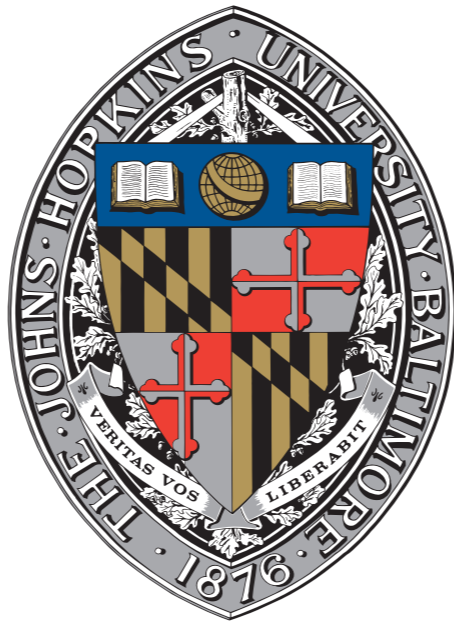


CP measurements with the Higgs boson at future colliders

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Johns Hopkins University



July 3, 2023

International Workshop on Circular e^+e^- Collider
University of Edinburgh, UK

CP-violating H(125) Couplings

- CP-violating H(125) couplings

- tiny in the SM, excellent null-test

- well-defined stand-alone reference measurement

- potential baryogenesis connected to the Higgs sector

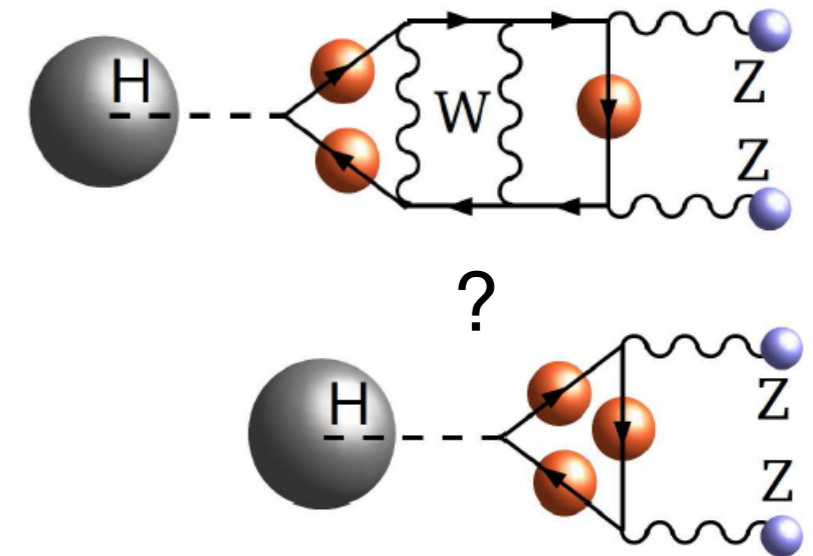
- $pp, e^+e^-, e^-p, \gamma\gamma, \mu^+\mu^- (\sqrt{s})$ have their unique features in CP of $H(125)$

- complementarity to the EDM measurements and Flavor Physics

- Identify key reference measurements to compare facilities

- focus on direct H production

- connect to indirect (virtual, low-energy) probes



Snowmass White Paper on Higgs CP

- Dedicated Snowmass White Paper: [arXiv:2205.07715](https://arxiv.org/abs/2205.07715) (update 29 Nov 2022)

Snowmass White Paper: Prospects of CP-violation measurements
with the Higgs boson at future experiments

Editor: Andrei V. Gritsan,¹ Contributors: Henning Bahl,² Rahool Kumar Barman,³ Ivanka Božović-Jelisavčić,⁴ Jeffrey Davis,¹ Wouter Dekens,⁵ Yanyan Gao,⁶ Dorival Gonçalves,³ Lucas S. Mandacarú Guerra,¹ Daniel Jeans,⁷ Kyoungchul Kong,⁸ Savvas Kyriacou,¹ Kirtimaan Mohan,⁹ Ren-Qi Pan,¹⁰ Jeffrey Roskes,¹ Nhan V. Tran,¹¹ Natasa Vukašinović,⁴ and Meng Xiao¹⁰

- Quick overview:

Snowmass-2022

TABLE I: List of expected precision (at 68% C.L.) of CP -sensitive measurements of the parameters f_{CP}^{HX} defined in Eq. (2). Numerical values are given where reliable estimates are provided, \checkmark mark indicates that feasibility of such a measurement could be considered. The $e^+e^- \rightarrow ZH$ projections are performed with $Z \rightarrow \ell\ell$ in Appendix B but scaled to a ten times larger luminosity to account for $Z \rightarrow q\bar{q}$.

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb ⁻¹)	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
HZZ/HWW	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	\checkmark	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$	\checkmark	\checkmark	\checkmark	\checkmark	$< 10^{-5}$
$H\gamma\gamma$	–	0.50	\checkmark	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
$HZ\gamma$	–	~ 1	\checkmark	–	–	–	~ 1	–	–	–	–	$< 10^{-2}$
Hgg	0.12	0.011	\checkmark	–	–	–	–	–	–	–	–	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	\checkmark	–	–	0.29	0.08	\checkmark	–	–	\checkmark	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	\checkmark	0.01	0.01	0.02	0.06	–	\checkmark	\checkmark	\checkmark	$< 10^{-2}$
$H\mu\mu$	–	–	–	–	–	–	–	–	–	\checkmark	–	$< 10^{-2}$

Starting Point: Snowmass-2013

- Start from Snowmass-2013, several developments in 9 years:
 - reliable **LHC results** on most measurements
 - more studies supporting **future proposals** (including White Papers)
 - **phenomenological** development, EFT...
- Focus on: *CP* in *HZZ/HWW, HZγ, Hγγ, Hgg, Htt, Hττ, Hμμ*

Same parameters of interest
as in Snowmass-2013
[arXiv:1310.8361](https://arxiv.org/abs/1310.8361)

$$f_{CP}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{CP \text{ odd}}}{\Gamma_{H \rightarrow X}^{CP \text{ odd}} + \Gamma_{H \rightarrow X}^{CP \text{ even}}}$$

not enough studies

Collider	<i>pp</i>	<i>pp</i>	<i>e⁺e⁻</i>	<i>e⁺e⁻</i>	<i>e⁺e⁻</i>	<i>e⁺e⁻</i>	<i>γγ</i>	<i>μ⁺μ⁻</i>	target
E (GeV)	14,000	14,000	250	350	500	1,000	126	126	(theory)
\mathcal{L} (fb ⁻¹)	300	3,000	250	350	500	1,000	250		
spin-2 _m ⁺	~10σ	≫10σ	>10σ	>10σ	>10σ	>10σ			>5σ
<i>VVH</i> [†]	0.07	0.02	✓	✓	✓	✓	✓	✓	< 10 ⁻⁵
<i>VVH</i> [‡]	4·10 ⁻⁴	1.2·10 ⁻⁴	7·10 ⁻⁴	1.1·10 ⁻⁴	4·10 ⁻⁵	8·10 ⁻⁶	–	–	< 10 ⁻⁵
<i>VVH</i> [◇]	7·10 ⁻⁴	1.3·10 ⁻⁴	✓	✓	✓	✓	–	–	< 10 ⁻⁵
<i>ggH</i>	0.50	0.16	–	–	–	–	–	–	< 10 ⁻²
<i>γγH</i>	–	–	–	–	–	–	0.06	–	< 10 ⁻²
<i>ZγH</i>	–	✓	–	–	–	–	–	–	< 10 ⁻²
<i>ττH</i>	✓	✓	0.01	0.01	0.02	0.06	✓	✓	< 10 ⁻²
<i>ttH</i>	✓	✓	–	–	0.29	0.08	–	–	< 10 ⁻²
<i>μμH</i>	–	–	–	–	–	–	–	✓	< 10 ⁻²

[†] estimated in *H* → *ZZ** decay mode

[‡] estimated in *V** → *HV* production mode

[◇] estimated in *V***V** → *H* (VBF) production mode

Snowmass-2013

General Comments

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	

pp LHC & HL-LHC - based on LHC

FCC-hh & SPPC expect $\times 100$

e^+e^- - keep lumi scenarios from 2013

scaling to $\times 10$ lumi available

e^-p - possible VBF and $\nu H t$

need compatible studies

$\gamma\gamma$ - focus on unique $H\gamma\gamma$ coupling

no recent projections

$\mu\mu$ - focus on unique $H\mu\mu$ coupling on-shell

associated H production at high energies

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
HZZ/HWW	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	-	0.50	✓	-	-	-	-	-	0.06	-	-	$< 10^{-2}$
$HZ\gamma$	-	~ 1	✓	-	-	-	~ 1	-	-	-	-	$< 10^{-2}$
Hgg	0.12	0.011	✓	-	-	-	-	-	-	-	-	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	✓	-	-	0.29	0.08	✓	-	-	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	-	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	-	-	-	-	-	-	-	-	-	✓	-	$< 10^{-2}$

Unique features of Facilities: $\gamma\gamma$ production

- Photon collider is unique with focus on $H\gamma\gamma$ coupling

- photon beam polarization is critical for CP
- most interesting parameter:

$$\mathcal{A}_3 = \frac{|A_{\parallel}|^2 - |A_{\perp}|^2}{|A_{\parallel}|^2 + |A_{\perp}|^2} = \frac{2\text{Re}(A_{--}^* A_{++})}{|A_{++}|^2 + |A_{--}|^2} = \frac{|a_2|^2 - |a_3|^2}{|a_2|^2 + |a_3|^2} = (1 - 2f_{CP})$$

Detecting and Studying Higgs Bosons at a Photon-Photon Collider: [arXiv:hep-ph/0110320](https://arxiv.org/abs/hep-ph/0110320)

- measure as asymmetry between \parallel and \perp linear polarizations

for $E_0 = 110$ GeV and $\lambda = 1 \mu\text{m}$: $f_{CP} = \sin^2(\alpha^{\gamma\gamma}) \sim \pm 0.06$

at $2.5 \cdot 10^{34} \times 10^7 = 250 \text{ fb}^{-1}$

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
$H\gamma\gamma$	–	0.50	✓	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
$HZ\gamma$	–	~ 1	✓	–	–	–	~ 1	–	–	–	–	$< 10^{-2}$

Unique features of Facilities: $\mu^+\mu^-$ production

- **Muon collider** is unique with focus on $H\mu\mu$ coupling
 - muon beam transverse polarization is critical for CP
 - not many **fermion couplings** can be tested with polarization and CP
 - later we will discuss $H\tau\tau$ and Htt (both 3rd family)
 - same transverse polarization \Rightarrow CP-even
 - opposite polarization \Rightarrow CP-odd

How Valuable is Polarization at a Muon Collider? A Test Case: Determining the CP Nature of a Higgs Boson:
[arXiv:hep-ph/0003091](https://arxiv.org/abs/hep-ph/0003091)

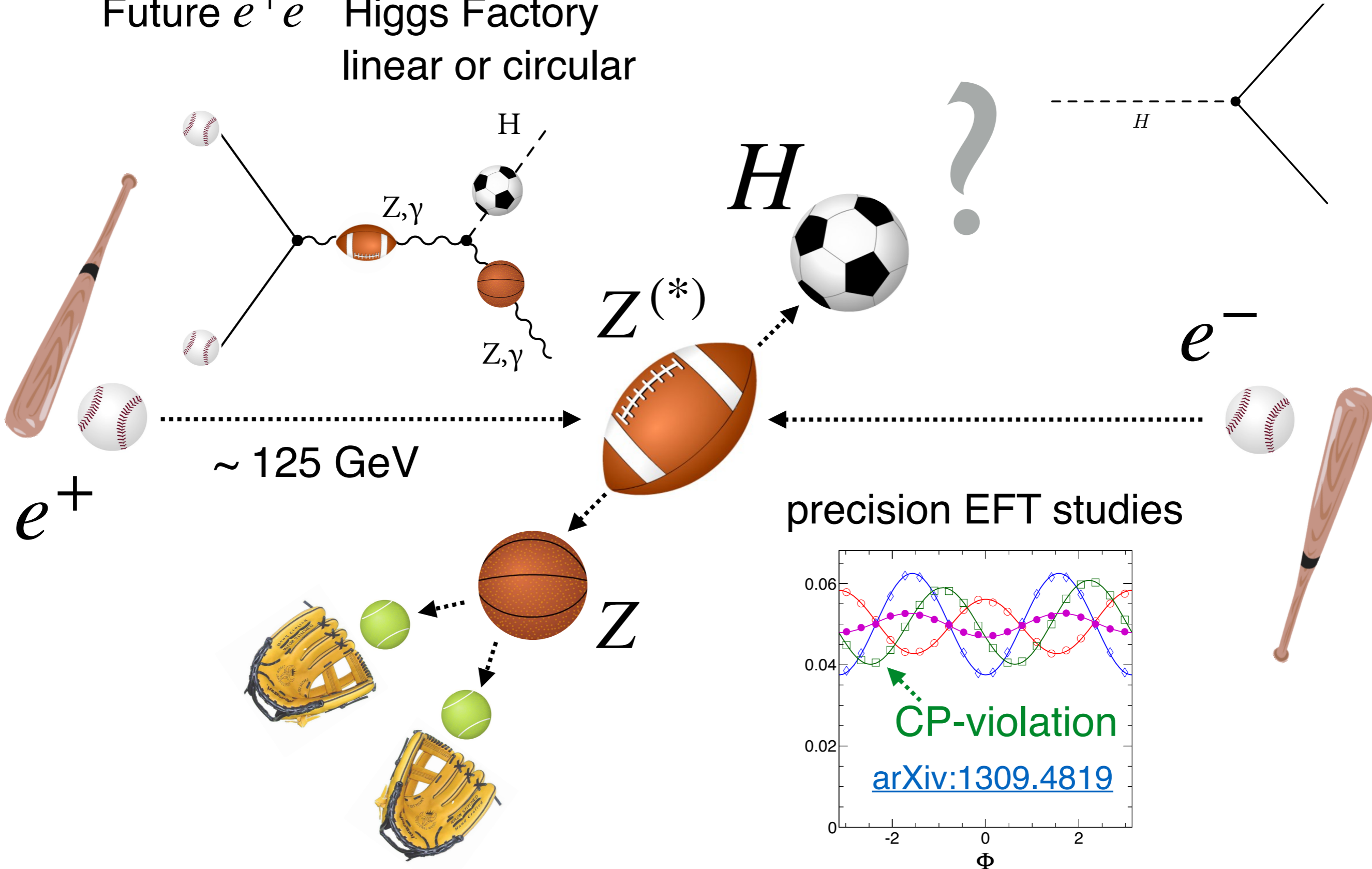
- Unique feature of the muon collider (CP in coupling to 2nd family)
 - though comes with a price of lumi, likely not a priority at first stage

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
$H\mu\mu$	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

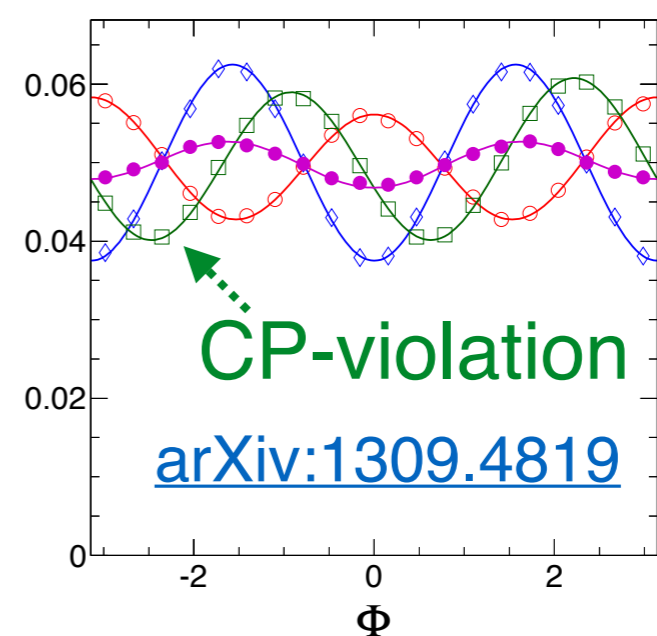
- High energy $\mu^+\mu^-$: associated production $t\bar{t}H$, VBF

Unique features of Facilities: e^+e^- production

Future e^+e^- Higgs Factory
linear or circular



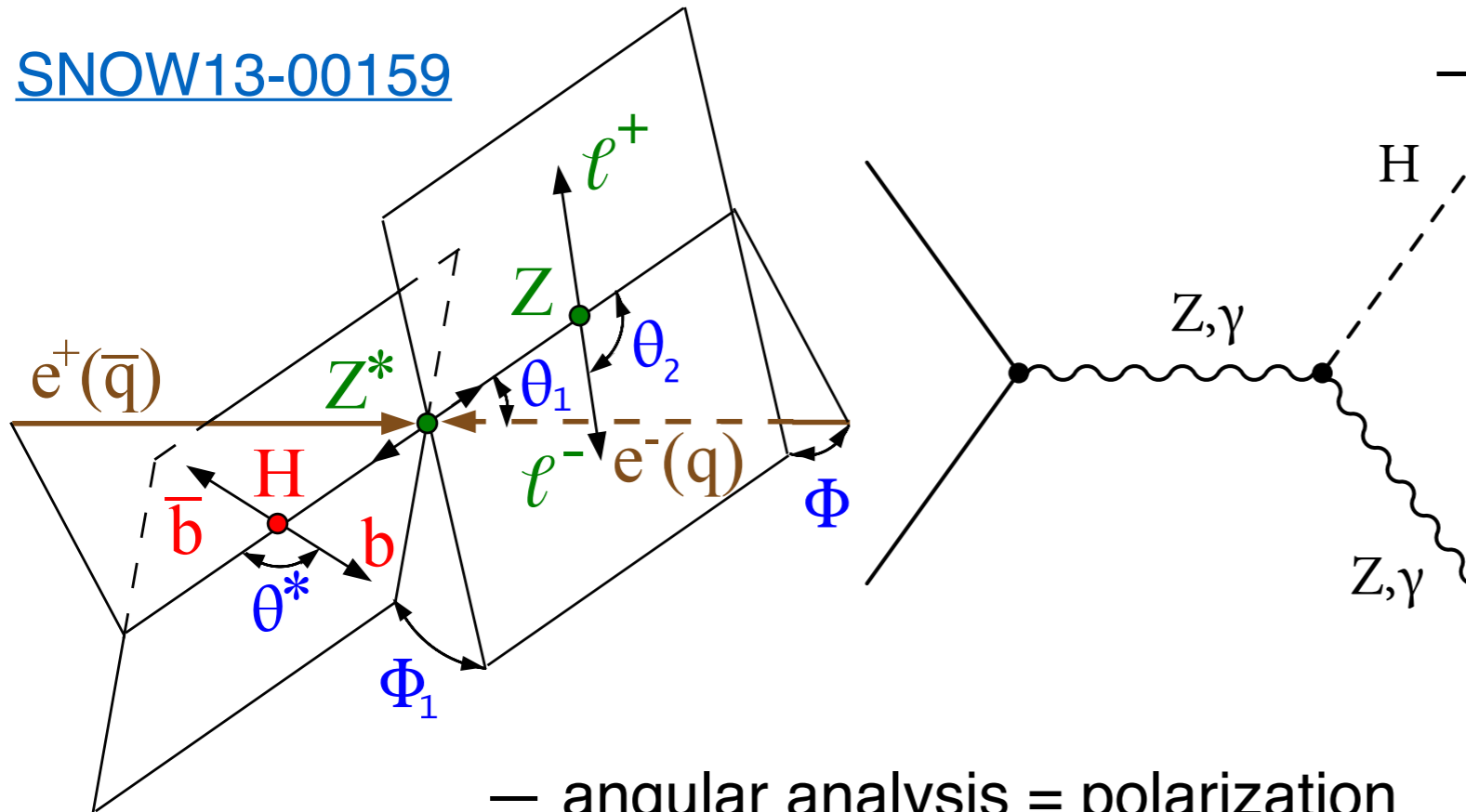
precision EFT studies



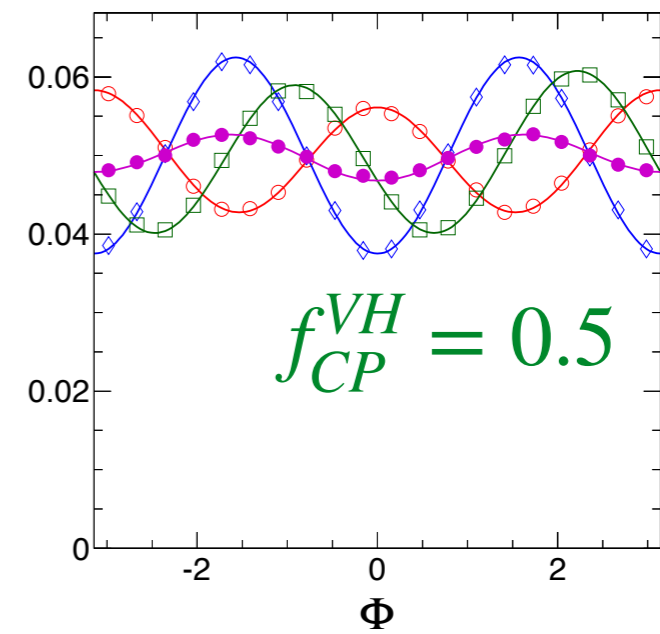
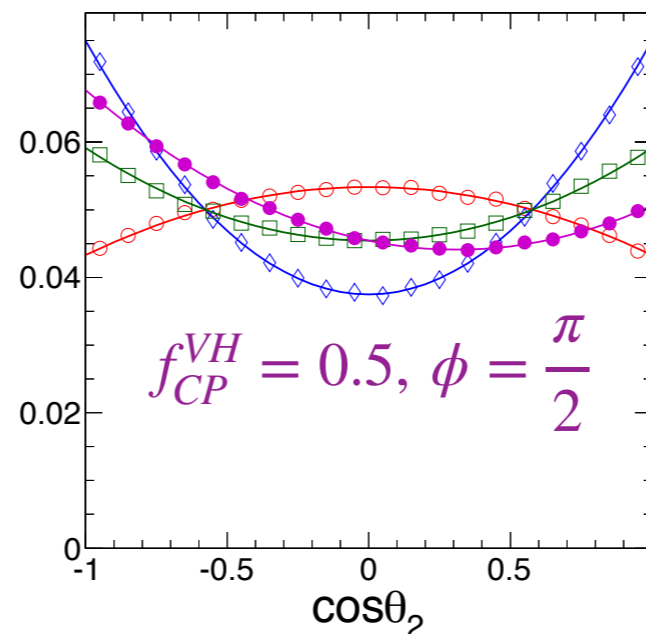
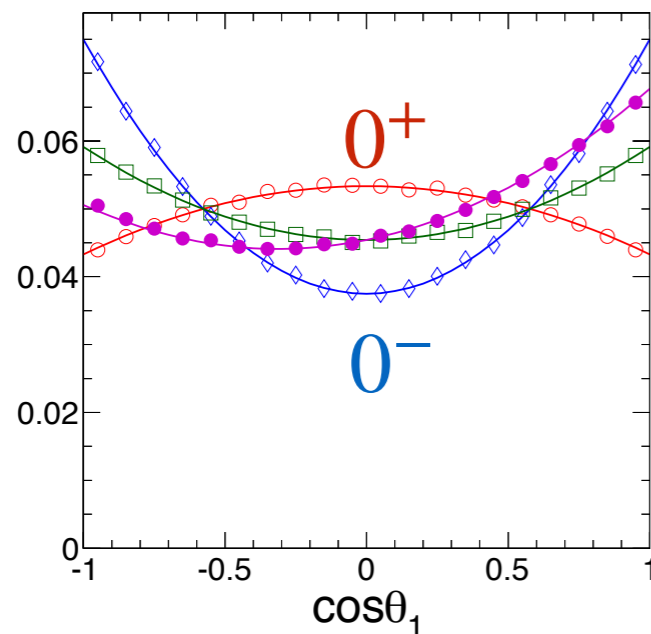
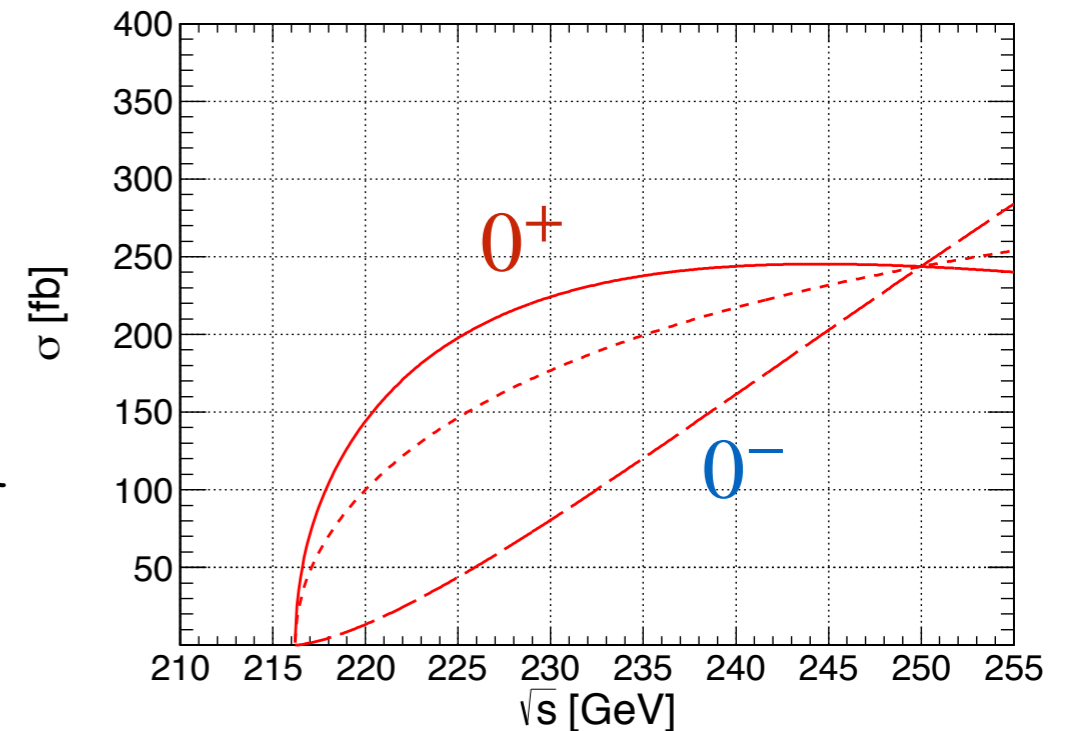
Unique features of Facilities: e^+e^- production

- e^+e^- collider $\rightarrow Z^* \rightarrow ZH \Rightarrow HZZ, HZ\gamma, H\gamma\gamma$ couplings

[SNOW13-00159](#)

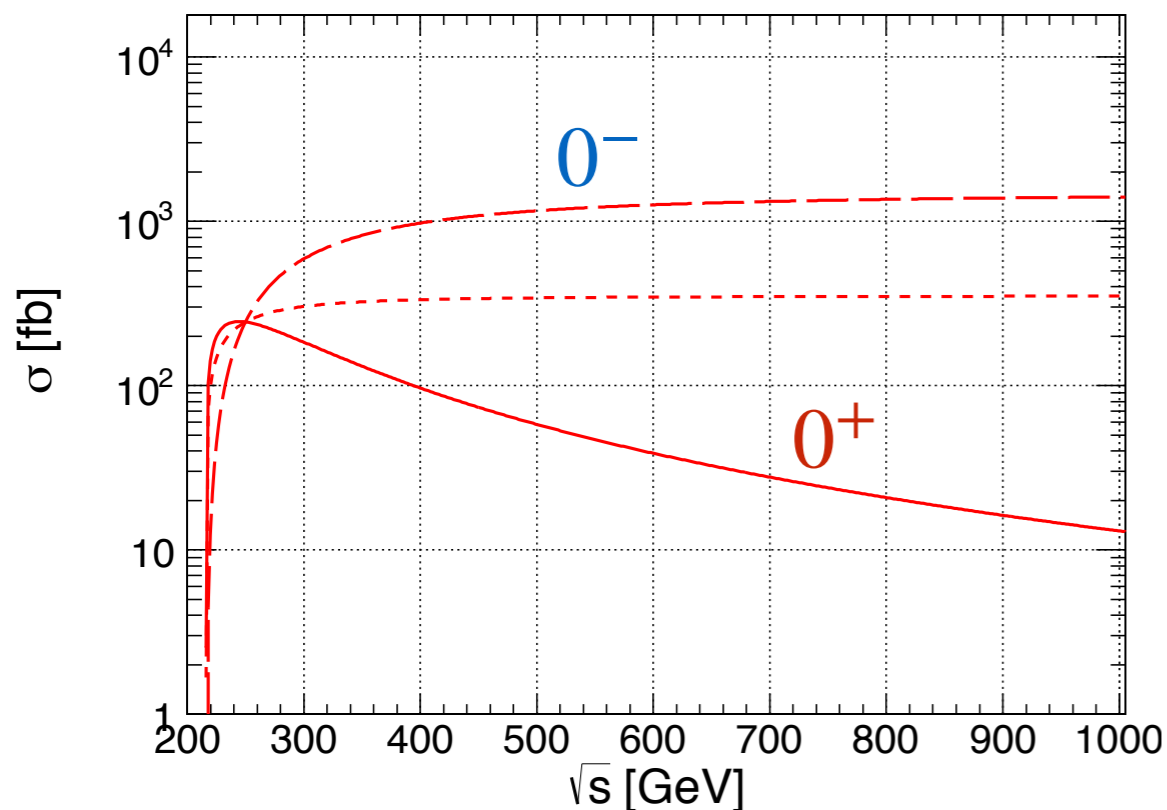


— threshold scan = q^2 dependence



e^+e^- production at higher energies (LC)

- e^+e^- collider $\rightarrow Z^* \rightarrow ZH$
 - Scan q^2 dependence of HVV
- \Rightarrow increased sensitivity (no cutoff)



[SNOW13-00159](#)

- VBF $e^+e^- \rightarrow \nu\bar{\nu}H$
- not much angular information
 q^2 -dependence through $p_T^H \dots$

- VBF $e^+e^- \rightarrow e^+e^-H$

recent study ([ICHEP-2022](#))
does not surpass $e^+e^- \rightarrow Z^* \rightarrow ZH$
at intermediate energies

Unique features of Facilities: e^+e^- production

- e^+e^- collider $\rightarrow Z^*/\gamma^* \rightarrow Z/\gamma^*H \Rightarrow HZZ, HZ\gamma, H\gamma\gamma$ couplings

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
HZZ/HWW	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	\checkmark	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$	\checkmark	\checkmark	\checkmark	\checkmark	$< 10^{-5}$
$H\gamma\gamma$	-	0.50	\checkmark	-	-	-	-	-	0.06	-	-	$< 10^{-2}$
$HZ\gamma$	-	~ 1	\checkmark	-	-	-	~ 1	-	-	-	-	$< 10^{-2}$

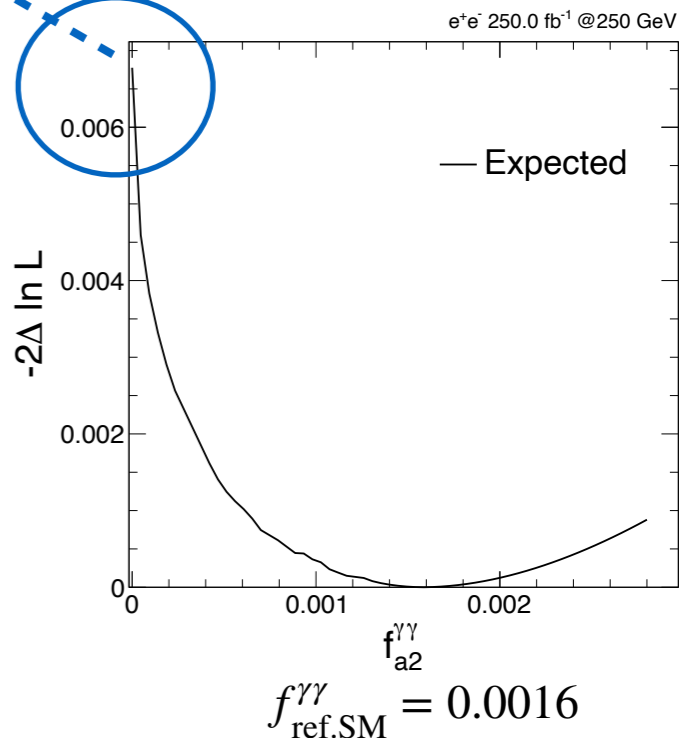
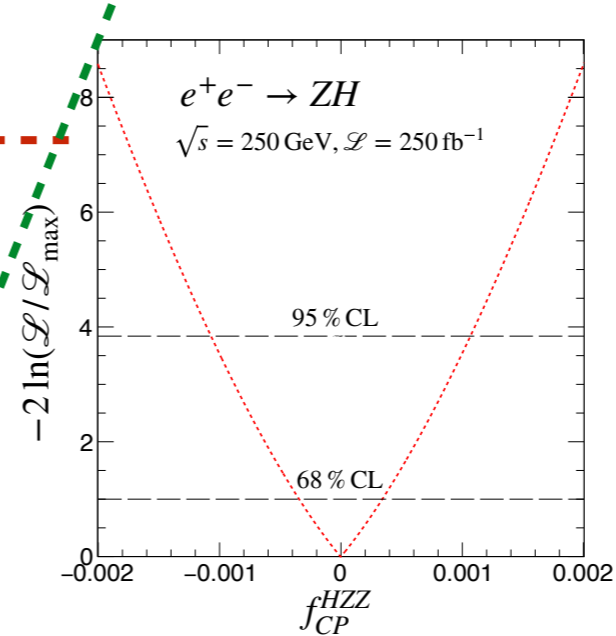
Appendix B: Recent updates of the studies at an electron-positron collider

see also [arXiv:2203.11707](https://arxiv.org/abs/2203.11707) in agreement

Contributed by Lucas S. Mandacarú Guerra and Savvas Kyriacou.

$\text{lumi, } \times 10^4 \text{ to cover } Z \rightarrow q\bar{q}$

E (GeV)	\mathcal{L} (fb^{-1})	f_{CP}^{HVV}	$f^{\gamma\gamma}$	$f^{Z\gamma}$	$f_{CP}^{\gamma\gamma}$	$f_{CP}^{Z\gamma}$
250	250	$\pm 3.4 \cdot 10^{-4}$	< 0.144	< 0.234	-	-
250	2,500	$\pm 3.9 \cdot 10^{-5}$	< 0.037	< 0.079	-	-
350	350	$\pm 1.2 \cdot 10^{-4}$	< 0.058	< 0.088	-	-
350	3,500	$\pm 2.9 \cdot 10^{-5}$	< 0.016	< 0.032	-	-
500	500	$\pm 4.3 \cdot 10^{-5}$	< 0.028	< 0.039	-	-
500	5,000	$\pm 1.3 \cdot 10^{-5}$	< 0.009	< 0.016	-	-
1,000	1,000	$\pm 1.0 \cdot 10^{-5}$	< 0.009	< 0.014	-	-
1,000	10,000	$\pm 3.0 \cdot 10^{-6}$	< 0.004	$0.0050^{+0.0026}_{-0.0028}$	-	± 0.96



fractions in $H \rightarrow 2e2\mu$: $f_{\text{ref.SM}}^{\gamma\gamma} = 0.0016$ $f_{\text{ref.SM}}^{Z\gamma} = 0.0050$

$f_{\text{ref.SM}}^{\gamma\gamma} = 0.0016$

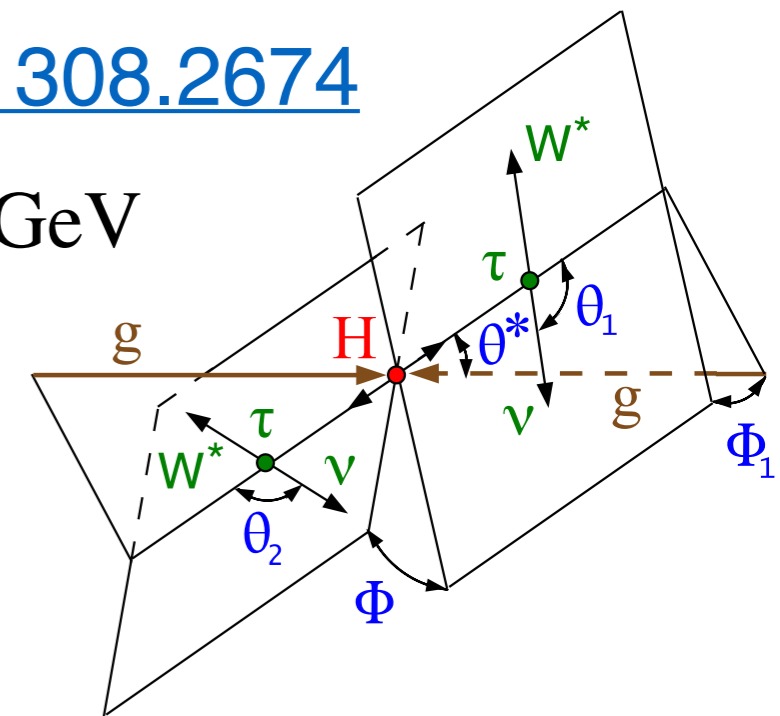
Fermion couplings at an e^+e^- collider

- e^+e^- pheno studies at Snowmass-2013: [arXiv:1308.2674](https://arxiv.org/abs/1308.2674)

- $H \rightarrow \tau\tau$ the only CP in Hff at e^+e^- $\sqrt{s} < 500$ GeV

- reach $f_{CP} \sim 0.008$ ($\alpha \sim 5^\circ$) at e^+e^- ref. lumi

note: worse at higher \sqrt{s} : no vertex in $e^+e^- \rightarrow \nu\bar{\nu}H$



- **Linear collider** $e^+e^- \rightarrow t\bar{t}H$

cross section dependence studied of 0^+ vs. 0^- at [Snowmass-2013](https://arxiv.org/abs/1308.2674)

recent similar study in [arXiv:1807.02441](https://arxiv.org/abs/1807.02441)

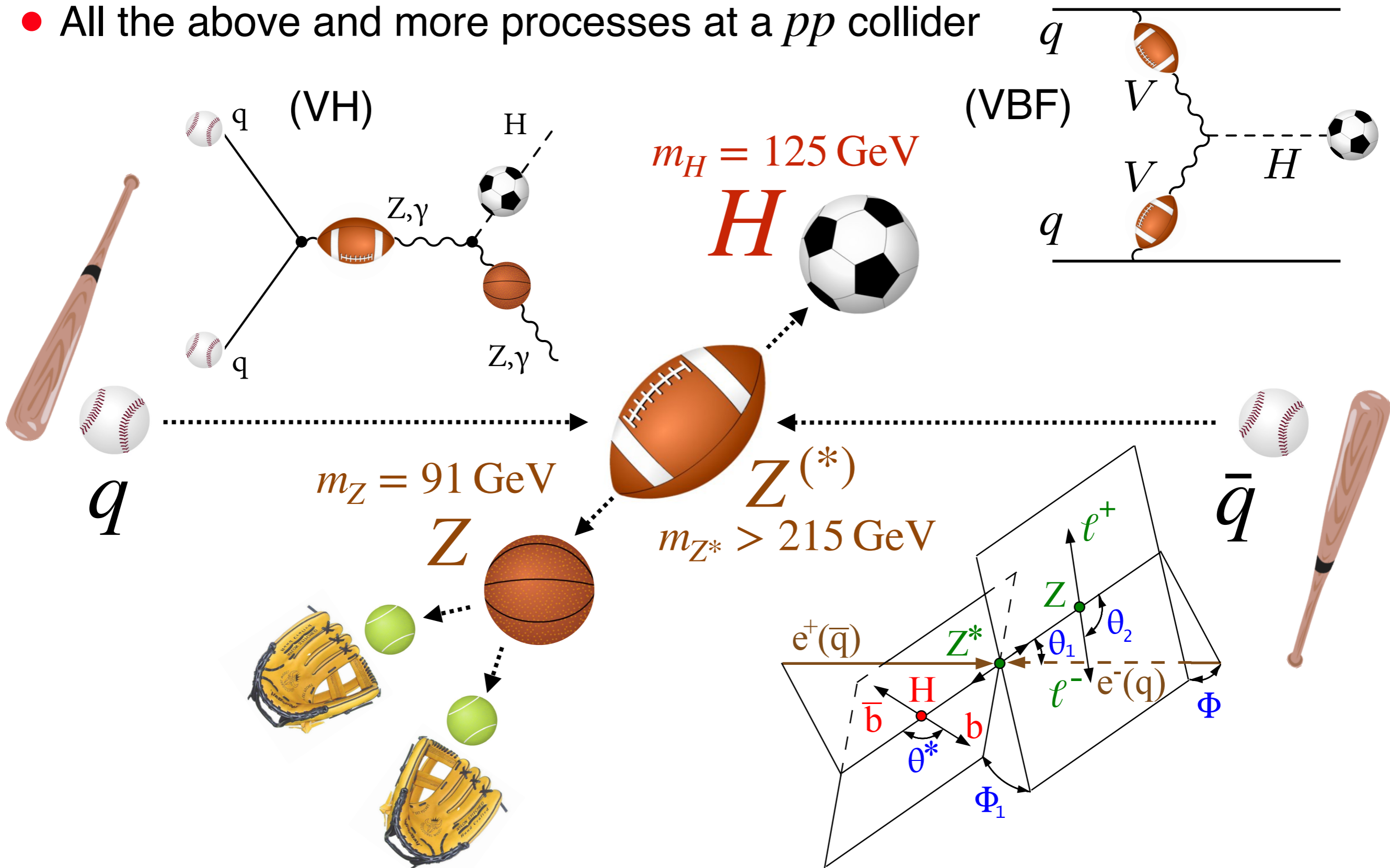
need dedicated CP -sensitive study (see LHC studies)

from Snowmass-2013

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
$Ht\bar{t}$	0.24	0.05	✓	–	–	0.29	0.08	✓	–	–	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	–	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

Unique features of Facilities: pp production

- All the above and more processes at a pp collider



Unique features of Facilities: pp production

- $pp \rightarrow V^* \rightarrow VH \Rightarrow HWW, HZZ, HZ\gamma, H\gamma\gamma, Hgg$ couplings

also VBF $V^*V^* \rightarrow H$ and decay $H \rightarrow VV$

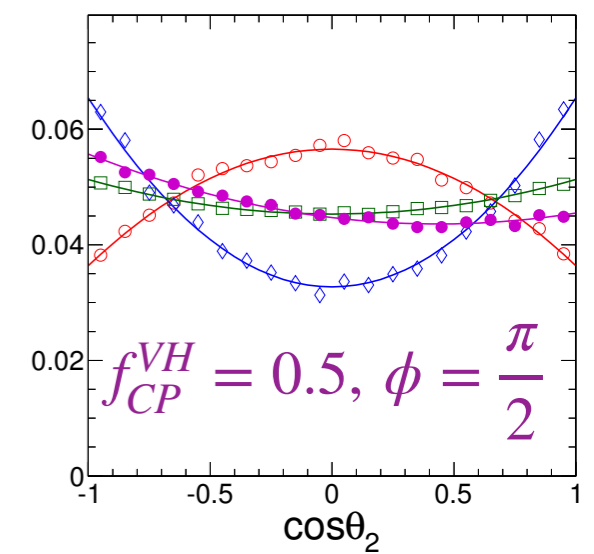
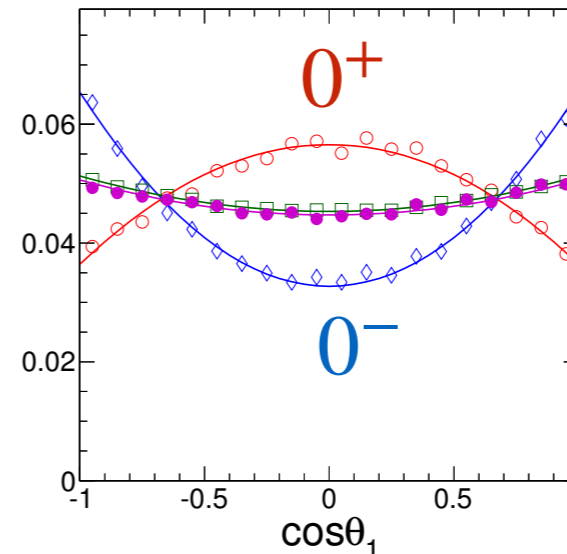
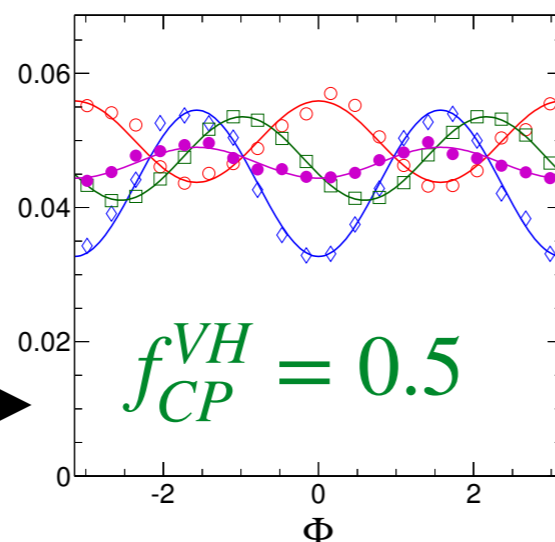
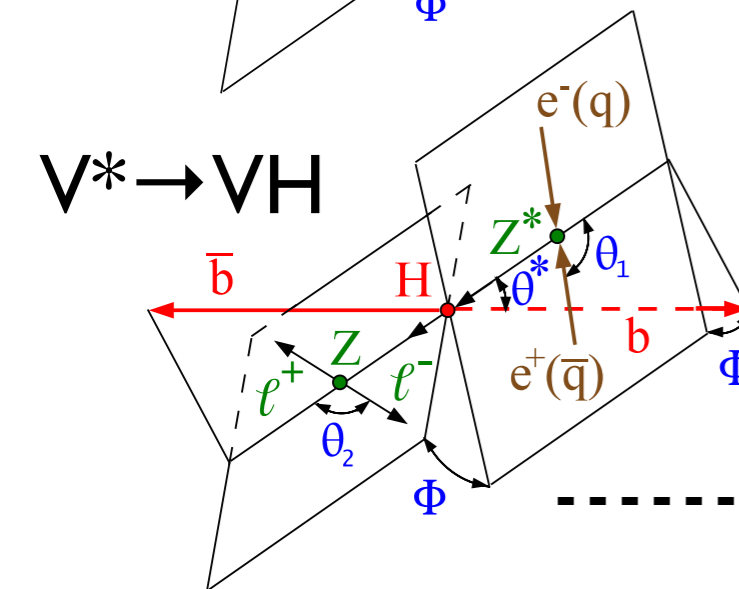
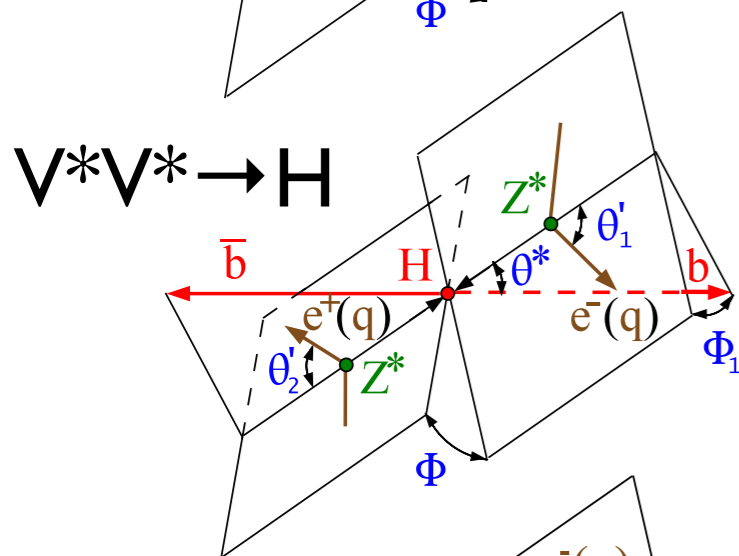
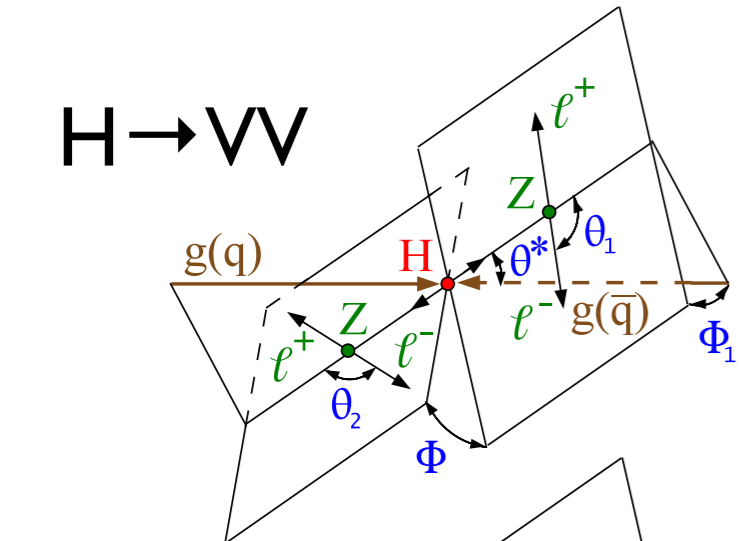
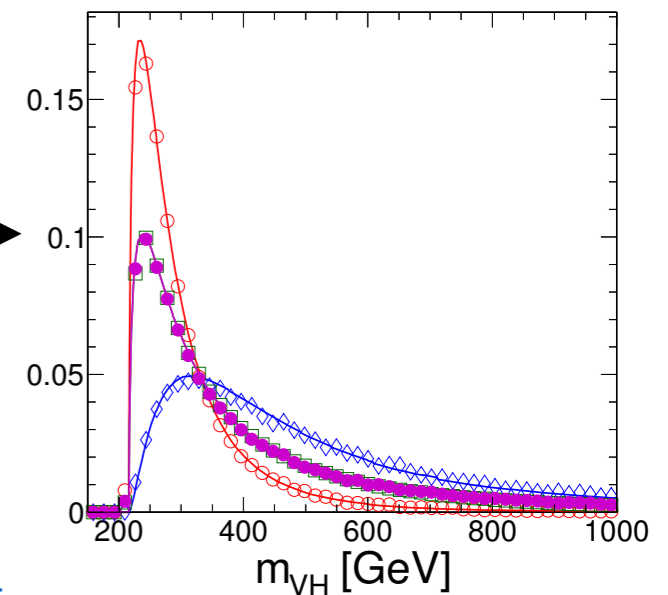
pp unique $gg \rightarrow H$

benefit from LHC experience

– scan of q^2 -dependence

– polarization measurement

[SNOW13-00159](#)

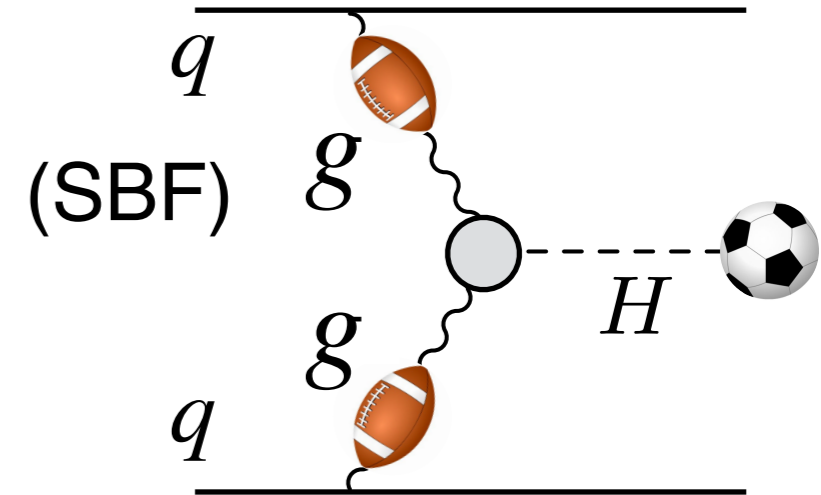


Gluon fusion in pp production

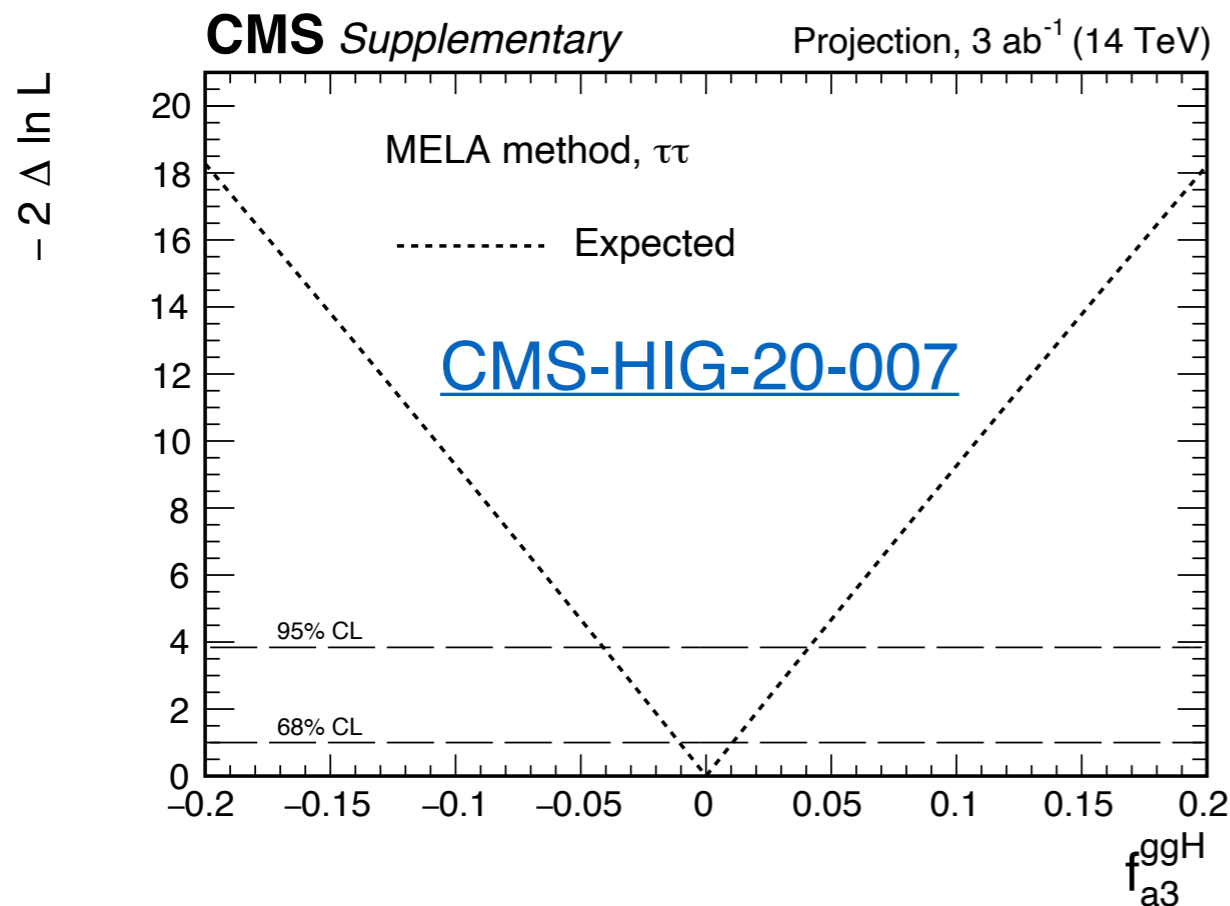
- pp is unique to measure Hgg coupling

BSM loop (point-like) or SM fermion loop

$$a_2^{gg} = -\alpha_s \kappa_Q / (6\pi) \quad \& \quad a_3^{gg} = -\alpha_s \tilde{\kappa}_Q / (4\pi)$$



- Update Snowmass-2013 ([pheno](#)) with recent LHC (mutual benefit):



Collider	pp	pp	pp
E (GeV)	14,000	14,000	100,000
\mathcal{L} (fb^{-1})	300	3,000	20,000
Hgg	0.12	0.011	✓

benefit from multiple H decay modes

$H\gamma\gamma, HZ\gamma$ in pp production

- CP in photon couplings appear challenging at all colliders

poor precision in VBF and VH

Appendix A: Recent updates of the studies at a hadron collider

Contributed by Jeffrey Davis, Savvas Kyriacou, and Jeffrey Roskes.

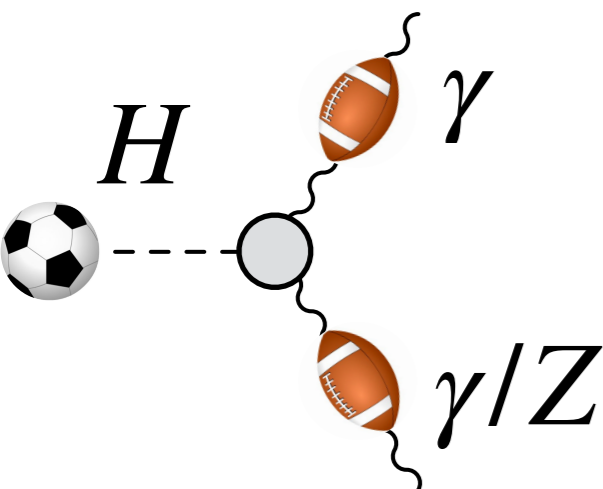
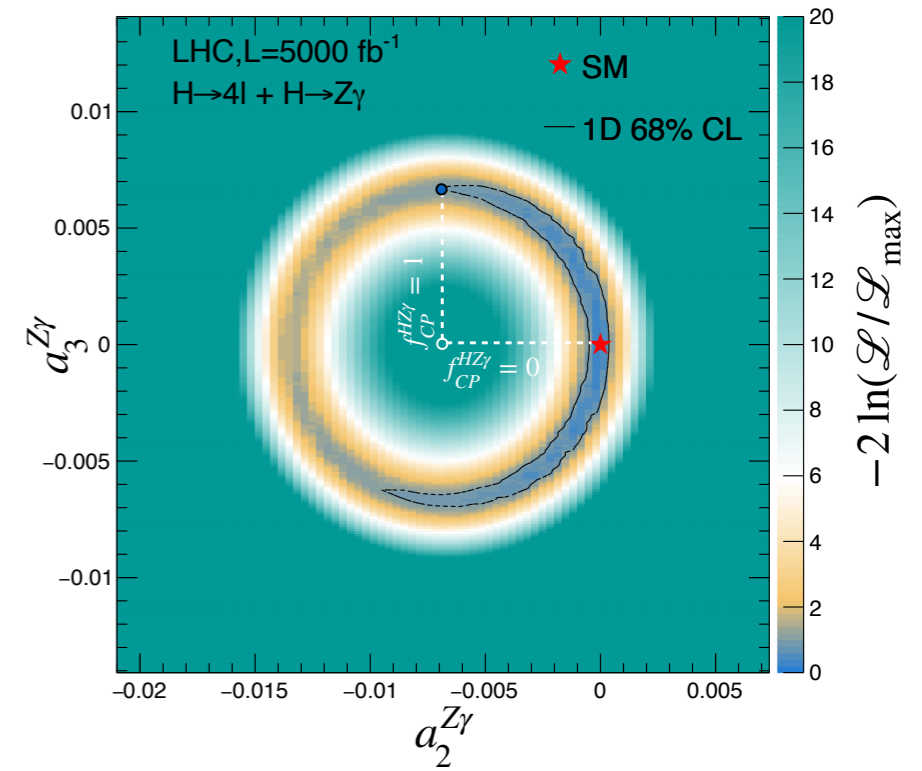
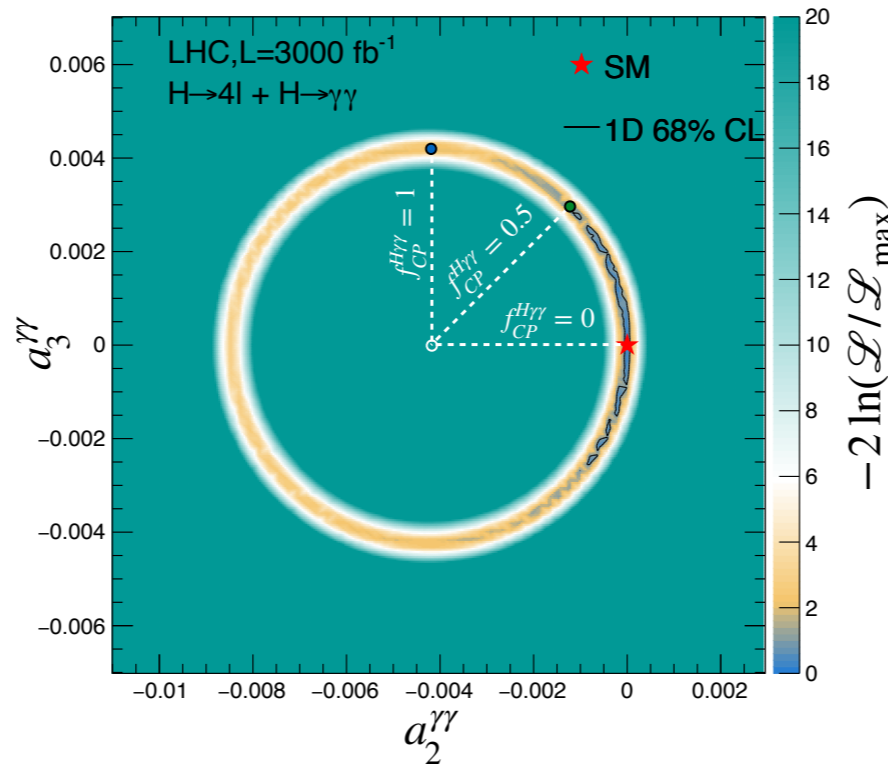
$$H \rightarrow \gamma\gamma(Z\gamma)$$

constrain $(a_2^{V\gamma})^2 + (a_3^{V\gamma})^2$

$$H \rightarrow \gamma^*\gamma^*(Z\gamma^*) \rightarrow 4\ell$$

resolve $a_2^{V\gamma}/a_3^{V\gamma}$

expect good constraints
at pp 100 TeV

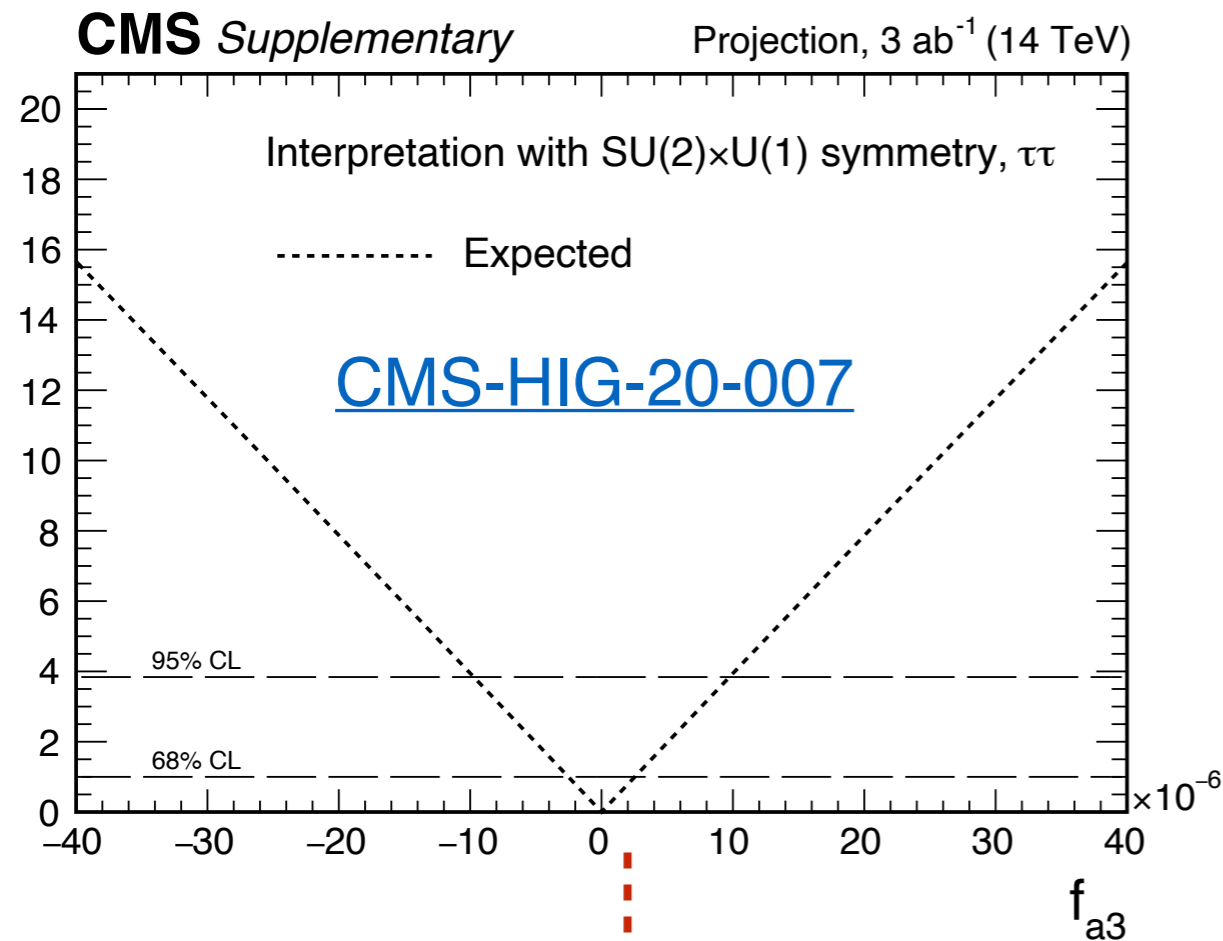


Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	

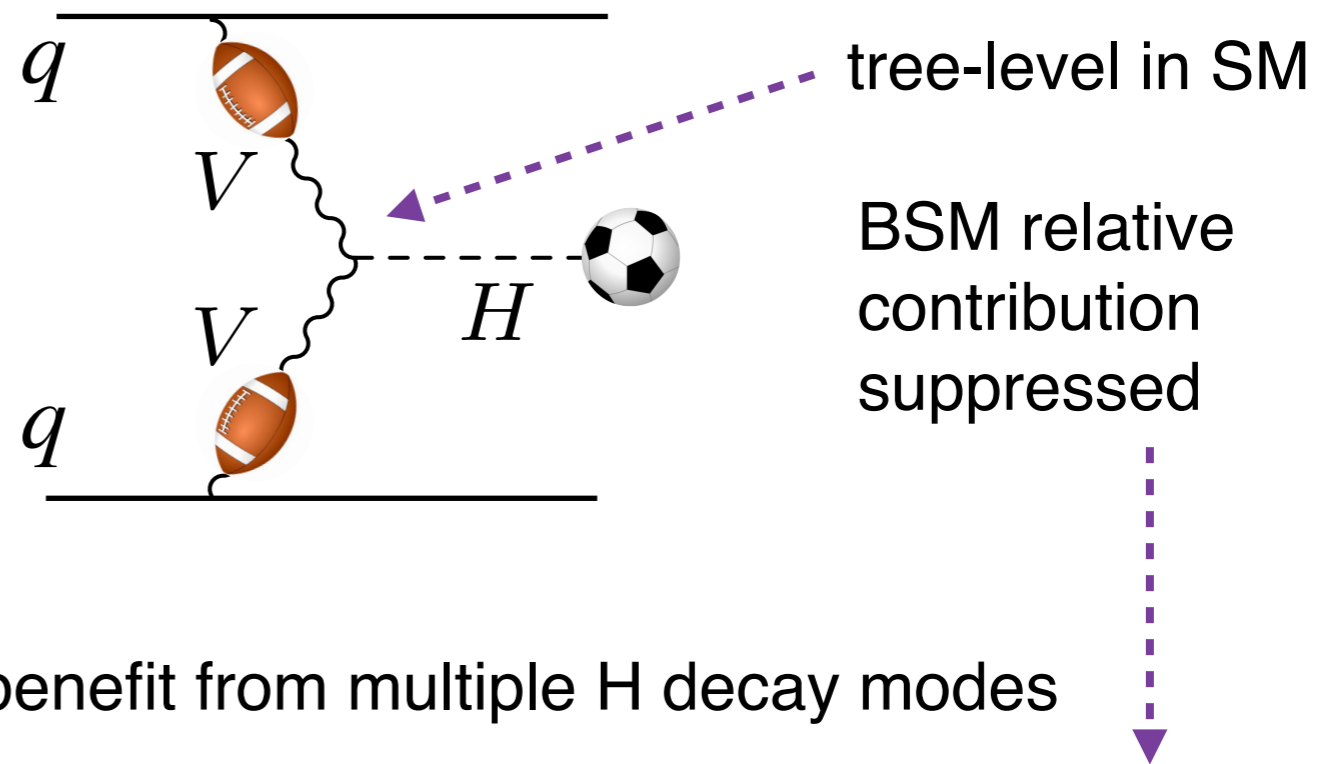
$H\gamma\gamma$	-	0.50	\checkmark	-	-	-	-	-	0.06	-	-	$< 10^{-2}$
$HZ\gamma$	-	~ 1	\checkmark	-	-	-	~ 1	-	-	-	-	$< 10^{-2}$

HZZ, HWW in pp production

- Update Snowmass-2013 ([pheno](#)) with recent LHC (mutual benefit):



mostly VBF topology (VH similar)
 $H \rightarrow VV$ not as sensitive due to low q^2



Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb ⁻¹)	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
HZZ/HWW	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$

$\sim 10^{-8}$ (?)

Fermion couplings: $t\bar{t}H$ at pp

- Very first test of CP in Hff in 2020:

- $t\bar{t}H$ spin-off from Snowmass-2013 ([arXiv:1606.03107](https://arxiv.org/abs/1606.03107))

pheno projection agreement with CMS/ATLAS

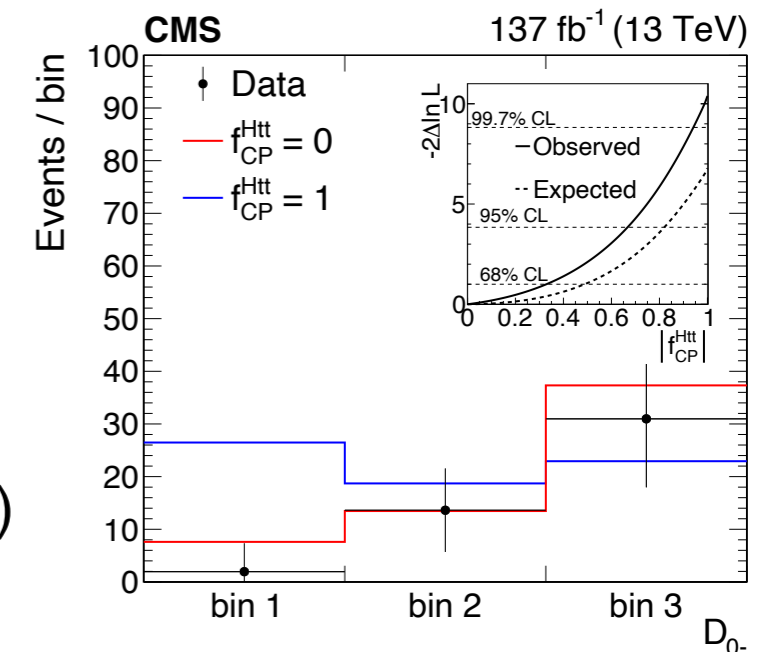
no sensitivity to $2\text{Re}\left(A_{\text{CP even}}A_{\text{CP odd}}^*\right)$ (semi-leptonic, hadronic)

- need di-lepton channel for CP interf: [arXiv:1507.07926](https://arxiv.org/abs/1507.07926)

- reach $f_{\text{CP}} \sim 0.05$ ($\alpha \sim 13^\circ$) at HL-LHC [arXiv:2110.07635](https://arxiv.org/abs/2110.07635)

pheno projection with di-leptonic, semi-leptonic, hadronic $t\bar{t}$ decay

- similar in tH ; no sensitivity to $b\bar{b}H$, or other light q



CMS [arXiv:2003.10866](https://arxiv.org/abs/2003.10866)

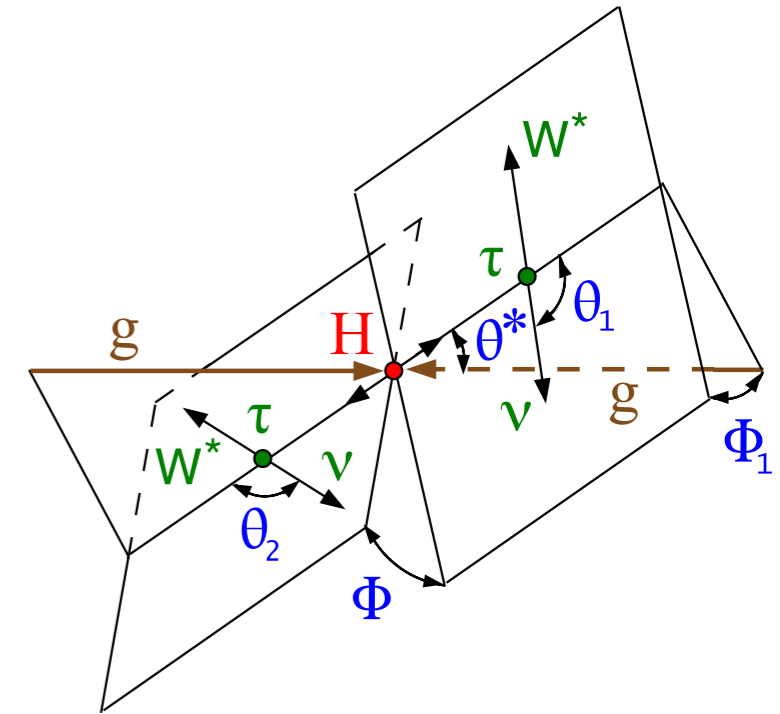
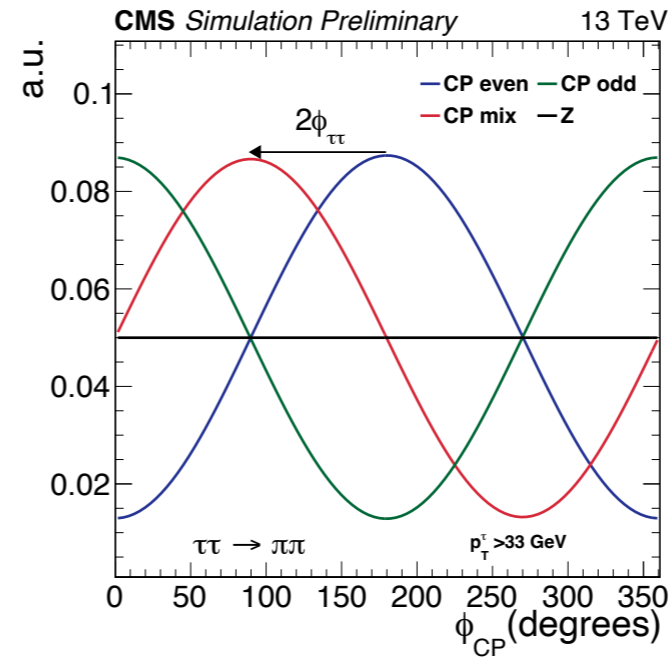
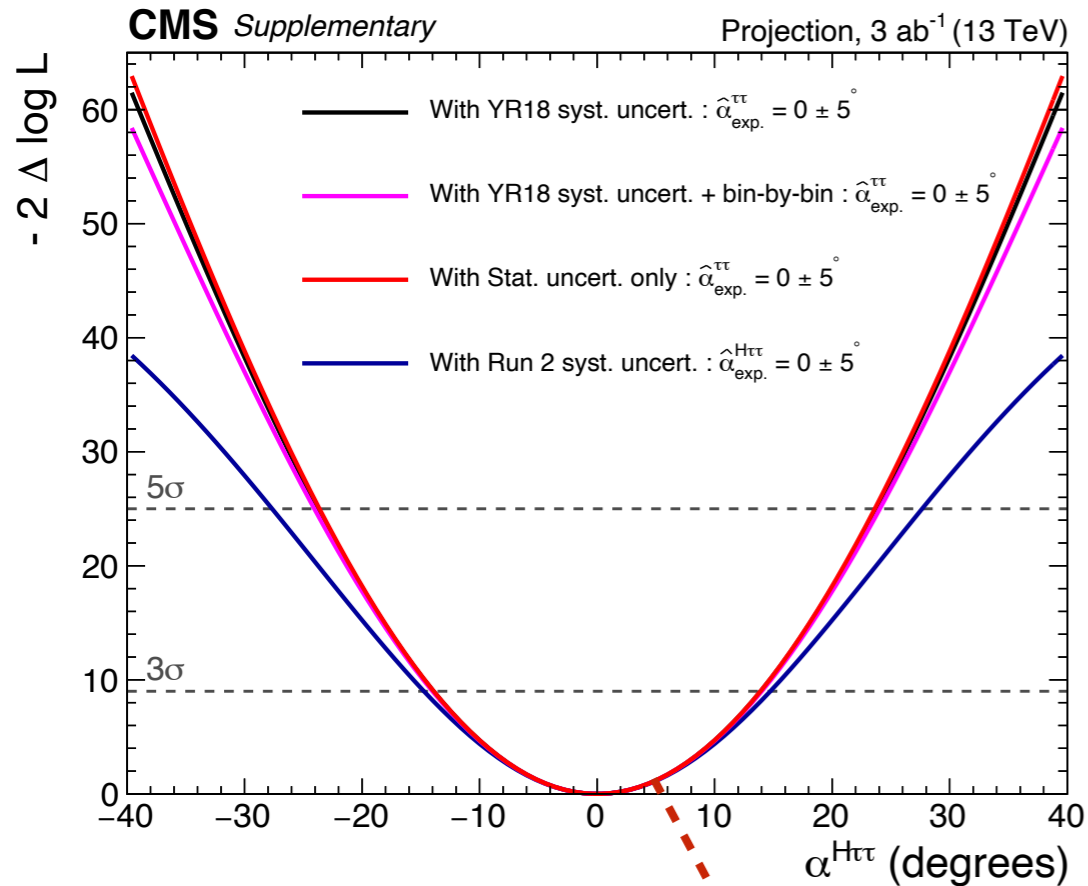
ATLAS [arXiv:2004.04545](https://arxiv.org/abs/2004.04545)

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
$Ht\bar{t}$	0.24	0.05	✓	–	–	0.29	0.08	✓	–	–	✓	$< 10^{-2}$

Decay: $H \rightarrow \tau^+ \tau^-$ at pp

- Very first test of CP in $H\tau\tau$ in 2020

CMS: [CMS-HIG-20-006](#)



pp pheno studies at Snowmass-2013: [arXiv:1308.1094](#)

— reach $f_{CP} \sim 0.008$ ($\alpha \sim 5^\circ$) at HL-LHC [CMS-HIG-20-006](#)

Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	—	✓	✓	✓	$< 10^{-2}$

Overview of Higgs CP at Colliders

- Now cover all couplings at pp and e^+e^- colliders:

new numerical estimates for the first time (since 2013)

new entries (since 2013)

pp 100 TeV would be the best by $\times 100$, but more distant ...

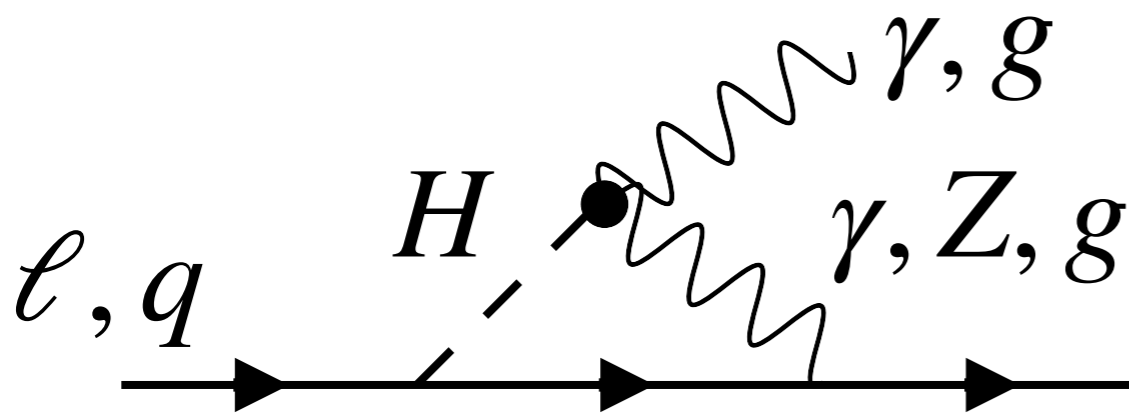
Collider	pp	pp	pp	e^+e^-	e^+e^-	e^+e^-	e^+e^-	e^-p	$\gamma\gamma$	$\mu^+\mu^-$	$\mu^+\mu^-$	target (theory)
E (GeV)	14,000	14,000	100,000	250	350	500	1,000	1,300	125	125	3,000	(theory)
\mathcal{L} (fb^{-1})	300	3,000	30,000	250	350	500	1,000	1,000	250	20	1,000	
HZZ/HWW	$4.0 \cdot 10^{-5}$	$2.5 \cdot 10^{-6}$	✓	$3.9 \cdot 10^{-5}$	$2.9 \cdot 10^{-5}$	$1.3 \cdot 10^{-5}$	$3.0 \cdot 10^{-6}$	✓	✓	✓	✓	$< 10^{-5}$
$H\gamma\gamma$	–	0.50	✓	–	–	–	–	–	0.06	–	–	$< 10^{-2}$
$HZ\gamma$	–	~ 1	✓	–	–	–	~ 1	–	–	–	–	$< 10^{-2}$
Hgg	0.12	0.011	✓	–	–	–	–	–	–	–	–	$< 10^{-2}$
$Ht\bar{t}$	0.24	0.05	✓	–	–	0.29	0.08	✓	–	–	✓	$< 10^{-2}$
$H\tau\tau$	0.07	0.008	✓	0.01	0.01	0.02	0.06	–	✓	✓	✓	$< 10^{-2}$
$H\mu\mu$	–	–	–	–	–	–	–	–	–	✓	–	$< 10^{-2}$

revised numerical estimates

new dedicated studies show not enough precision

Higgs CP from EDM

- Electric Dipole Moment (EDM) of electron $d_e < 1.1 \times 10^{-29} e \text{ cm}$
- atoms/molecules $d_n < 1.8 \times 10^{-26} e \text{ cm}$
- $d_e^{\text{SM}} \sim 10^{-38} e \text{ cm}$



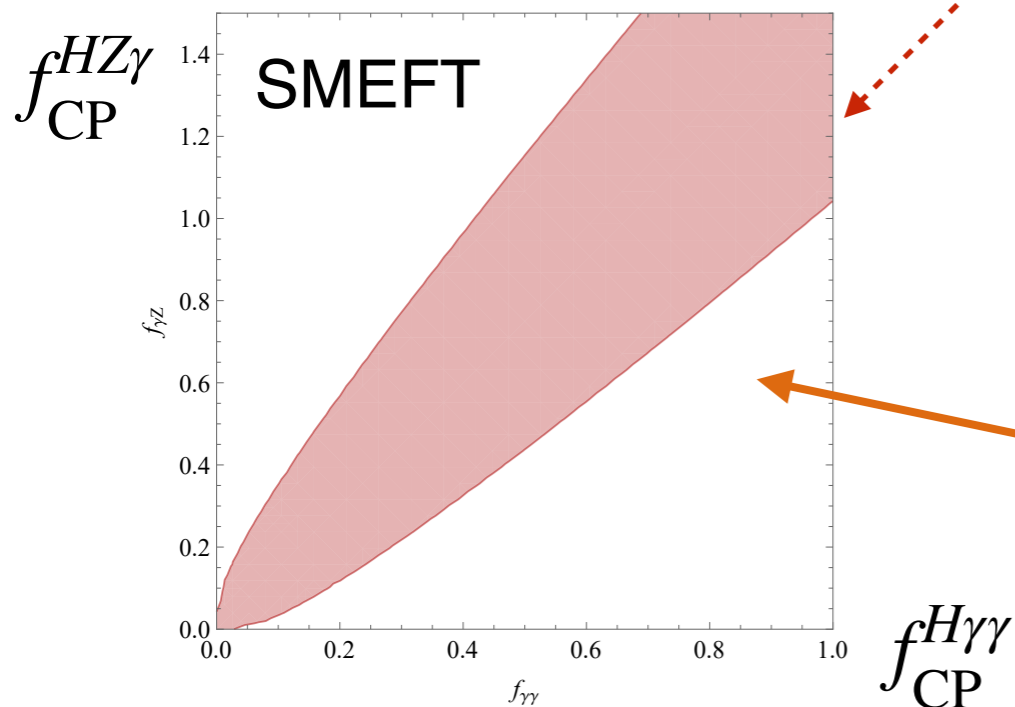
expect $\times 10^{-2}$ in ~ 10 years [arXiv:2203.08103](https://arxiv.org/abs/2203.08103)

Appendix C: EDM constraints

Contributed by Wouter Dekens.

HX coupling	Hgg	$H\gamma\gamma$	$HZ\gamma$	HZZ	$Ht\bar{t}$	$Hu\bar{u}$	Hdd	$H\tau\tau$	$H\mu\mu$	Hee
$f_{CP}^{HX} / (1 - f_{CP}^{HX}) <$	0.12	$2.4 \cdot 10^{-8}$	$4.4 \cdot 10^{-8}$	$1.2 \cdot 10^{-13}$	$4.3 \cdot 10^{-7}$	0.72	0.039	$2.2 \cdot 10^{-2}$	36	$1.1 \cdot 10^{-6}$

only EDM



— assuming CP -even SM coupling to 1st family

— assuming one CP -odd coupling at a time

lost tight constraints with 3 couplings already

$$f_{CP}^{H\gamma\gamma}, f_{CP}^{HZ\gamma}, f_{CP}^{HZZ}$$

Summary on Higgs CP

- Higgs CP is a good **reference measurement** for **Snowmass-2022**
 - **Snowmass-2013** was already a good starting point
- Reached several conclusions on colliders:
 - pp reach full spectrum of Higgs CP , **except $H\mu\mu$**
 - e^+e^- comparable to HL-LHC in Higgs CP , **except Hgg**
 - $\gamma\gamma$ at 125 GeV + polarize unique **CP in $H\gamma\gamma$**
 - $\mu^+\mu^-$ at 125 GeV + polarize unique **CP in $H\mu\mu$** (2nd family)
 - e^-p allow CP in VBF
 - pp at 100 TeV the furthest reach, including **CP in $HV\gamma$**
- EDM constraints on Higgs CP
 - strongest, but assuming **one CP -odd coupling at a time**
 - assuming **CP -even SM coupling to 1st family**

HWW, HZZ
 $HZ\gamma, H\gamma\gamma, Hgg$
 $Htt, H\tau\tau, H\mu\mu$