



UNIVERSITY OF  
LIVERPOOL

## UKQCD Review

Nicolas Garron

University of Liverpool

Dirac Day, Edinburgh 8<sup>th</sup> of September 2016

# Outline

- UKQCD
- Standard Model and new Physics
- Lattice QCD and Standard Model results
- Beyond the Standard Model
- Finite Temperature and density

According to

<http://pyweb.swan.ac.uk/~allton/ukqcd/web/information.html>

The list of member institutions is

- Cambridge
- Edinburgh
- Glasgow
- Liverpool
- Oxford
- Plymouth
- Southampton
- Swansea

# UKQCD collaborations

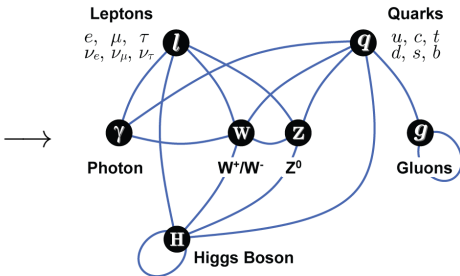
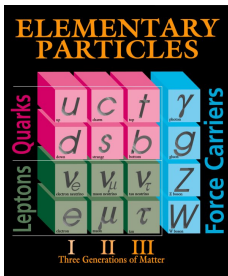
- HPQCD (UK: Cambridge-Glasgow-Plymouth; Canada, Spain, US)
- QCDSF-UKQCD (UK: Edinburgh, Liverpool; Australia, Germany)
- RBC-UKQCD (UK: Edinburgh, Liverpool, Southampton; Canada, China, Japan, US, . . . )
- Hadron Spectrum Collaboration (UK: Cambridge; Ireland, US)
- + unnamed collaborations

Theoretical Particle Physics using large-scale numerical simulations

- QCD, Flavour physics, precision tests of the Standard Model
- Beyond the Standard Model and Non-QCD studies
- Finite Temperature and Finite Density

# Standard Model: a beautiful theory

- Common description (Lagrangian) of electromagnetism, strong and weak interaction.
- Based on symmetry principles, combines Einstein's special relativity and quantum mechanics.
- Only a few free parameters (19, if we don't take neutrinos masses into account)
- Extremely accurate description over a large range of phenomena.  
Example: muonic anomalous magnetic moment  $g_\mu - 2 = 11659208.0(5.4)(3.3)[6.3] 10^{-10}$
- 2012: Observation of a Higgs-like particle → last missing piece of the puzzle ?



# Why do look for new physics ?

- No gravity : the SM is not a “theory of everything”
- Cannot explain Matter-antimatter asymmetry in the universe (CP violation)
- Dark matter and dark energy
- Hierarchy problem(s), ...
- Mathematically not well defined in the strong regime

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A lattice discretisation is the only way to define the theory properly



# Need for Lattice simulations

- BSM effects very hard to detect, need to have all errors under control
- The strong force (which binds the quarks together) is **strong**
- In the hardonic regime, Perturbation theory does not make sense
- Need non-perturbative method,

⇒ Numerical simulations of Lattice of **Q**uantum- **C**hromo- **D**ynamics

- Allows for *ab-initio* computations (model-independent)
- Theoretically well-defined

## QCD and Particle Physics Phenomenology

# QCD and Phenomenology

For example, compute the free parameters of the Standard Model

- Quark masses (RBC-UKQCD, HPQCD)
- Coupling constant (QCDSF-UKQCD, HPQCD)

Or the ones related to quark flavour mixing (CKM matrix): UKQCD

# Light and heavy quarks

The light quark sector ( $u,d,s$ ) is “mature”

- Ab-initio simulations,
- Simulations with physical quark masses, various lattice spacings
- Several discretisations

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- $b$ - sector: Most of the results traditionally use “effective theory”
- Fewer available discretisations
- However the situation is evolving quickly

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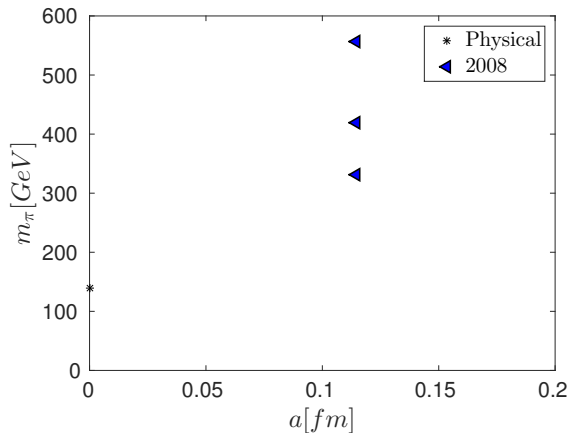
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For the charm sector, we are an intermediate situation

There is an impressive effort by the lattice community, both for the  $c$  and the  $b$

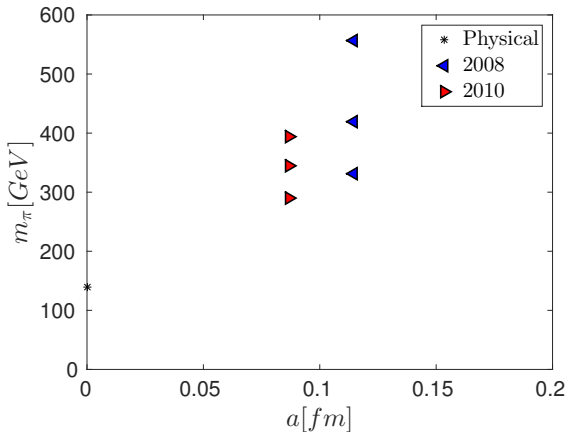
# Going light

RBC-UKQCD  $N_f = 2 + 1$  DWF - Landscape (since 2008)



# Going light

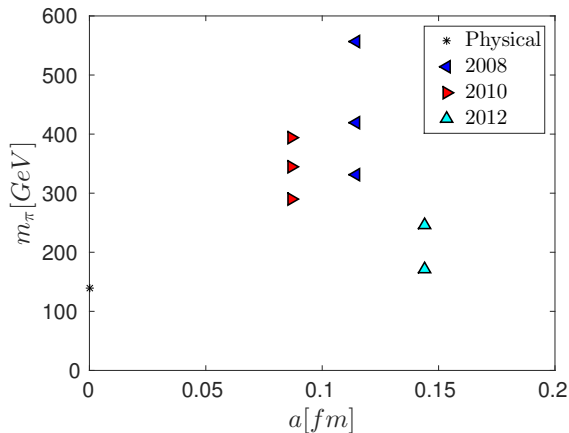
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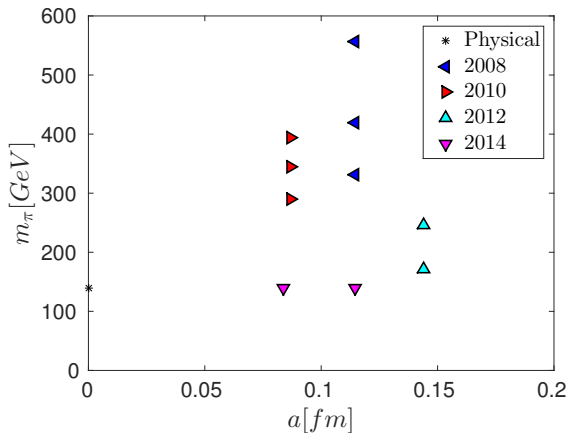
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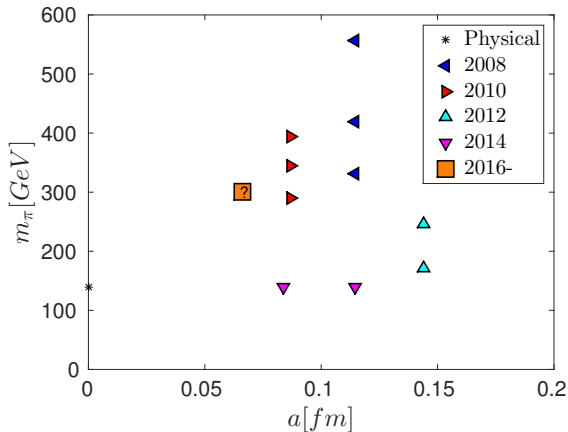
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# Light quarks - Kaon physics

RBC-UKQD has a broad Kaon project, very successful thanks to DiRAC

- $K \rightarrow \pi\pi$ : Matter-Antimatter asymmetry in the Standard Model
  - ⇒ First every realistic computation of a decay amplitude
- Kaon semi-leptonic decay: Determination of  $V_{us}$
- Rare kaon decays: New strategy, important sensitivity to New Physics
- ...

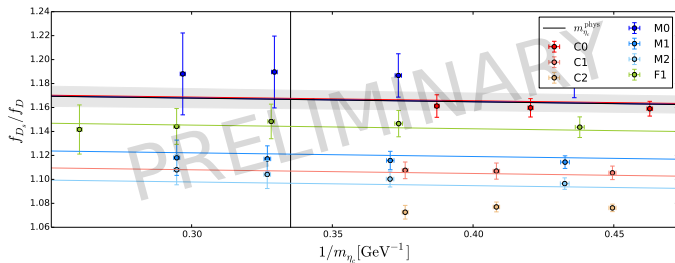
Very important impact in phenomenology !

# D mesons

Decay constant of the  $D(c, \bar{d})$  and the  $D_s(c, \bar{s})$

RBC-UKQCD

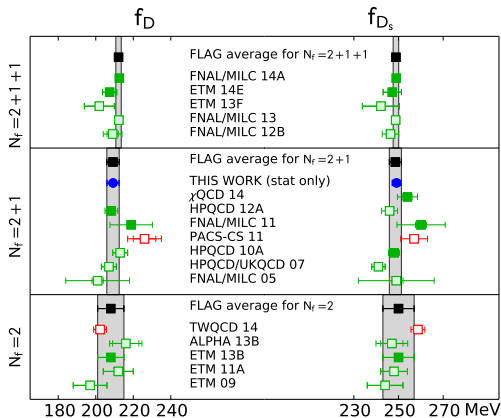
P. Boyle, L. Del Debbio, A. Jüttner, A. Khamseh, M. Marinković, F. Sanfilippo, T. Tsang



Thanks to Andreas Jüttner and Tobias Tsang

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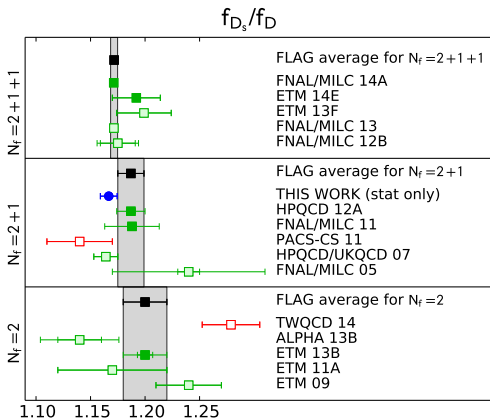
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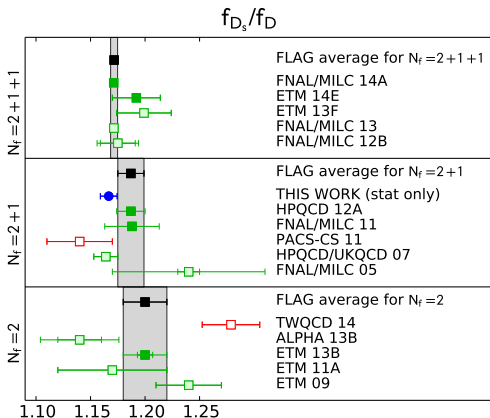
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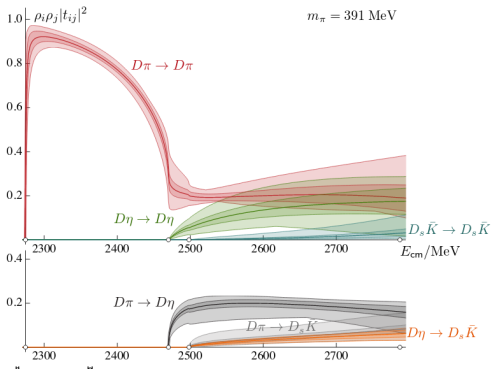
See Poster by Tobias Tsang



# Scattering and spectra

## Hadron Spectrum Collaboration

G Moir, M Peardon, S M Ryan, C E Thomas, D J Wilson

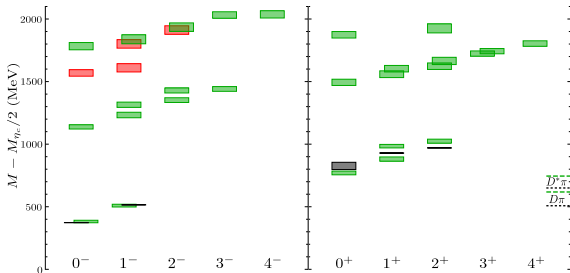


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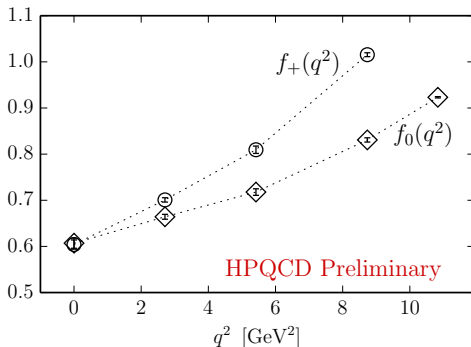


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# B mesons

HPQCD A Lytle, B Colquhoun, C Davies, J Koponen, C McNeile  
See talk by A. Lytle at B-physics conference 2016

Form factors of semi-leptonic decay  $B_c = (\bar{b}, c)$  to  $\eta_c = (\bar{c}, c)$



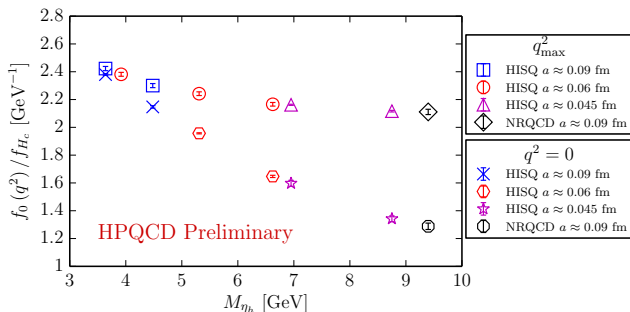
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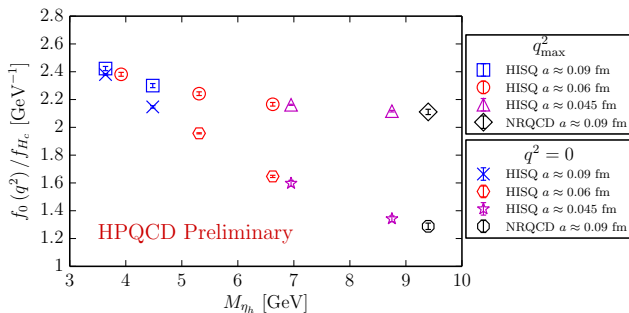
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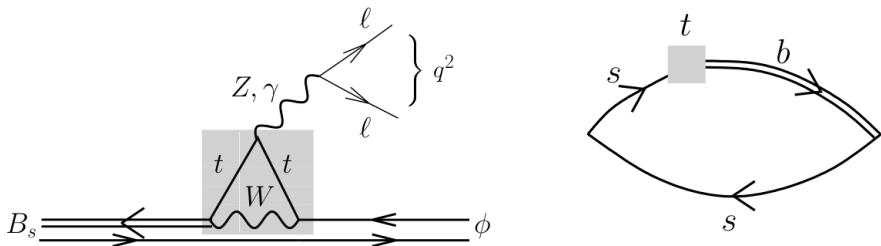
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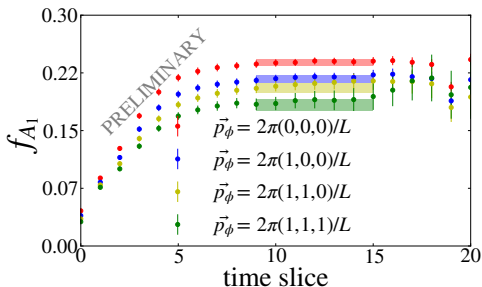
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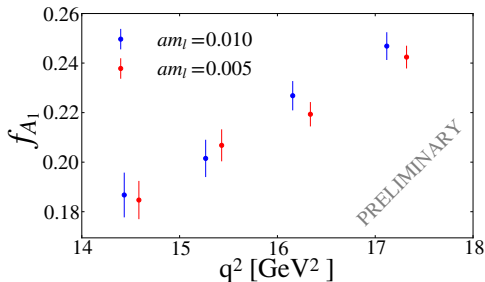
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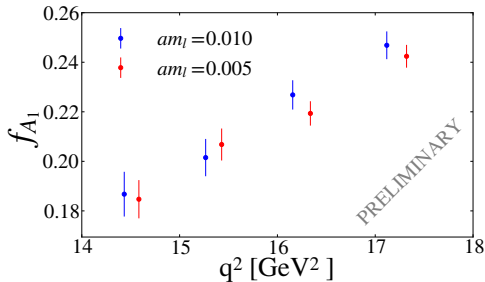
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See Poster by Oliver Witzel

## Internal structure of the proton

# Internal structure of the nucleon

Proton and neutron have spin, what is the contribution of the quarks ?

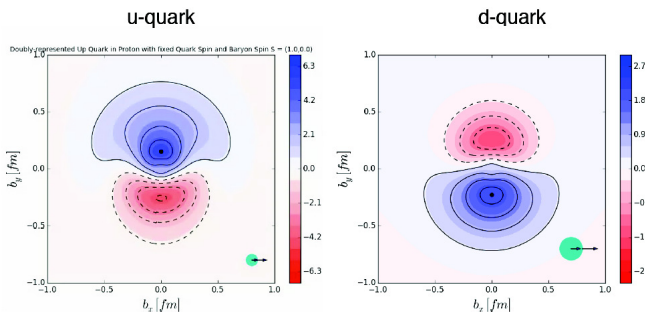
# Internal structure of the nucleon

QCDSF-UKQCD

Bickerton, Horsley, Nakamura, Rakow, Schierholz, Shanahan, Young, Zanotti

See talk by J. Zanotti at lattice 2016

## Spin densities - proton



Courtesy of Roger Horsley

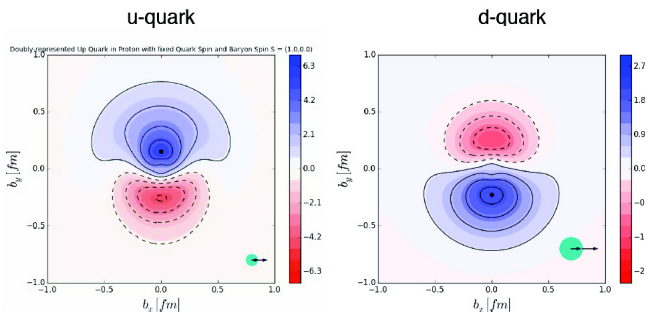
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## Anomalous magnetic moment of the muon

# Anomalous magnetic moment of the muon

An elementary particle of spin  $1/2$ , of spin angular momentum  $\vec{S}$ , charge  $e$ , mass  $m$  has a magnetic moment  $\vec{\mu} = g \frac{e}{2m} \vec{S}$ ,

$g$  is the gyromagnetic ratio, for the muon  $\mu$  the classical value is  $g_{\mu} = 2$

The anomalous moment is a the relative deviation from this value

$$a_{\mu} = \frac{g_{\mu} - 2}{2}$$

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$$a_{\mu} = \frac{g_{\mu} - 2}{2}$$

Known very precisely both experimentally and theoretically

$$a_{\mu}^{exp} = 0.001\,165\,920\,91(54)(33)$$

$$a_{\mu}^{the} = 0.001\,165\,918\,03(49)$$

The numbers agree up to  $10^{-8}$ , however there is a steady  $\sim 3 - 4\sigma$  deviation



# Anomalous magnetic moment of the muon

- We are dealing with “small” quantum effects which are very sensitive to new physics
- This quantity can be computed at an impressive level of precision
- New experiment coming up should decrease the experimental error by a factor 4 after a year of running

# Anomalous magnetic moment of the muon

## Contributions to $a_\mu$ PDG, 2015

Contribution	$a_\mu \times 10^{11}$	Uncertainty
QED (5-loop)	116584718.95	0.08
Electroweak (2-loop)	153.6	1.0
LO hadronic (HVP)	6923	42
NLO hadronic	7	26
Theory Total	116591803	49.4
Experiment Total	116592091	63.3

Courtesy of Matt Spraggs

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# Anomalous magnetic moment of the muon

A lot of work is done with DiRAC, recently:

- HPQCD B. Chakraborty, C. T. H. Davies, P. G. de Oliveira, J. Koponen, G. P. Lepage,
- B. Chakraborty, C. T. H. Davies, J. Koponen, G. P. Lepage, M. J. Peardon, S. M. Ryan, PRD'16
- Eric B. Gregory & Craig McNeile
- RBC-UKQCD  
T. Blum, P.A. Boyle, L. Del Debbio, R.J. Hudspith, T. Izubuchi, A. Jüttner, C. Lehner, R. Lewis, K. Maltman, M. Krstić Marinković, A. Portelli, M. Spraggs, JHEP'16  
T. Blum, P.A. Boyle, T. Izubuchi, L. Jin, A. Jüttner, C. Lehner, K. Maltman, M. Marinkovic, A. Portelli, M. Spraggs, PRL'16
- ...

See talk by Christine Davies.  
2pm

## Beyond the Standard Model

# Beyond the Standard Model (BSM)

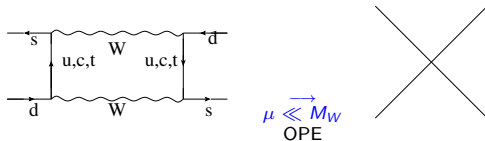
## Different applications, approaches

- New physics effects are important at high energy, but QCD remains a valid description of the strong interaction at low energy. New interaction (at high energy) is visible at low energy through new “effective” operators (e.g. new four-quark operators)
- Lattice simulations can be used to simulate other non-perturbative theory (not QCD), composite Higgs model and Electroweak Symmetry Breaking, strongly interacting Dark Matter ... For example, work by UKQCD-BSM

## Neutral kaon mixing

# Neutral kaon mixing in the SM

Indirect CP violation related to neutral kaon oscillations  
in the SM this occurs though box diagrams with W exchange

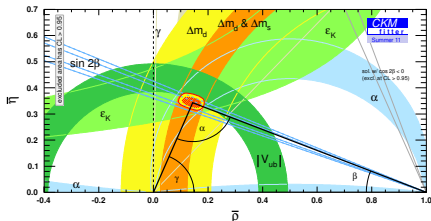


Factorise the non-perturbative contribution into

$$\langle \bar{K}^0 | \mathcal{O}_{LL}^{\Delta S=2}(\mu) | K^0 \rangle = \frac{8}{3} F_K^2 M_K^2 B_K(\mu) \quad \text{w/ } \mathcal{O}_{LL}^{\Delta S=2} = (\bar{s}\gamma_\mu(1-\gamma_5)d)(\bar{s}\gamma^\mu(1-\gamma_5)d)$$

Related to  $\varepsilon$  via CKM parameters, schematically

$$\varepsilon \sim \text{known factors} \times V_{CKM} \times C(\mu) \times B_K(\mu)$$



[CKMfitter'11]



## and beyond

In the SM, neutral kaon mixing occurs through W-exchanges  $\rightarrow (V - A)$

$$O_1^{\Delta s=2} = (\bar{s} (V - A) d) (\bar{s} (V - A) d)$$

Beyond the SM, other Dirac structure appear in the generic Hamiltonian  $H^{\Delta s=2} = \sum_{i=1}^5 C_i(\mu) O_i^{\Delta s=2}(\mu)$ .

We express them in terms of Lorentz matrices **V**ector, **A**xial, **S**calar, **P**seudo-scalar, **T**ensor

$$(V - A) \times (V + A)$$

$$(S - P) \times (S + P)$$

$$(S - P) \times (S - P)$$

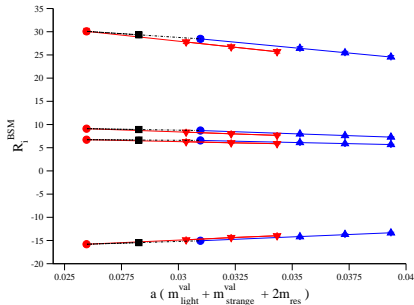
$$TT \times TT$$

$\Rightarrow$  On the lattice, we compute  $\langle \bar{K}^0 | O_i^{\Delta s=2} | K^0 \rangle$  in a model independent way

# Results

- I show the ratios

$$R_i^{\text{BSM}} \sim \frac{\langle \bar{K}^0 | O_i | K^0 \rangle}{\langle \bar{K}^0 | O_1 | K^0 \rangle} \sim \text{BSM/SM}$$



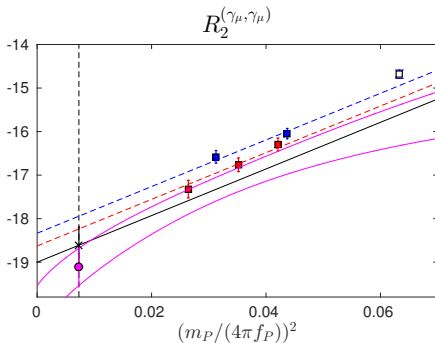
$$R_i^{\text{BSM}} \sim O(10)$$

⇒ combined with experimental values of  $\Delta m_K$  and  $\varepsilon$ , provides important constraints on BSM theories.

## RBC-UKQCD

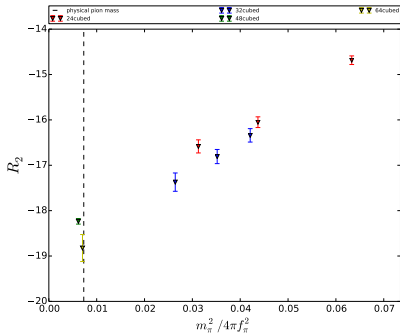
N.G., Hudspith, Lytle

Current work



# BSM kaon mixing - Results

Work in progress  
See poster by Julia Kettle at Lattice 2016



Courtesy of Julia Kettle

## Energy Momentum Tensor

## UKQCD-BSM

F Capponi, L Del Debbio, A Patella, A Rago

See talk by F Capponi at lattice 2016

The renormalization of the Energy Momentum Tensor plays a crucial role in many aspects of non perturbative physics, from the thermodynamics of strongly interacting theories to the study of BSM models.

### Thermodynamic quantities

$$\langle \epsilon - 3p \rangle_T = - \langle \hat{T}_{\mu\mu} \rangle_T \quad ; \quad \langle s \rangle_T = \left( - \langle \hat{T}_{00} \rangle_T + \sum_{i=1}^3 \langle \hat{T}_{ii} \rangle_T \right) / T$$

### Transport coefficients

$$\eta = \pi \lim_{\omega \rightarrow 0} \text{Im} \left\{ \left[ i \int_0^\infty dt e^{i\omega t} \int d^3x \langle \hat{T}_{12}(t, x) \hat{T}^{12}(0, 0) \rangle_T \right] \right\}$$

### Study of conformal field theories:

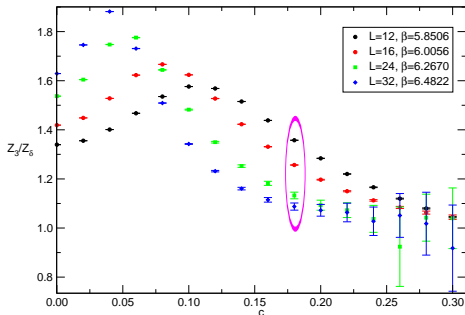
$\langle \mathcal{T}_\mu^\mu(x) \rangle$  as order parameter

# EMT

## UKQCD-BSM

F Capponi, L Del Debbio, A Patella, A Rago

See talk by F Capponi at lattice 2016



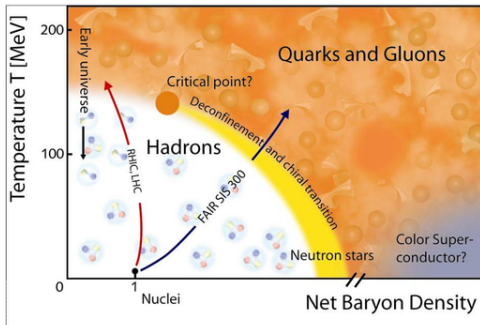
Courtesy of Francesco Capponi

## QCD under extreme conditions



# QCD phase diagram

So far I have only discussed  $T = \mu = 0$ , but the phase diagram is rich



# QCD under extreme conditions

For  $T, \mu \neq 0$ , standard MonteCarlo methods fail (sign-problem)

Recent development using DiRAC

- Complex Langevin (Swansea, ...)
- Density of states (Liverpool, Plymouth, Swansea)

# Conclusions and outlook

Lattice QCD plays a crucial role in our understanding of Particle Physics

Thanks to DiRAC, the UK has massive impact in this field !

- Precision phenomenology
- New strategies, new observables
- Not only traditional QCD, but also BSM and QCD under extreme conditions

## BACKUP SLIDES

Enter at your own risks

## BSM kaon mixing - Results

	ETM 12	ETM 15	RBC – UKQCD 12	SWME 15
	<i>RI – MOM</i>	<i>RI – MOM</i>	<i>RI – MOM</i>	1 – loop
$B_2$	0.47(2)	0.46(3)	0.43(5)	0.525(1)(23)
$B_3$	0.78(4)	0.79(5)	0.75(9)	0.772(5)(35)
$B_4$	0.75(3)	0.78(5)	0.69(7)	0.981(3)(61)
$B_5$	0.60(3)	0.49(4)	0.47(6)	0.751(8)(68)

⇒ Important discrepancy for  $B_4$  and  $B_5$

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⇒ Important discrepancy for  $B_4$  and  $B_5$

New RBC-UKQCD results [N.G., R.Hudspith, A.T. Lytle] (in preparation)

	RBC – UKQCD 16(prelim.)	
	<i>RI – SMOM</i>	<i>RI – MOM</i>
$B_2$	0.488(7)(17)(2)	0.417(6)(2)(2)
$B_3$	0.743(14)(64)(3)	0.655(12)(44)(2)
$B_4$	0.920(12)(12)(4)	0.745(9)(28)(3)
$B_5$	0.707(8)(34)(3)	0.555(6)(53)(2)

Difference seems to come from the renormalisation procedure

## Heavy-dense QCD

Based on [\[NG & Langfeld, 1605.02709\]](#)

## Moment expansion