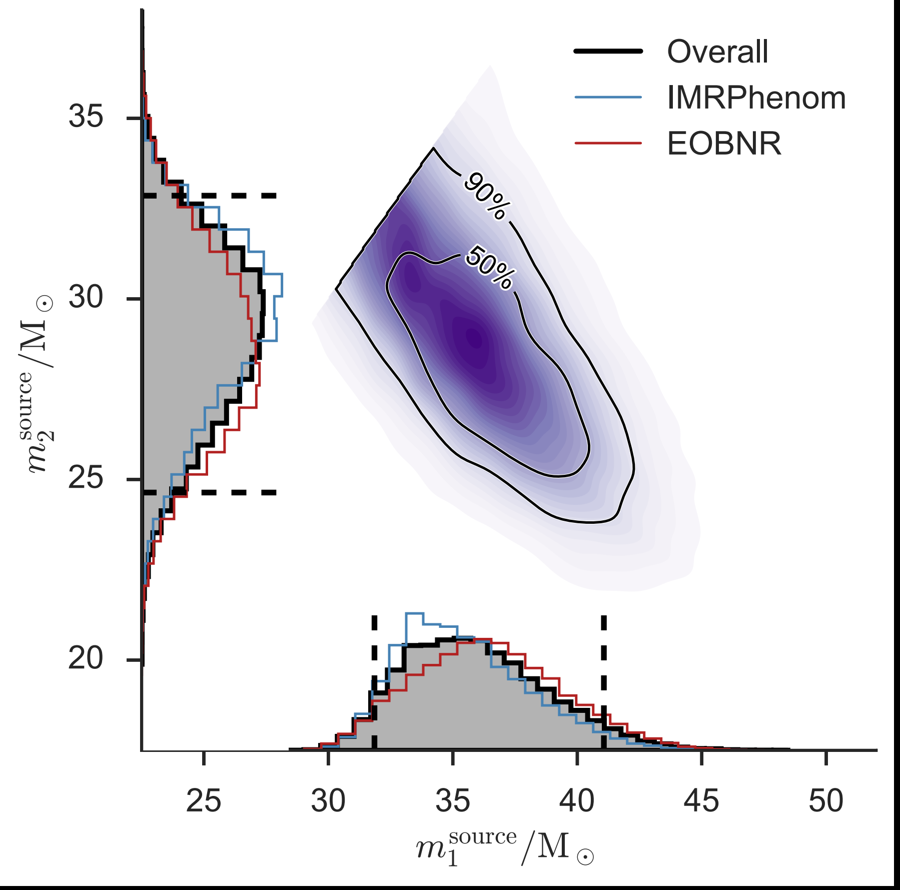
Prior
IMRPhenom
χ_{eff}
1.00
0.75
0.50
0.25
0.00
−0.25
−0.50
−0.75
−1.00
50%
90%
0.00 0.25 0.50 0.75 1.00
χ_p

[LVC (2016)]

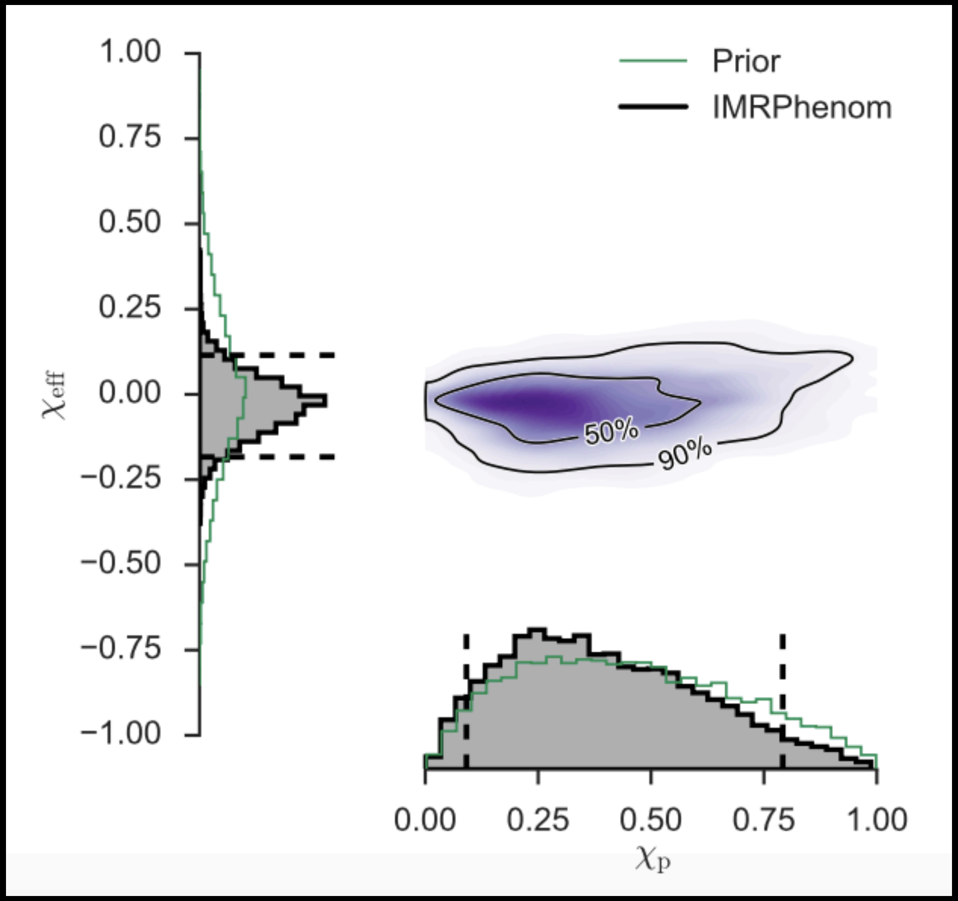
Follow-up simulations

- Perform simulations near "best-guess" parameters
- Study systematic errors in the waveform models
- "Local" models could improve measurements
- 100s of simulations (SXS, Cardiff-UIB, GATech, RIT)
- DiRAC: 29 simulations on Cosma.
  - Required ~1 million CPU hours

G
W
1
5
0
9
1
4

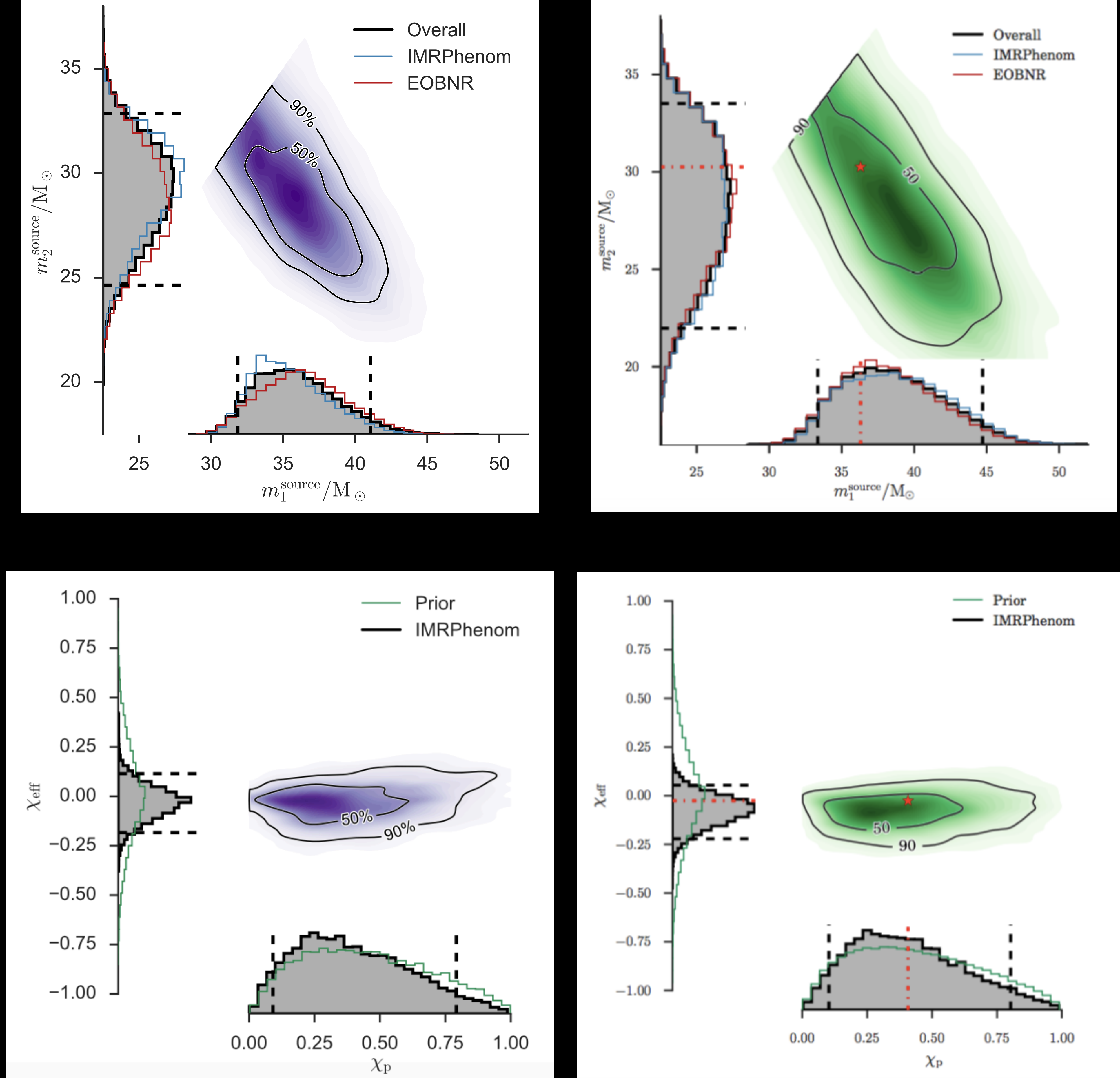


Overall
IMRPhenom
EOBNR
90%
50%
35
30
25
20
$m_2^{\mathrm{source}}/\mathrm{M}_\odot$
25
30
35
40
45
50
$m_1^{\mathrm{source}}/\mathrm{M}_\odot$



Prior
IMRPhenom
50%
90%
1.00
0.75
0.50
0.25
0.00
−0.25
−0.50
−0.75
−1.00
χ_{eff}
0.00
0.25
0.50
0.75
1.00
χ_{p}

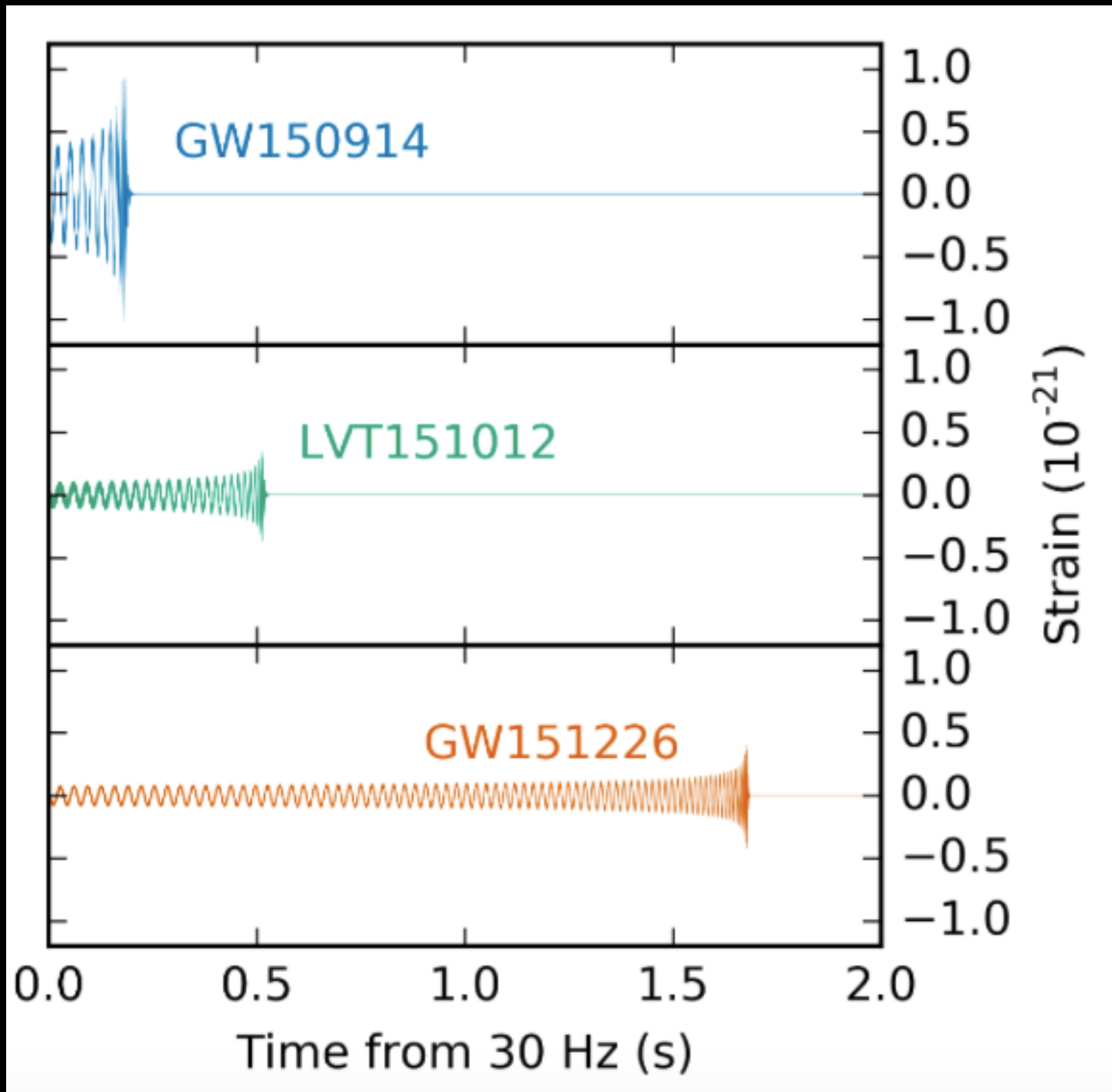
GW150914



NR Injection

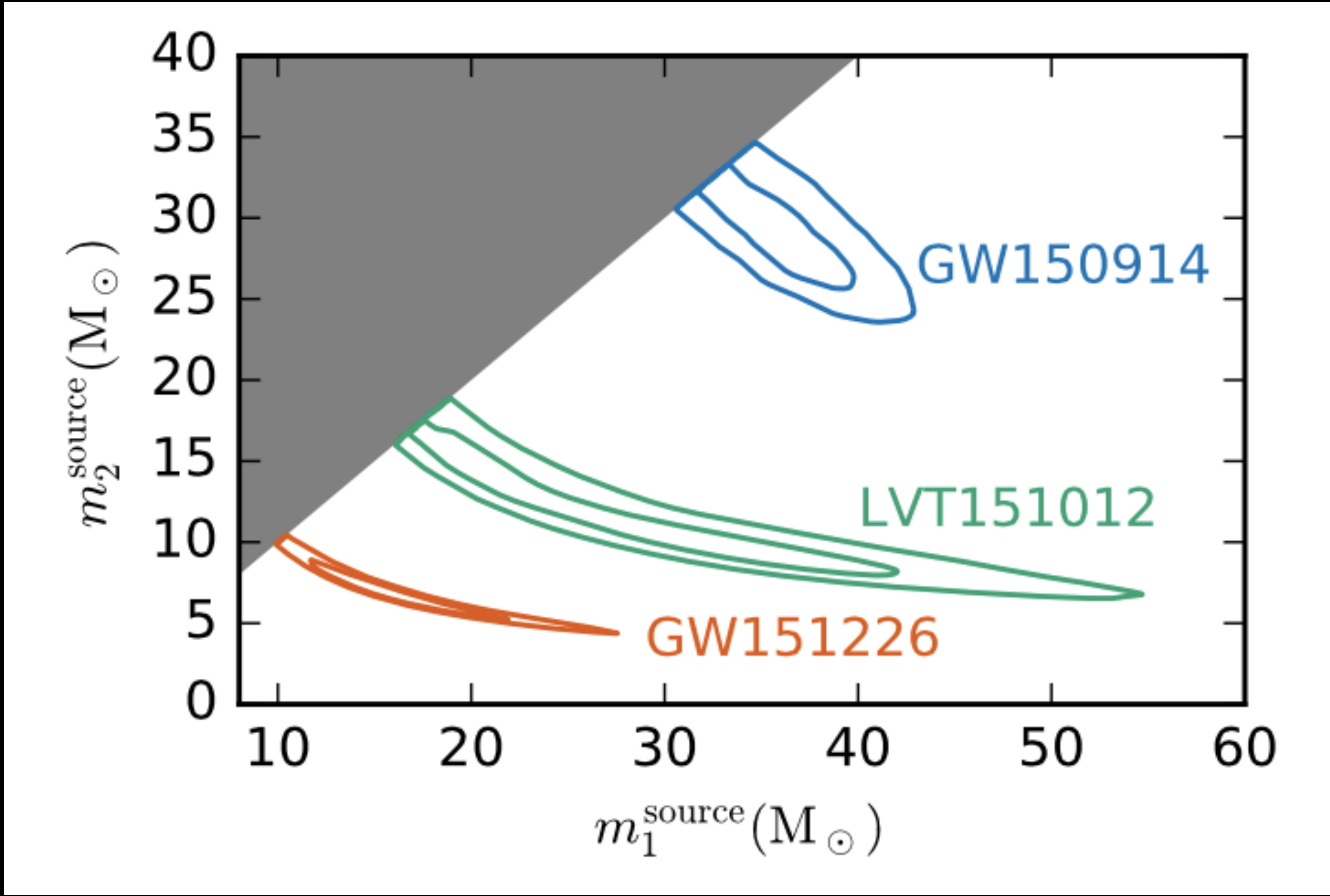
[LVC, in preparation (2016)]

All observations



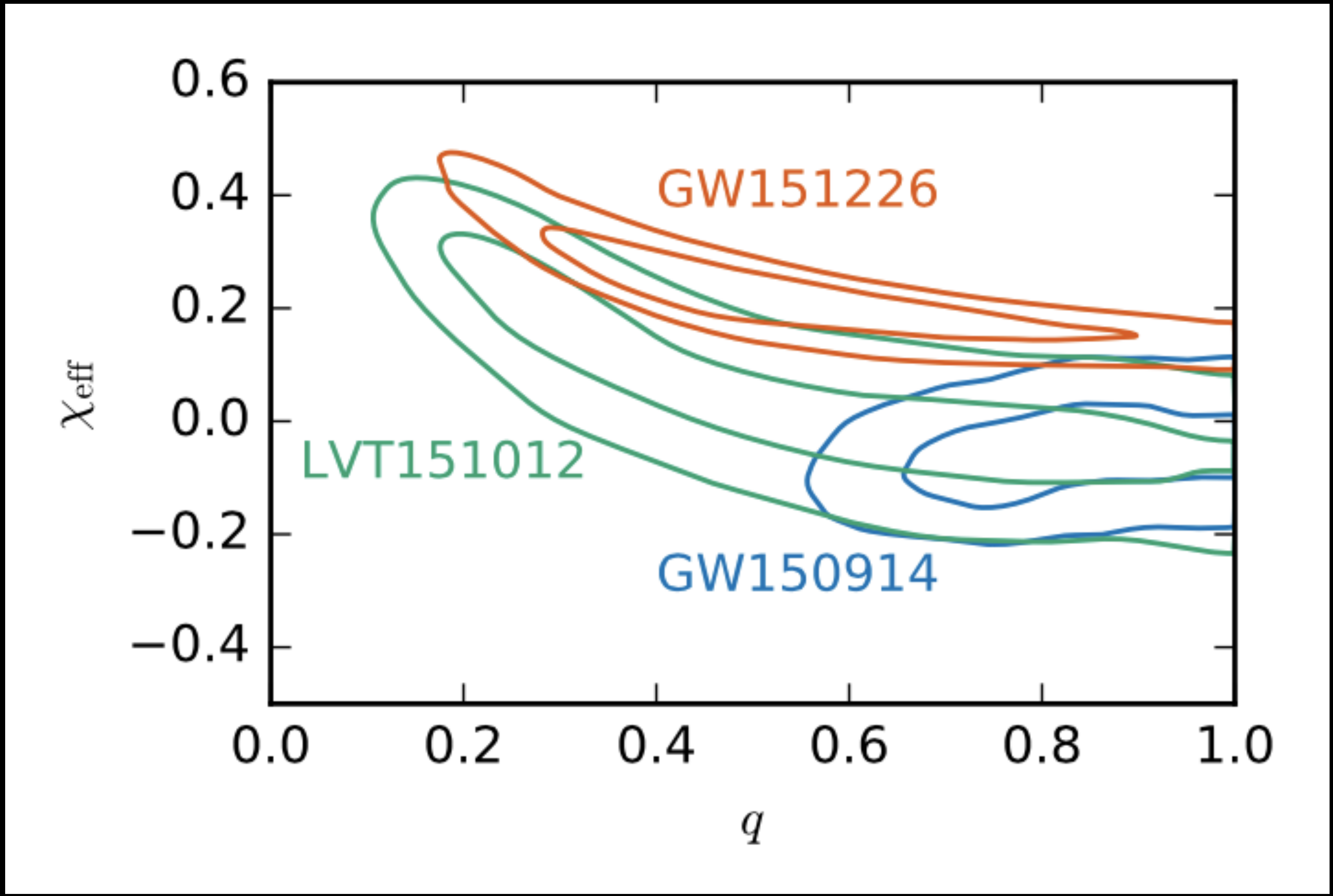
[LVC (2016)]

All observations



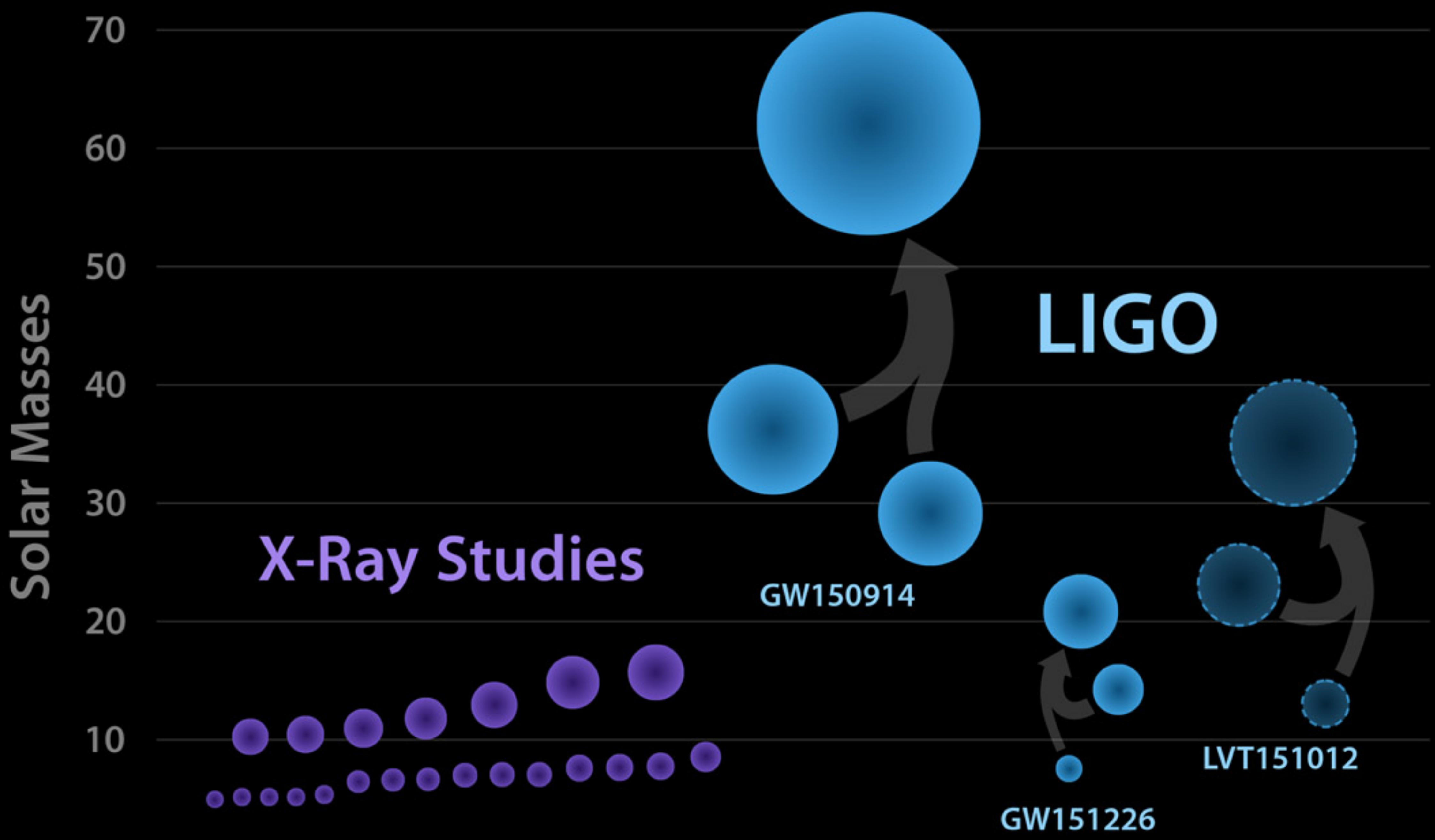
[LVC (2016)]

All observations

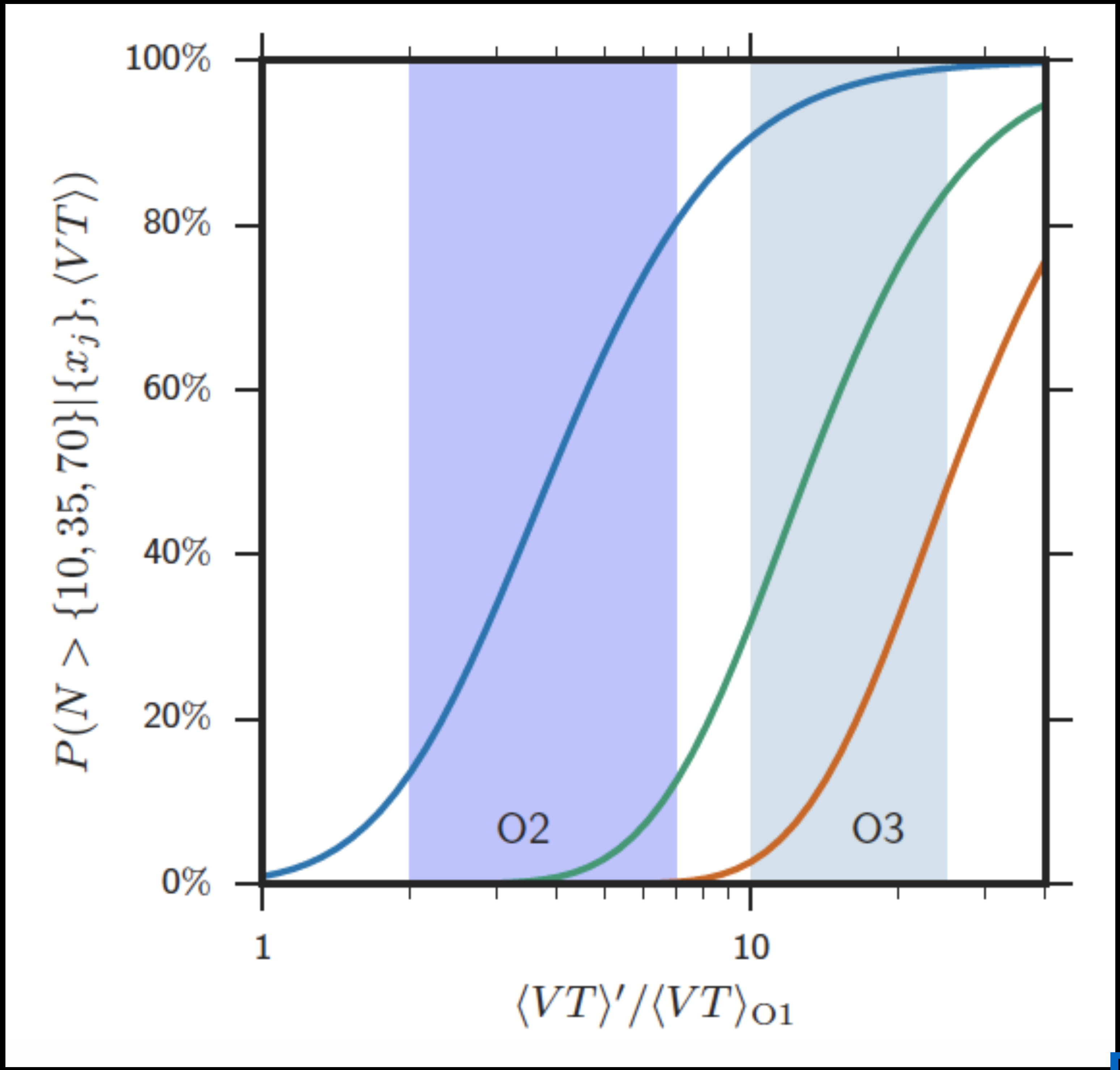


[LVC (2016)]

Black Holes of Known Mass

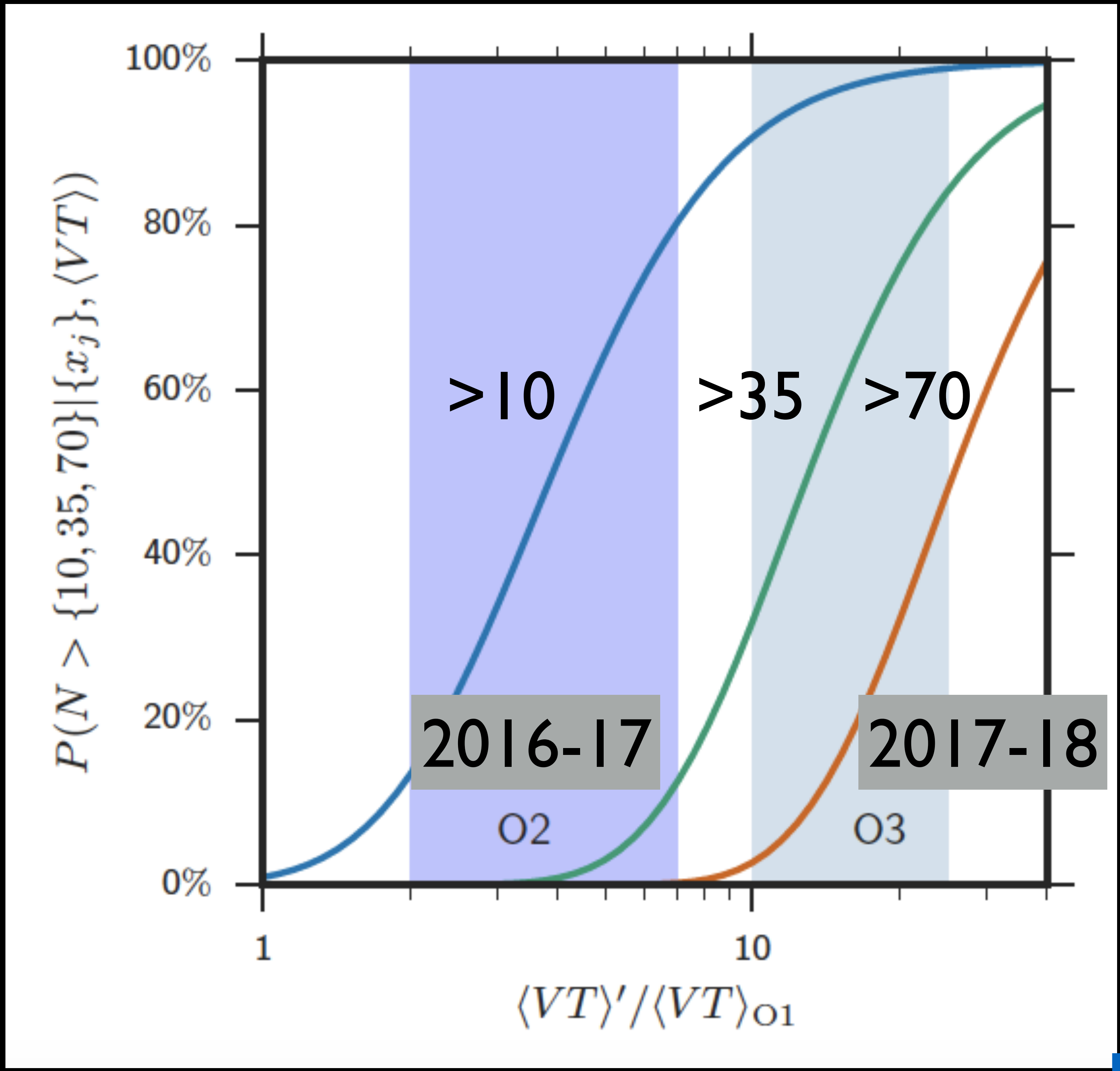


Future observations



[LVC (2016)]

Future observations



[LVC (2016)]

The future

- The field of gravitational-wave astronomy has begun!
- 100s of black hole observations expected in next 5 years
- We need to be ready to extract the maximum science!

- For future signals, we will need better models:
  - higher harmonics
  - more precession physics
- A large NR simulation campaign is underway…