

# New Approaches to Dark Matter

Justin Khoury (U. Penn)

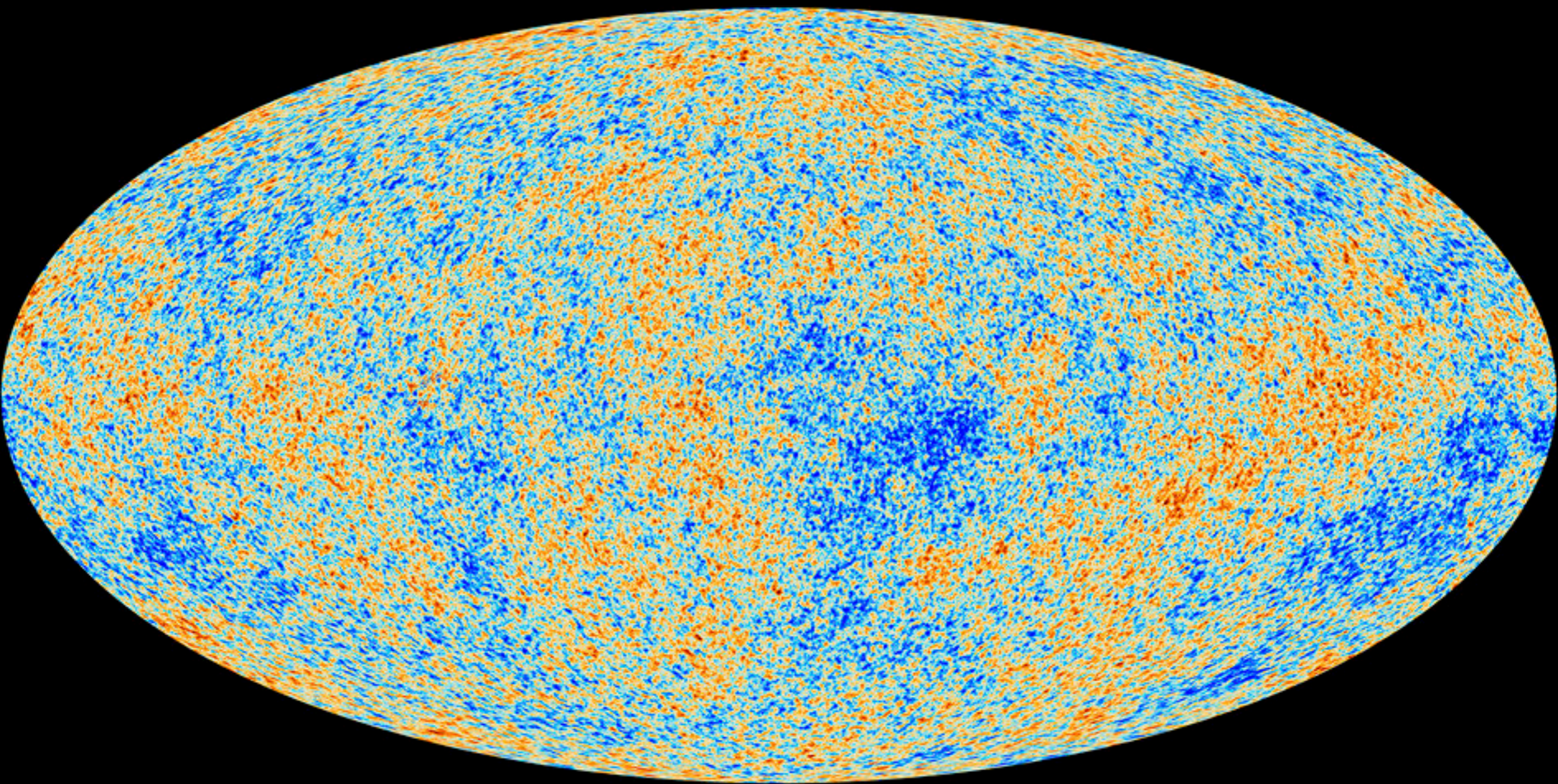
L. Berezhiani & JK, 1506.07877 + 1507.01019

JK 1602.05691

Ongoing work with

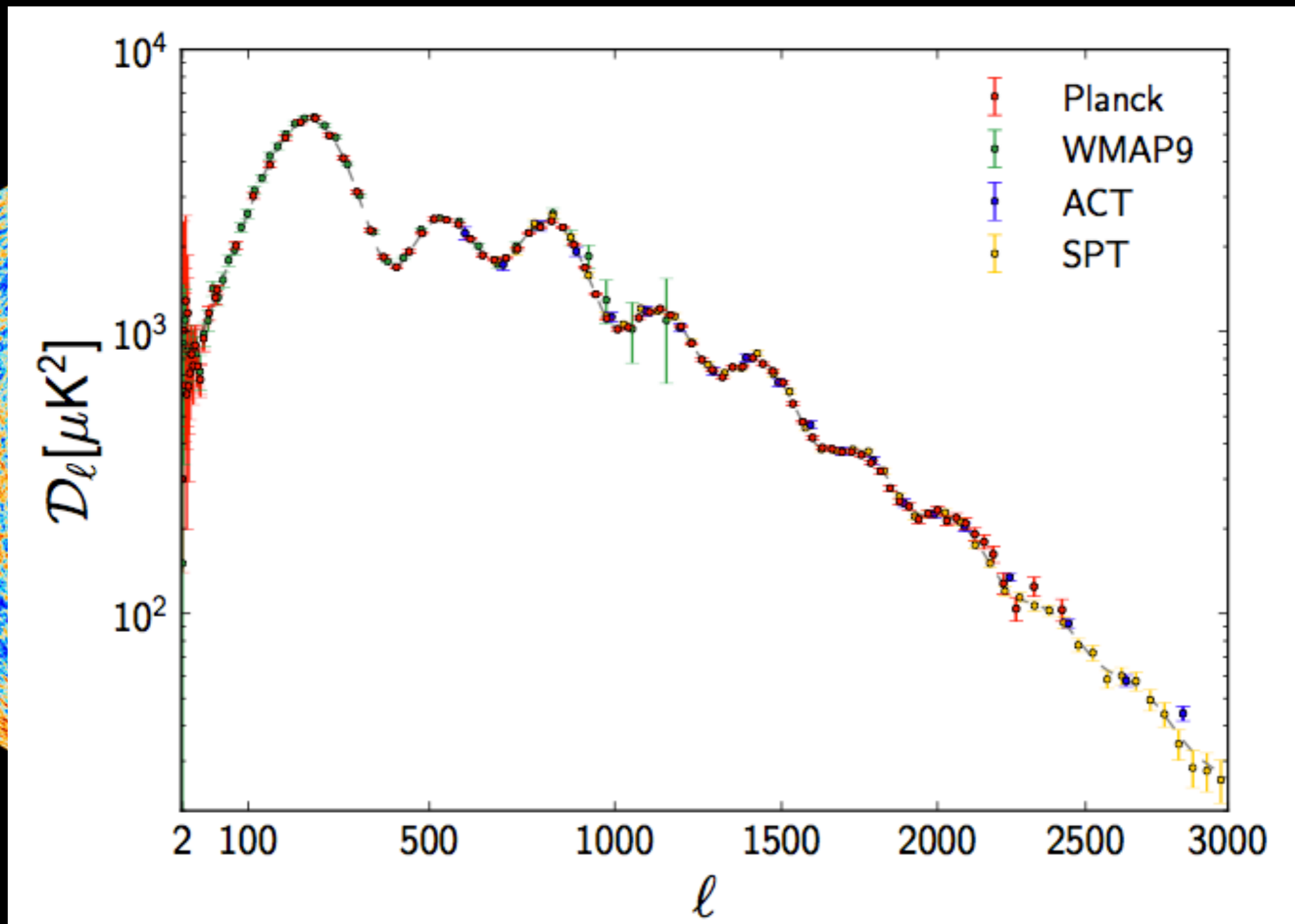
L. Berezhiani, B. Elder, B. Famaey, G. Kartvelishvili, T. Lubensky,  
V. Miranda, A. Sharma, A. Solomon

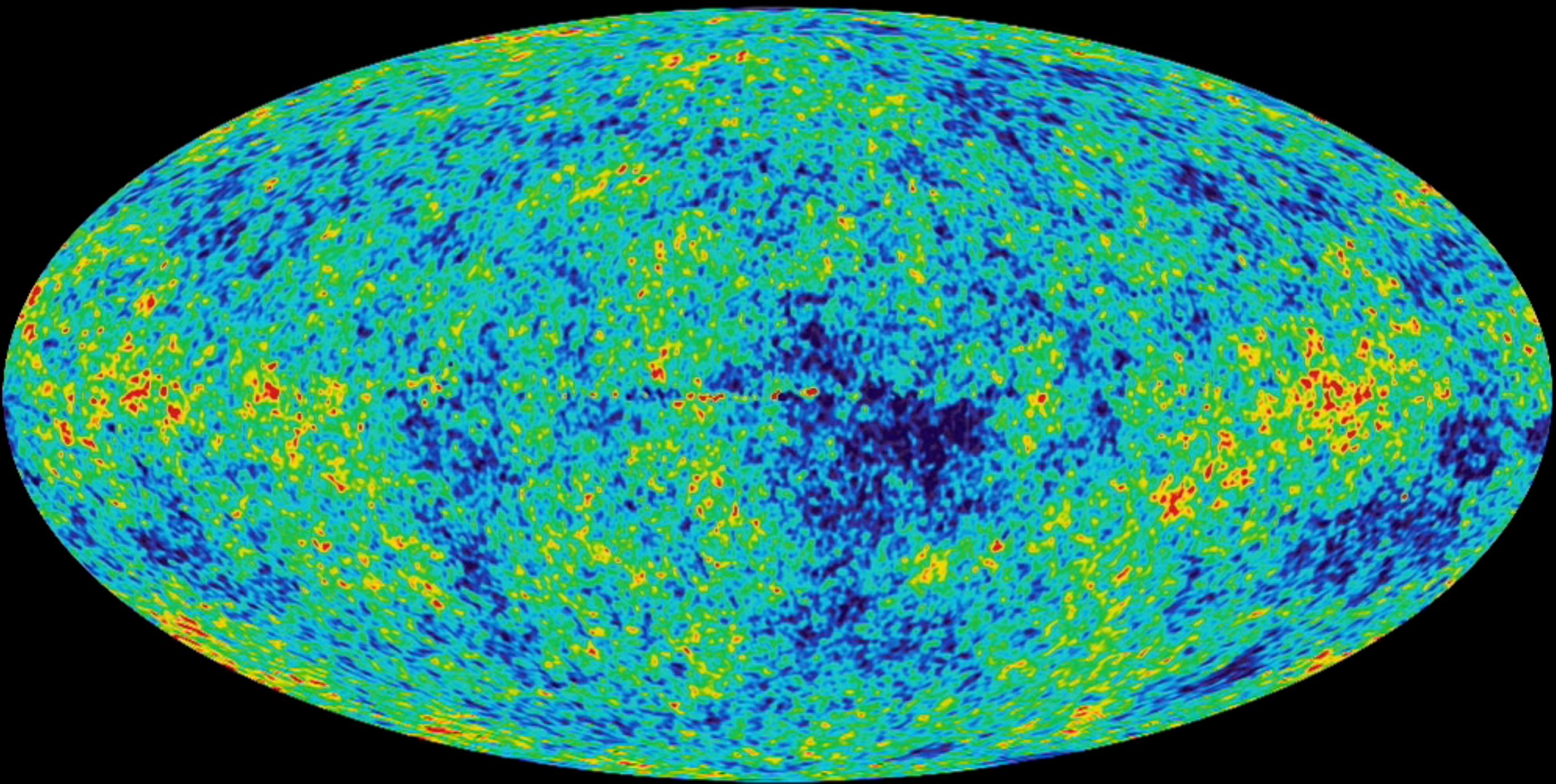
Large-scale evidence



ESA Planck Science Team

# Large-scale evidence





NASA/WMAP Science Team

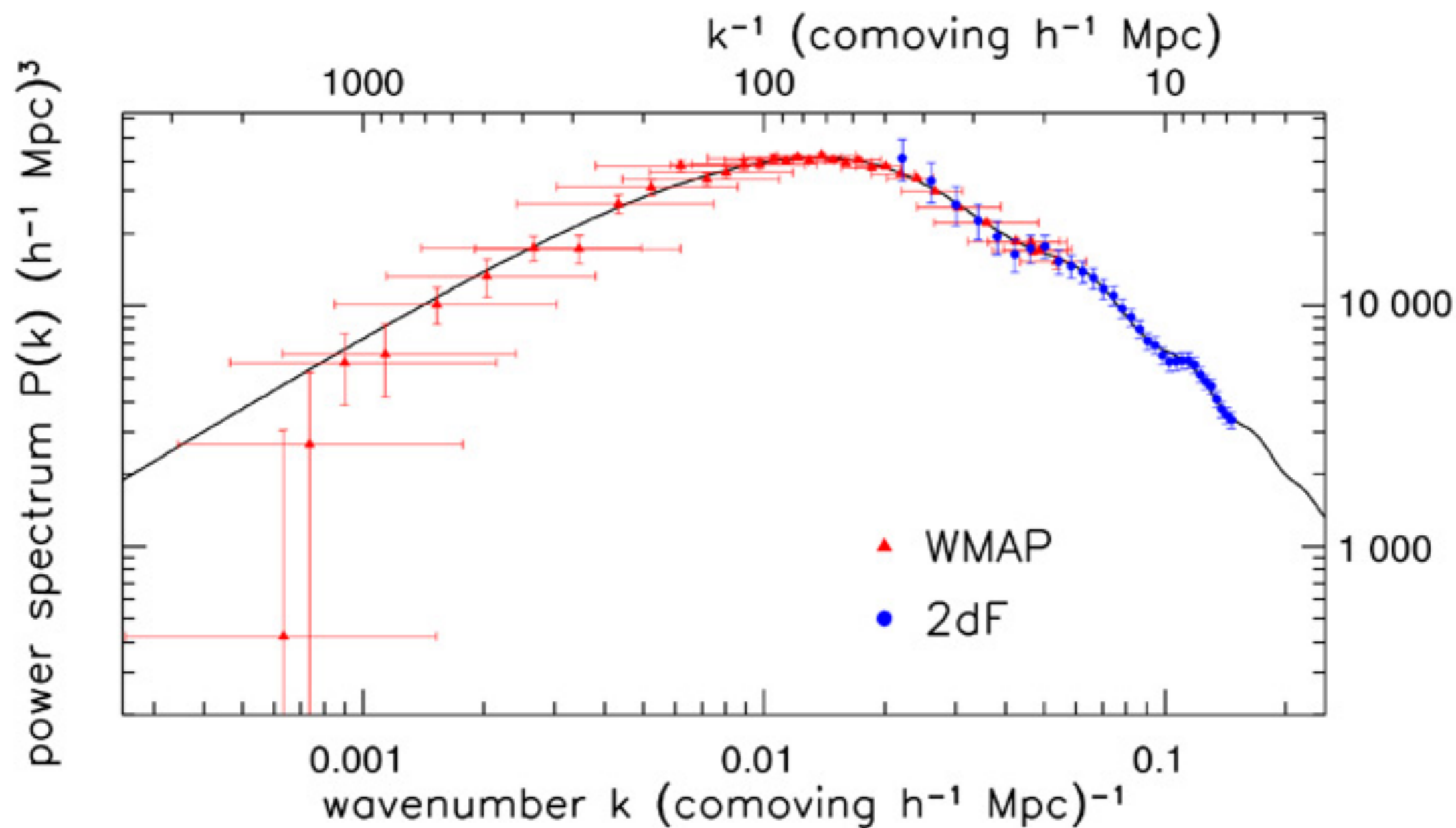


Fig 8.17 (A. Sanchez) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

# The coarse-grained success

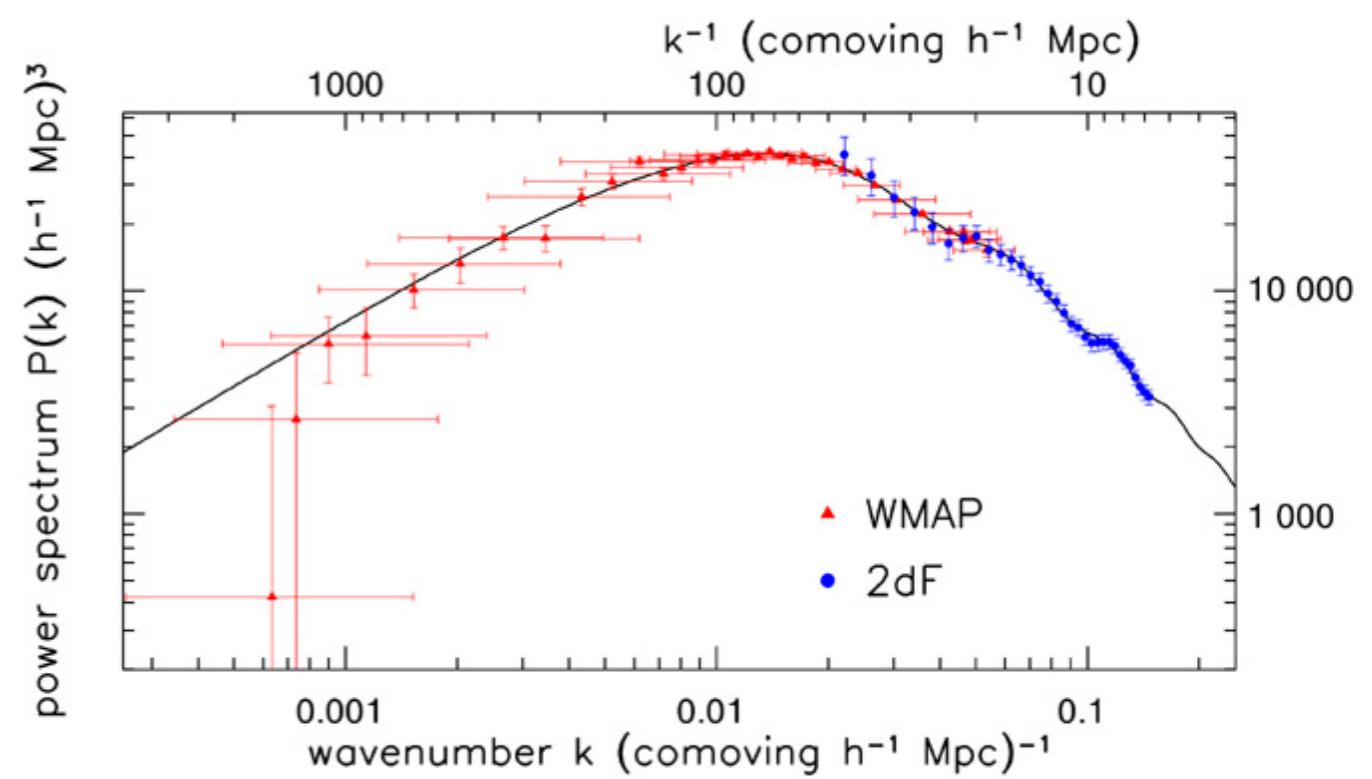
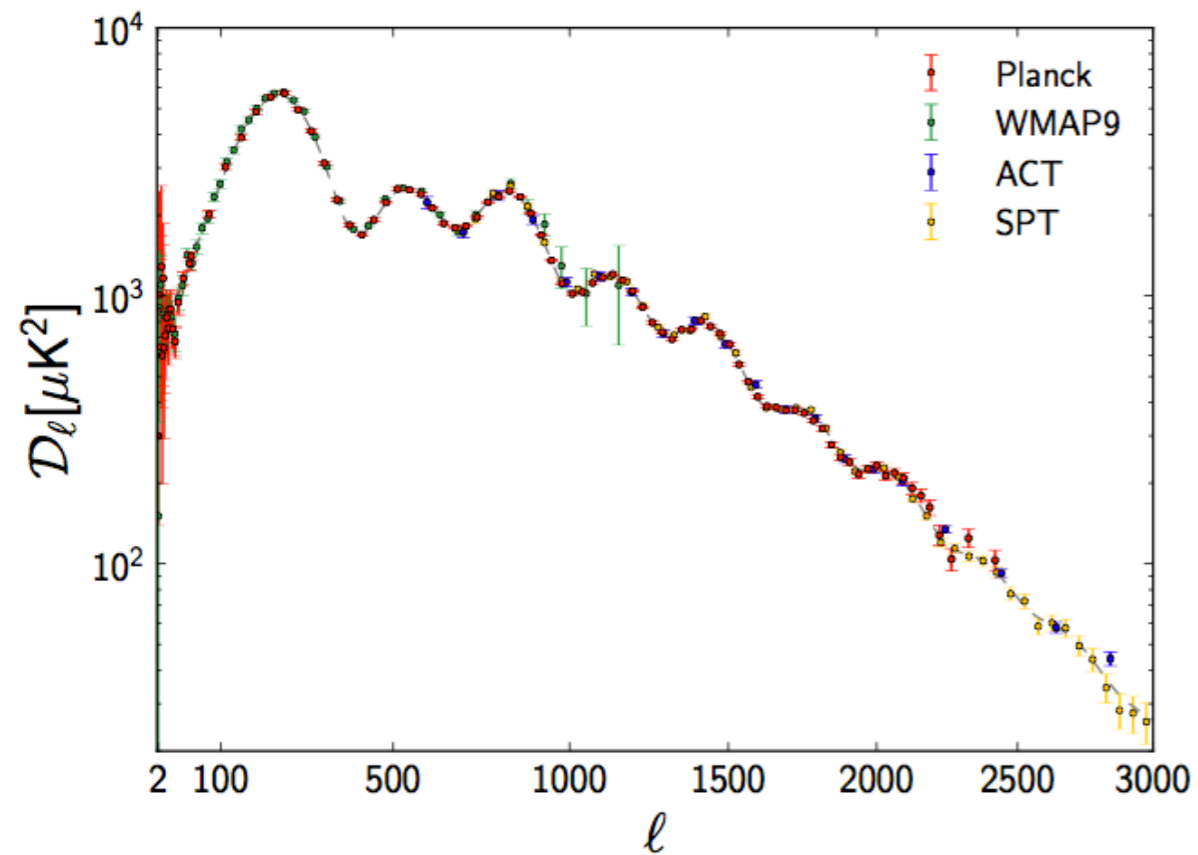


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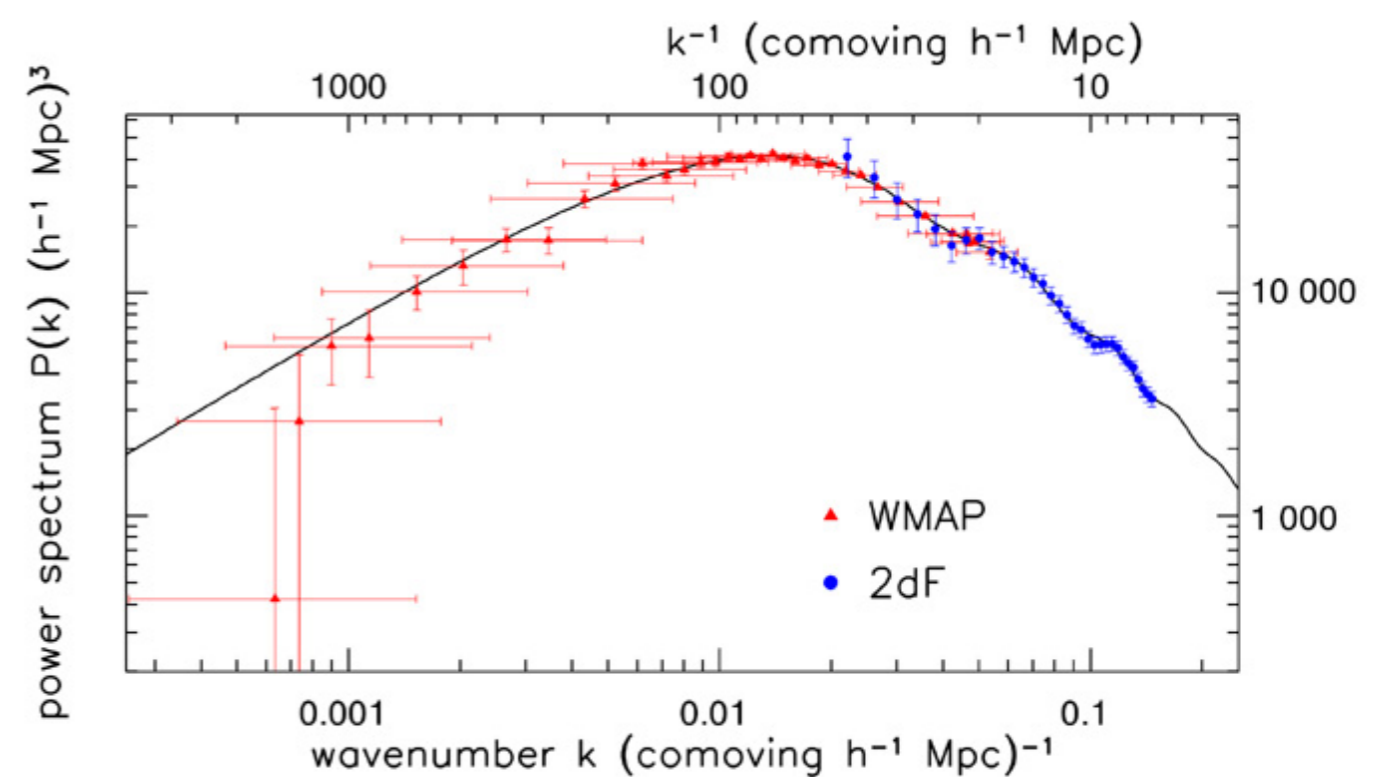
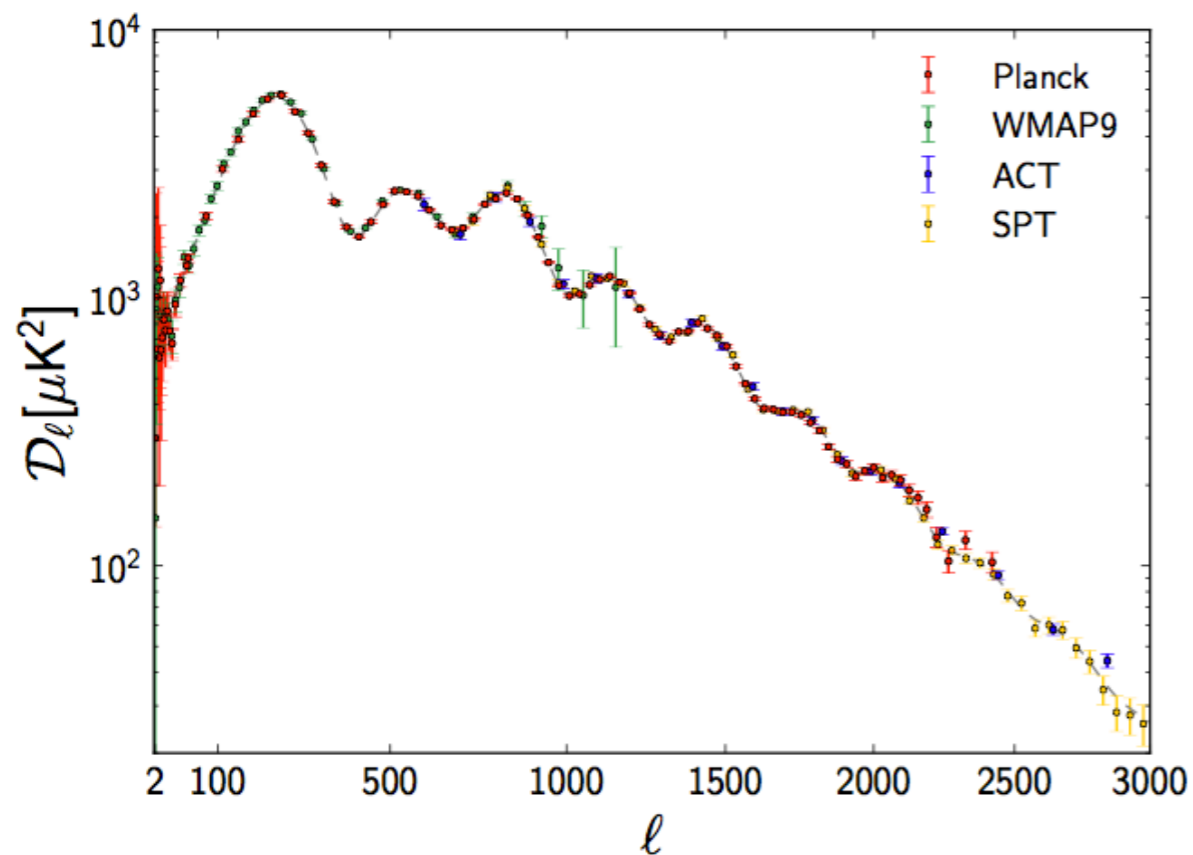


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- On large (linear) scales, only use the hydrodynamical limit of DM

$$T_{\mu\nu} = (\rho + P)u_{\mu}u_{\nu} + P g_{\mu\nu}$$

⇒ Any perfect fluid with  $P \simeq 0$  and  $c_s \simeq 0$  does the job.

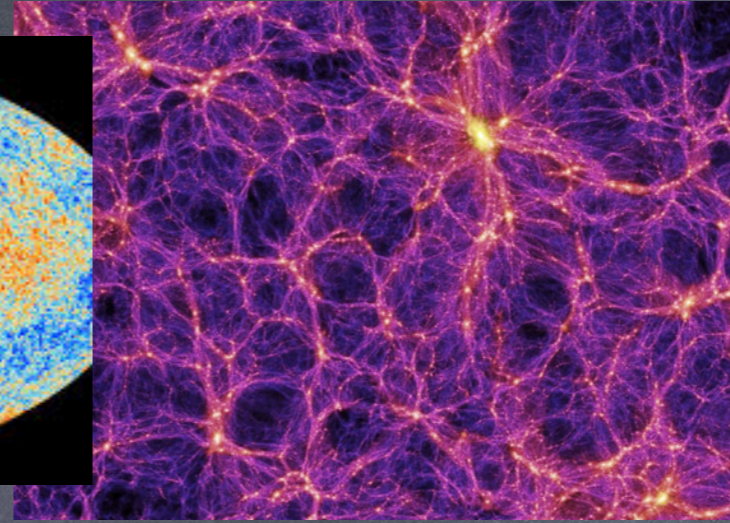
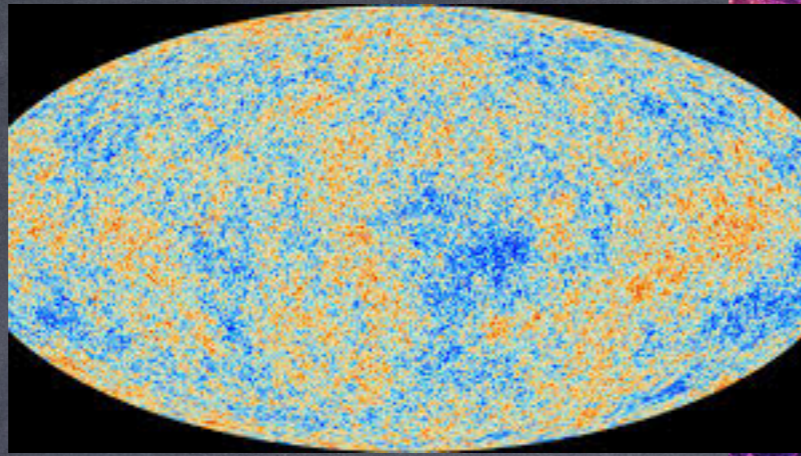
Cleanest evidence for DM, but does not offer much information about DM microphysics

Dark matter is generally assumed to consist of subatomic particles (WIMPs, axions, etc.), with negligible interactions among themselves and with ordinary matter (other than gravity).





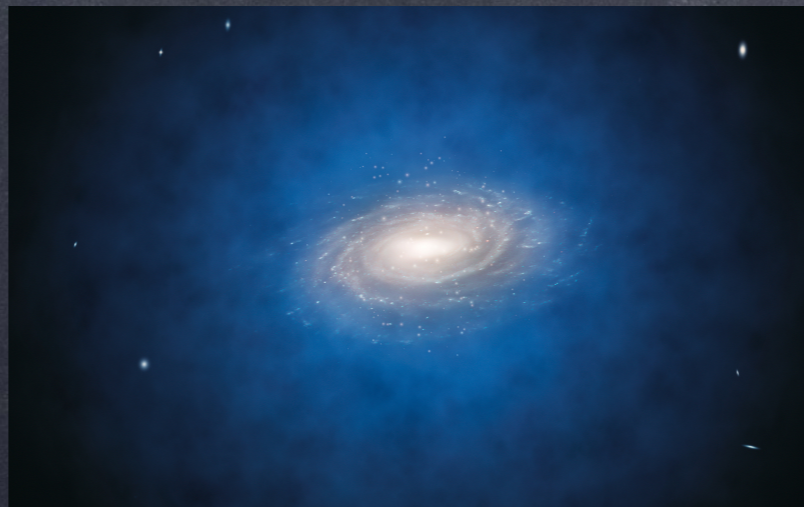
Cosmic web



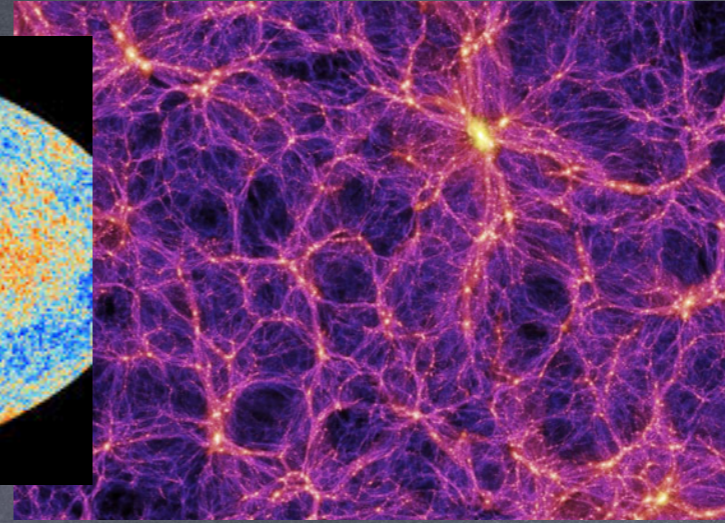
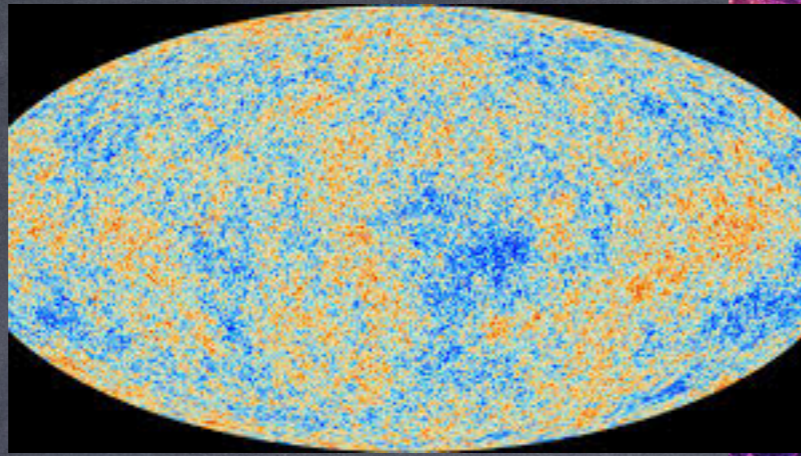
Galaxy clusters



Galaxies



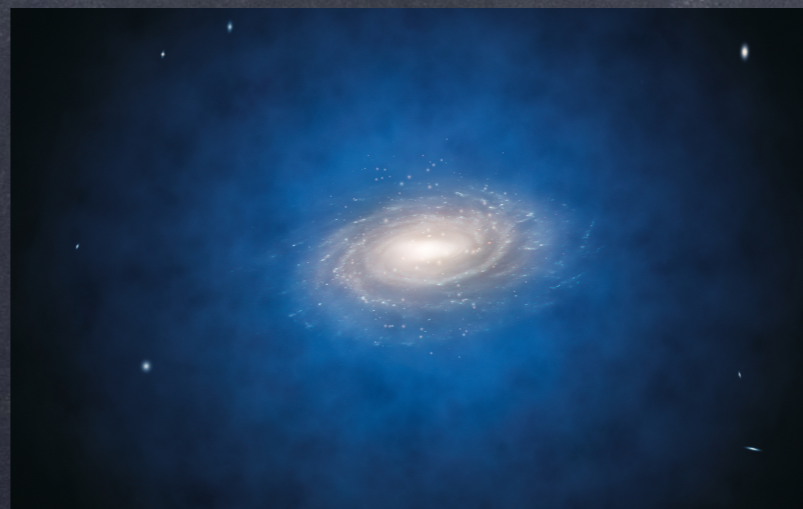
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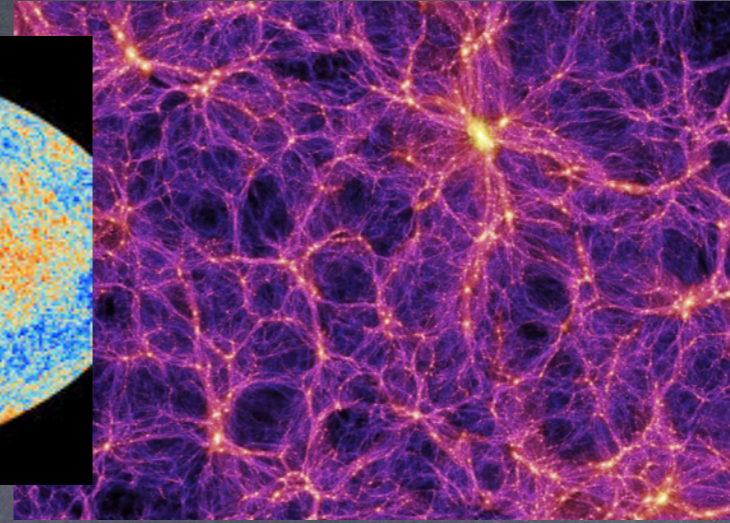
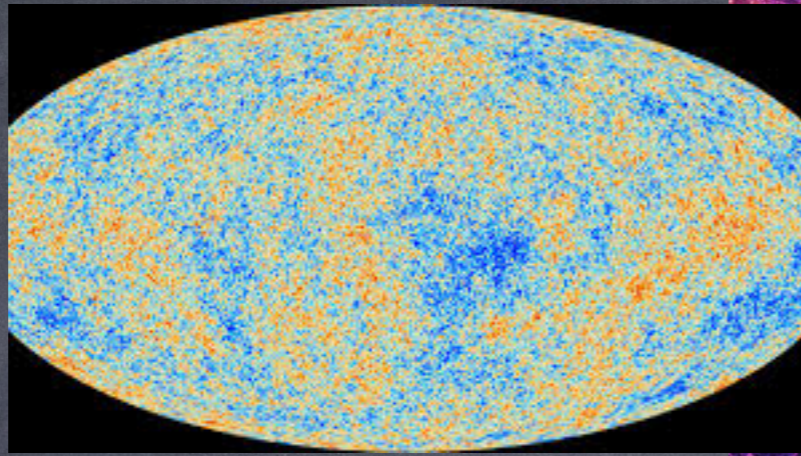
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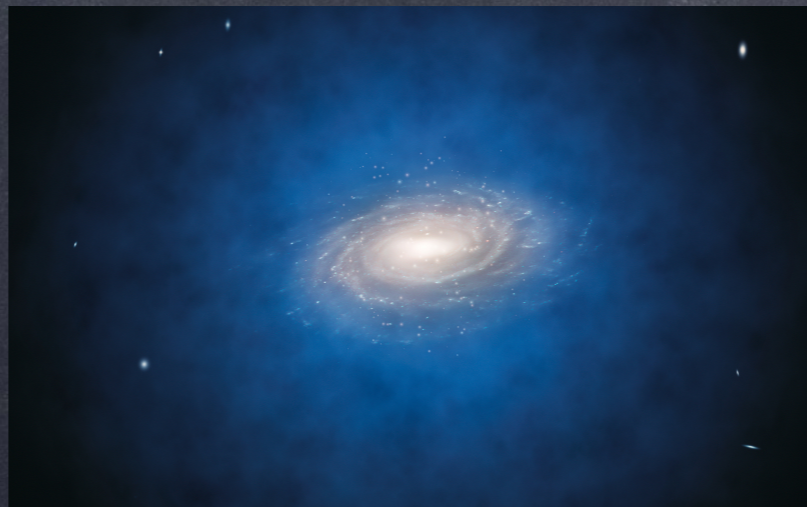
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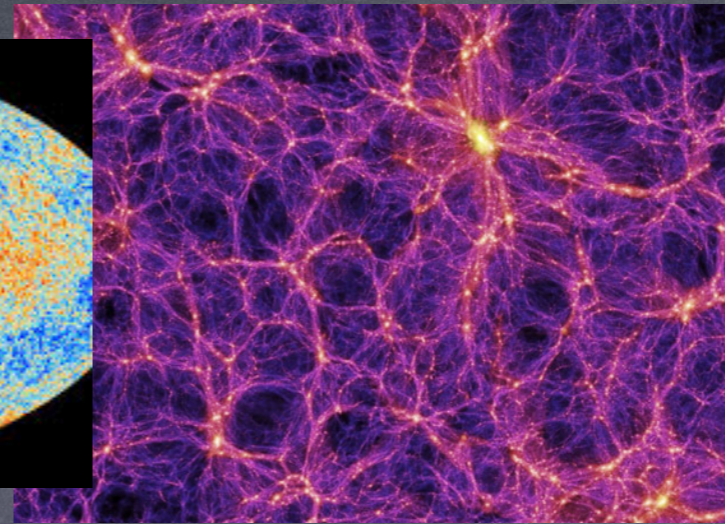
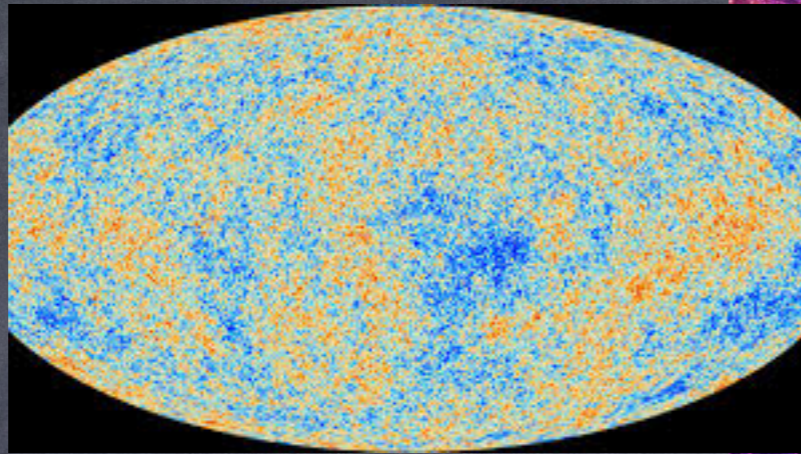
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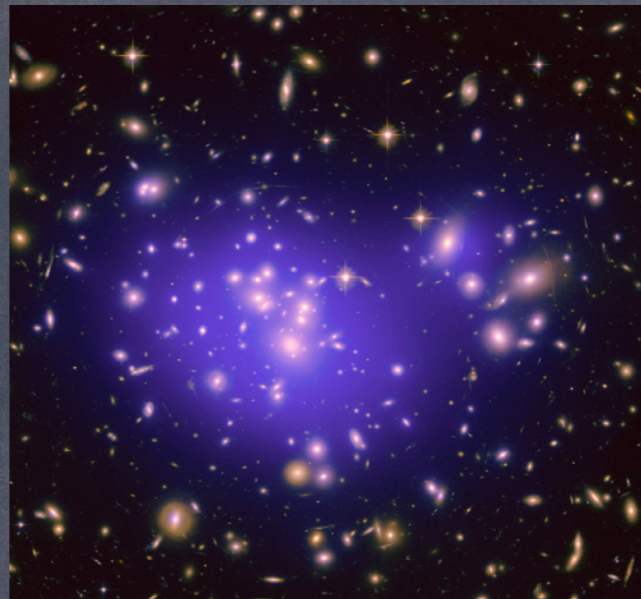
Galaxies



Cosmic web



Galaxy clusters



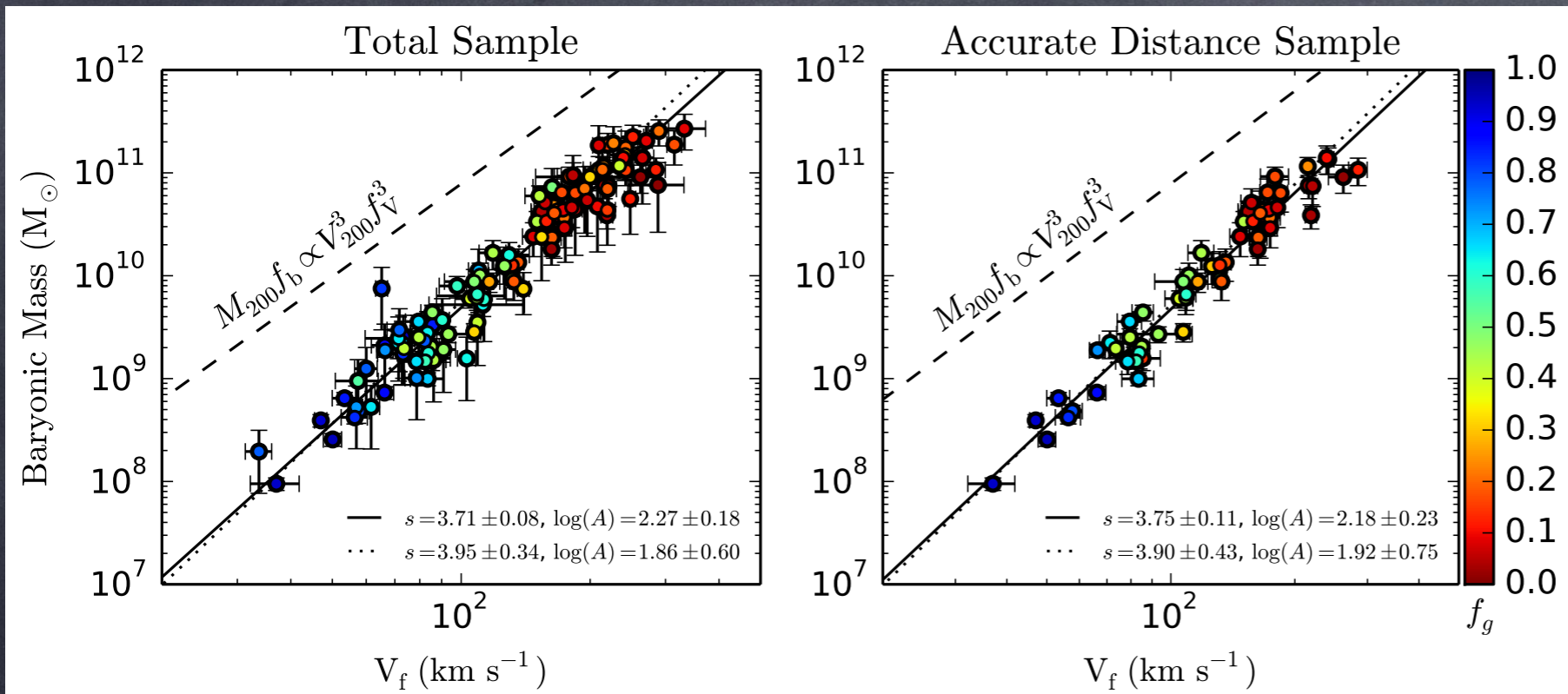
Galaxies



# The Conspiracy in Galaxies

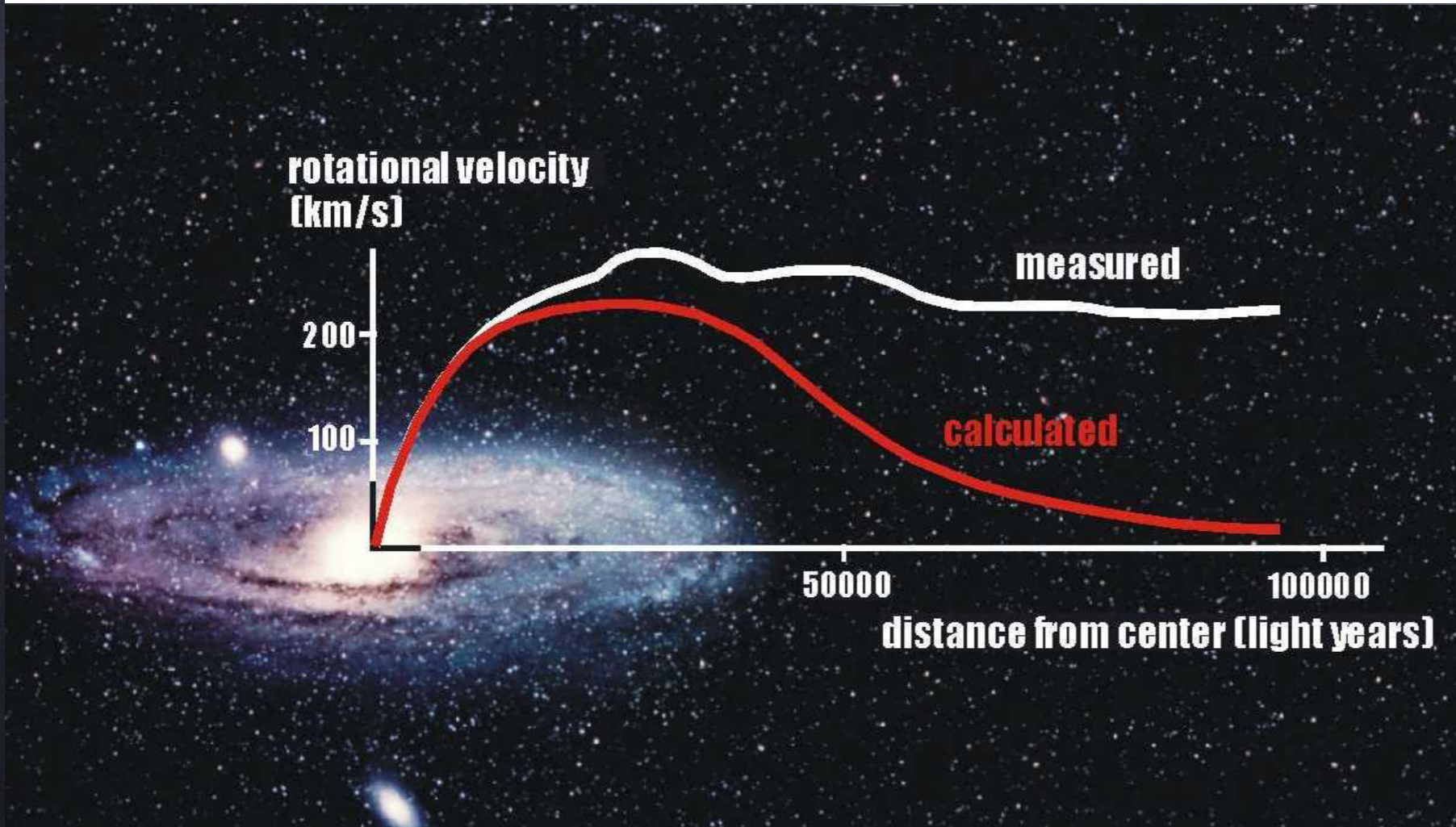
# Baryonic Tully-Fisher relation

McGaugh (2015)



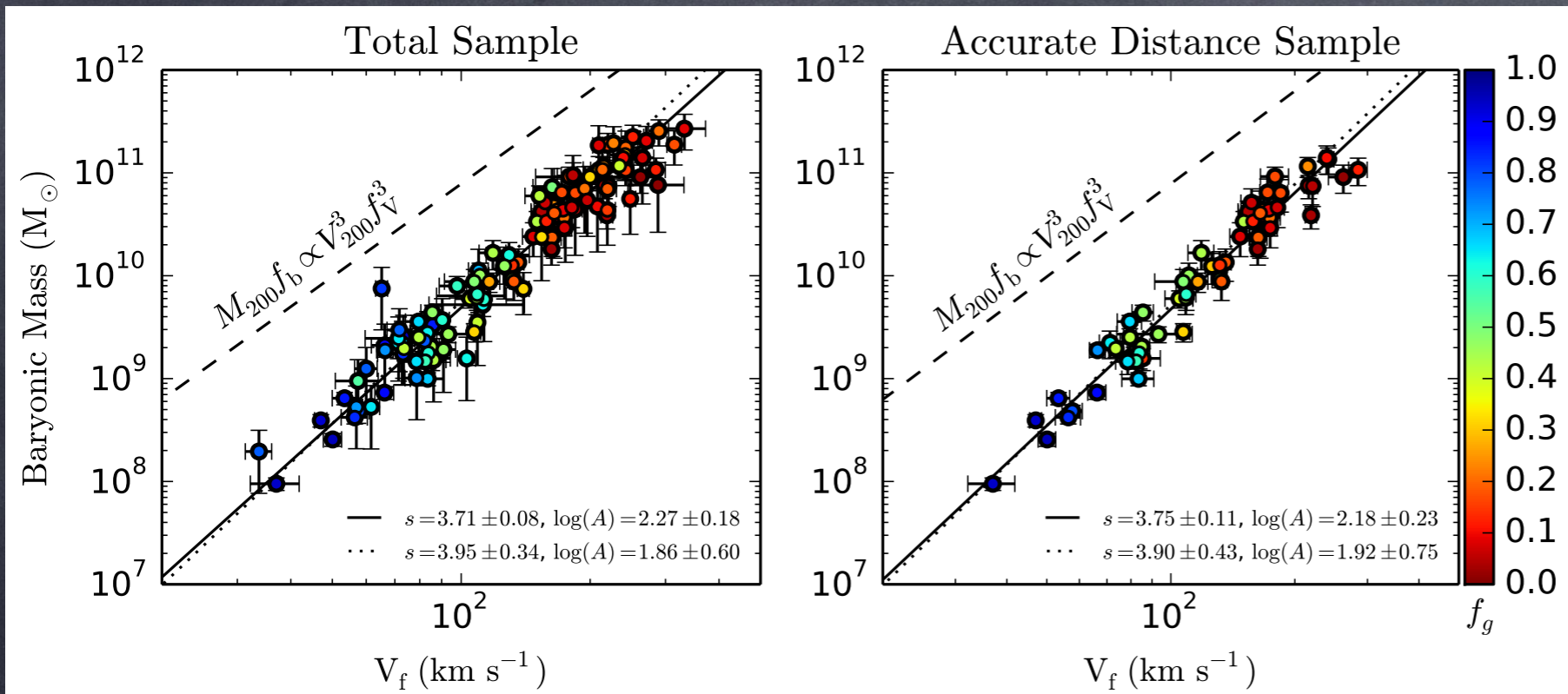
$$v_{\text{flat}}^4 = a_0 G_N M_b$$

$$a_0 = 1.2 \times 10^{-8} \text{ cm/s}^2$$



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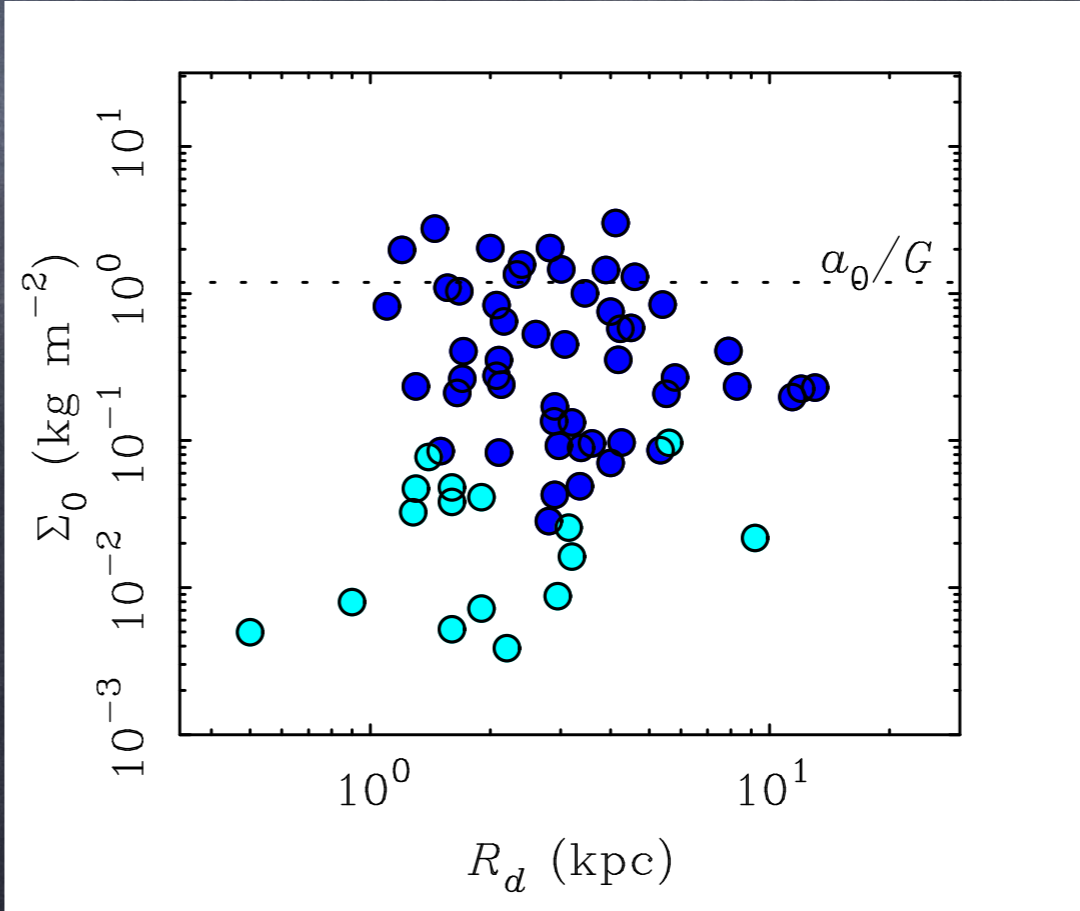
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# Freeman limit

$\Sigma \equiv$  surface brightness

$$\Sigma \lesssim \frac{a_0}{G_N}$$



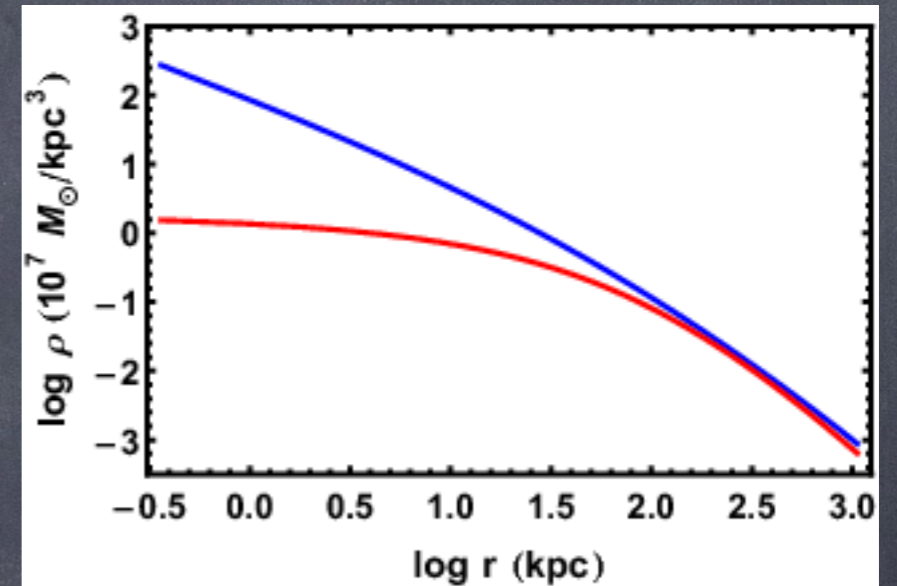
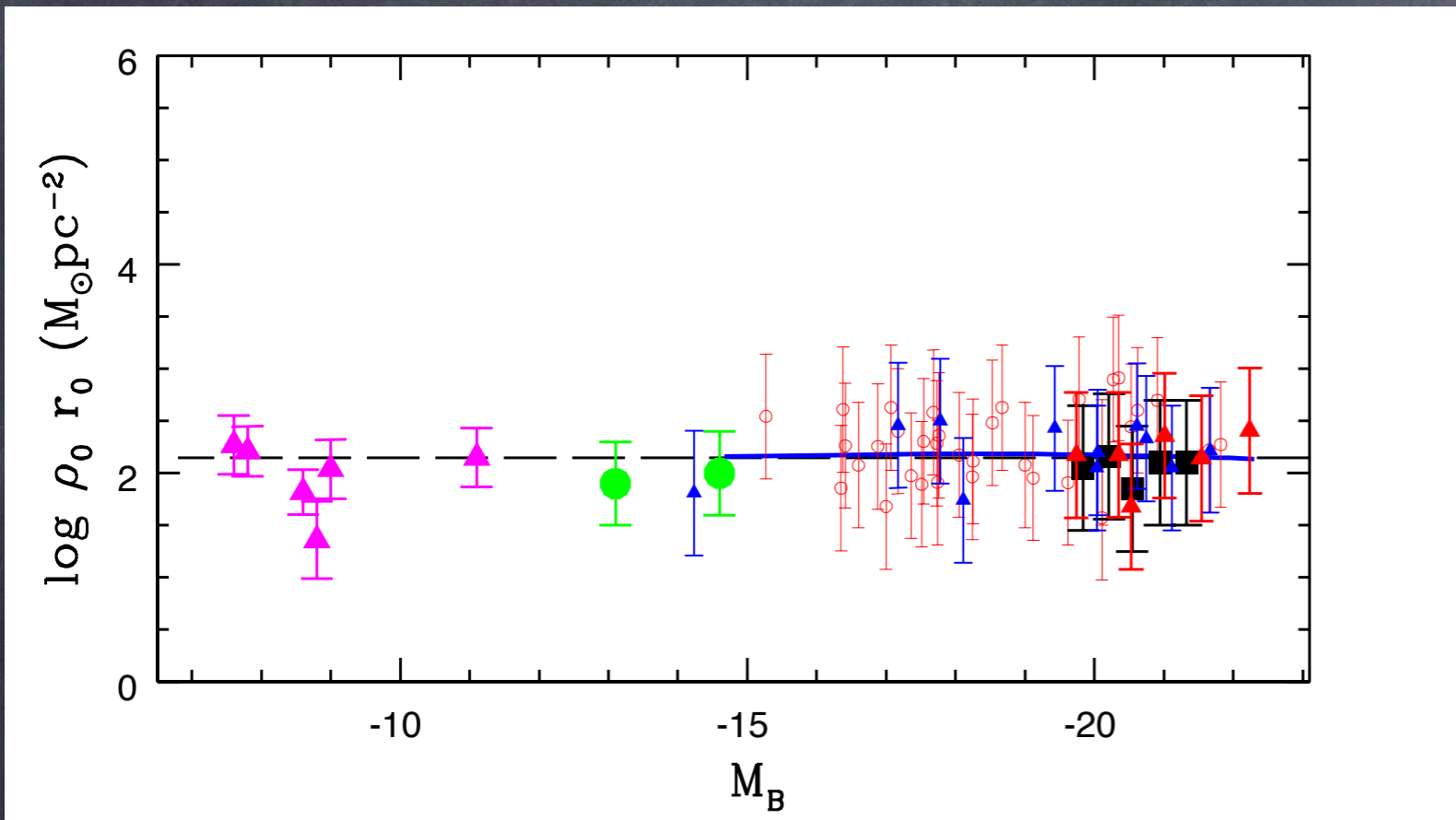


# Universal DM central "surface brightness"

Donato et al. (2009)

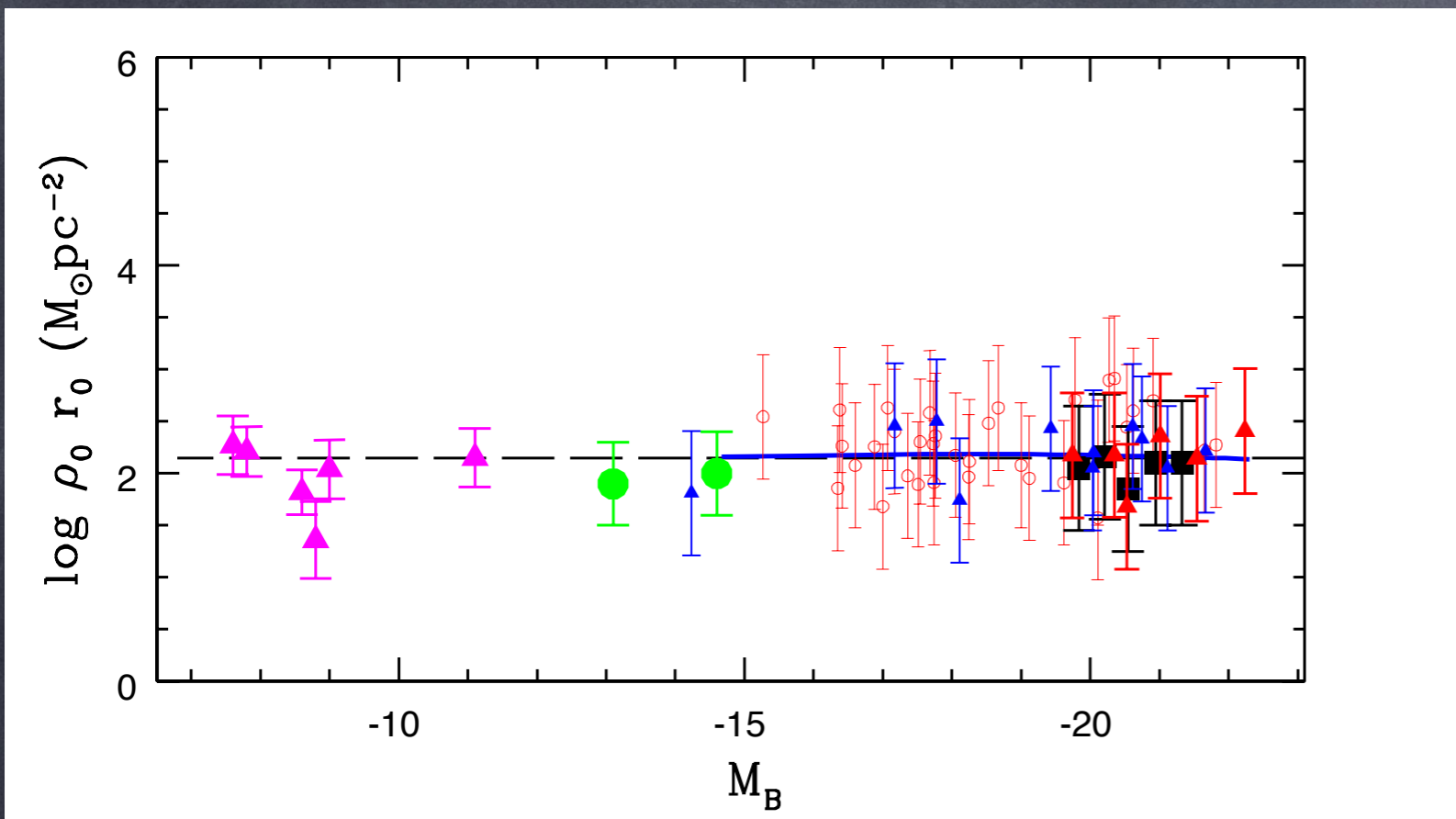
Fit to Burkert profile:

$$\rho(r) = \frac{\rho_0 r_0^3}{(r + r_0)(r^2 + r_0^2)}$$



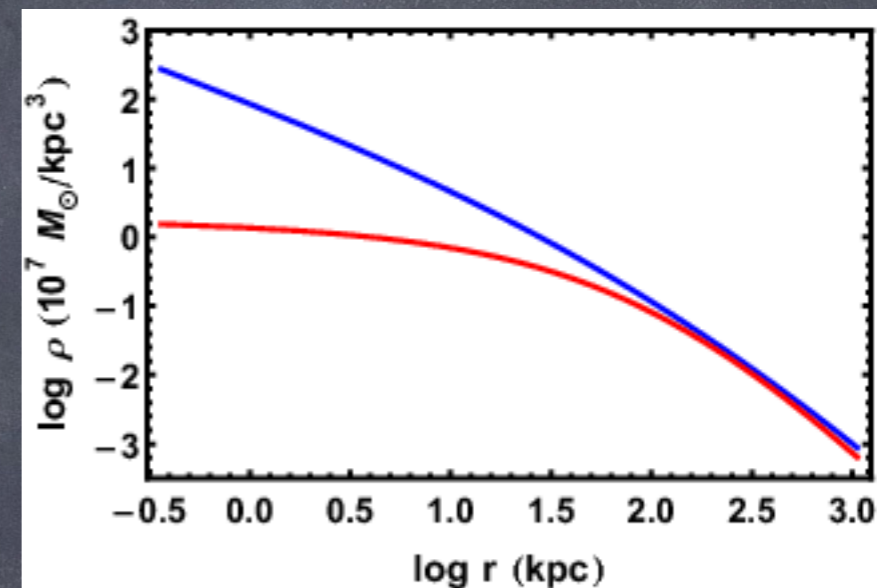
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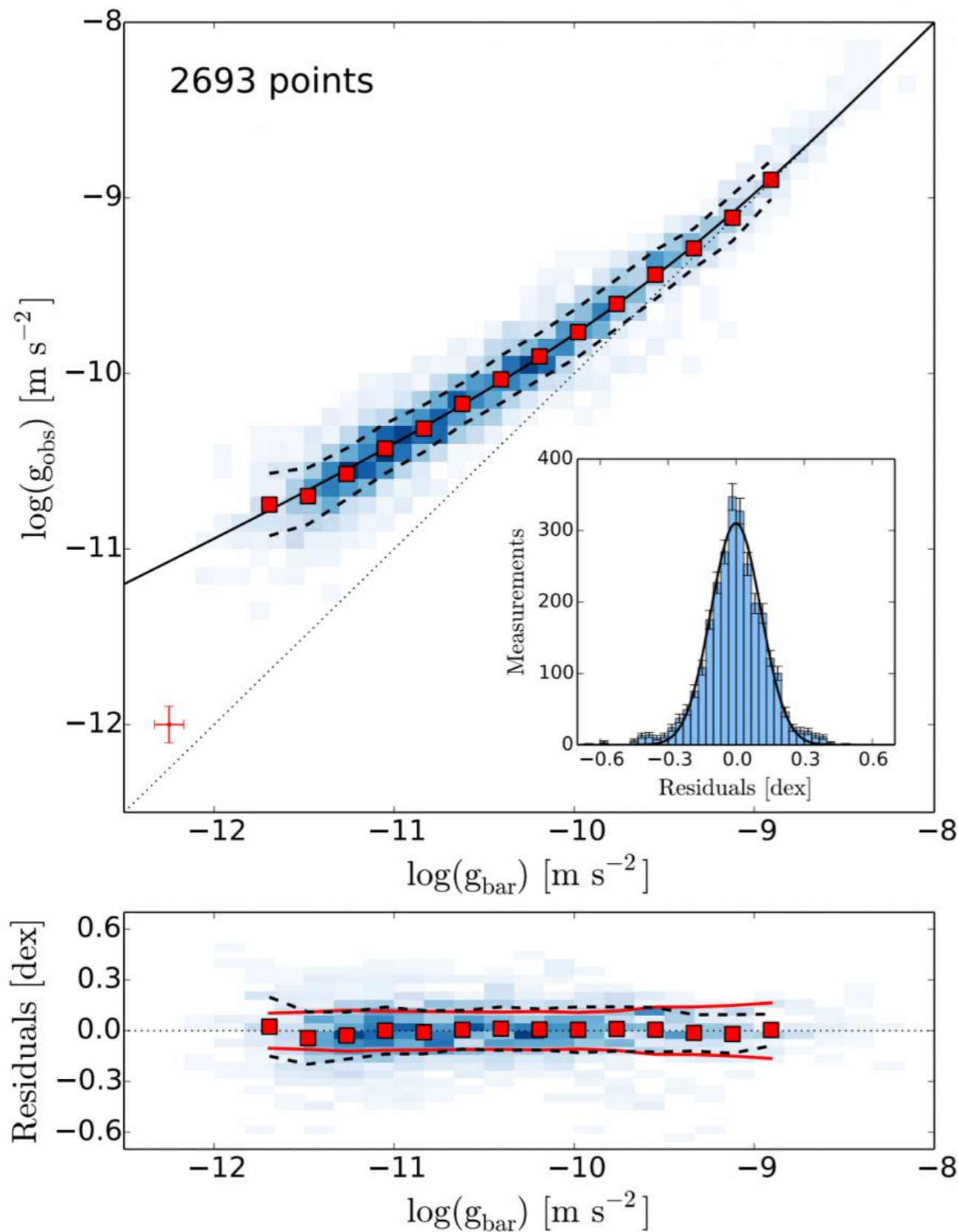


$$\rho_0 r_0 = 140^{+80}_{-30} M_\odot/\text{pc}^2$$

Note:  $\frac{a_0}{2\pi G_N} = 138 M_\odot/\text{pc}^2$

# Baryons dictate everything!

McGaugh, Lelli & Schombert, 1609.05917



- 153 galaxies analyzed

- Fitting form:

$$g_{\text{obs}} = \frac{g_{\text{bar}}}{1 - e^{-\sqrt{g_{\text{bar}}/g_*}}}$$

$$g_* = \left(1 \pm 0.2 \text{ (syst.)}\right) \times a_0$$

Those are facts.

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The acceleration scale  $a_0$  is in the data.

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Can take one of 3 attitudes...

# One extreme: It's all feedback!

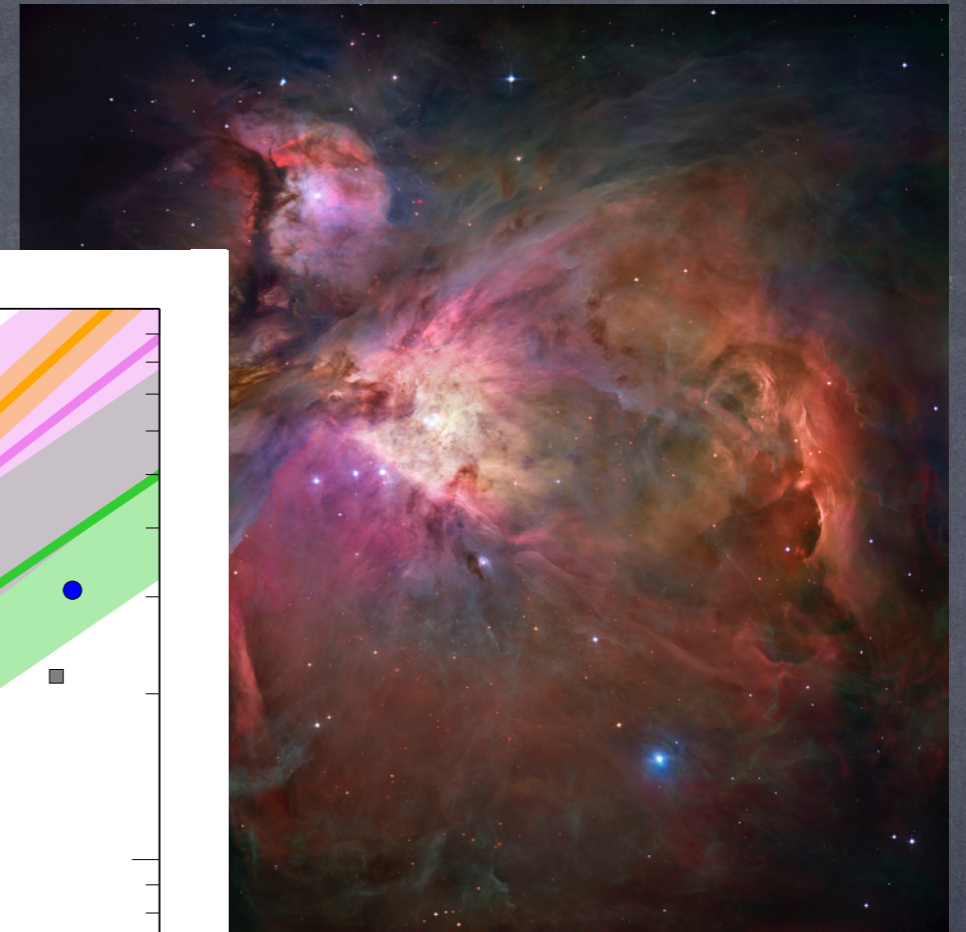
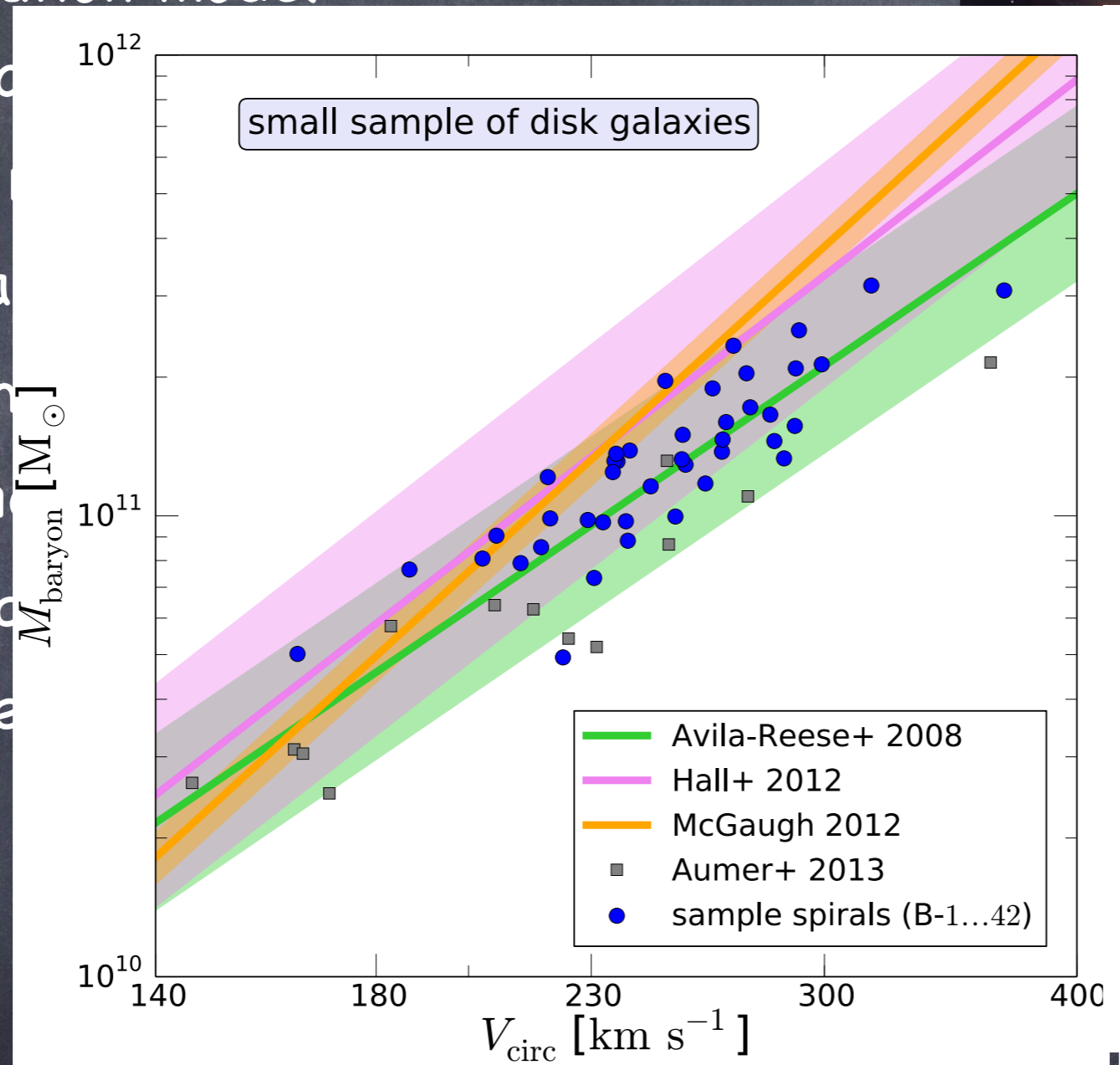
- Star formation model
- Stellar evolution
- Mass and metal return
- Supernovae rates
- Gas enrichment
- Cooling and heating rates
- Self-shielding
- Stellar feedback
- Local and non-local SNII feedback
- Black hole and AGN feedback



Can these feedback processes, which are inherently stochastic, result in tight correlation displayed in Tully-Fisher relation?

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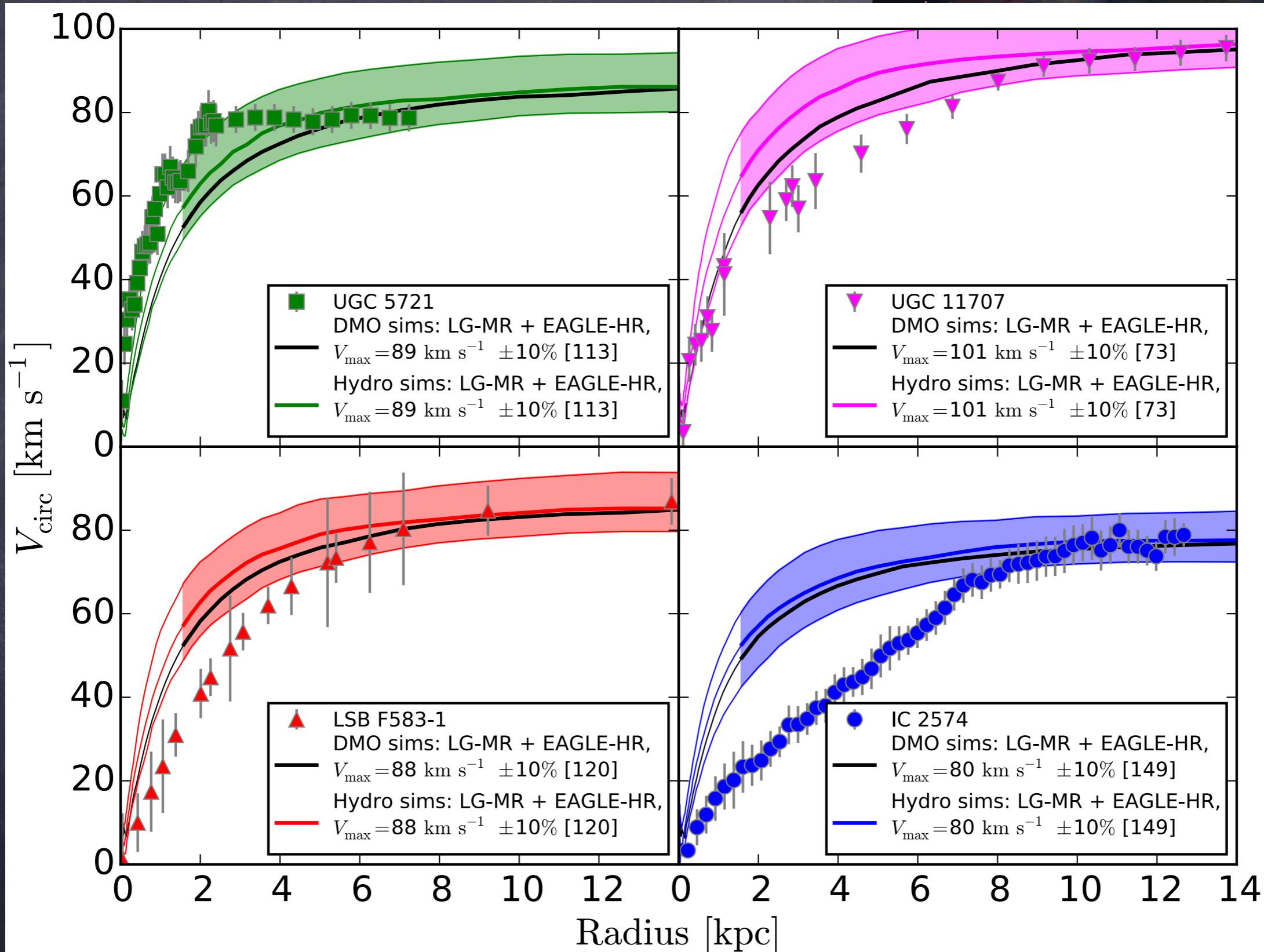


Vogelsberger et al.  
(2014)

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# One extreme: It's all feedback!



er et al.

astic,  
?

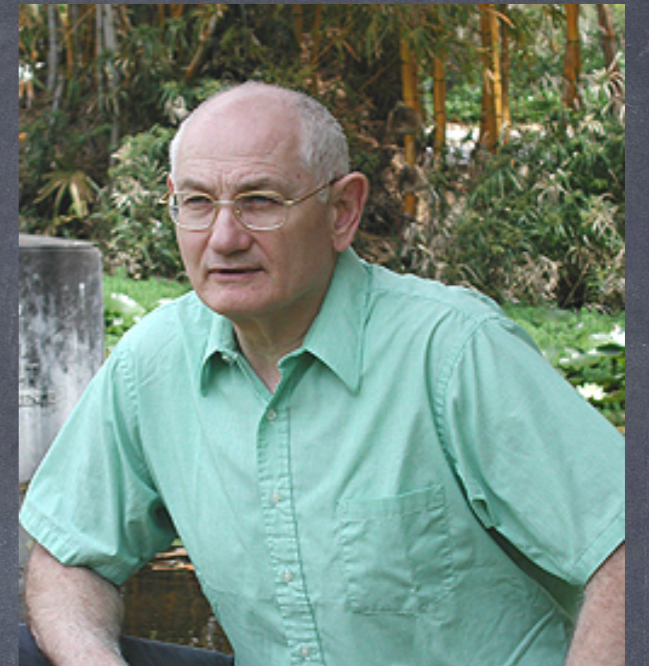
“The unexpected diversity of dwarf galaxy rotation curves”

Oman et al. (2016)

The other extreme: it's all modified gravity!

## Modified Newtonian Dynamics (MOND)

Milgrom (1983)



- No dark matter
- Newtonian gravity fails at low acceleration

$$a = \begin{cases} a_N & a_N \gg a_0 \\ \sqrt{a_N a_0} & a_N \ll a_0 \end{cases}$$

$$a_N = \frac{G_N M_b(r)}{r^2}$$

$$a_0 \simeq 1.2 \times 10^{-8} \text{ cm/s}^2$$

MOND effective theory:

Bekenstein & Milgrom (1984)

$$\mathcal{L}_{\text{MOND}} = -\frac{2M_{\text{Pl}}^2}{3a_0} \left( (\partial\phi)^2 \right)^{3/2} + \frac{\phi}{M_{\text{Pl}}} \rho_b$$

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MOND? For static, spherically-symmetric source,

$$\vec{\nabla} \cdot \left( \frac{|\vec{\nabla}\phi|}{a_0} \vec{\nabla}\phi \right) = 4\pi G_N \rho$$

$$\Rightarrow \phi' = \sqrt{a_0 \frac{G_N M(r)}{r^2}} = \sqrt{a_0 a_N}$$

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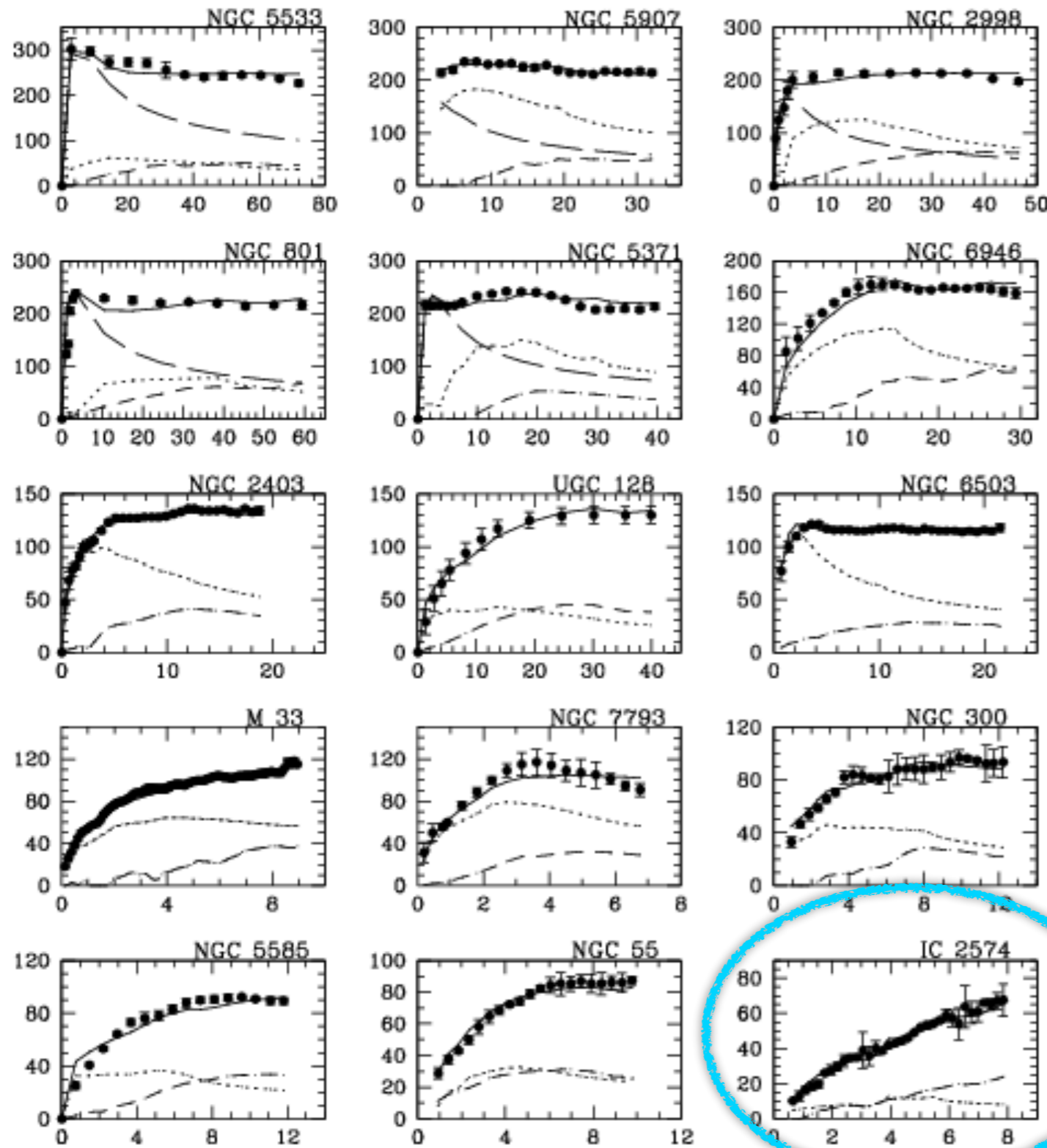
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$$\Rightarrow a_{\text{tot}} = a_N + a_\phi = a_N + \sqrt{a_0 a_N}$$

# Milgrom's MOND empirical law

Milgrom (1983)

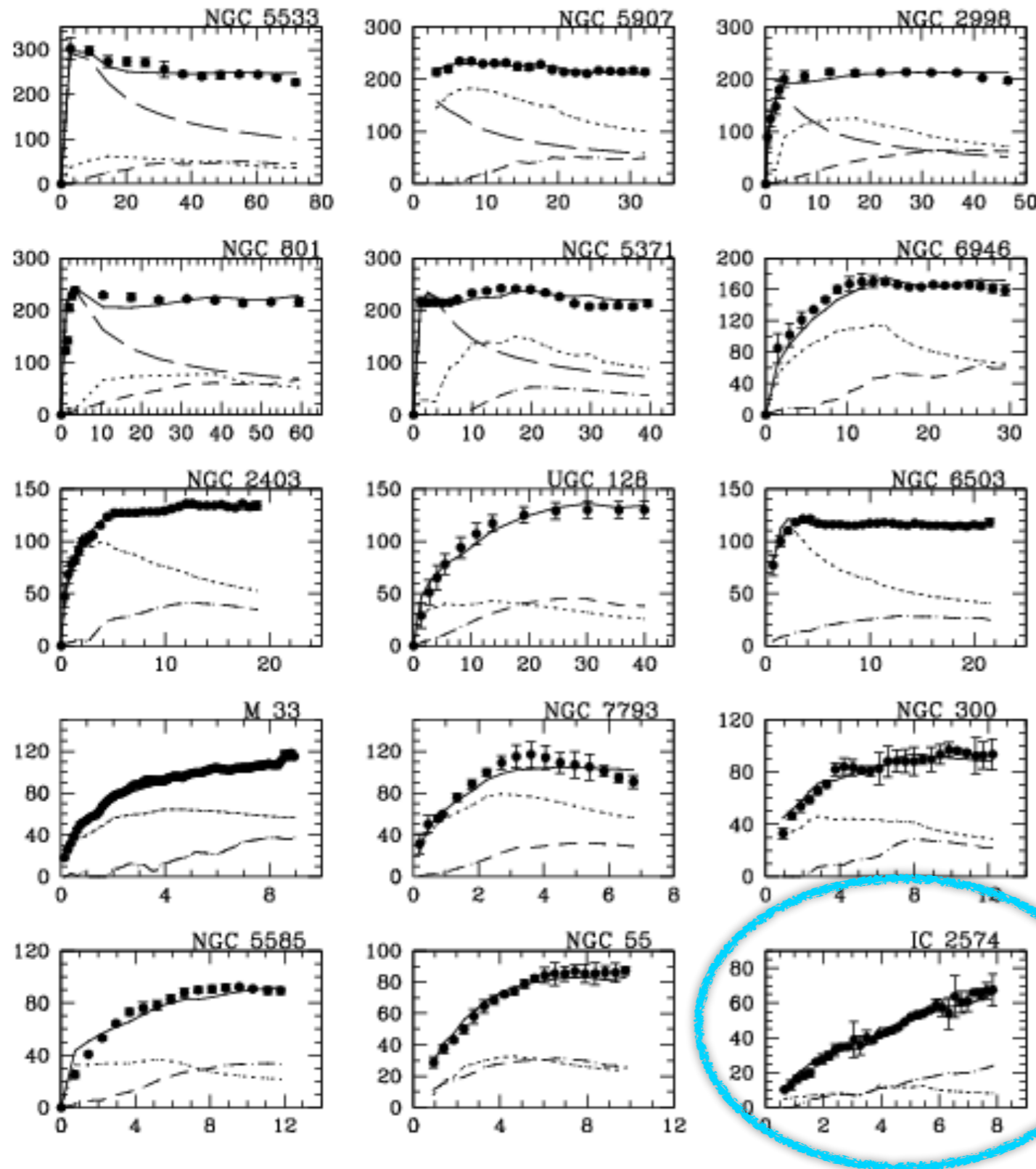


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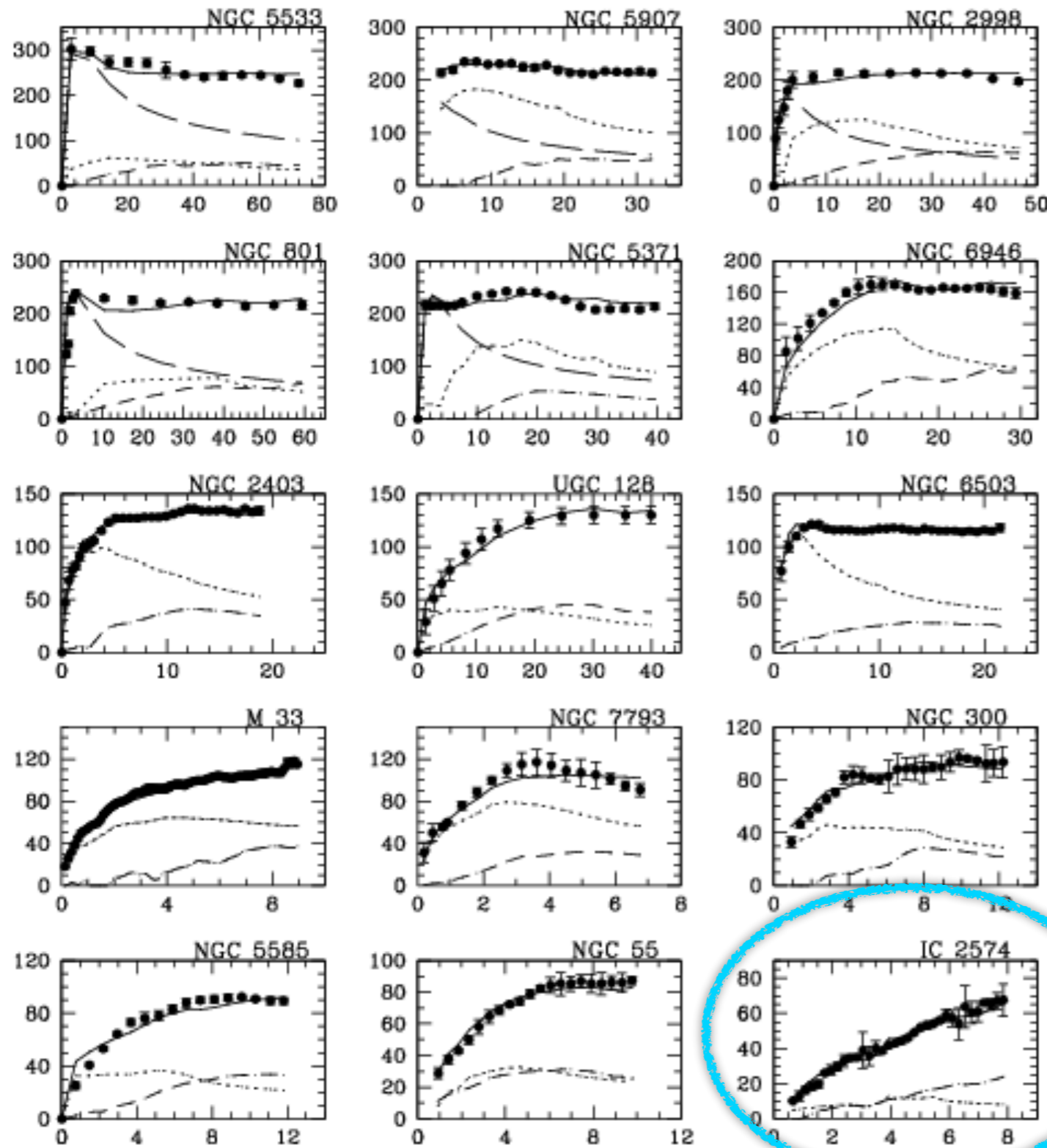
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Effective surface brightness (in HSB galaxies):

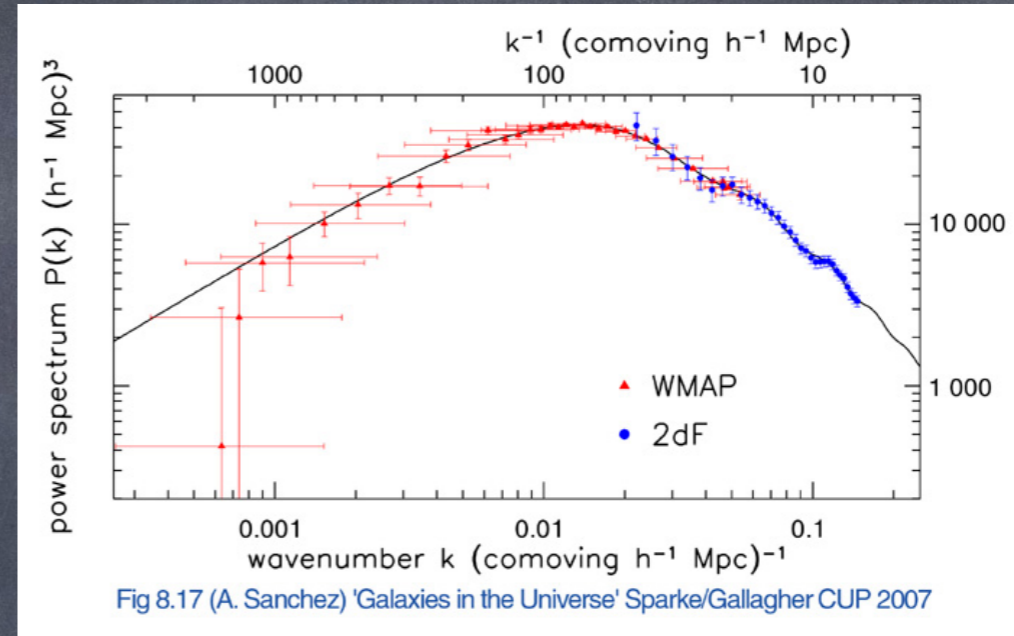
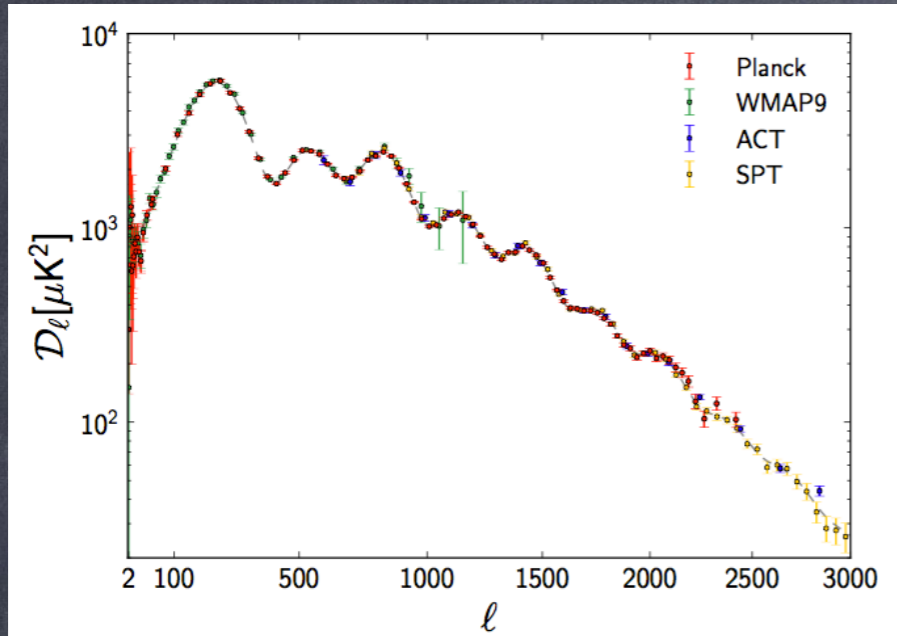
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# Obvious problems

What about large scales?



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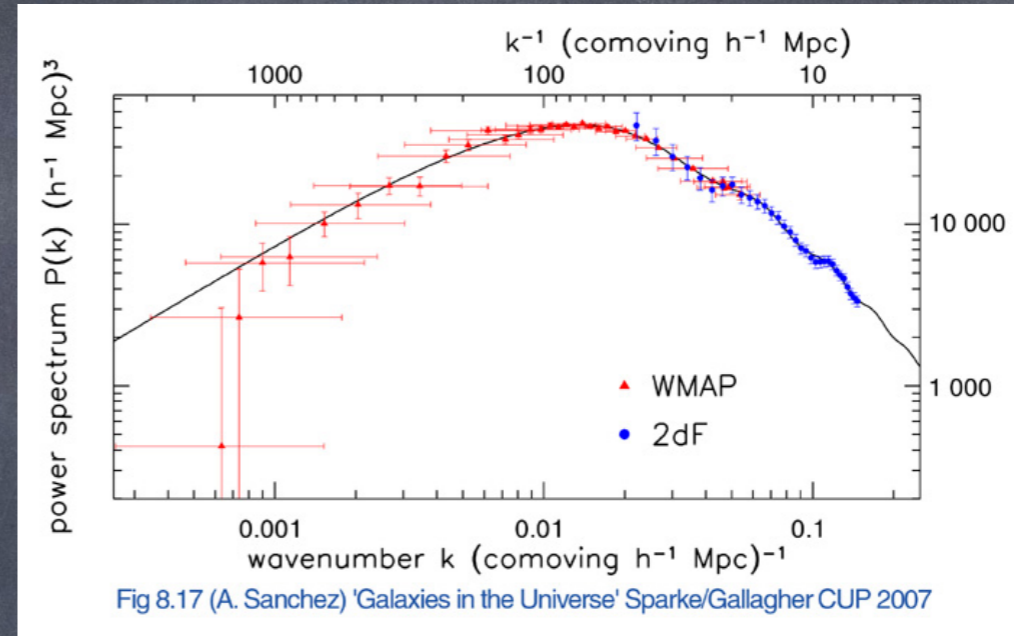
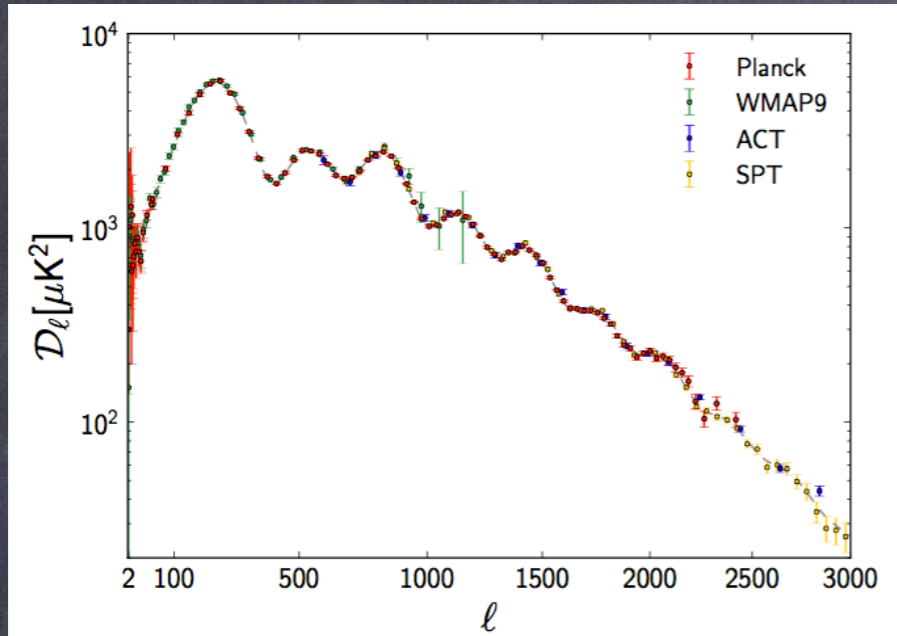
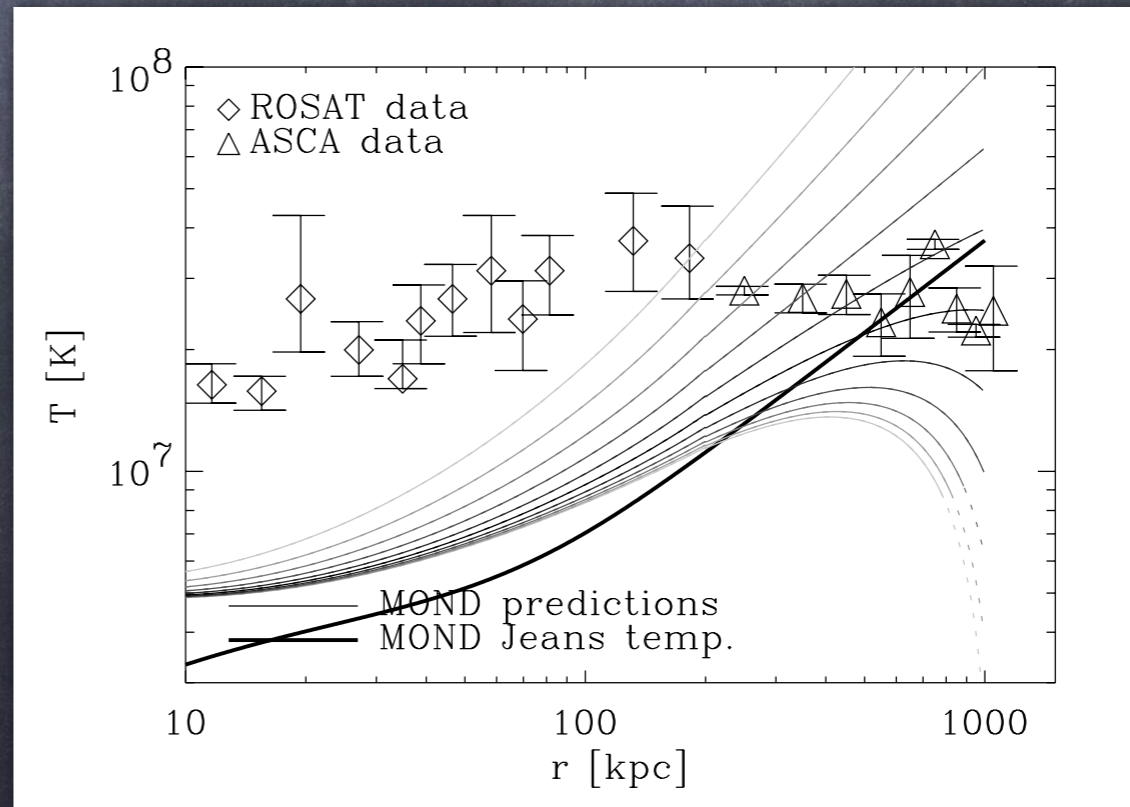


Fig 8.17 (A. Sanchez) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007

Poor fit to galaxy clusters:

Aguirre (2001)



The middle ground:

Blanchet (2006); Bruneton et al. (2008);  
Ho, Minic & Ng (2009); JK (2014); Verlinde (2016)

- Dark matter exists and behaves like a cold, collisionless fluid on large scales.

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e.g. in this talk: **DM superfluidity**

BBC FOUR

BBC FOUR

## 2 Conditions for DM Condensation

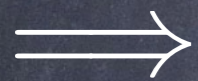


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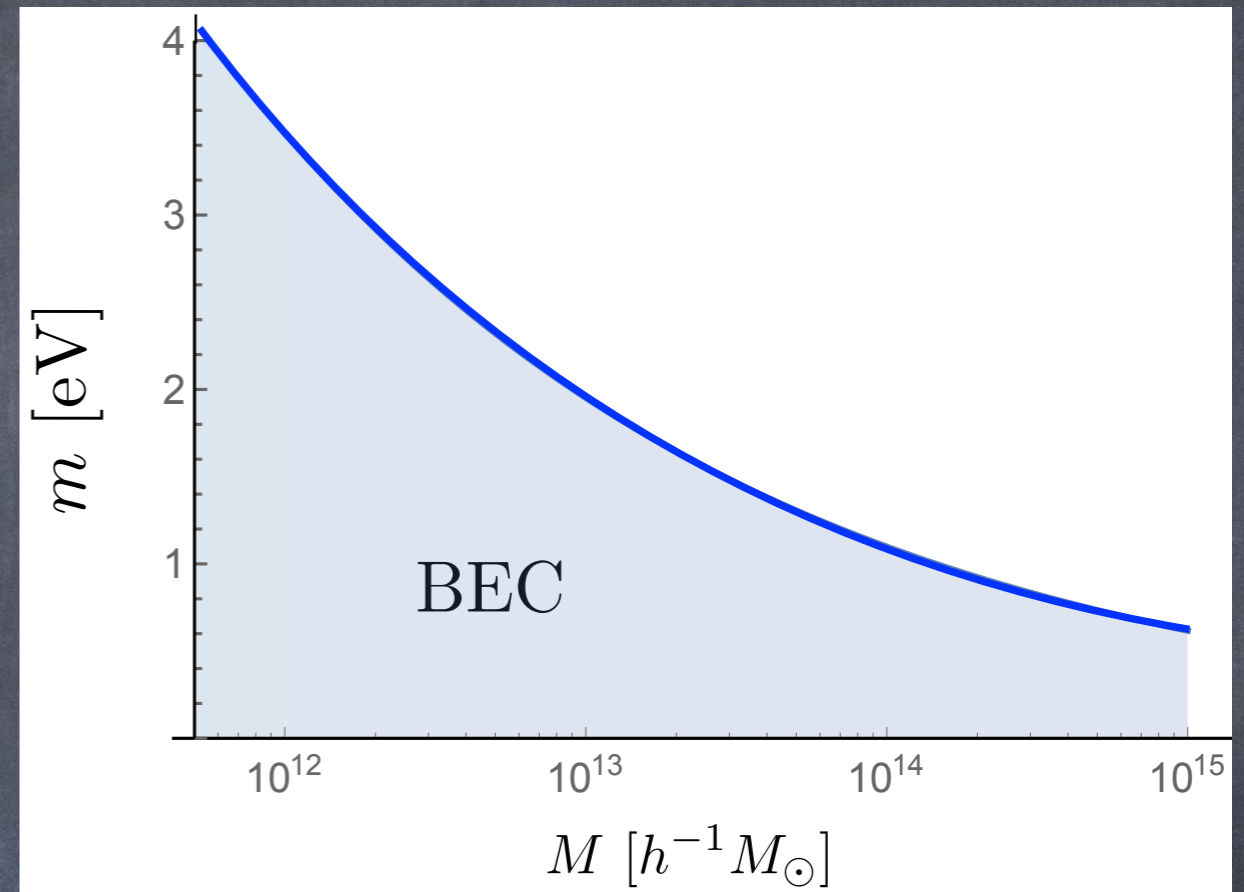
- Overlapping de Broglie wavelength



$$\lambda_{\text{dB}} \sim \frac{1}{mv} \gtrsim \ell \sim \left( \frac{m}{\rho_{\text{vir}}} \right)^{1/3}$$



$$m \lesssim 2 \text{ eV}$$

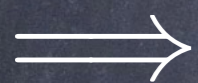


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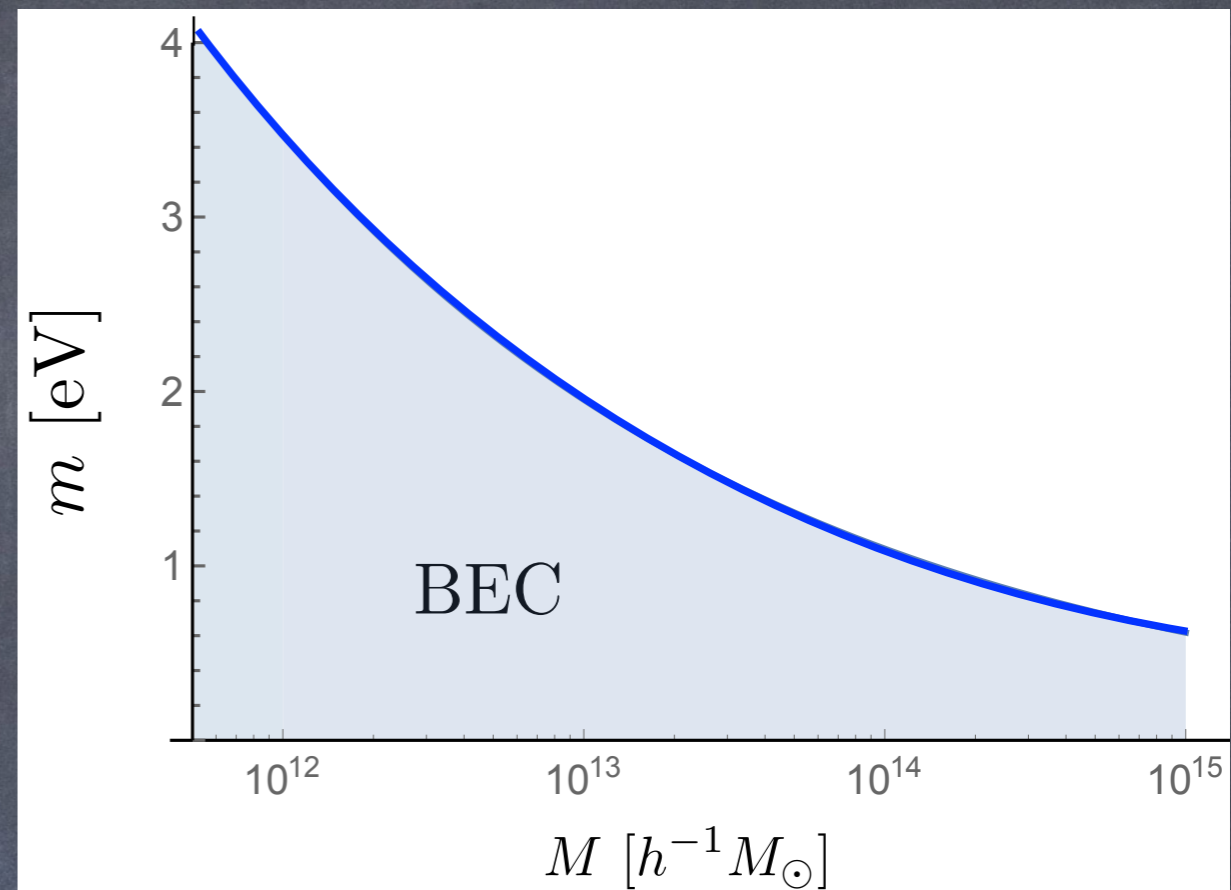
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- Thermal equilibrium

$$\Gamma \sim \mathcal{N} v \sigma \frac{\rho_{\text{vir}}}{m} \gtrsim t_{\text{dyn}}^{-1} \implies$$

$$\frac{\sigma}{m} \gtrsim \left( \frac{m}{\text{eV}} \right)^4 \frac{\text{cm}^2}{g}$$

Current bound:  $\frac{\sigma}{m} \lesssim 0.5 \frac{\text{cm}^2}{g}$  Harvey et al. (2015)



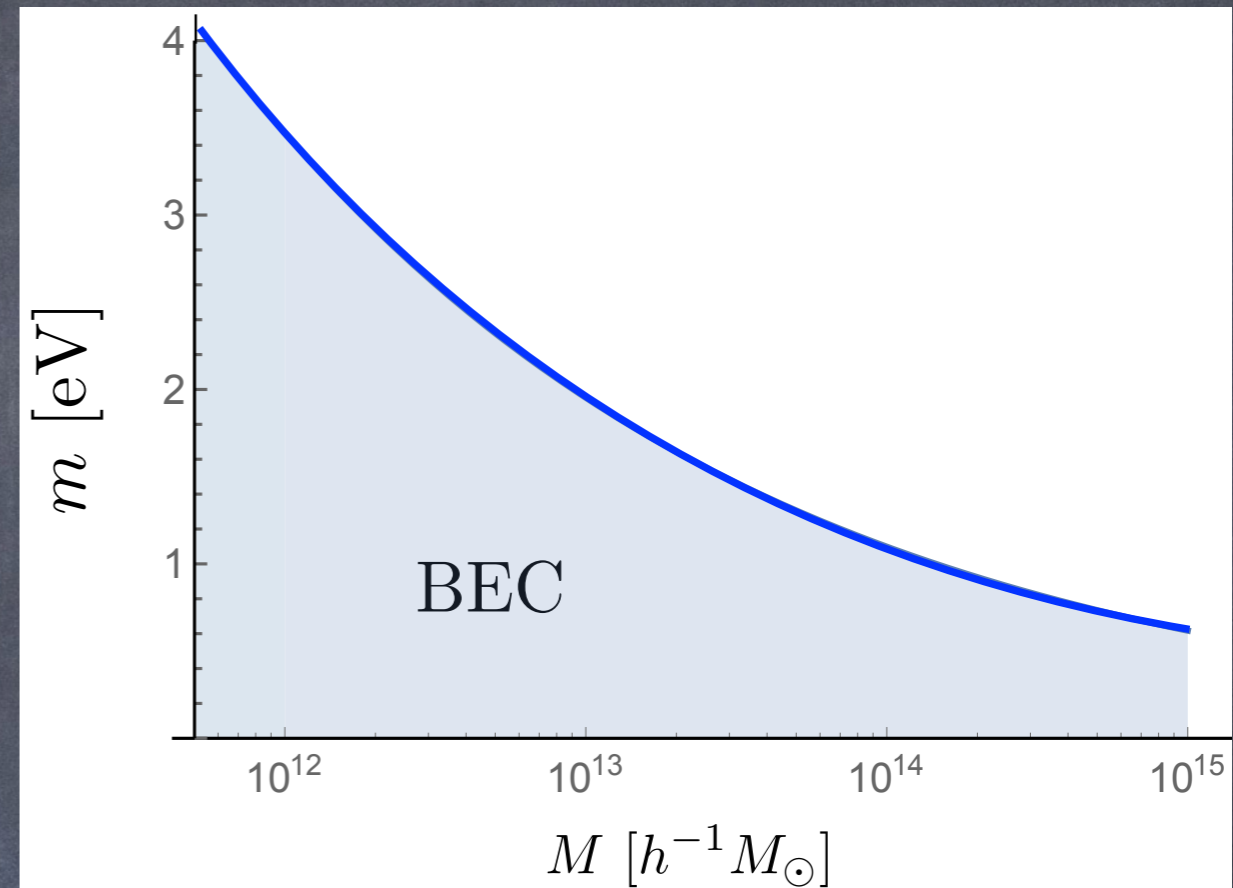
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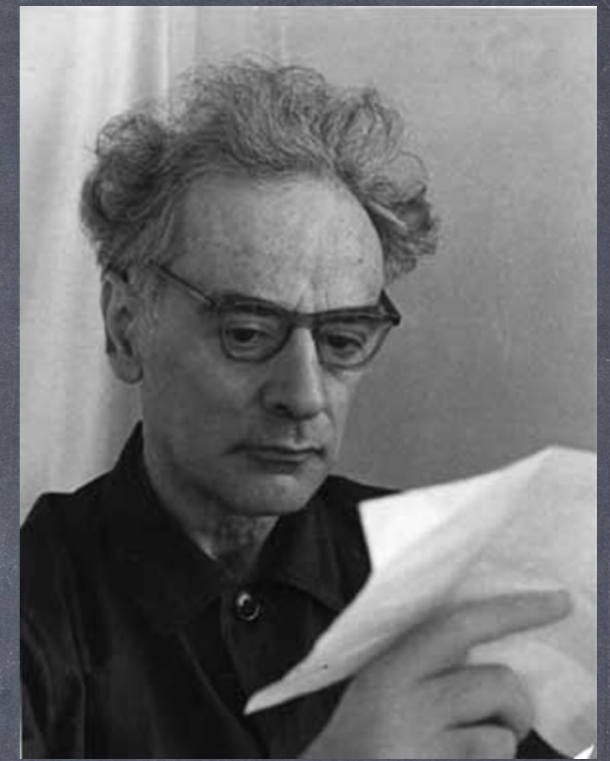
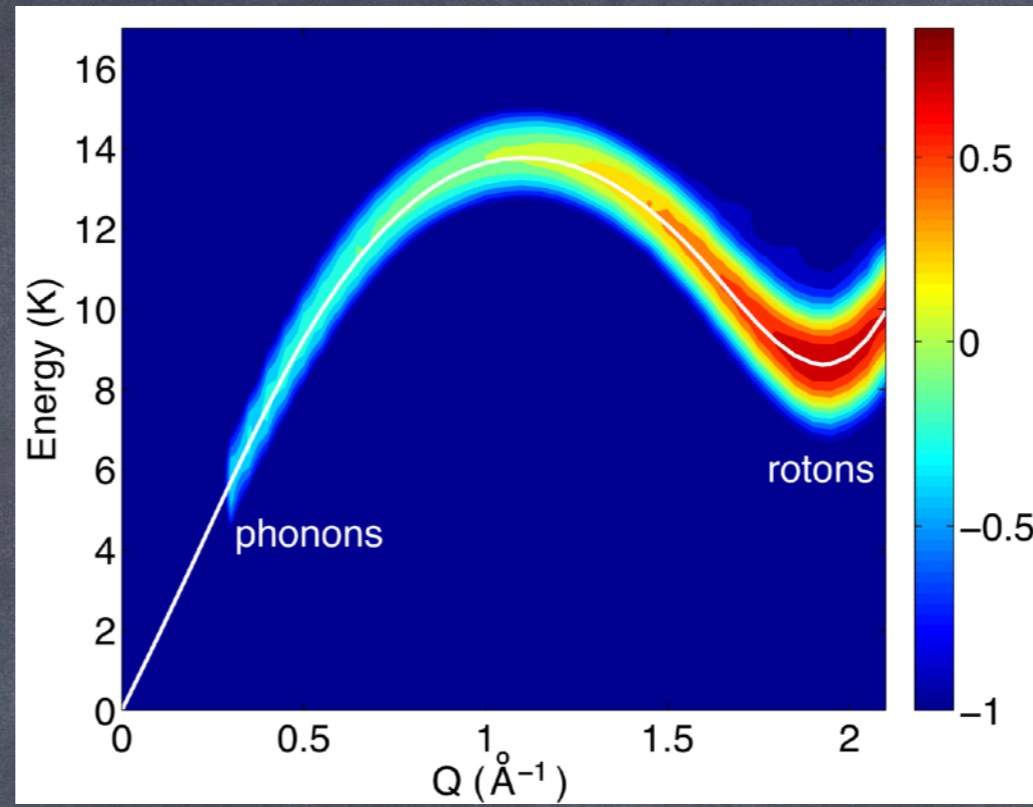
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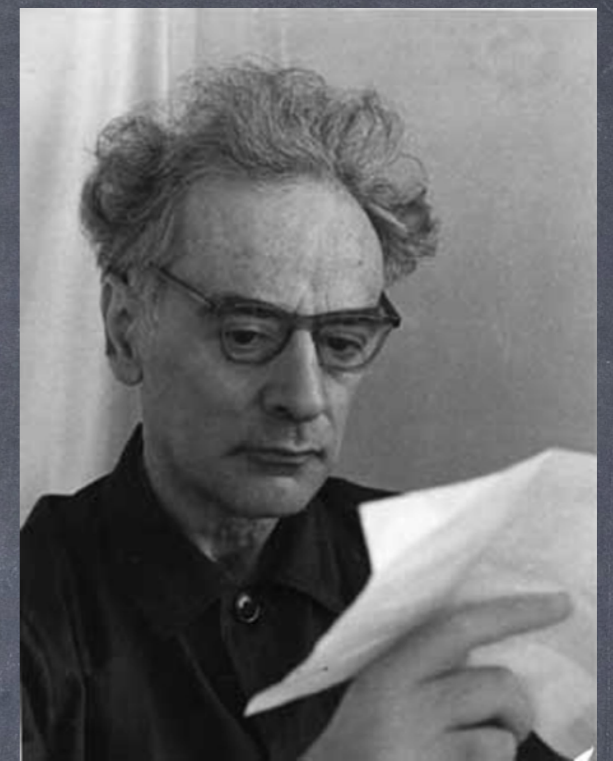
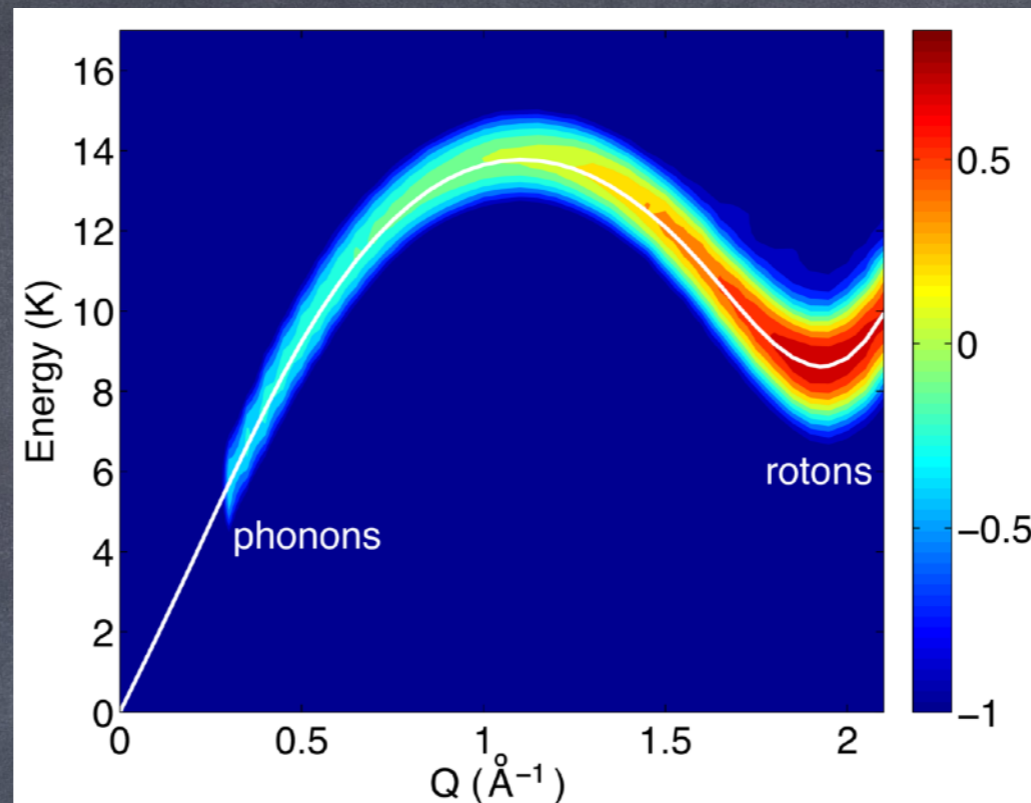
DM is quite cold:  $T_c = 6.5 \left( \frac{\text{eV}}{m} \right)^{5/3} (1 + z_{\text{vir}})^2 \text{ mK}$

( ${}^7\text{Li}$  atoms  $\implies T_c \sim 0.2 \text{ mK}$ )

# Two-fluid model



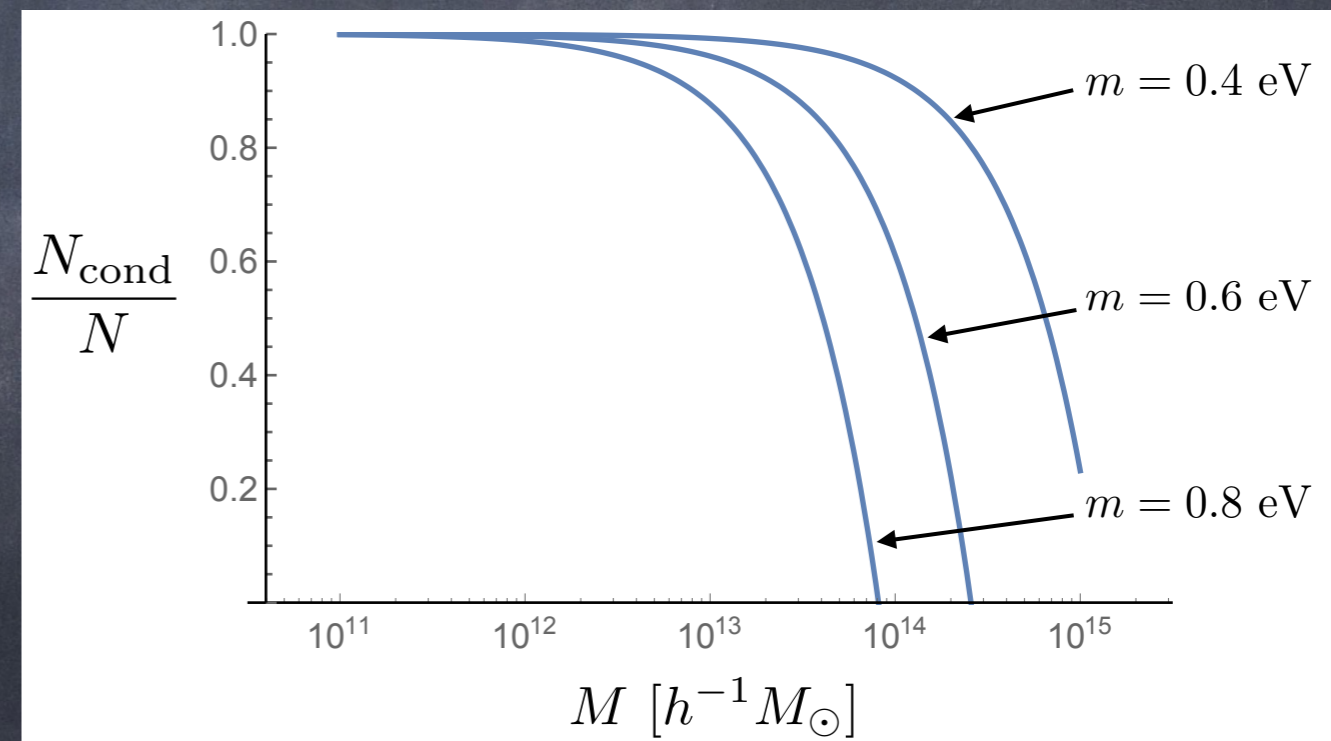
# Two-fluid model



## Free bose gas:

$$\frac{N_{\text{cond}}}{N} = 1 - \left( \frac{T}{T_c} \right)^{3/2}$$

- Galaxies are mostly condensed
- Galaxy clusters are in mixed or normal phase



Can generalize to include interactions.

Khoury, Lubensky, Miranda & Sharma (to appear)

Temperature set by how rapidly DM particles move

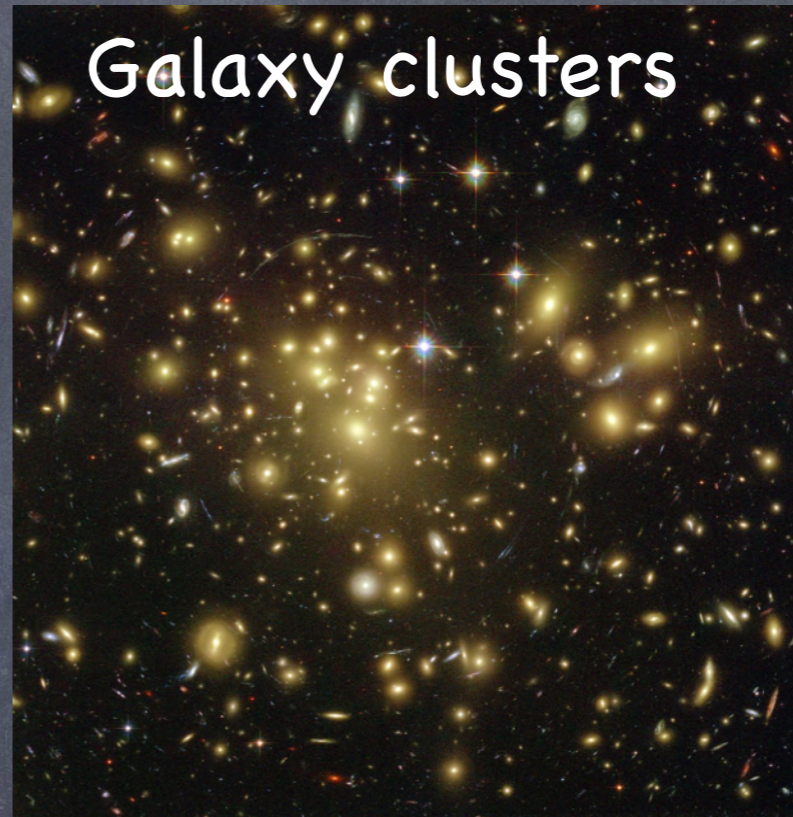
$$T \sim mv^2$$



$$T_{\text{galaxy}} \sim 0.1 \text{ mK}$$

⇒ Superfluid

⇒ MOND



$$T_{\text{cluster}} \sim 10 \text{ mK}$$

⇒ NO Superfluid

⇒ NO MOND



Naturally distinguishes between galaxies (where MOND works) and galaxy clusters (where MOND doesn't work).

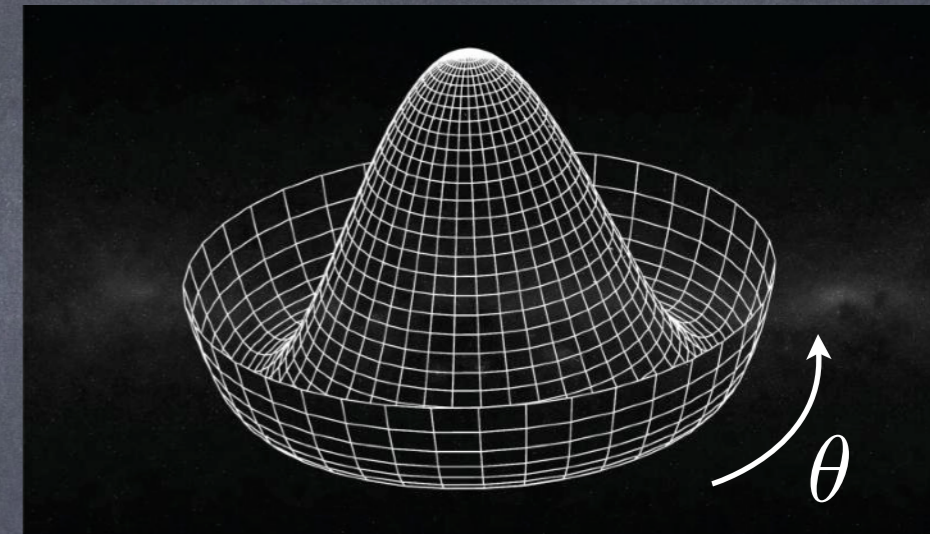
# Effective Description of Superfluids

Greiter, Wilczek & Witten (1989)

A superfluid phase is defined as:

- Global U(1) symmetry, spontaneously broken

$\implies$  Goldstone boson  $\theta \rightarrow \theta + c$



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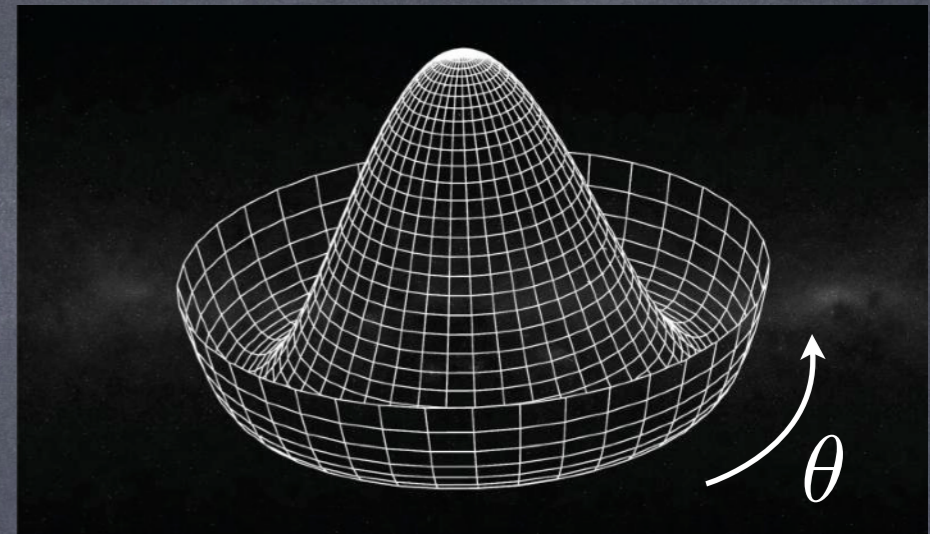
- State has finite charge density,  $\langle J^0 \rangle \sim \langle \dot{\theta} \rangle \neq 0$

By redefining field, can set

$$\theta = \mu t + \phi$$

chemical potential

phonons





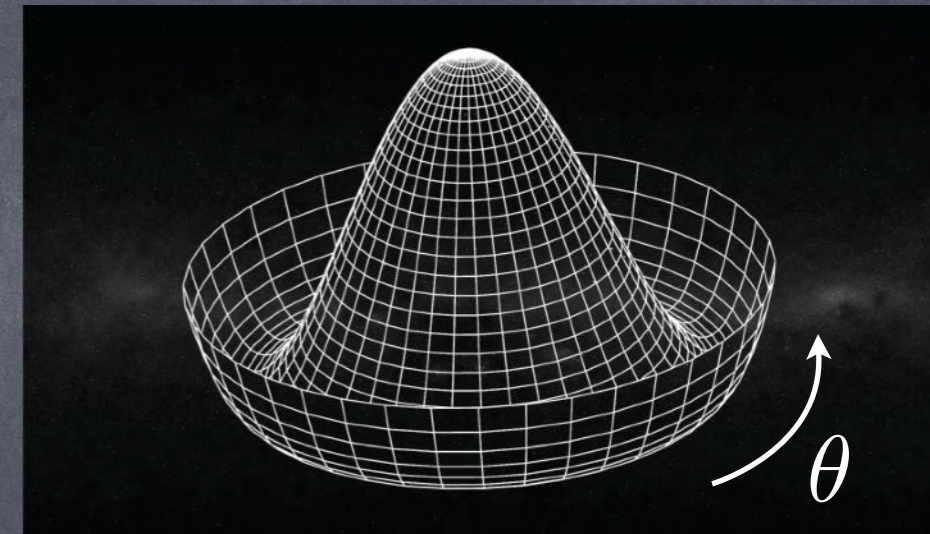
# Effective Description of Superfluids

Greiter, Wilczek & Witten (1989)

A superfluid phase is defined as:

- Global U(1) symmetry, spontaneously broken

$$\implies \text{Goldstone boson } \theta \rightarrow \theta + c$$



- State has finite charge density,  $\langle J^0 \rangle \sim \langle \dot{\theta} \rangle \neq 0$

By redefining field, can set

$$\theta = \underbrace{\mu t}_{\text{chemical potential}} + \underbrace{\phi}_{\text{phonons}}$$

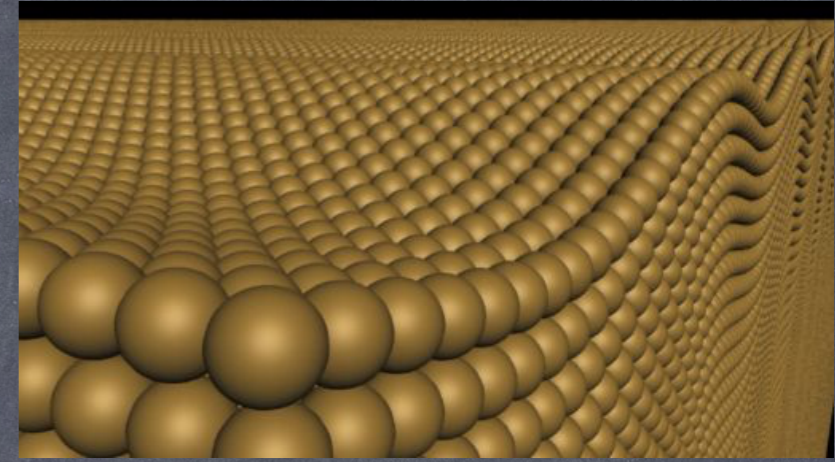
Hence, at lowest order in derivatives the EFT of phonons is

$$\mathcal{L} = P(X); \quad X = \mu + \dot{\phi} - \frac{(\vec{\nabla} \phi)^2}{2m}$$

# Superfluid phonons

At lowest order in derivatives, the zero temperature effective action is

$$\mathcal{L} = P(X); \quad X = \mu + \dot{\phi} - \frac{(\vec{\nabla}\phi)^2}{2m}$$

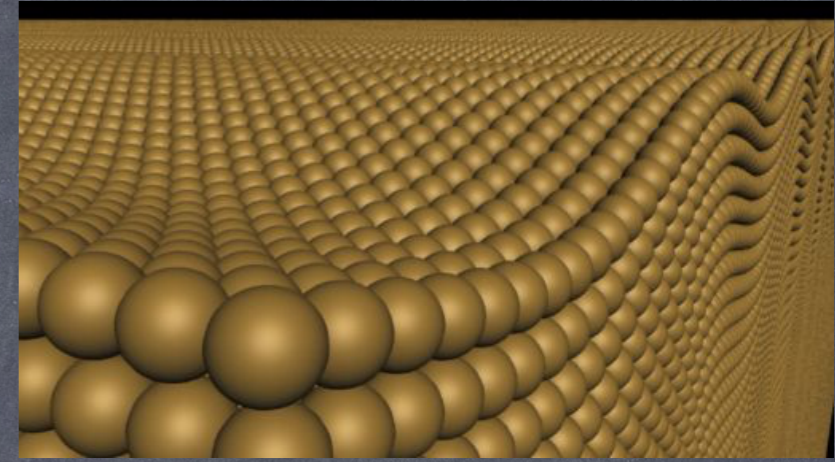


Greiter, Wilczek & Witten (1989); Son and Wingate (2005)

# Superfluid phonons

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Greiter, Wilczek & Witten (1989); Son and Wingate (2005)

Conjecture: DM superfluid phonons are governed by MOND action

$$P_{\text{MOND}}(X) = \frac{2\Lambda(2m)^{3/2}}{3} X \sqrt{|X|}$$

Phonons couple to baryons:  $\mathcal{L}_{\text{coupling}} = -\frac{\Lambda}{M_{\text{Pl}}} \phi \rho_{\text{b}}$

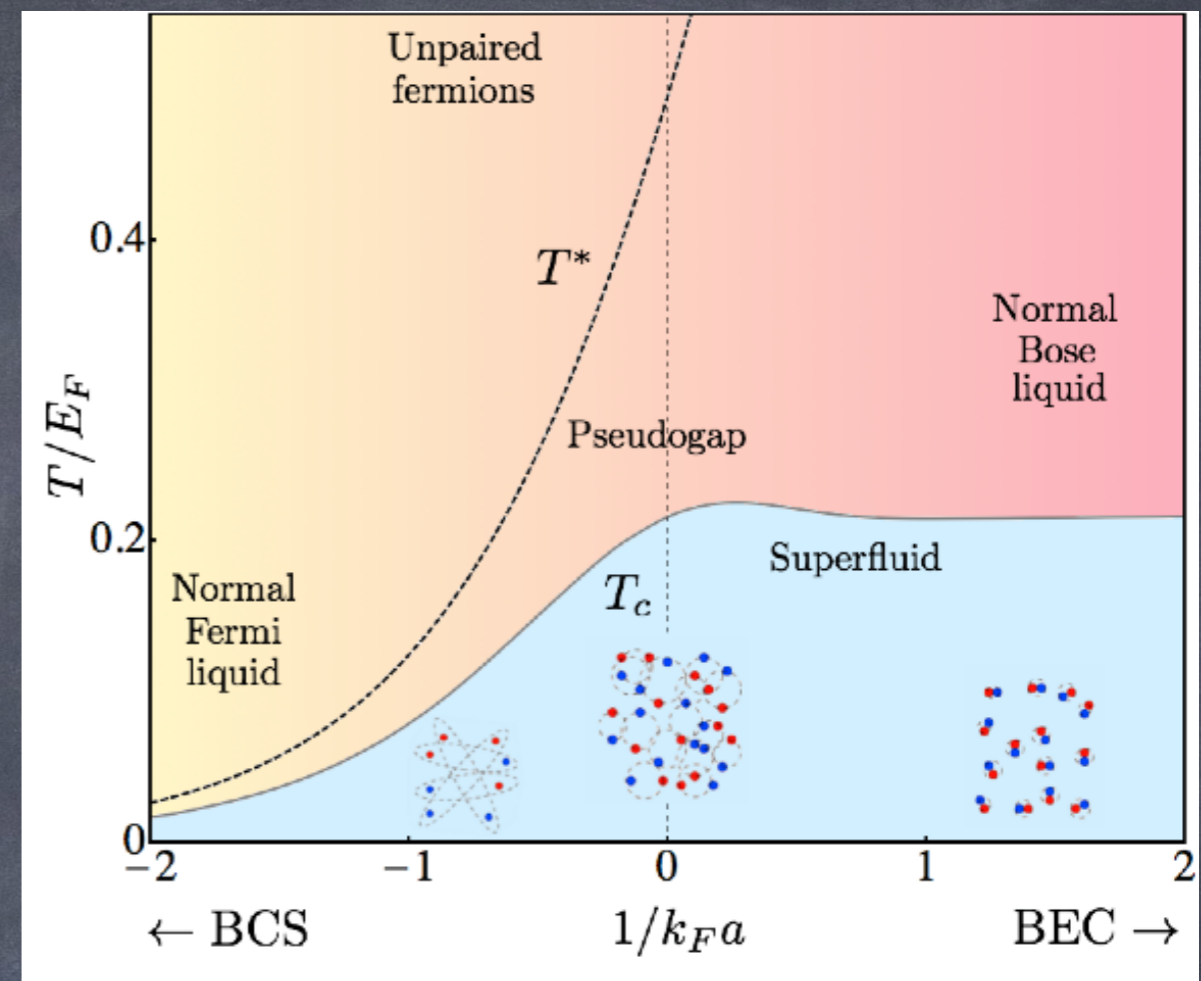
$$\Lambda = \sqrt{a_0 M_{\text{Pl}}} \simeq 0.8 \text{ meV}$$

(Match to MOND scale)

• Cold Atoms Analogue?

$$\mathcal{L}_{\text{UFG}} \sim m^{3/2} X^{5/2}$$

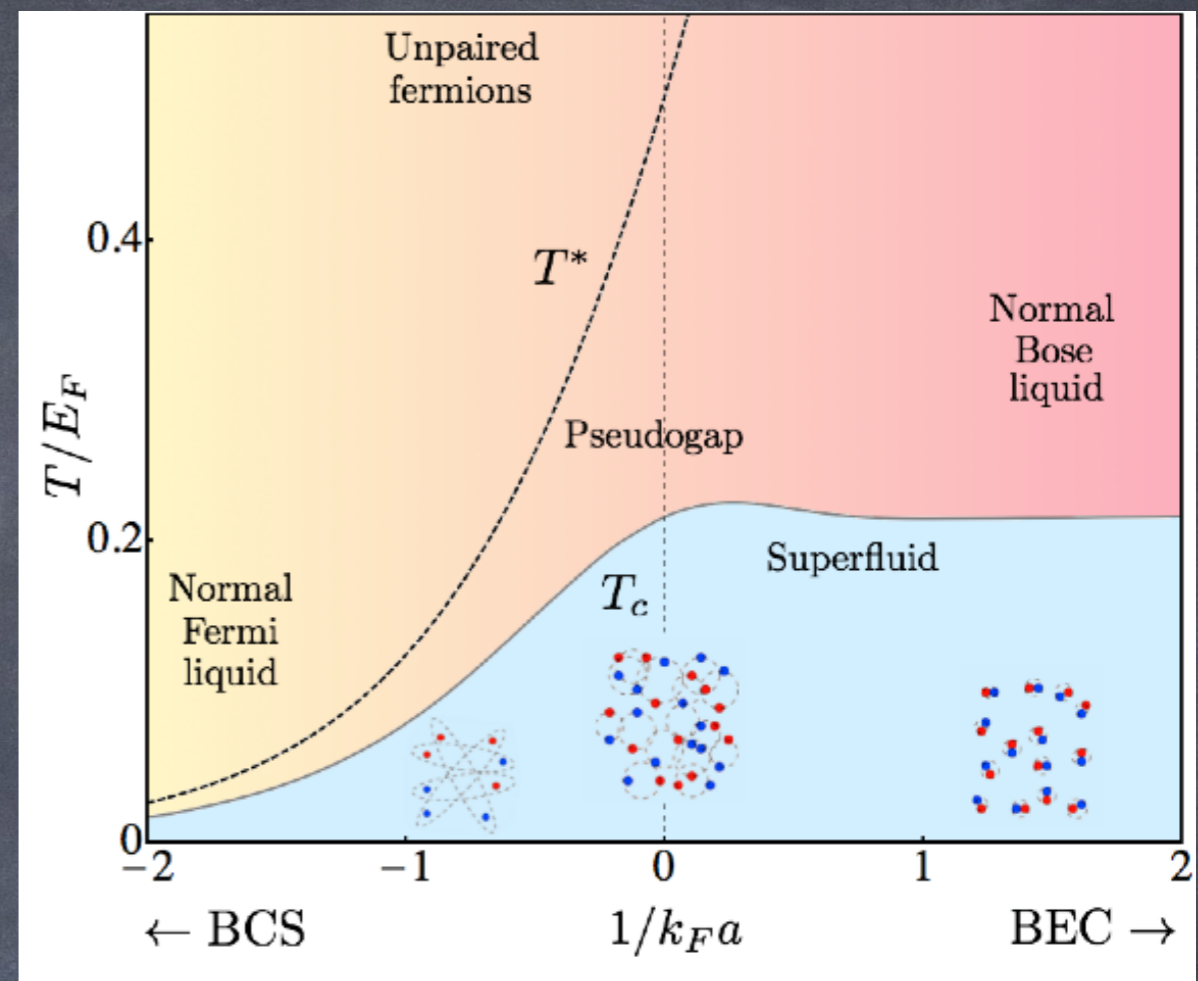
Son & Wingate (2005)



• Cold Atoms Analogue?

$$\mathcal{L}_{\text{UFG}} \sim m^{3/2} X^{5/2}$$

Son & Wingate (2005)



• 3-body interactions?

$$\mathcal{L} = \frac{i}{2} (\Psi \partial_t \Psi^* - \Psi^* \partial_t \Psi) - \frac{|\vec{\nabla} \Psi|^2}{2m} - \frac{\lambda}{24m^3} |\Psi|^6$$

Split into  $\Psi = \sqrt{2m\rho} e^{i\theta}$ , and integrate out  $\rho$ ,

$$\implies \mathcal{L} = \frac{4}{3} \frac{m^{3/2}}{\sqrt{\lambda}} X^{3/2}$$

# Condensate properties

Action uniquely fixes properties of the condensate through standard thermodynamics

• Pressure: 
$$P_{\text{cond}} = \frac{2\Lambda}{3} (2m\mu)^{3/2}$$

• Number density: 
$$n_{\text{cond}} = \frac{\partial P_{\text{cond}}}{\partial \mu} = \Lambda (2m)^{3/2} \mu^{1/2}$$

In the non-relativistic approx'n,  $\rho_{\text{cond}} = mn_{\text{cond}}$ , therefore:

$$P_{\text{cond}} = \frac{\rho_{\text{cond}}^3}{12\Lambda^2 m^6}$$

- Polytropic equation of state, with index  $n = 1/2$
- Different than BEC DM, where  $P_{\text{cond}} \sim \rho_{\text{cond}}^2$

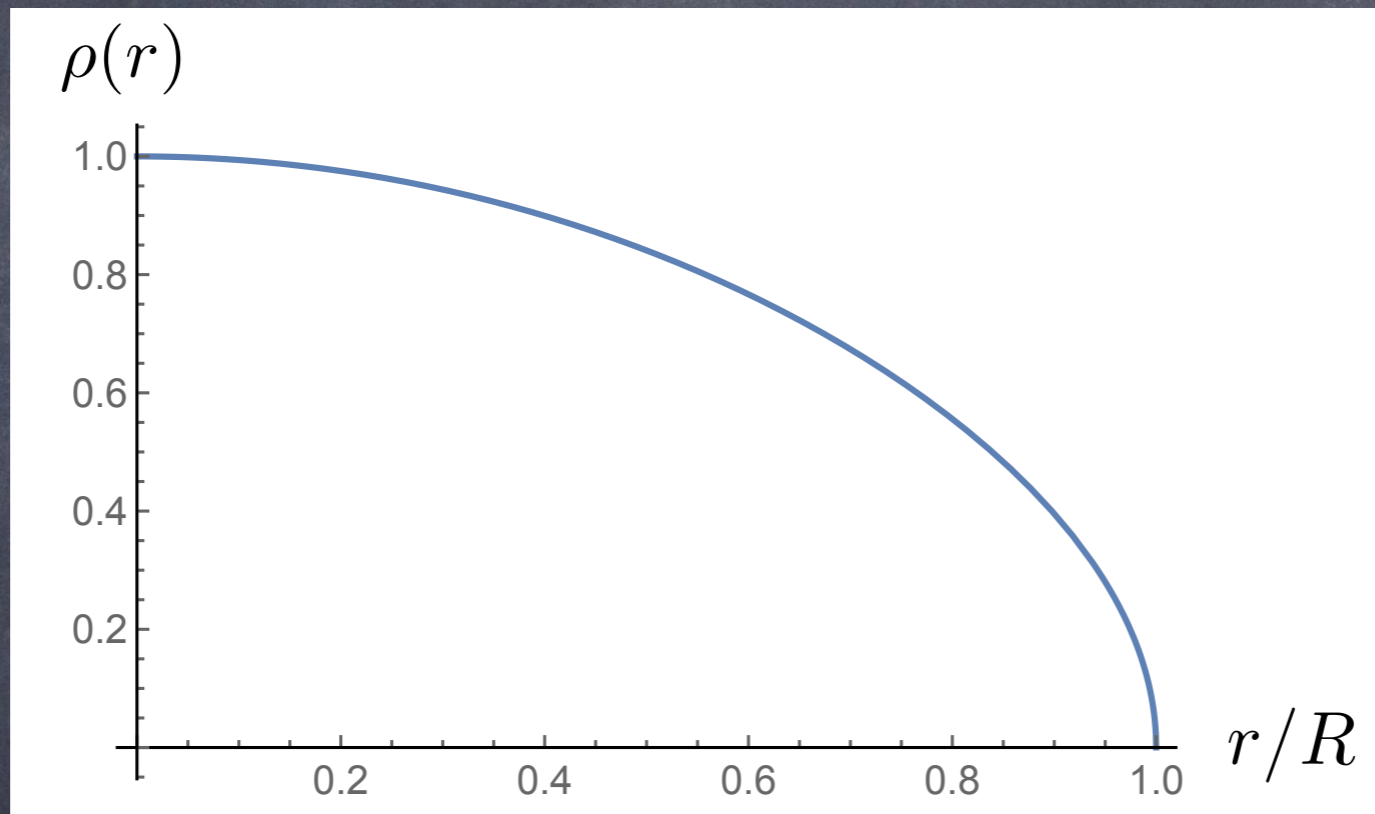
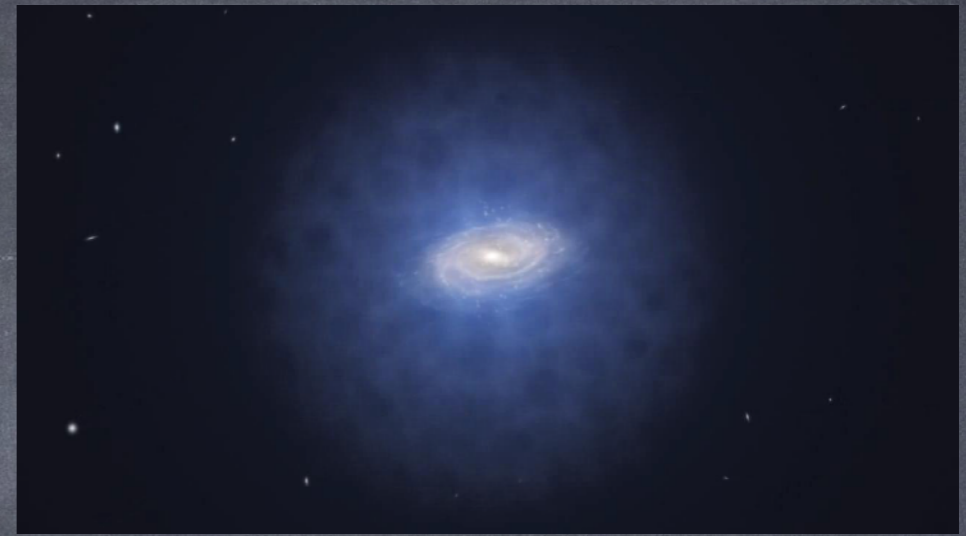
Sin (1994), Goodman (2000), Peebles (2000), Boehmer & Harko (2007)

# Density profile

Assuming hydrostatic equilibrium,

$$\frac{1}{\rho_{\text{cond}}(r)} \frac{dP_{\text{cond}}(r)}{dr} = -\frac{4\pi G_{\text{N}}}{r^2} \int_0^r dr' r'^2 \rho(r')$$

Using equation of state  $P_{\text{cond}} \sim \rho_{\text{cond}}^3$ , find:



Cored density profile

$$R_{\text{core}} = \left( \frac{M}{10^{12} M_{\odot}} \right)^{1/6} (1 + z_{\text{vir}})^{1/4} \left( \frac{m}{\text{eV}} \right)^{-9/5} \left( \frac{\Lambda}{\text{meV}} \right)^{-3/5} 21 \text{ kpc}$$

Remarkably, realistic size cores with  $m \sim \text{eV}$  and  $\Lambda \sim \text{meV}$  !

SF

$\rho_s \simeq \text{const.}$

normal  
 $\rho_n \sim \frac{1}{r^2}$

normal  
 $\rho_n \sim \frac{1}{r^3}$



# Rotation curves

w. L. Berezhiani & B. Famaey (to appear)

$$m = 0.6 \text{ eV}$$

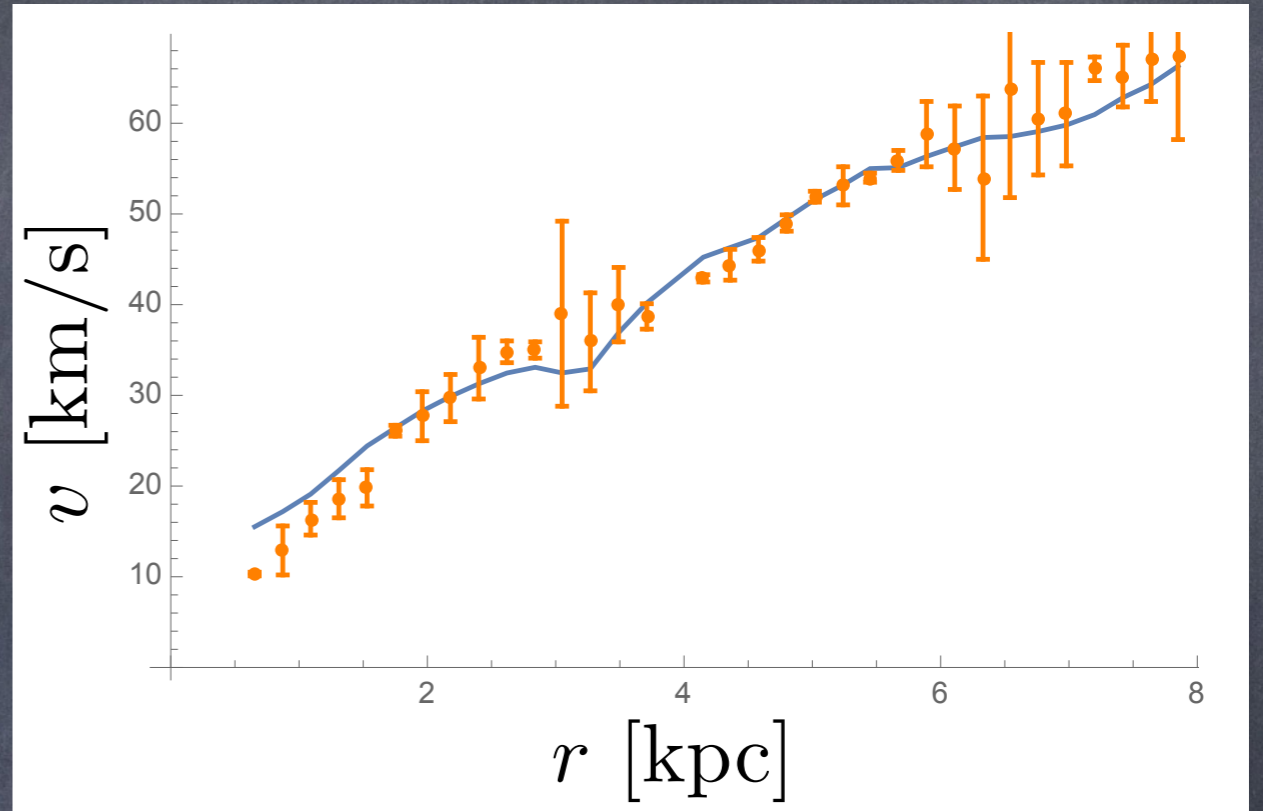
$$\Lambda = 0.3 \text{ meV}$$

$$a_0 = 0.87 \times 10^{-8} \text{ cm/s}^2$$

LSB galaxy  
(IC 2574)



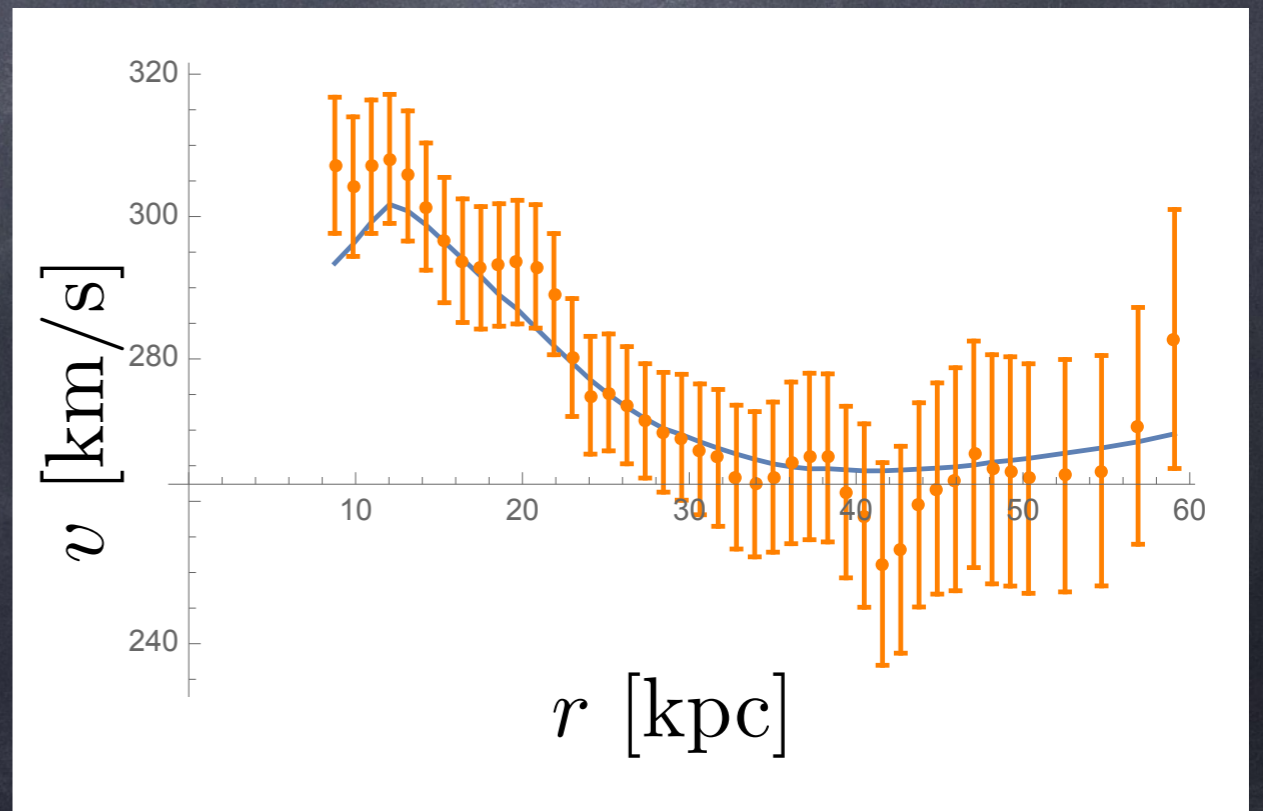
$$R_{\text{core}} = 37.5 \text{ kpc}$$



HSB galaxy  
(UGC 2953)

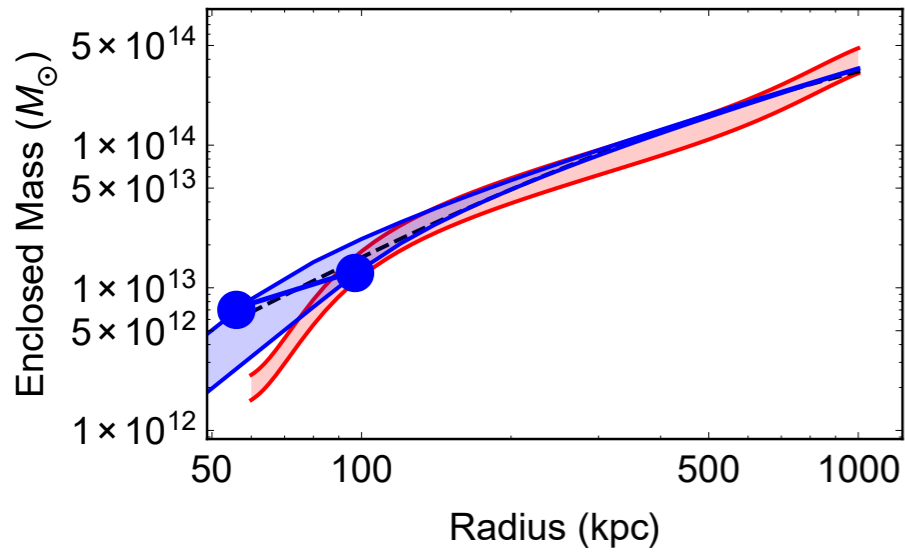


$$R_{\text{core}} = 73.2 \text{ kpc}$$

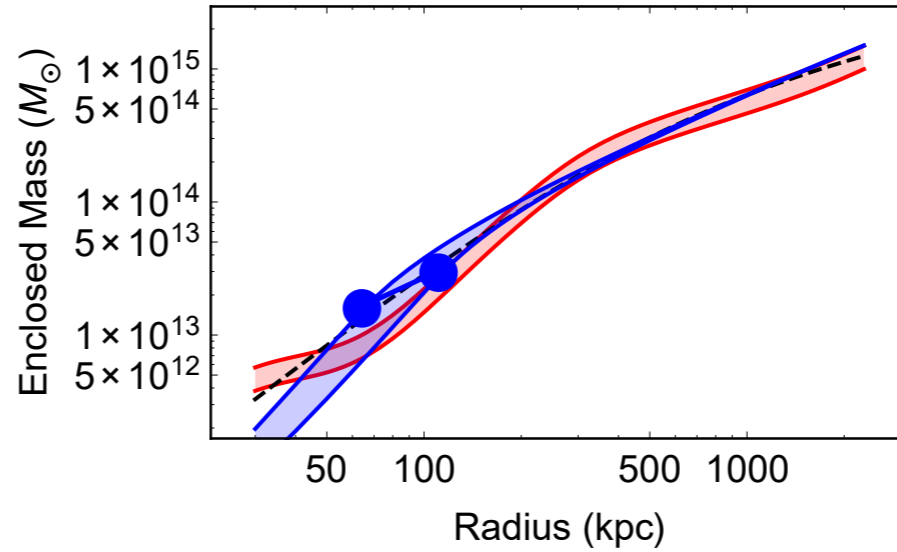


# Galaxy clusters

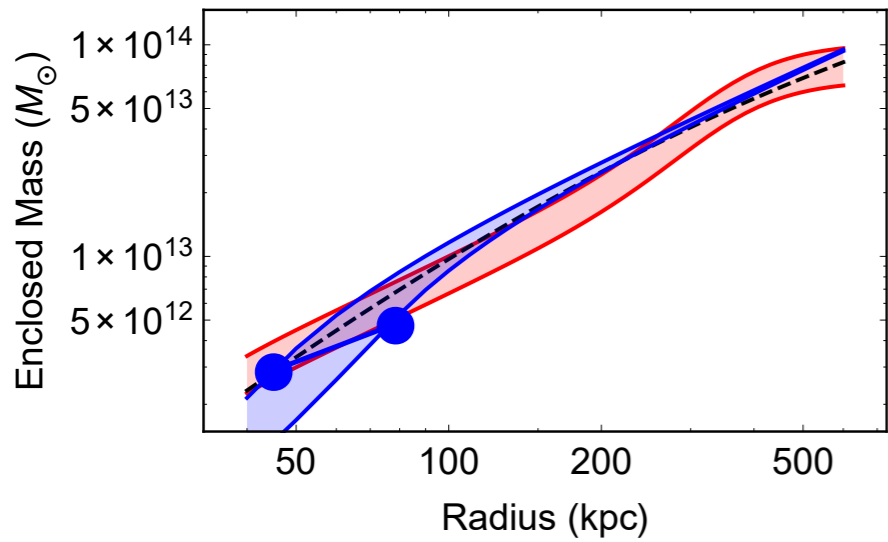
Hodson, Zhao, Khoury & Famaey, 1611.05876



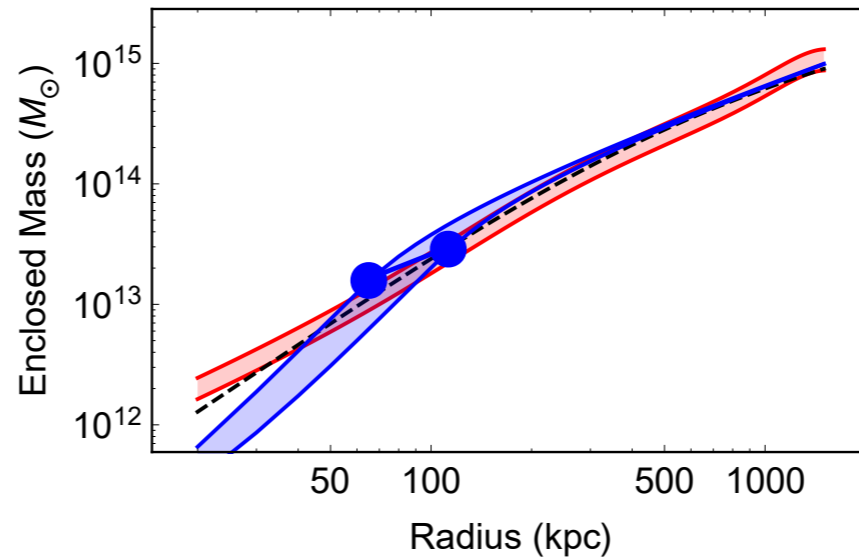
A133



A478



A262



A413

# Observational Signatures

# Vortices

When spun faster than critical velocity, superfluid develops vortices.

$$\omega_{\text{cr}} \sim \frac{1}{mR^2} \sim 10^{-41} \text{s}^{-1}$$

For a halo of density  $\rho$ ,

$$\omega \sim \lambda \sqrt{G_N \rho} \sim 10^{-18} \lambda \text{s}^{-1}; \quad 0.01 < \lambda < 0.1$$

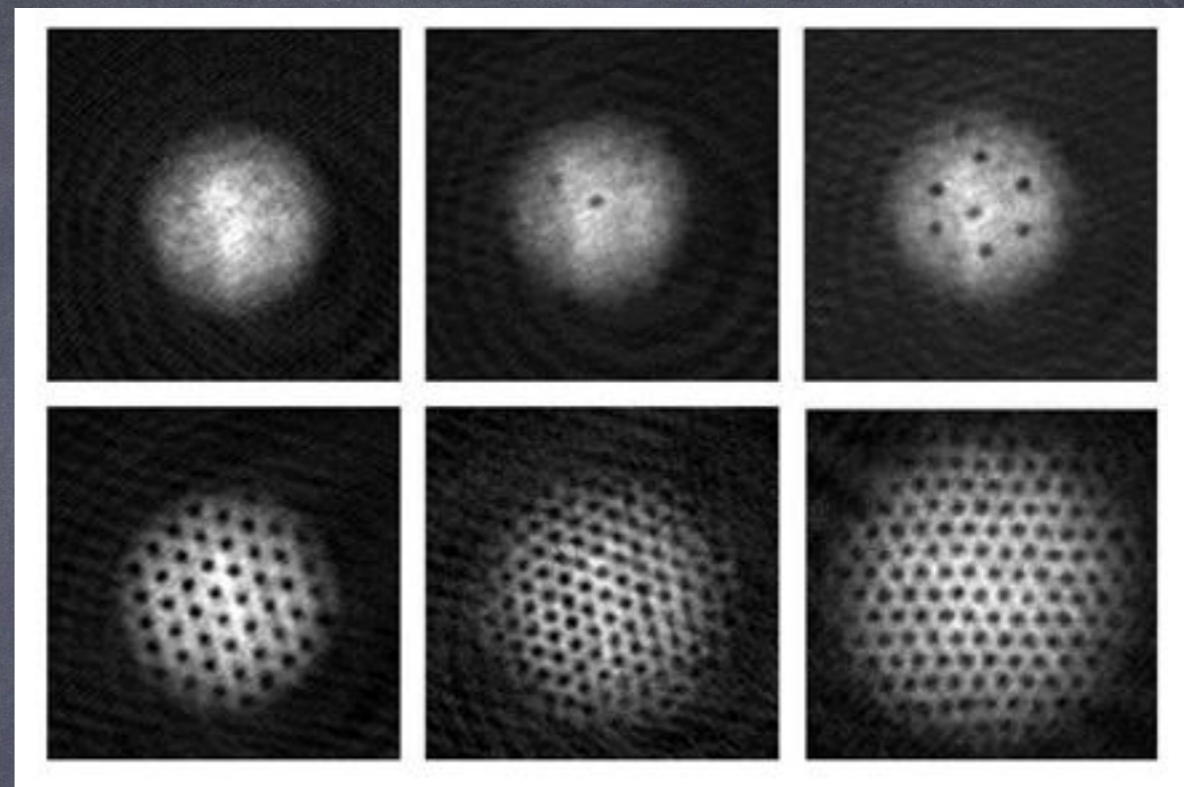
$\implies$  Vortex formation is unavoidable

Line density:

$$\sigma_v \sim m\omega \sim 10^2 \lambda \text{ AU}^{-2}$$

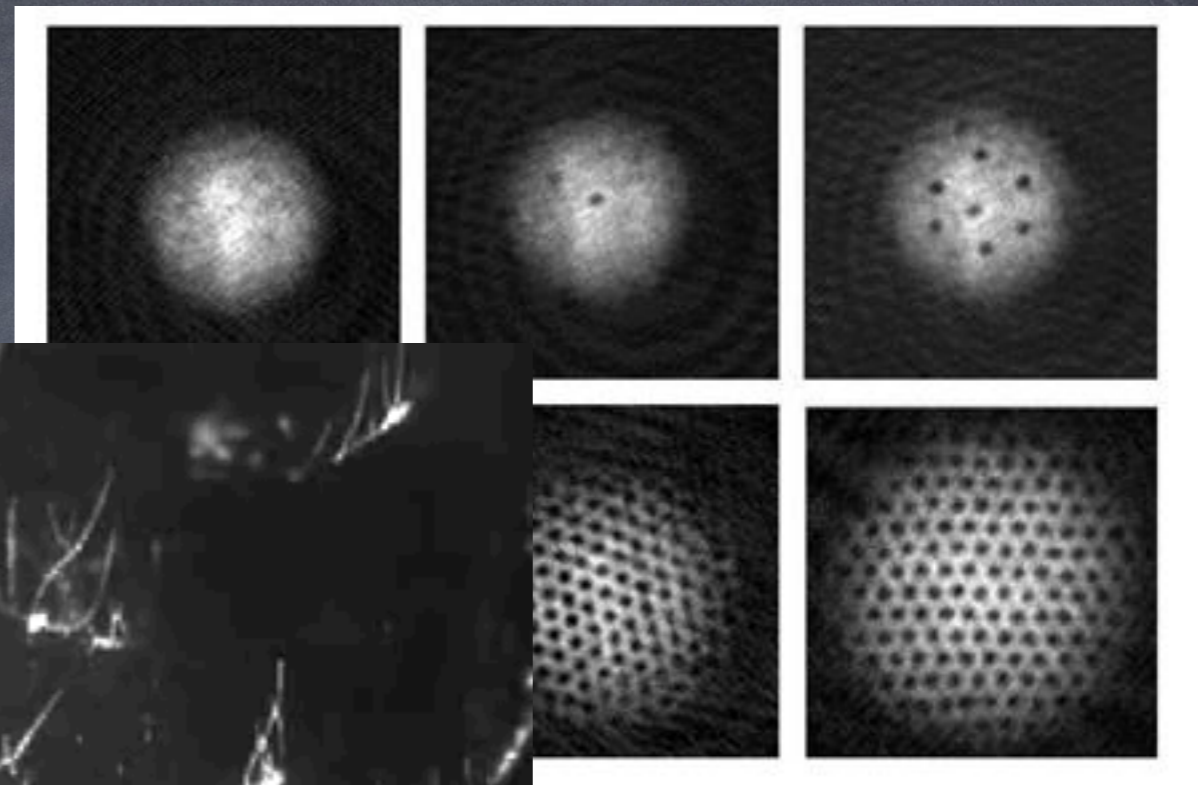
cf. Silverman & Mallett (2002);  
Rindler-Daller & Shapiro (2012)

Observational consequences?



# Vortices

When spun faster than critical velocity, superfluid develops vortices.



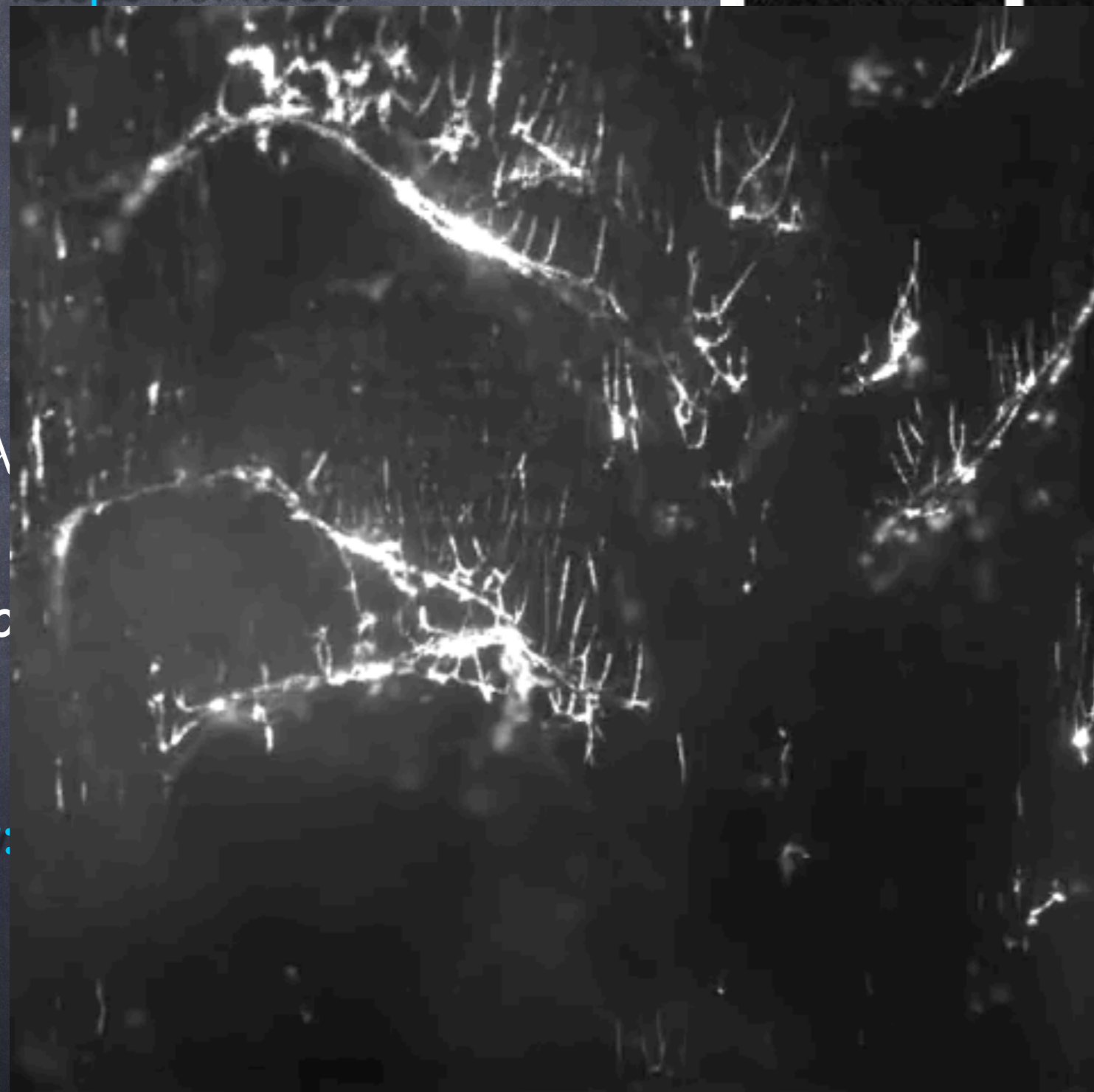
$$\omega_{cr} \sim$$

For a halo of

$$\omega \sim \lambda$$

$$\Rightarrow V_c$$

Line density:



erman & Mallett (2002);  
Daller & Shapiro (2012)

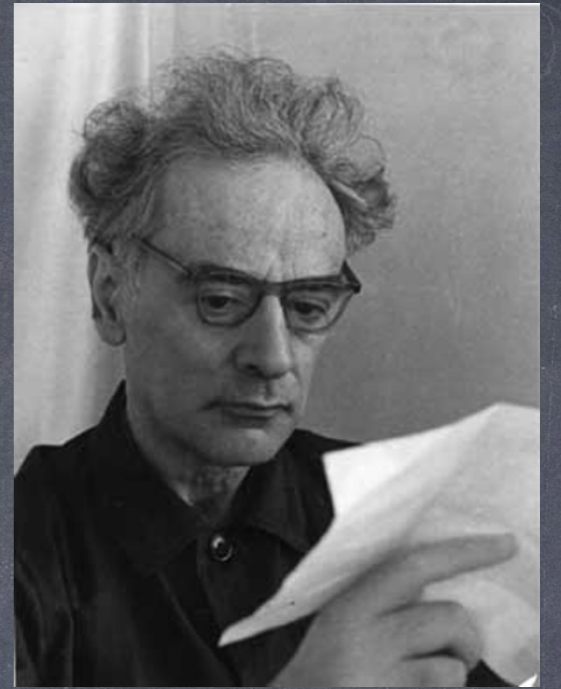
Galaxy mergers

Elder, JK, Mota & Winther, in progress

Superfluid cores should pass through each other with negligible dissipation if

$$v_{\text{infall}} \lesssim c_s$$

(Landau's criterion)



# Galaxy mergers

Elder, JK, Mota & Winther, in progress

Superfluid cores should pass through each other with negligible dissipation if

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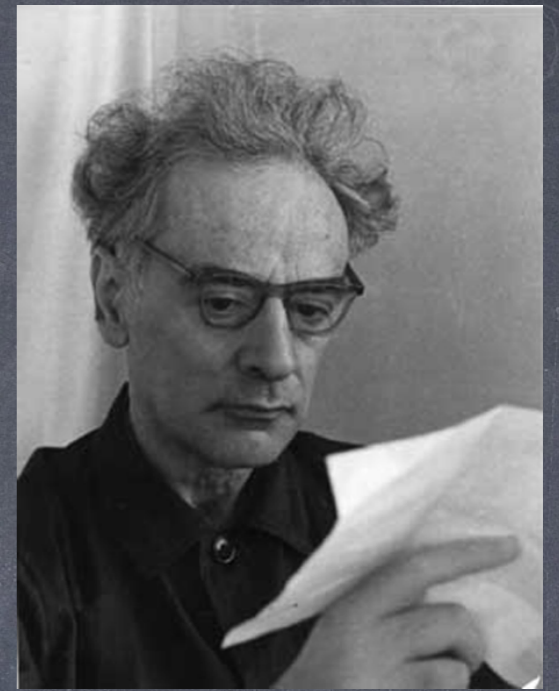
(Landau's criterion)

• If  $v_{\text{infall}} < c_s \sim 200 \text{ km/s}$ , then negligible dynamical friction between superfluids

⇒ Longer merger time scale + multiple encounters

• If  $v_{\text{infall}} > c_s$ , then encounter will excite DM particles out of the condensate, which will result in dynamical friction

⇒ Merged halo thermalize and settle back to condensate

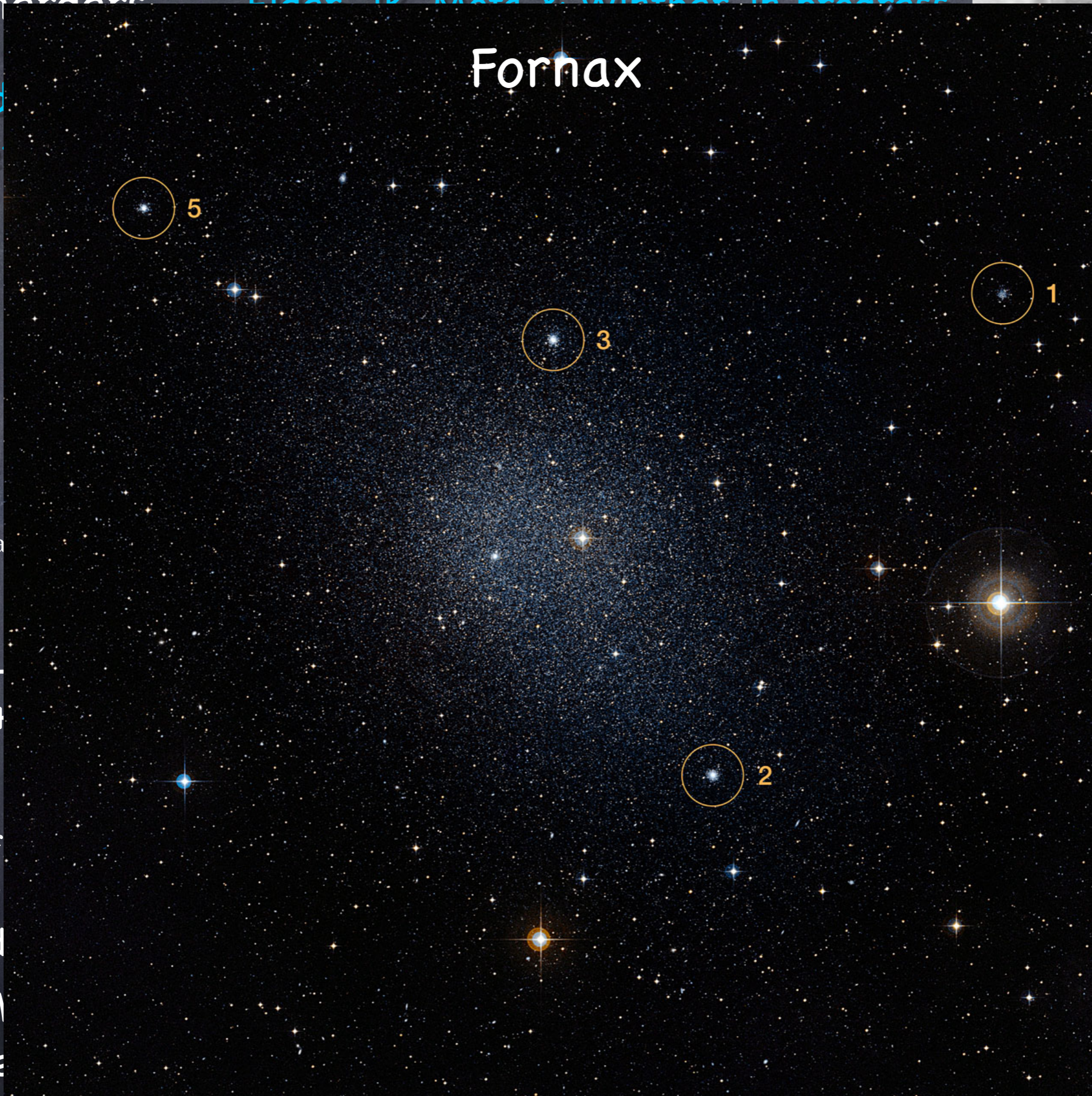


Galaxy mergers

Elder TK Meta 8 Winter in progress

Superfluid  
each other

# Fornax



👁️ If  $v_{\text{infa}}$   
dynamical



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+

👁️ If  $v_{\text{inf}}$   
DM partic  
result in d

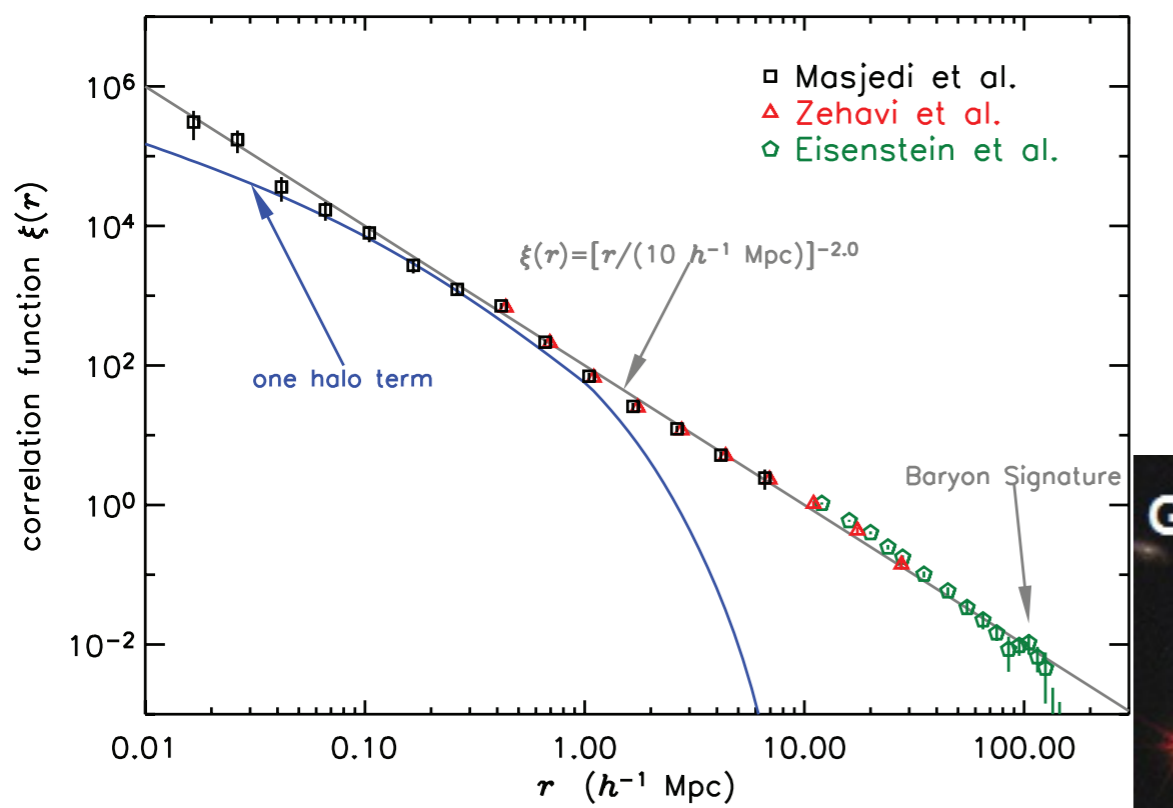


M  
se





# Reduced dynamical fraction?



Masjedi et al. (2006)

## Galaxy Abell 2261-BCG

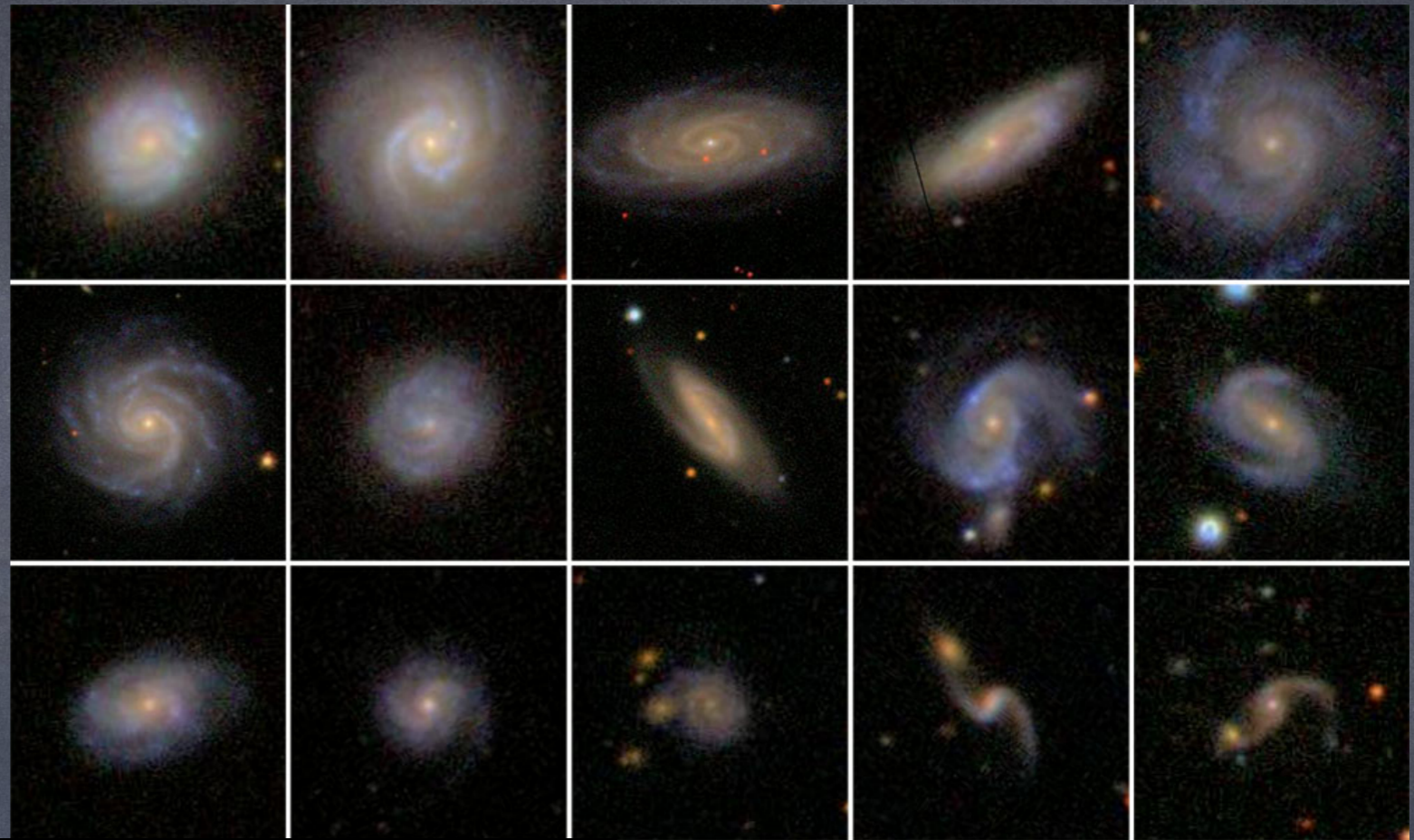


500,000 Light Years  
153 Kiloparsecs

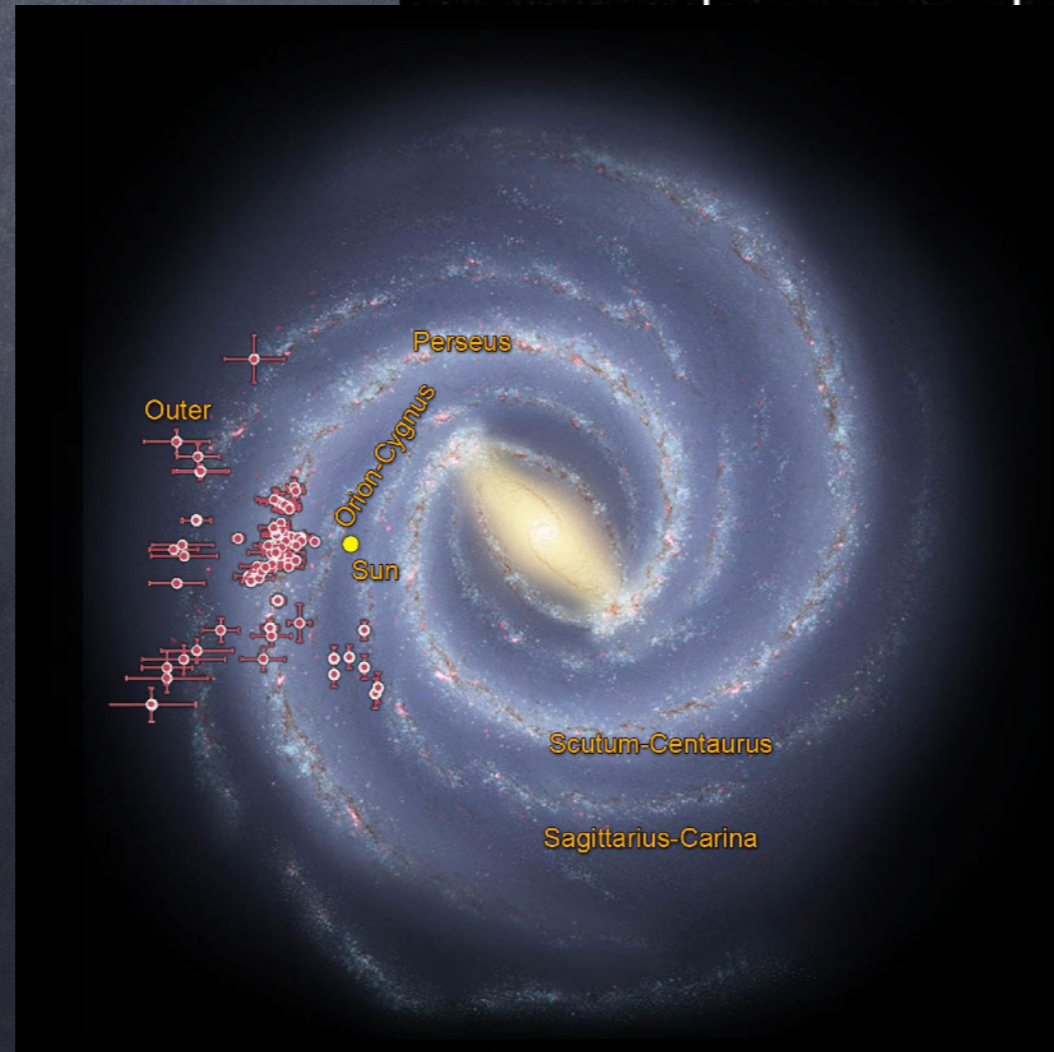
“This is surprising, as one might expect the direct interactions between galaxies (e.g., dynamical friction, galaxy merger, tidal impulses, etc.) to create features in the correlation function.”

# Reduced dynamical fraction?

- Bulgeless galaxies

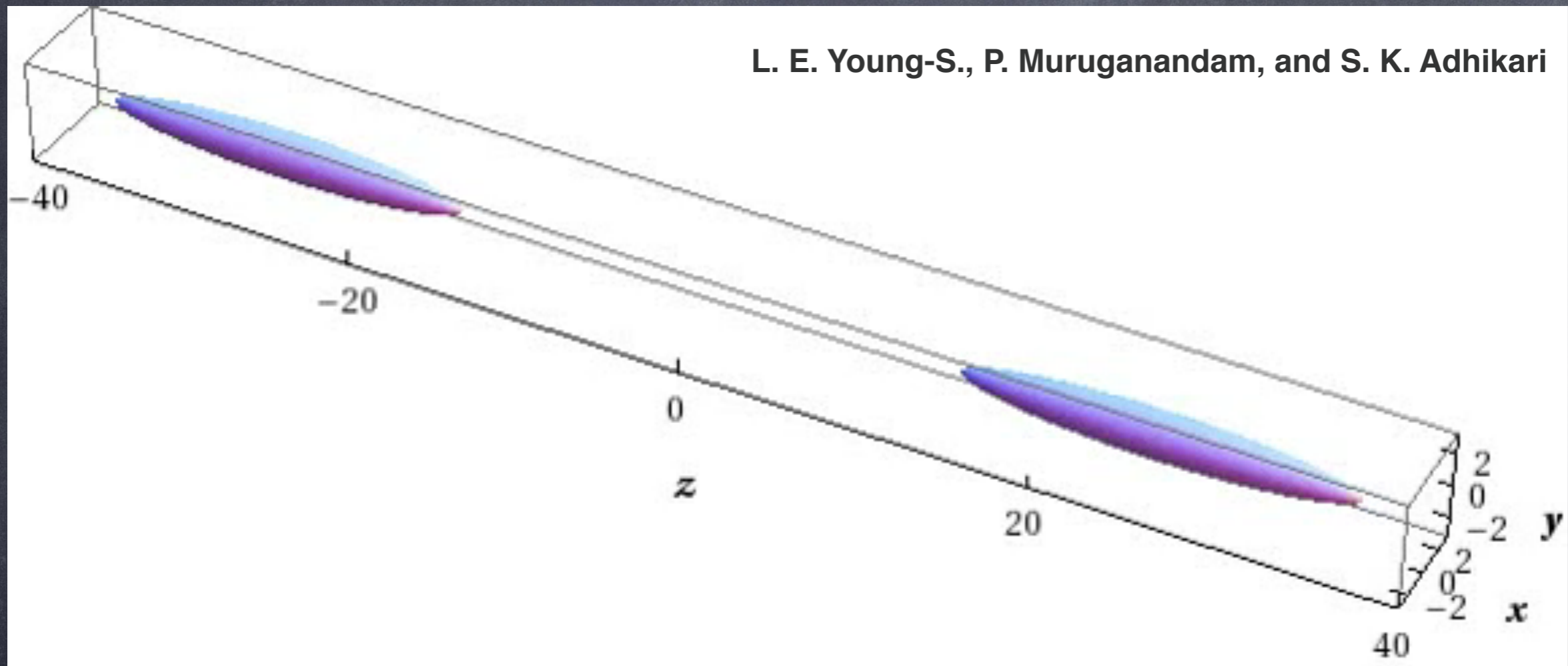


- Galactic bars



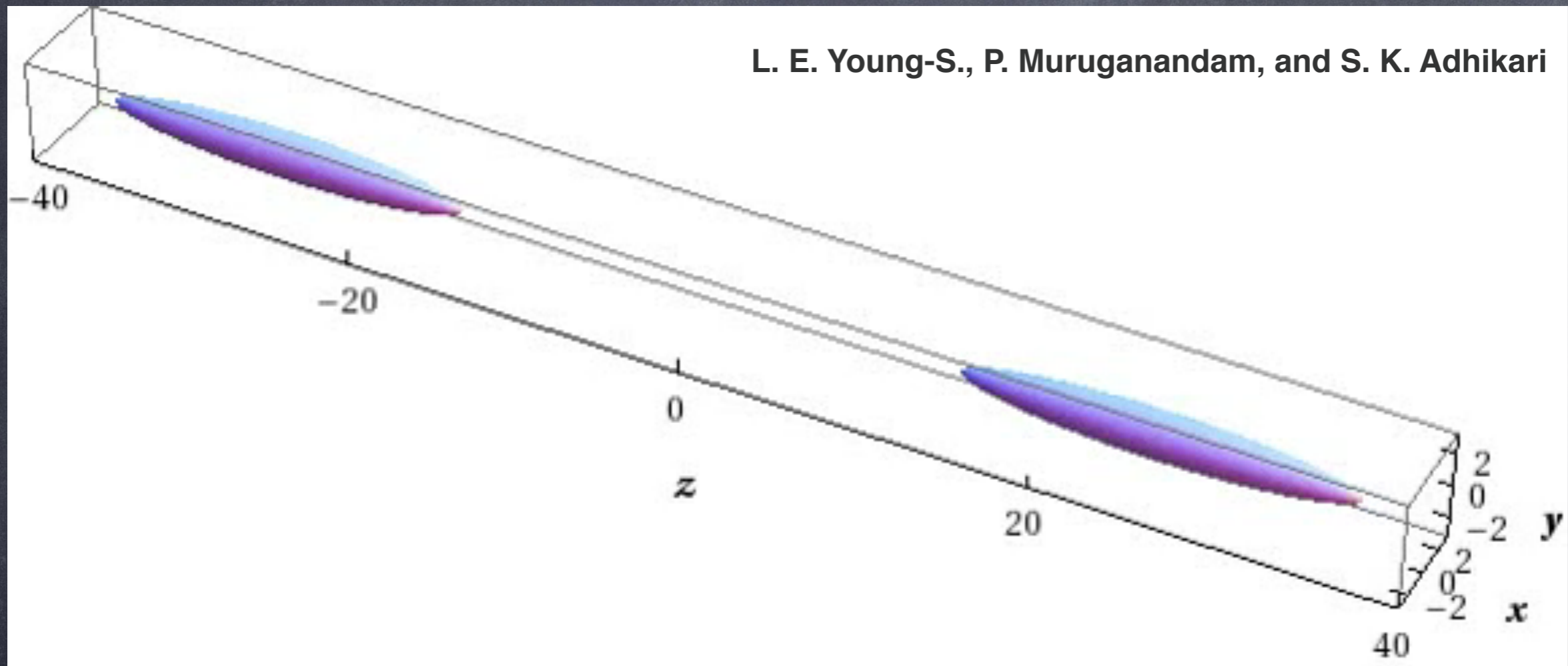
# When superfluids collide

L. E. Young-S., P. Muruganandam, and S. K. Adhikari

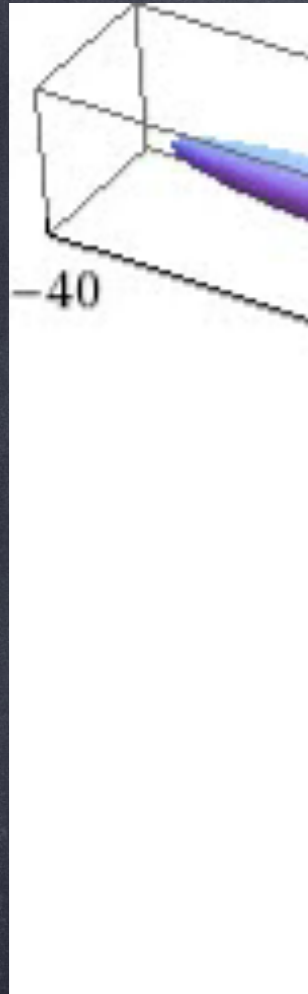


# When superfluids collide

L. E. Young-S., P. Muruganandam, and S. K. Adhikari



# When superfluids collide



dhikari

2  
0  
-2 **y**  
2  
2 **x**

No DM  $\implies$  No MOND



Globular clusters

Ibata et al. (2011)



Tidal dwarfs

Lelli et al. (2015)

No DM  $\implies$  No MOND



Globular clusters

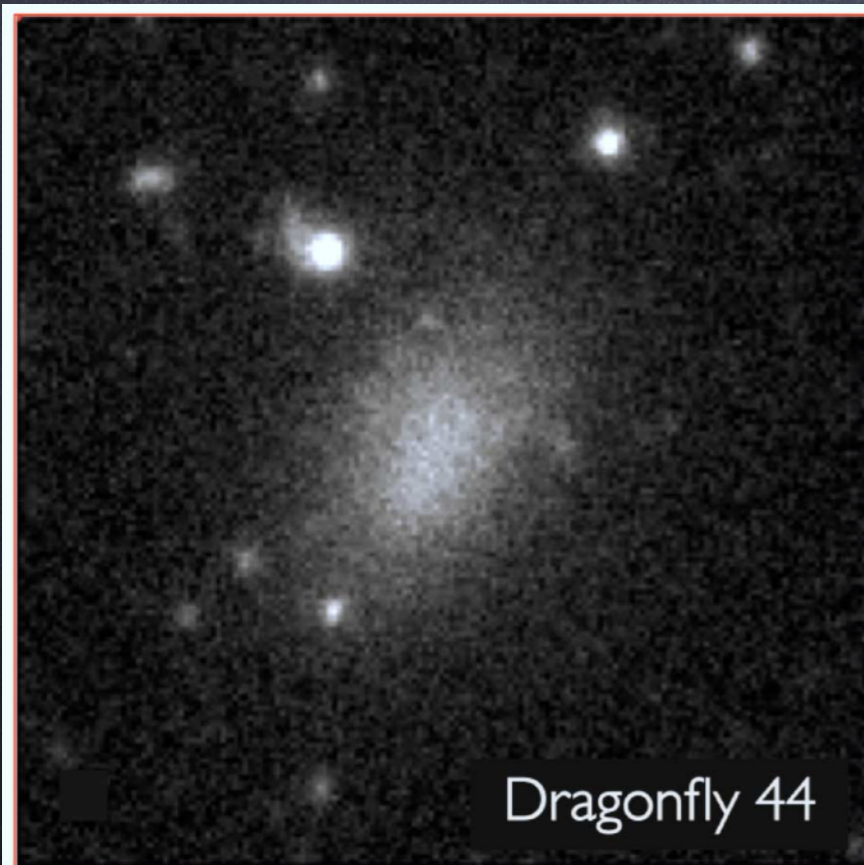
Ibata et al. (2011)



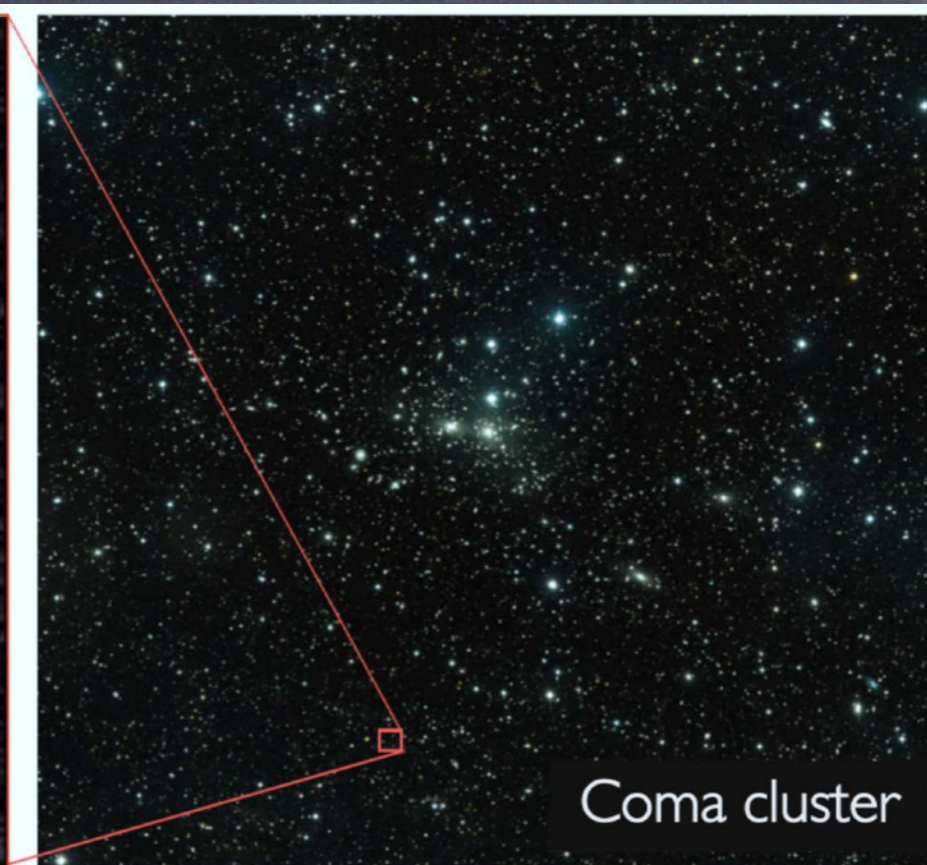
Tidal dwarfs

Lelli et al. (2015)

No superfluid  $\implies$  No external field effect



Dragonfly 44



Coma cluster

Ultra-diffuse galaxies

van Dokkum et al. (2015);  
Koda et al. (2015)

# Take-home messages



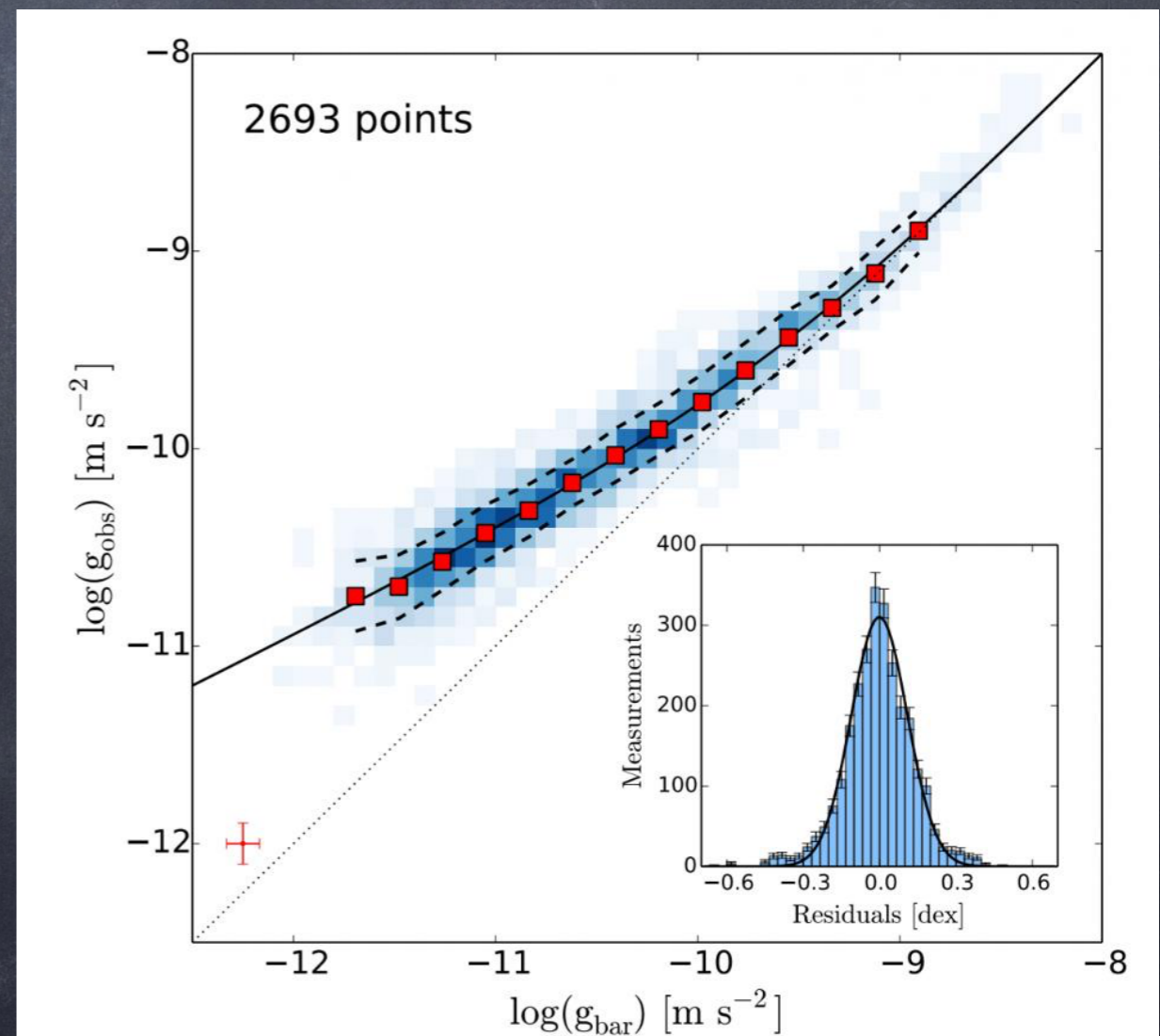
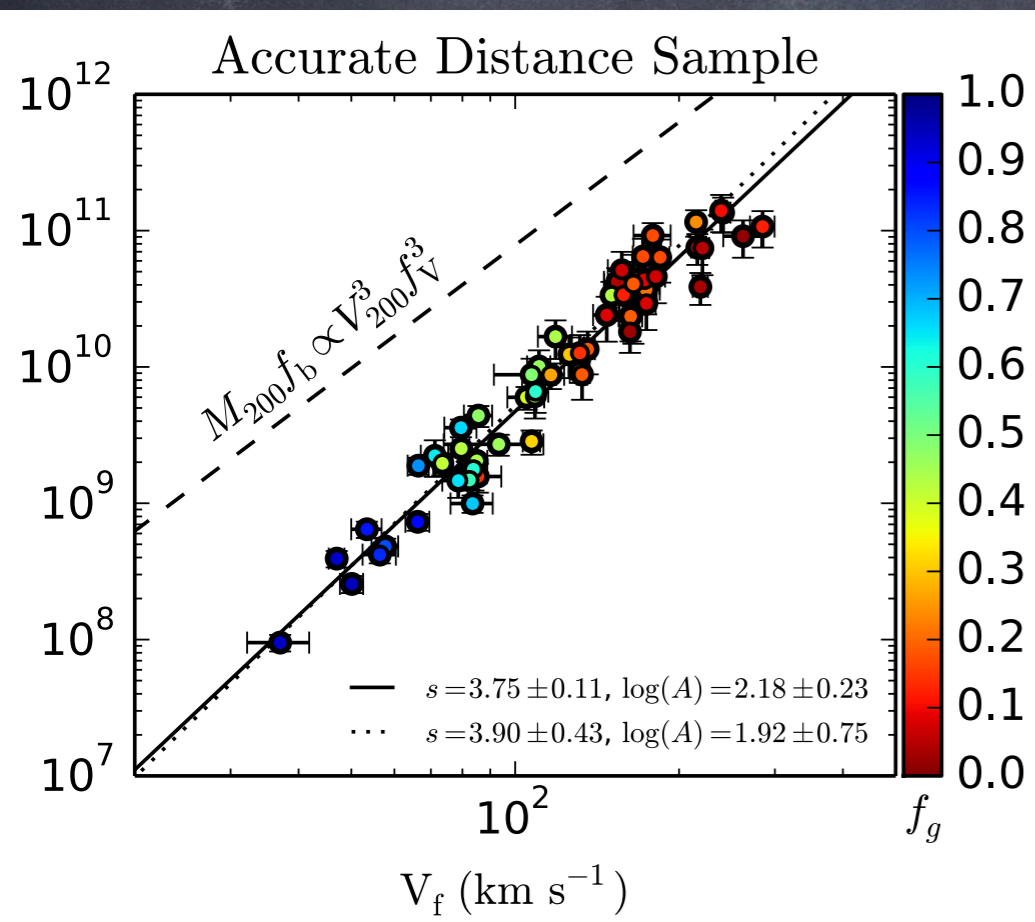
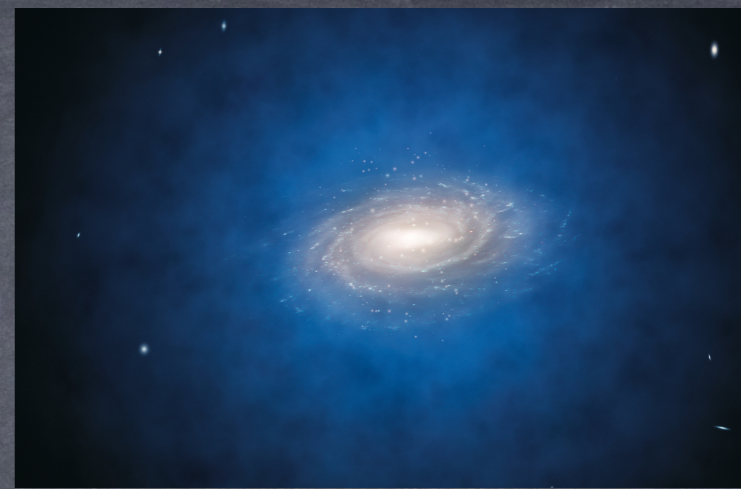
# Take-home messages

Believe in conspiracies!



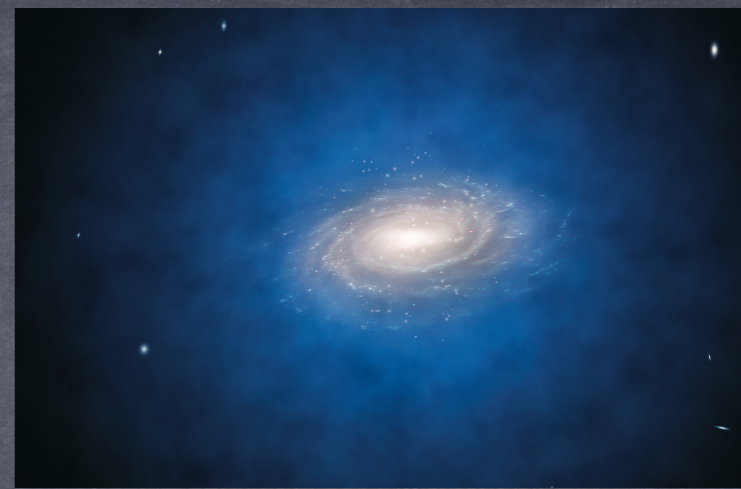
# Take-home messages

- Cold, collisionless DM works exquisitely well on largest scales, but **something is going on with galaxies**



# Take-home messages

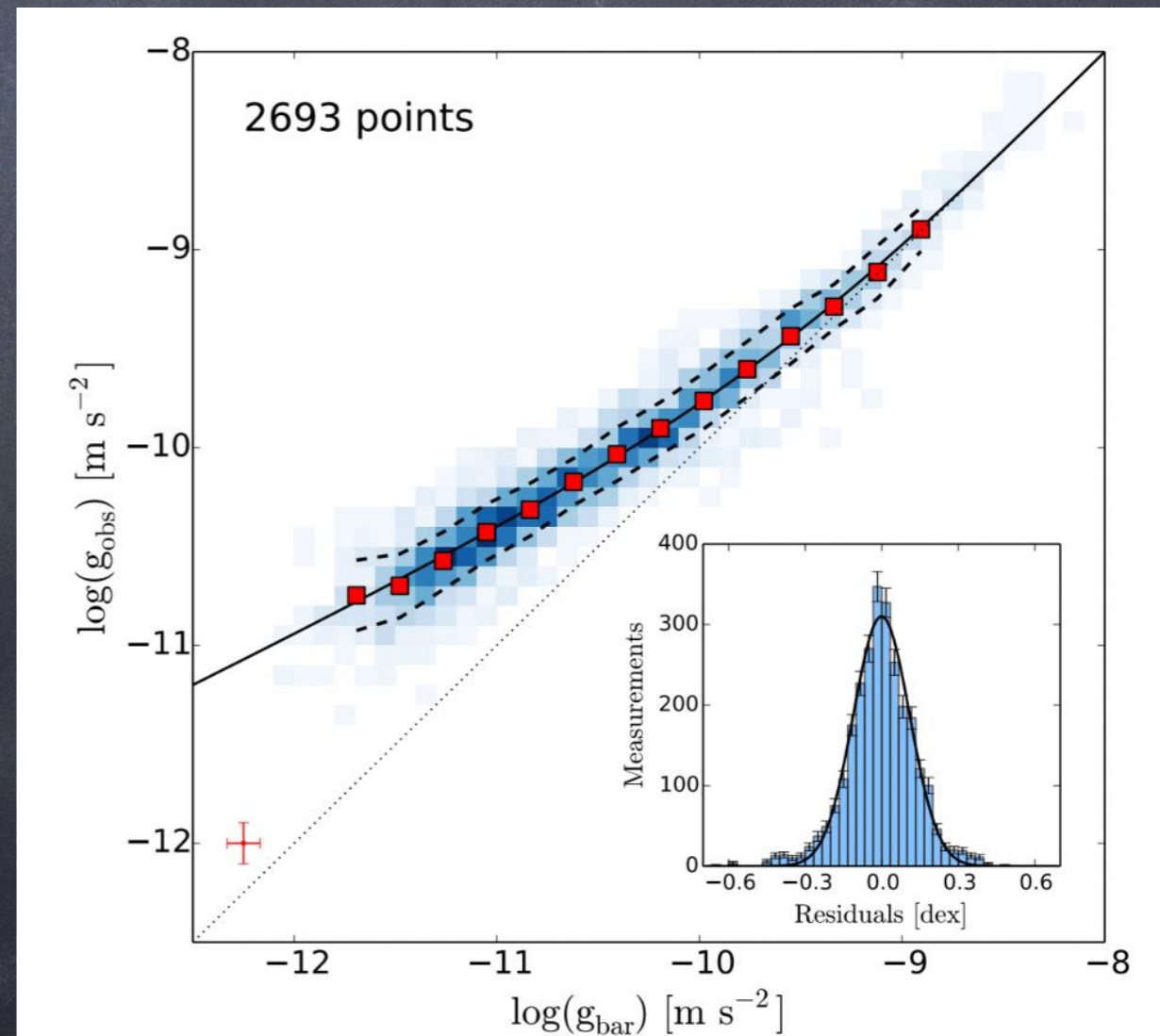
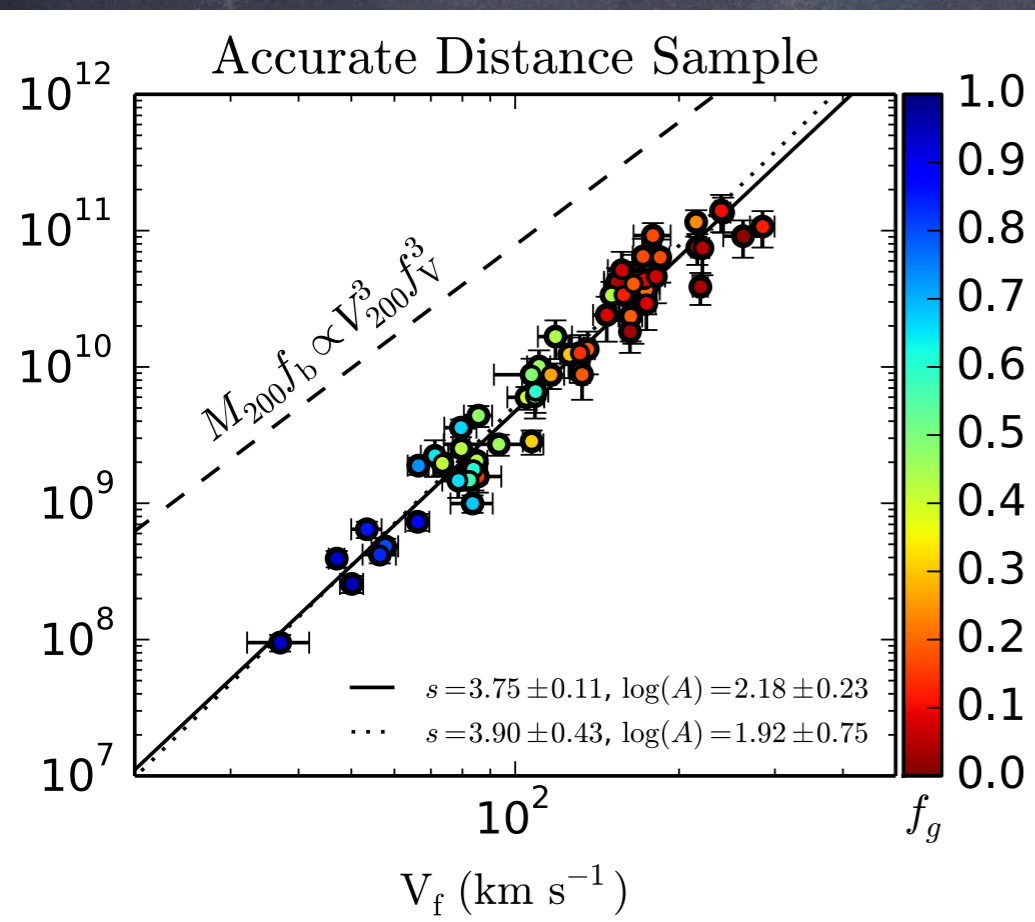
- Cold, collisionless DM works exquisitely well on largest scales, but **something is going on with galaxies**



The left-wing hippies  
"Modified gravity!"

The middle-ground  
"It's non-standard DM."

The right-wing evangelicals  
"It's all feedback!"



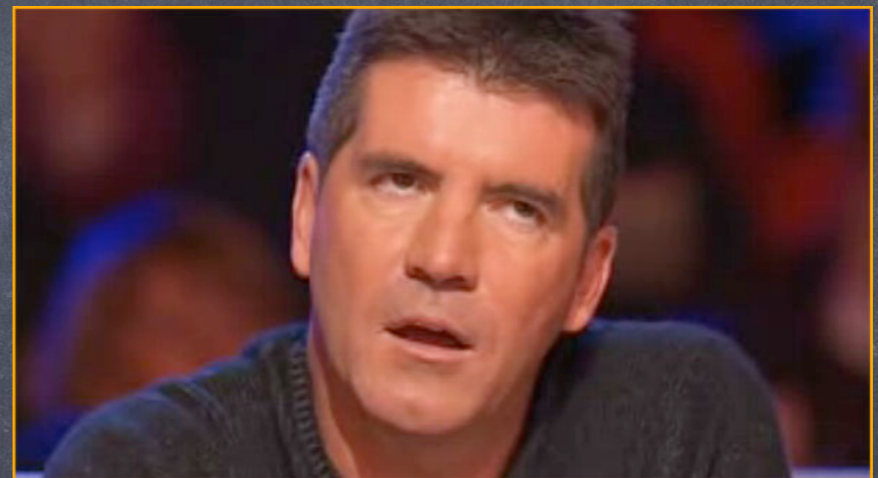
Galaxies are giving us strong hints about the fundamental nature of dark matter...

Galaxies are giving us strong hints about the fundamental nature of dark matter...

Nature is singing loud and clear!



Mother Nature



Cosmologist



How does dark energy fit into the picture?



