

# Global Fits at CEPC

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# Why lepton colliders?

- ▶ **Build large colliders → go to high energy → discover new particles!**

- ▶ Higgs and nothing else?



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LHC will definitely find new physics!

- ▶ What's next?
  - ▶ Build an even larger collider ( $\sim 100$  TeV)?
  - ▶ No guaranteed discovery!

# Why lepton colliders?

- ▶ **Build large colliders** → go to high energy → discover new particles!



**do precision measurements → discover new physics indirectly!**

- ▶ Higgs and nothing else?



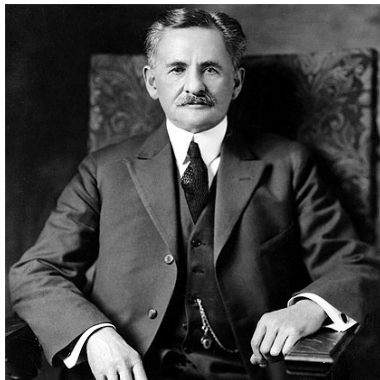
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LHC will definitely find new physics!

- ▶ What's next?

- ▶ Build an even larger collider ( $\sim 100 \text{ TeV}$ )?
- ▶ No guaranteed discovery!
- ▶ **Higgs factory!** (A lepton collider at  $\sqrt{s} \sim 240\text{-}250 \text{ GeV}$  or above.)
- ▶ **More than just a Higgs factory!** (Z, W, top, ...)
- ▶ **Standard Model Effective Field Theory** (model independent approach)
- ▶ Specific models (SUSY, 2HDM ...)

## Precision is the key!

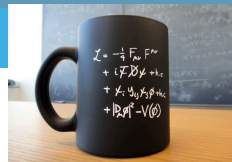


“Our future discoveries must be looked for in the sixth place of decimals.”

— Albert A. Michelson



# The Standard Model Effective Field Theory

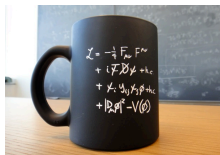


- ▶  $[\mathcal{L}_{\text{SM}}] \leq 4$ . Why?
  - ▶ ~~Bad things happen when we have non-renormalizable operators!~~
  - ▶ Everything is fine as long as we are happy with finite precision in perturbative calculation.
- ▶ **d=5:**  $\frac{c}{\Lambda} LLHH \sim \frac{c\nu^2}{\Lambda} \nu\nu$ , Majorana neutrino mass.
- ▶ Assuming Baryon and Lepton numbers are conserved,

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_j \frac{c_j^{(8)}}{\Lambda^4} \mathcal{O}_j^{(8)} + \dots$$

- ▶ If  $\Lambda \gg v, E$ , then **SM + dimension-6 operators** are sufficient to parameterize the physics around the electroweak scale.

# The Standard Model Effective Field Theory



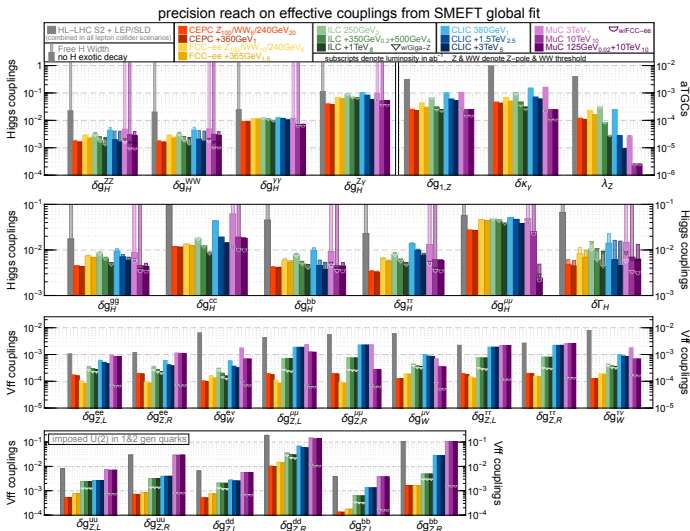
+

$X^3$		$\psi^4$ and $\psi^3 D^2$	$\psi^3 \psi^3$	$(LL)(LL)$		$(RR)(RR)$	$(LL)(RR)$
$Q_{G1}$	$f^{ABC}G^{AB}G^{BC}G^{CA}$	$Q_{\psi^4}$	$(\psi^\dagger\psi)^4$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger_\mu\psi)(\psi^\dagger_\mu\psi)$
$Q_{G2}$	$f^{ABC}G^{AB}G^{BC}G^{CA}$	$Q_{\psi^3 D^2}$	$(\psi^\dagger\psi)(\psi^\dagger\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger_\mu\psi)(\psi^\dagger_\mu\psi)$
$Q_{W1}$	$\epsilon^{IJK}W^{IJ}W^{JK}W^{KI}$	$Q_{\psi^3 D^2}$	$(\psi^\dagger D_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger_\mu\psi)(\psi^\dagger_\mu\psi)$
$Q_{\psi^3}$	$\epsilon^{IJK}\bar{W}^{IJ}W^{JK}W^{KI}$	$Q_{\psi^3 D^2}$	$(\psi^\dagger D_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger_\mu\psi)(\psi^\dagger_\mu\psi)$
$X^3\psi^2$		$\psi^2 X\psi$	$\psi^2\psi^2 D$	$(LL)(RL)$ and $(LR)(LR)$		$B$ -violating	
$Q_{G1}$	$\psi^\dagger\psi G^{AB}G^{BC}G^{CA}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{G2}$	$\psi^\dagger\psi G^{AB}G^{BC}G^{CA}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W1}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W2}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W3}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W4}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W5}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W6}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W7}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W8}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W9}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$
$Q_{W10}$	$\psi^\dagger\psi W^{IJ}W^{JK}W^{KI}$	$Q_{W1}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$	$Q_{\psi^3\psi}$	$(\psi^\dagger\psi)(\psi^\dagger_\mu\psi)$

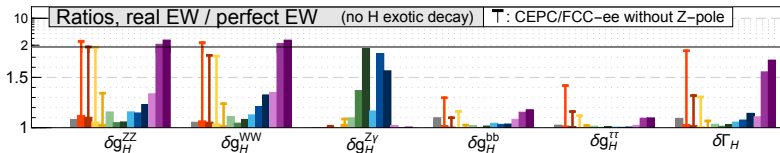
- Write down all possible (non-redundant) dimension-6 operators ...
- 59 operators (76 parameters) for 1 generation, or 2499 parameters for 3 generations. [arXiv:1008.4884] Grzadkowski, Iskrzyński, Misiak, Rosiek, [arXiv:1312.2014] Alonso, Jenkins, Manohar, Trott.
- A full global fit with all measurements to all operator coefficients?
  - We usually only need to deal with a subset of them, e.g.  $\sim 20-30$  parameters for Higgs and electroweak measurements.
- Do a global fit and present the results with some fancy bar plots!

# Higgs + EW, Results from the Snowmass 2021 (2022) study

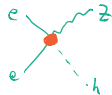
[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou



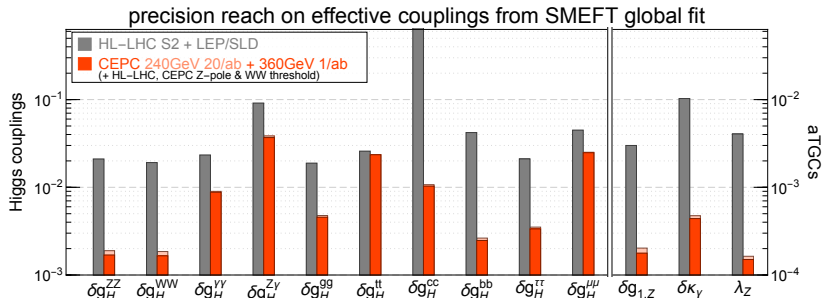
# Impacts of (lack of) the Z-pole run



- ▶ Without good Z-pole measurements, the  $eeZh$  contact interaction may have a significant impact on the Higgs coupling determination.
- ▶ Current (LEP) Z-pole measurements are not good enough for CEPC/FCC-ee Higgs measurements!
  - ▶ **A future Z-pole run is important!**
- ▶ Linear colliders suffer less from the lack of a Z-pole run. **(Win Win!)**

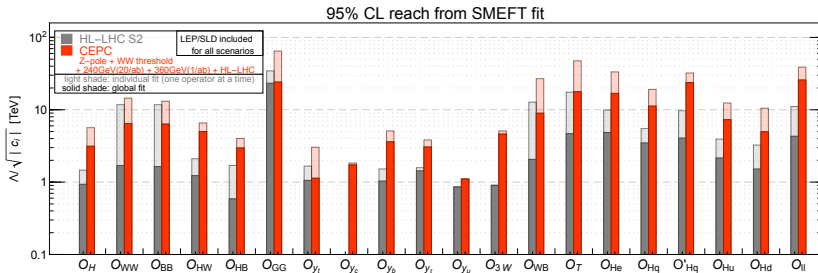


# SMEFT global fit (effective coupling precision) CEPC Snowmass report [2205.08553]



- ▶ 28-parameter fit projected on Higgs couplings and anomalous triple gauge couplings.
- ▶  $\delta g_H^{ZZ} \approx \delta g_H^{WW}$  from theoretical constraints (gauge invariance & custodial symmetry) and EW measurements.
- ▶ Non-negligible improvement from the 360 GeV run.

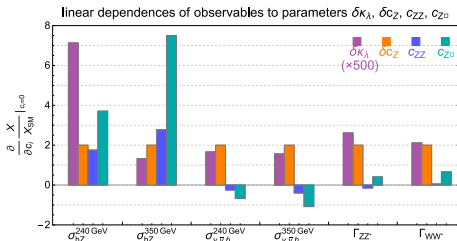
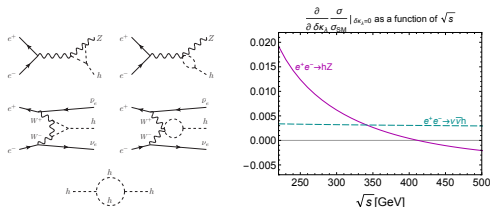
# SMEFT global fit (reach on new physics scale)



- 20-parameter fit (assuming flavor universality in gauge-fermion couplings).

# Triple Higgs coupling at one-loop order

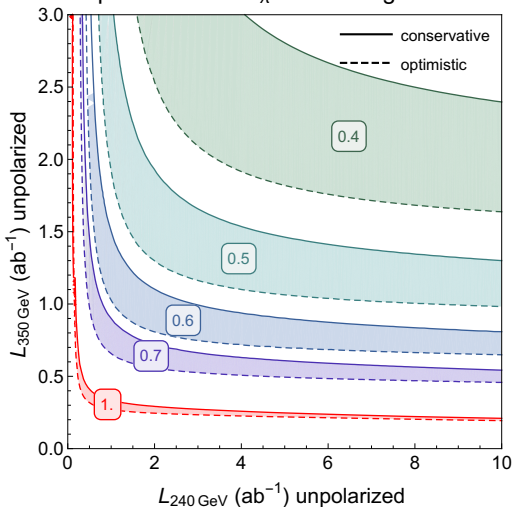
[arXiv:1711.03978] Di Vita, Durieux, Grojean, JG, Liu, Panico, Riembau, Vantalon



- ▶  $\kappa_\lambda \equiv \frac{\lambda_{hhh}}{\lambda_{SM}^{hhh}}$ ,  
 $\delta\kappa_\lambda \equiv \kappa_\lambda - 1 = C_6 - \frac{3}{2}C_H$ ,  
 with  $\mathcal{L} \supset -\frac{c_6\lambda}{v^2}(H^\dagger H)^3$ .
- ▶ One loop corrections to all Higgs couplings (production and decay).
- ▶ 240 GeV:  $hZ$  near threshold (more sensitive to  $\delta\kappa_\lambda$ )
- ▶ at 350-365 GeV:
  - ▶ WW fusion
  - ▶  $hZ$  at a different energy
- ▶  $h \rightarrow WW^*/ZZ^*$  also have some discriminating power (but turned out to be not enough).

# Triple Higgs coupling from EFT global fits

precision on  $\delta\kappa_\lambda$  from EFT global fit



- Runs at two different energies (240 GeV and 350/365 GeV) are needed to obtain good constraints on the triple Higgs coupling in a global fit!



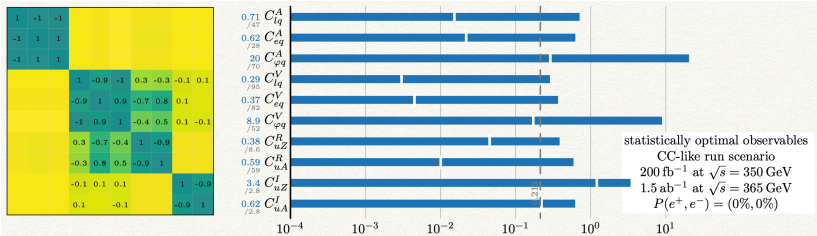
# Probing Top operators with $e^-e^+ \rightarrow t\bar{t}$

[arXiv:1807.02121] Durieux, Perelló, Vos, Zhang

$$\begin{aligned}
 O_{\varphi q}^1 &\equiv \frac{y_t^2}{2} \bar{q}\gamma^\mu q \varphi^\dagger i\overleftrightarrow{D}_\mu \varphi, & O_{uG} &\equiv y_t g_s \bar{q} T^A \sigma^{\mu\nu} u \epsilon \varphi^* G_{\mu\nu}^A, \\
 O_{\varphi q}^3 &\equiv \frac{y_t^2}{2} \bar{q}\tau^I \gamma^\mu q \varphi^\dagger i\overleftrightarrow{D}_\mu \varphi, & O_{uW} &\equiv y_t g_W \bar{q}\tau^I \sigma^{\mu\nu} u \epsilon \varphi^* W_{\mu\nu}^I, \\
 O_{\varphi u} &\equiv \frac{y_t^2}{2} \bar{u}\gamma^\mu u \varphi^\dagger i\overleftrightarrow{D}_\mu \varphi, & O_{dW} &\equiv y_t g_W \bar{q}\tau^I \sigma^{\mu\nu} d \epsilon \varphi^* W_{\mu\nu}^I, \\
 O_{\varphi ud} &\equiv \frac{y_t^2}{2} \bar{u}\gamma^\mu d \varphi^T \epsilon iD_\mu \varphi, & O_{uB} &\equiv y_t g_Y \bar{q}\sigma^{\mu\nu} u \epsilon \varphi^* B_{\mu\nu},
 \end{aligned}$$

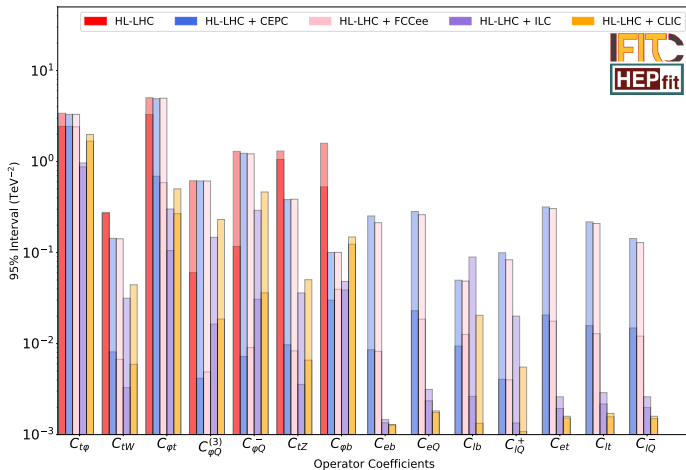
$$\begin{aligned}
 O_{lq}^1 &\equiv \frac{1}{2} \bar{q}\gamma_\mu q \bar{l}\gamma^\mu l, \\
 O_{lq}^3 &\equiv \frac{1}{2} \bar{q}\tau^I \gamma_\mu q \bar{l}\tau^I \gamma^\mu l, \\
 O_{lu} &\equiv \frac{1}{2} \bar{u}\gamma_\mu u \bar{l}\gamma^\mu l, \\
 O_{eq} &\equiv \frac{1}{2} \bar{q}\gamma_\mu q \bar{e}\gamma^\mu e, \\
 O_{eu} &\equiv \frac{1}{2} \bar{u}\gamma_\mu u \bar{e}\gamma^\mu e,
 \end{aligned}$$

- ▶ Also need to include **top dipole** interactions and **eett** contact interactions!
- ▶ Hard to resolve the **top couplings** from **4f** interactions with just the 365 GeV run.
  - ▶ Can't really separate  $e^+e^- \rightarrow Z/\gamma \rightarrow t\bar{t}$  from  $e^+e^- \rightarrow Z' \rightarrow t\bar{t}$ .
  - ▶ Is that a big deal?



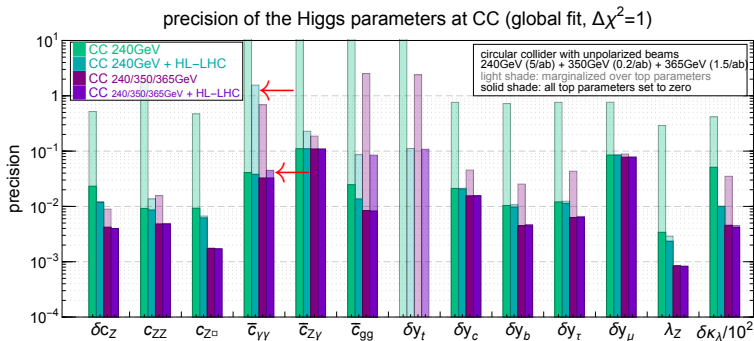
# Results from the recent snowmass study

[2206.08326] de Blas, Du, Grojean, JG, Miralles, Peskin, Tian, Vos, Vryonidou

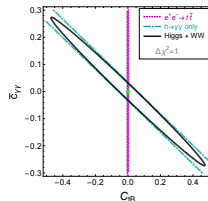


# Top operators in loops (Higgs processes)

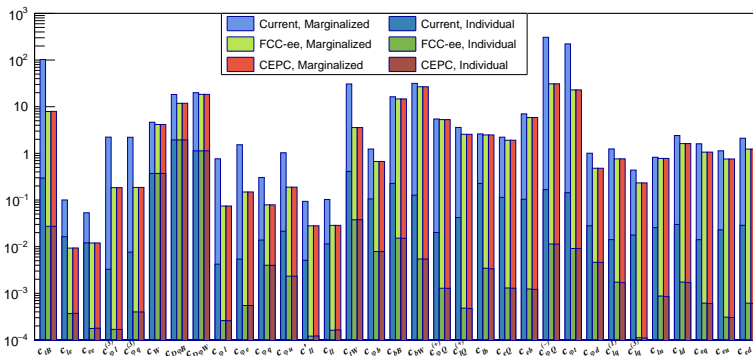
[1809.03520] G. Durieux, JG, E. Vryonidou, C. Zhang



- ▶  $O_{tB} = (\bar{Q}\sigma^{\mu\nu}t)\tilde{\varphi}B_{\mu\nu} + h.c.$  is not very well constrained at the LHC, and it generates dipole interactions that contributes to the  $h\gamma\gamma$  vertex.
- ▶ Deviations in  $h\gamma\gamma$  coupling  $\Rightarrow$  run at  $\sim 365$  GeV to confirm?



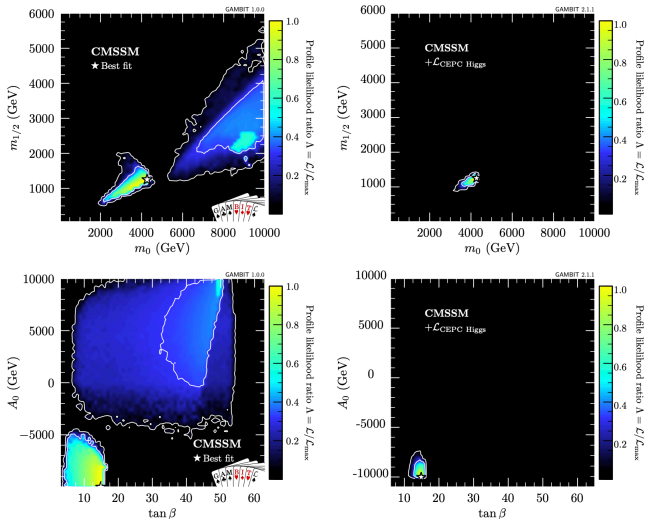
# Top operators in loops (EW processes) [2205.05655] Y. Liu, Y. Wang, C. Zhang, L. Zhang, JG



- ▶ Top operators (1-loop) + EW operators (tree, including bottom dipole operators)
- ▶ Good sensitivities, but too many parameters for a global fit...
- ▶ It shows the importance of directly measuring  $e^+e^- \rightarrow t\bar{t}$ .

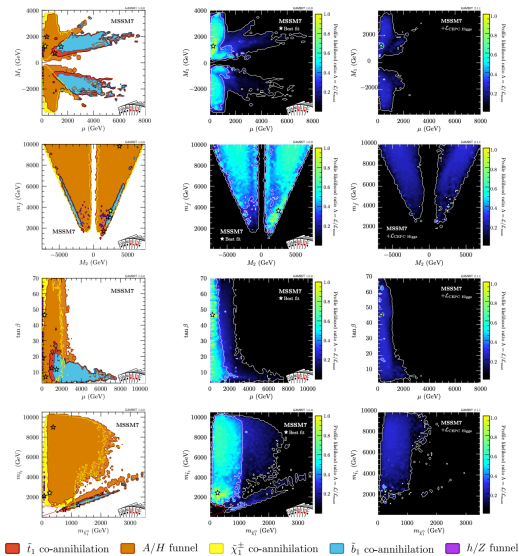
# SUSY fits at future Higgs factories

[2203.04828] Athron, Balazs, Fowlie, Lv, Su, Wu, Yang, Zhang



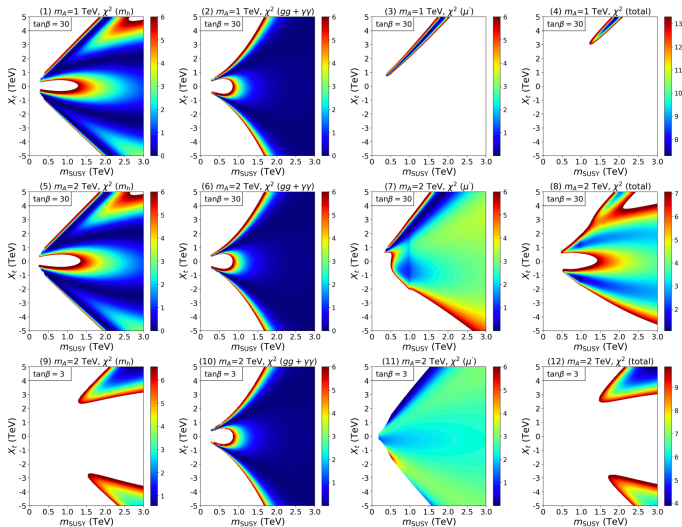
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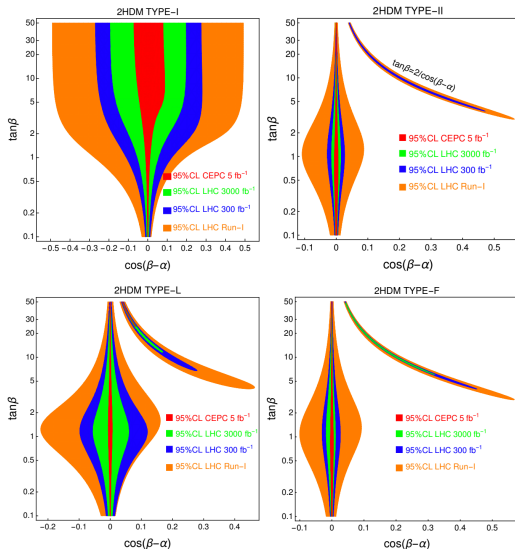
# SUSY fits at future Higgs factories

[2010.09782] Li, Song, Su, Su, Yang



# 2HDM fits at future Higgs factories

[1709.06103] JG, Li, Liu, Su, Su





# Conclusion

- ▶ **We have no idea what is the new physics beyond the Standard Model.**
- ▶ **One important direction to move forward is to do precision measurements of the Standard Model processes.**
  - ▶ A future lepton collider is an ideal machine for that.
- ▶ **SMEFT is a good model-independent framework.**
- ▶ **Specific model studies (such as SUSY and 2HDM) are also important.**

# Conclusion



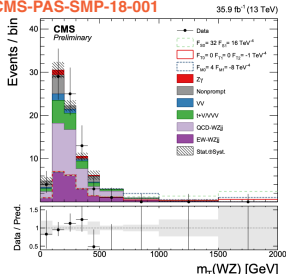
**Waiting for the CEPC to be built...**

backup slides

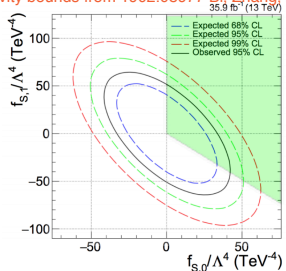
# Probing dimension-8 operators?

- ▶ The dimension-8 contribution has a large energy enhancement ( $\sim E^4/\Lambda^4$ )!
- ▶ It is difficult for LHC to probe these bounds.
  - ▶ Low statistics in the high energy bins.
  - ▶ Example: Vector boson scattering.
  - ▶  $\Lambda \lesssim \sqrt{s}$ , the EFT expansion breaks down!
- ▶ Can we separate the dim-8 and dim-6 effects?
  - ▶ Precision measurements at several different  $\sqrt{s}$ ?  
(A **very** high energy lepton collider?)
  - ▶ Or find some special process where dim-8 gives the leading new physics contribution?

CMS-PAS-SMP-18-001



positivity bounds from 1902.08977 Bi, Zhang, Zhou

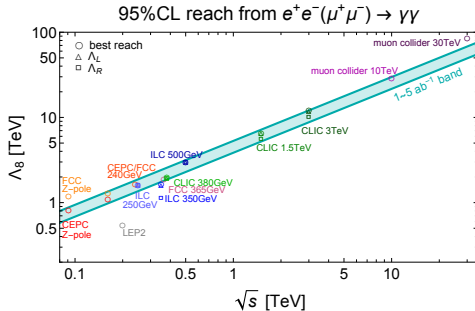
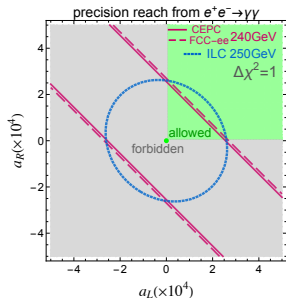


# The diphoton channel [arXiv:2011.03055] Phys.Rev.Lett. 129, 011805, JG, Lian-Tao Wang, Cen Zhang

- ▶  $e^+e^- \rightarrow \gamma\gamma$  (or  $\mu^+\mu^- \rightarrow \gamma\gamma$ ), SM, non-resonant.
- ▶ Leading order contribution: **dimension-8 contact interaction**.  
( $f^+f^- \rightarrow \bar{e}_L e_L$  or  $e_R \bar{e}_R$ )

$$\mathcal{A}(f^+f^-\gamma^+\gamma^-)_{\text{SM+d8}} = 2e^2 \frac{\langle 24 \rangle^2}{\langle 13 \rangle \langle 23 \rangle} + \frac{a}{v^4} [13][23] \langle 24 \rangle^2.$$

- ▶ Can probe dim-8 operators (and their positivity bounds) at a **Higgs factory** ( $\sim 240$  GeV)!



# Machine learning in SMEFT analyses

Machine learning is not physics!



past

真香！

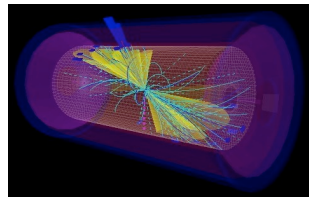
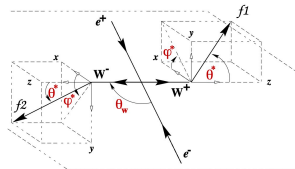


now

- ▶ Current work with Shengdu Chai (柴声都), Lingfeng Li (李凌风) on  $e^+e^- \rightarrow WW$ .
- ▶ Current work with Yifan Fei (费昶帆), Tong Shen (沈同) and Kerun Yu (余柯润) on  $e^+e^- \rightarrow t\bar{t}$ .

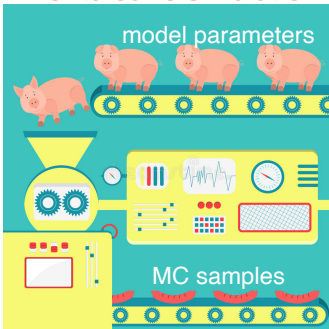
# Why Machine learning?

- ▶ In many cases, the new physics contributions are sensitive to the differential distributions.
  - ▶  $e^+e^- \rightarrow WW \rightarrow 4f \Rightarrow 5 \text{ angles}$
  - ▶  $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^- \rightarrow 6f \Rightarrow 9 \text{ angles}$
  - ▶ How to extract information from the differential distribution?
  - ▶ If we have the full knowledge of  $\frac{d\sigma}{d\Omega} \Rightarrow$  matrix-element method, optimal observables...
- ▶ The ideal  $\frac{d\sigma}{d\Omega}$  we can calculate is not the  $\frac{d\sigma}{d\Omega}$  that we actually measure!
  - ▶ detector acceptance, measurement uncertainties, ISR/beamstrahlung ...
  - ▶ In practice we only have **MC samples**, not analytic expressions, for  $\frac{d\sigma}{d\Omega}$ .

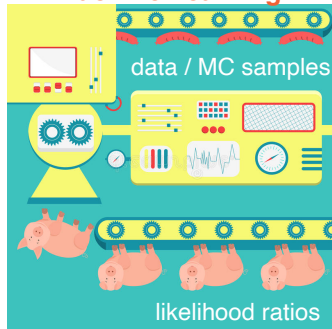


# The “inverse problem”

## Monte Carlo simulation



## Machine Learning



- ▶ **Forward:** From model parameters we can calculate the ideal  $\frac{d\sigma}{d\Omega}$ , simulate complicated effects and produce MC samples.
- ▶ **Inverse:** From data / MC samples, how do we know the model parameters?
- ▶ With **Neural Network** we can (in principle) reconstruct  $\frac{d\sigma}{d\Omega}$  (or likelihood ratios) from MC samples.



# A rough sketch

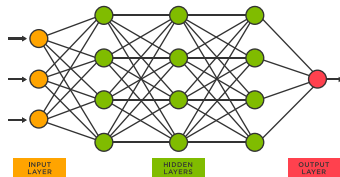
- ▶ We have a theory (SMEFT) that gives a differential cross section  $\frac{d\sigma}{d\Omega}$  which is a function of the parameters of interest  $\mathbf{c}$  (Wilson coefficients).
  - ▶ For simplicity, let's ignore the total rate and focus on  $\frac{1}{\sigma} \frac{d\sigma}{d\Omega} \equiv p(\mathbf{x}|\mathbf{c})$ , i.e. it's a probability density function of the observables  $\mathbf{x}$ .
  - ▶ Define the likelihood function  $\mathcal{L}(\mathbf{c}|\mathbf{x}) \equiv p(\mathbf{x}|\mathbf{c})$ . For a sample of  $N$  events, maximizing the joint likelihood  $\prod_{i=1}^N \mathcal{L}(\mathbf{c}|\mathbf{x}_i)$  (or the log likelihood) gives the best estimator for  $\mathbf{c}$ . (matrix-element method)
- ▶ Suppose we have two equal-size samples  $\{\mathbf{x}_{i,\mathbf{c}_0}\} \sim p(\mathbf{x}|\mathbf{c}_0)$  and  $\{\mathbf{x}_{i,\mathbf{c}_1}\} \sim p(\mathbf{x}|\mathbf{c}_1)$ , one could define the cross-entropy loss function(al)

$$L(\hat{s}) = -\sum_{i=1}^N \log \hat{s}(\mathbf{x}_{i,\mathbf{c}_1}) - \sum_{i=1}^N \log (1 - \hat{s}(\mathbf{x}_{i,\mathbf{c}_0})) ,$$

which is minimized by the optimal decision function

$$s(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1) = \frac{p(\mathbf{x}|\mathbf{c}_1)}{p(\mathbf{x}|\mathbf{c}_0) + p(\mathbf{x}|\mathbf{c}_1)} .$$

# A rough sketch



- From **neural network** we can construct a function  $\hat{s}(\mathbf{x})$ . By minimizing  $L(\hat{s})$  with respect to  $\hat{s}(\mathbf{x})$  we can obtain an estimator for the likelihood ratio

$$\hat{r}(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1) = \frac{1 - \hat{s}(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1)}{\hat{s}(\mathbf{x}|\mathbf{c}_0, \mathbf{c}_1)} = \frac{\hat{p}(\mathbf{x}|\mathbf{c}_0)}{\hat{p}(\mathbf{x}|\mathbf{c}_1)},$$

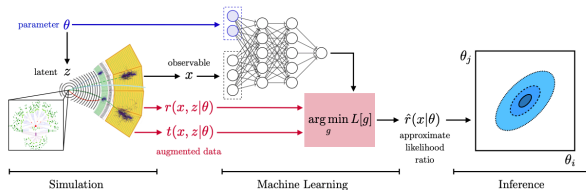
which is the same as the true likelihood ratio in the ideal limit (large sample, perfect training).

- There are many other ways to construct a loss function(al)....
- With additional assumptions on how  $\frac{d\sigma}{d\Omega}$  depends on  $\mathbf{c}$  (i.e., a quadratic relation), we only need to train a finite number of times to know how the likelihood ratio depend on  $\mathbf{c}$ .

# Particle physics structure

- One could make use of **latent variable “ $z$ ”** (the parton level analytic result for  $\frac{d\sigma}{d\Omega}$ ) to increase the performance of ML.

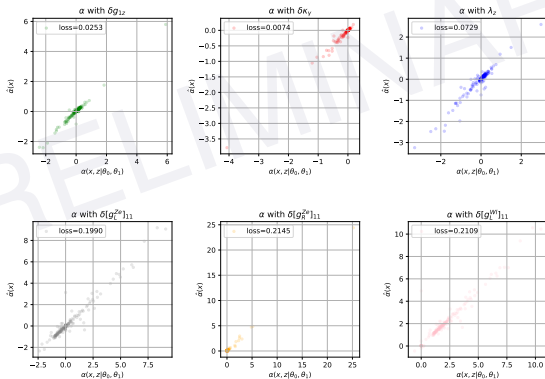
[1805.00013, 1805.00020] Brehmer, Cranmer, Louppe, Pavez



- Assuming linear dependences  $\frac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} c_i$ , there is a method called **SALLY** (Score approximates likelihood locally).
  - In this case, for each parameter we only need to train once to obtain  $\alpha_i \equiv \frac{S_{1,i}}{S_0}$ . (It is basically the ML version of Optimal Observables.)
  - We can calculate the “ideal”  $\alpha(z)$  which will help us train the actual  $\alpha(x)$ .

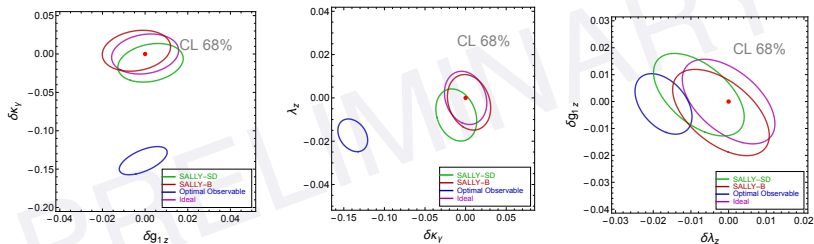
$$L[\hat{\alpha}(x)] = \sum_{x_i, z_i \sim \text{SM}} |\alpha(z_i) - \hat{\alpha}(x_i)|^2.$$

# Machine Learning in $e^+e^- \rightarrow WW$ (preliminary results, Shengdu Chai, JG, Lingfeng Li)



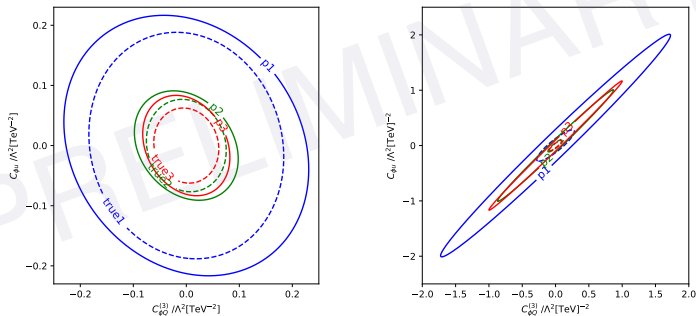
- Semileptonic channel, MadGraph/Pythia/Delphes (CEPC detector card), with ZZ backgrounds.

# Machine Learning in $e^+e^- \rightarrow WW$ (preliminary results, Shengdu Chai, JG, Lingfeng Li)



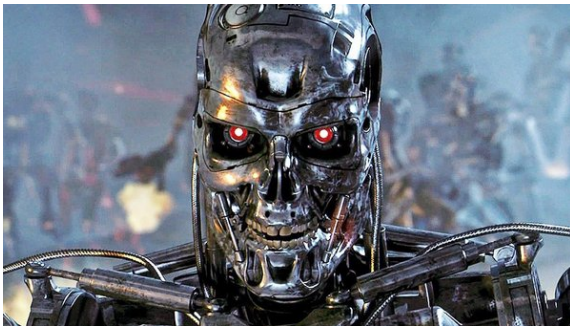
- ▶ 3-aTGC fit, scaled to  $10^4$  events.
  - ▶ OO+classifier: hybrid method that uses a classifier to discriminate background.
- ▶ Naively applying truth-level optimal observables could lead to a large bias!
- ▶ It's easier for machine learning to take care of systematics!

# Machine Learning in $e^+e^- \rightarrow t\bar{t}$ (very preliminary results, Yifan Fei, JG, Tong Shen, Kerun Yu)



- ▶  $e^+e^- \rightarrow t\bar{t}$ , 3 different channels (no background yet)
- ▶ **Left:**  $\sqrt{s}=1\text{TeV}$ , **Right:**  $\sqrt{s}=360\text{ GeV}$

# Machine learning



- ▶ **When will Machine take over?**
  - ▶ Before or after a future lepton collider is built?

# $e^+e^- \rightarrow WW$ with Optimal Observables

- ▶ TGCs (and additional EFT parameters) are sensitive to the differential distributions!

- ▶ One could do a fit to the binned distributions of all angles.
- ▶ Not the most efficient way of extracting information.
- ▶ Correlations among angles are sometimes ignored.

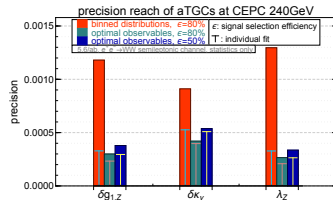
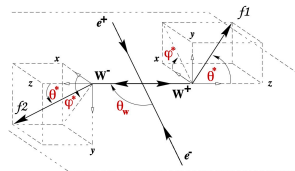
- ▶ What are optimal observables?

(See e.g. Z.Phys. C62 (1994) 397-412 Diehl & Nachtmann)

- ▶ In the limit of large statistics (everything is Gaussian) and small parameters (linear contribution dominates), the **best possible reaches** can be derived analytically!

$$\frac{d\sigma}{d\Omega} = S_0 + \sum_i S_{1,i} g_i, \quad c_{ij}^{-1} = \int d\Omega \frac{S_{1,i} S_{1,j}}{S_0} \cdot \mathcal{L},$$

- ▶ The optimal observables are given by  $\mathcal{O}_i = \frac{S_{1,i}}{S_0}$ , and are functions of the 5 angles.

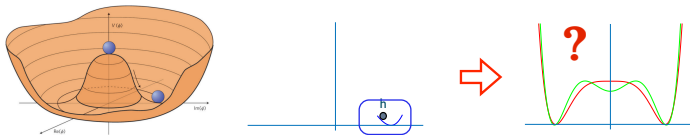


[arXiv:1907.04311] de Blas, Durieux, Grojean, JG, Paul



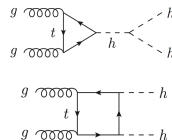
# Higgs self-coupling

- ▶ We know very little about the Higgs potential!

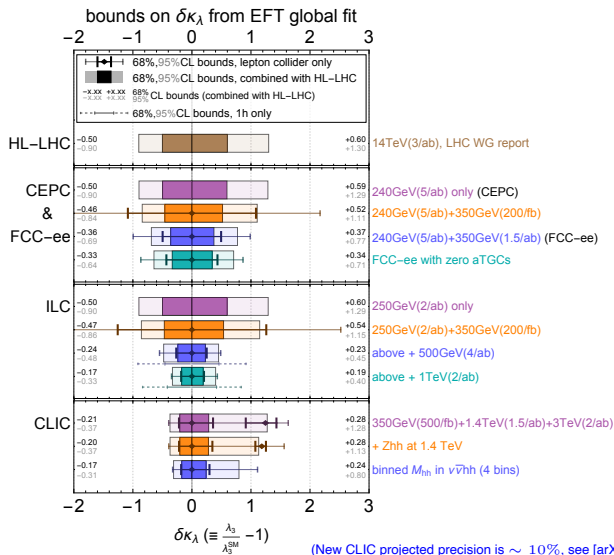


- ▶ To know more about the Higgs potential, we need to measure the Higgs self-couplings (**hhh** and **hhhh** couplings).
- ▶ The  $(H^\dagger H)^3$  operator can modify the Higgs self-couplings.
- ▶ Probing the **hhh** coupling at Hadron colliders.

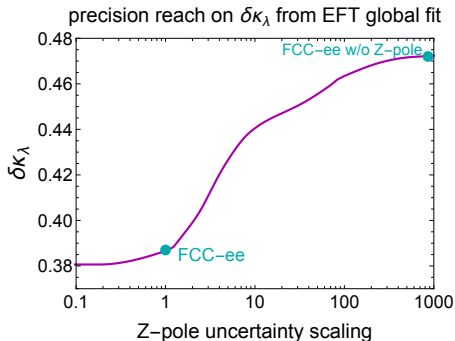
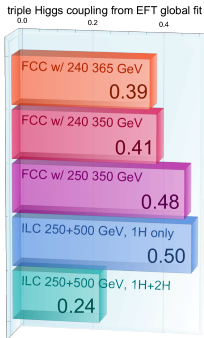
- ▶  $gg \rightarrow hh$
- ▶  $\lesssim 50\%$  at HL-LHC.
- ▶  $\lesssim 5\%$  at a 100 TeV collider.



# Triple Higgs coupling from global fits [arXiv:1711.03978]



# Updates on the triple Higgs coupling determination from EFT global fits

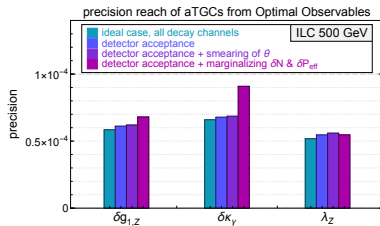
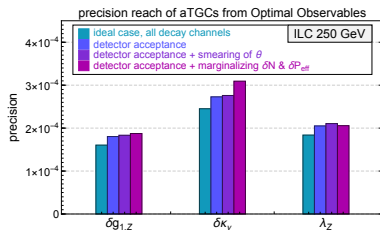


- ▶ 240, 365 GeV are better than 250, 350 GeV.
- ▶ Impacts of Z-pole measurements are not negligible.  
( $eeZ(h)$  contact interaction enters  $e^+e^- \rightarrow hZ$ .)



# Updates on the WW analysis with Optimal Observables

- ▶ How well can we do it in practice?
  - ▶ detector acceptance, measurement uncertainties, ...
- ▶ What we have done  
(current work for the snowmass study)
  - ▶ detector acceptance  
( $|\cos \theta| < 0.9$  for jets,  $< 0.95$  for leptons)
  - ▶ some smearing  
(production polar angle only,  $\Delta = 0.1$ )
  - ▶ ILC: marginalizing over total rate ( $\delta N$ ) and effective beam polarization ( $\delta P_{eff}$ )
- ▶ Constructing full EFT likelihood and feed it to the global fit. (For illustration, only showing the 3-aTGC fit results here.)
- ▶ Further verifications (by experimentalists) are needed.

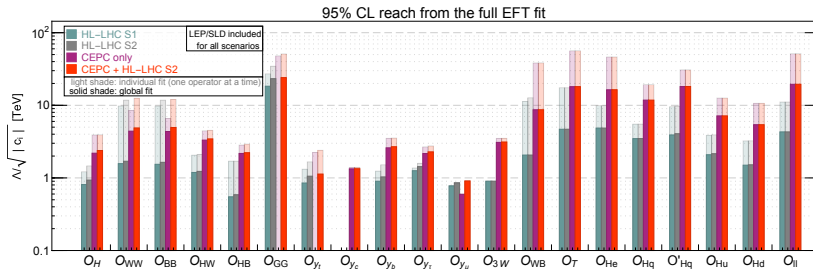


# D6 operators

$\mathcal{O}_H = \frac{1}{2}(\partial_\mu  H ^2)^2$	$\mathcal{O}_{GG} = g_s^2  H ^2 G_{\mu\nu}^A G^{A,\mu\nu}$
$\mathcal{O}_{WW} = g^2  H ^2 W_{\mu\nu}^a W^{a,\mu\nu}$	$\mathcal{O}_{y_u} = y_u  H ^2 \bar{q}_L H u_R + \text{h.c.} \quad (u \rightarrow t, c)$
$\mathcal{O}_{BB} = g'^2  H ^2 B_{\mu\nu} B^{\mu\nu}$	$\mathcal{O}_{y_d} = y_d  H ^2 \bar{q}_L H d_R + \text{h.c.} \quad (d \rightarrow b)$
$\mathcal{O}_{HW} = ig' (D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a$	$\mathcal{O}_{y_e} = y_e  H ^2 \bar{l}_L H e_R + \text{h.c.} \quad (e \rightarrow \tau, \mu)$
$\mathcal{O}_{HB} = ig' (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$	$\mathcal{O}_{3W} = \frac{1}{3!} g \epsilon_{abc} W_\mu^{a\nu} W_{\nu\rho}^b W^{c\rho\mu}$
$\mathcal{O}_W = \frac{ig}{2} (H^\dagger \sigma^a \overleftrightarrow{D}_\mu H) D^\nu W_{\mu\nu}^a$	$\mathcal{O}_B = \frac{ig'}{2} (H^\dagger \overleftrightarrow{D}_\mu H) \partial^\nu B_{\mu\nu}$
$\mathcal{O}_{WB} = gg' H^\dagger \sigma^a H W_{\mu\nu}^a B^{\mu\nu}$	$\mathcal{O}_{H\ell} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{\ell}_L \gamma^\mu \ell_L$
$\mathcal{O}_T = \frac{1}{2} (H^\dagger \overleftrightarrow{D}_\mu H)^2$	$\mathcal{O}'_{H\ell} = iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{\ell}_L \sigma^a \gamma^\mu \ell_L$
$\mathcal{O}_{\ell\ell} = (\bar{\ell}_L \gamma^\mu \ell_L)(\bar{\ell}_L \gamma_\mu \ell_L)$	$\mathcal{O}_{H\bar{e}} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{e}_R \gamma^\mu e_R$
$\mathcal{O}_{Hq} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{q}_L \gamma^\mu q_L$	$\mathcal{O}_{Hu} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{u}_R \gamma^\mu u_R$
$\mathcal{O}'_{Hq} = iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{q}_L \sigma^a \gamma^\mu q_L$	$\mathcal{O}_{Hd} = iH^\dagger \overleftrightarrow{D}_\mu H \bar{d}_R \gamma^\mu d_R$

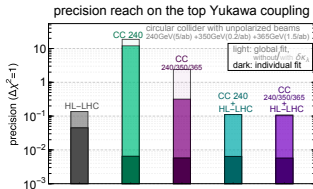
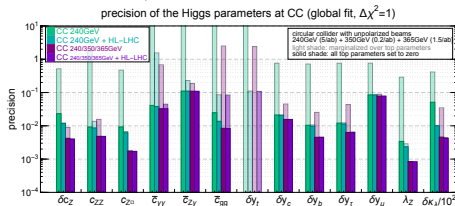
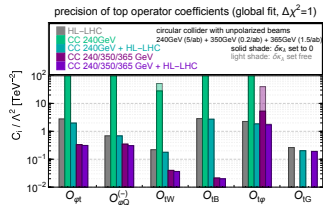
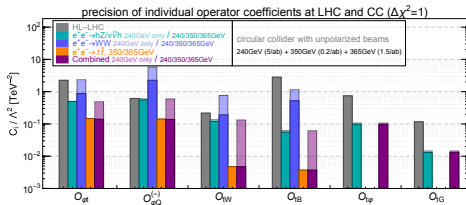
- ▶ SILH' basis (eliminate  $\mathcal{O}_{WW}$ ,  $\mathcal{O}_{WB}$ ,  $\mathcal{O}_{H\ell}$  and  $\mathcal{O}'_{H\ell}$ )
- ▶ Modified-SILH' basis (eliminate  $\mathcal{O}_W$ ,  $\mathcal{O}_B$ ,  $\mathcal{O}_{H\ell}$  and  $\mathcal{O}'_{H\ell}$ )
- ▶ Warsaw basis (eliminate  $\mathcal{O}_W$ ,  $\mathcal{O}_B$ ,  $\mathcal{O}_{HW}$  and  $\mathcal{O}_{HB}$ )

# Reach on the scale of new physics



- ▶ Reach on the scale of new physics  $\Lambda$ .
- ▶ Note: reach depends on the couplings  $c_i$ !

# Top operators in loops [arXiv:1809.03520] G. Durieux, JG, E. Vryonidou, C. Zhang



- ▶ Higgs precision measurements have sensitivity to the top operators in the loops.
  - ▶ But it is challenging to discriminate many parameters in a global fit!
- ▶ HL-LHC helps, but a 360 or 365 GeV run is better.
- ▶ Indirect bounds on the top Yukawa coupling.

# You can't really separate Higgs from the EW gauge bosons!

$$\begin{aligned}\mathcal{O}_{H\ell} &= iH^\dagger \overleftrightarrow{D}_\mu H \bar{\ell}_L \gamma^\mu \ell_L, \\ \mathcal{O}'_{H\ell} &= iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H \bar{\ell}_L \sigma^a \gamma^\mu \ell_L, \\ \mathcal{O}_{He} &= iH^\dagger \overleftrightarrow{D}_\mu H \bar{e}_R \gamma^\mu e_R\end{aligned}$$

(or the ones with quarks)

- ▶ modifies gauge couplings of fermions,
- ▶ also generates  $hVff$  type contact interaction.



$$\begin{aligned}\mathcal{O}_{HW} &= ig(D^\mu H)^\dagger \sigma^a (D^\nu H) W_{\mu\nu}^a, \\ \mathcal{O}_{HB} &= ig' (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}\end{aligned}$$

- ▶ generate **aTGCs**  $\delta g_{1,Z}$  and  $\delta \kappa_\gamma$ ,
- ▶ also generates **HVV anomalous couplings** such as  $hZ_\mu \partial_\nu Z^{\mu\nu}$ .





# You also have to measure the Higgs!

- ▶ Some operators can only be probed with the **Higgs particle**.
- ▶  $|H|^2 W_{\mu\nu} W^{\mu\nu}$  and  $|H|^2 B_{\mu\nu} B^{\mu\nu}$ 
  - ▶  $H \rightarrow \nu/\sqrt{2}$ , corrections to gauge couplings?
  - ▶ **Can be absorbed by field redefinition!** This applies to any operators in the form  $|H|^2 \mathcal{O}_{\text{SM}}$ .

$$\begin{aligned}
 c_{\text{SM}} \mathcal{O}_{\text{SM}} \quad \text{vs.} \quad & c_{\text{SM}} \mathcal{O}_{\text{SM}} + \frac{c}{\Lambda^2} |H|^2 \mathcal{O}_{\text{SM}} \\
 &= (c_{\text{SM}} + \frac{c v^2}{2 \Lambda^2}) \mathcal{O}_{\text{SM}} + \text{terms with } h \\
 &= c'_{\text{SM}} \mathcal{O}_{\text{SM}} + \text{terms with } h
 \end{aligned}$$

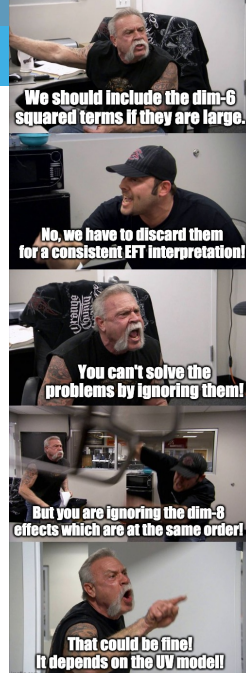
- ▶ probed by measurements of the  $h\gamma\gamma$  and  $hZ\gamma$  couplings, or the  $hWW$  and  $hZZ$  **anomalous** couplings.
  - ▶ or Higgs in the loop (different story...)
- ▶ Yukawa couplings, Higgs self couplings, ...

# Why lepton colliders?

- ▶ EFT is good for lepton colliders.
  - ▶ A systematic parameterization of Higgs (and other) couplings.
- ▶ Lepton colliders are also good for EFT!
  - ▶ High precision  $\Rightarrow E \ll \Lambda$   
**Ideal for EFT studies!**
  - ▶ LHC is built for discovery, but ....

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**Ideal for EFT studies!**
  - ▶ LHC is built for discovery, but ....
  
- ▶ **Energy vs. Precision**
  - ▶ Poor measurements at the high energy tails lead to problems in the interpretation of EFT...



## A lesson from history

- ▶ In 1875, a young Max Planck was told by his advisor Philipp von Jolly not to study physics, since there was nothing left to be discovered.

- ▶ **Planck did not listen.**

- ▶ In 1887, Michelson and Morley tried to find ether, the postulated medium for the propagation of light that was widely believed to exist.

- ▶ **They didn't find it.**

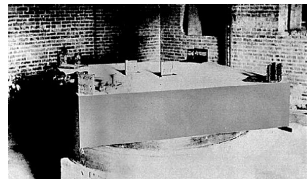
- ▶ **“Our future discoveries must be looked for in the sixth place of decimals.” — Albert A. Michelson**

Max Planck:

Before  
quantum physics:



After  
quantum physics:



# A lesson from Christopher Columbus (哥伦布发现美洲大陆)

- ▶ **You need to have a theory.**
  - ▶ The earth is round, India is in the east...
- ▶ **Your theory can be wrong!**
  - ▶ Columbus did not find India, but found America instead...
- ▶ **You need to ask money from the government!**
  - ▶ Columbus convinced the monarchs of Spain to sponsor him.
- ▶ **Will we discover the new world?**

