



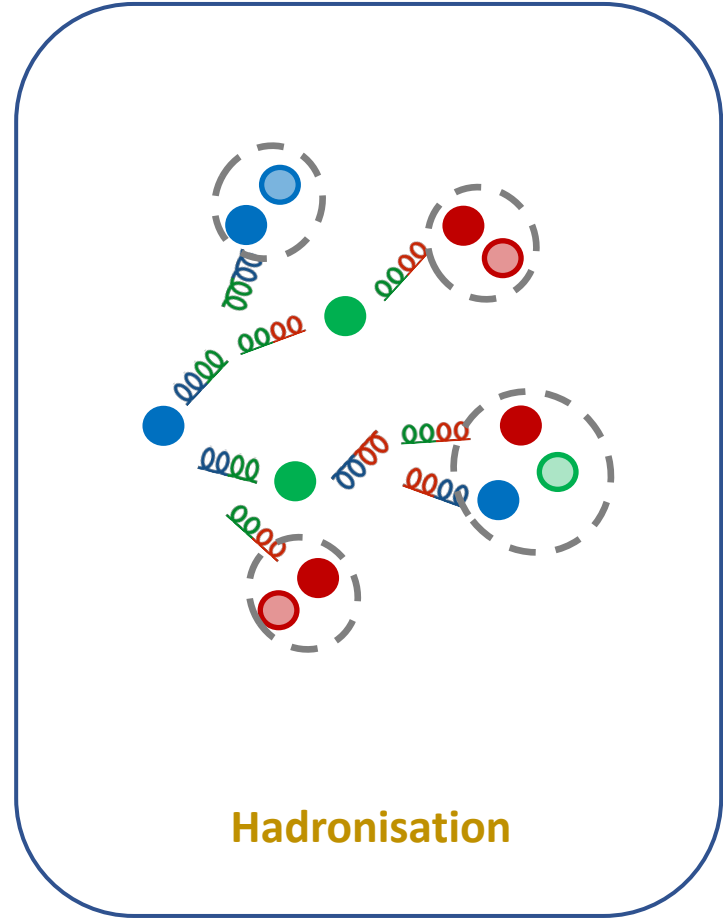
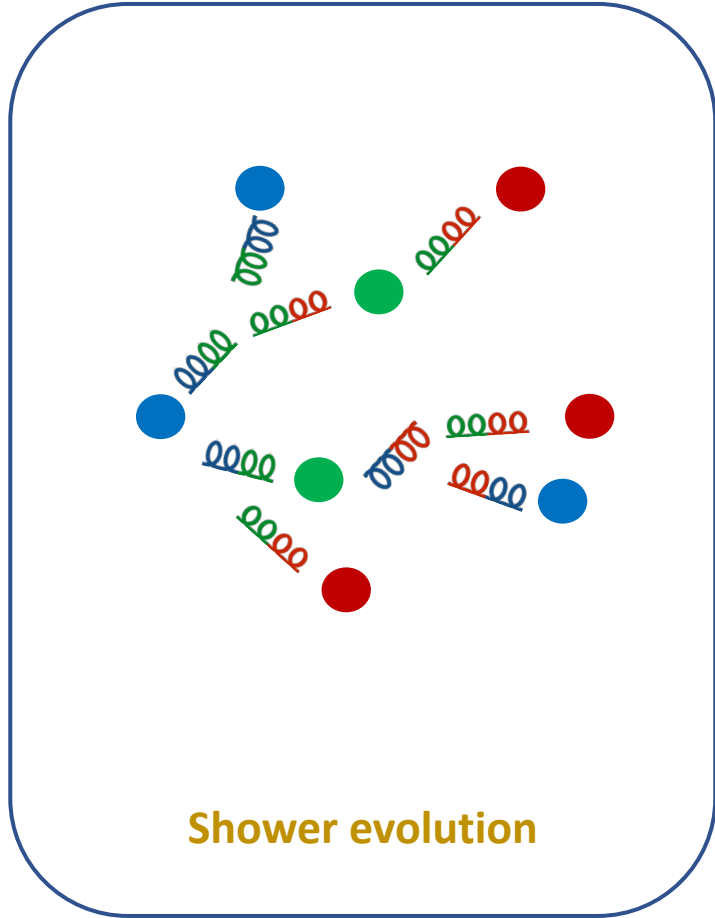
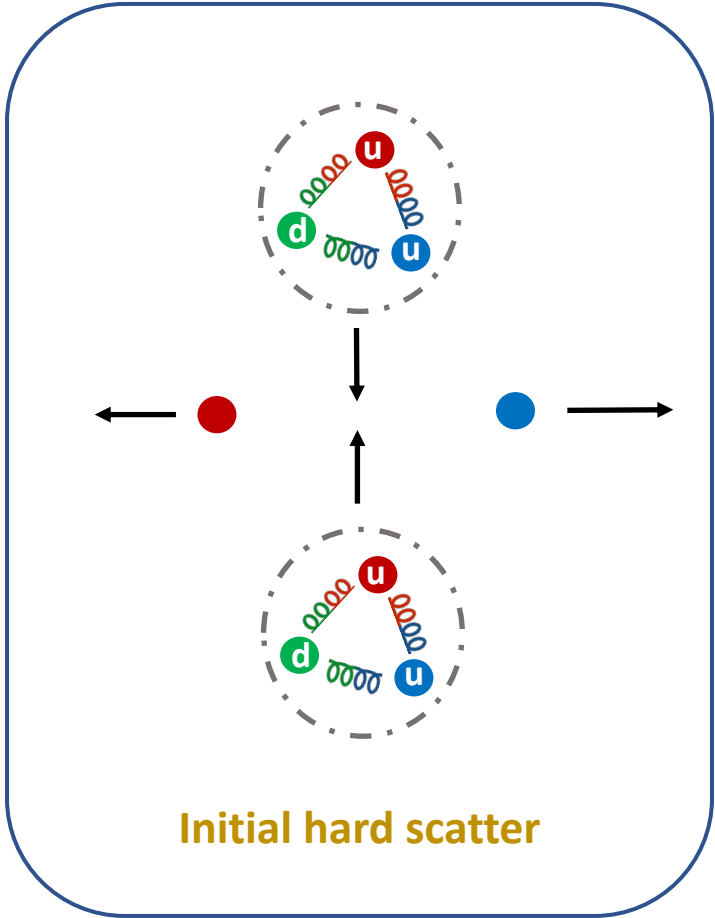
ALICE

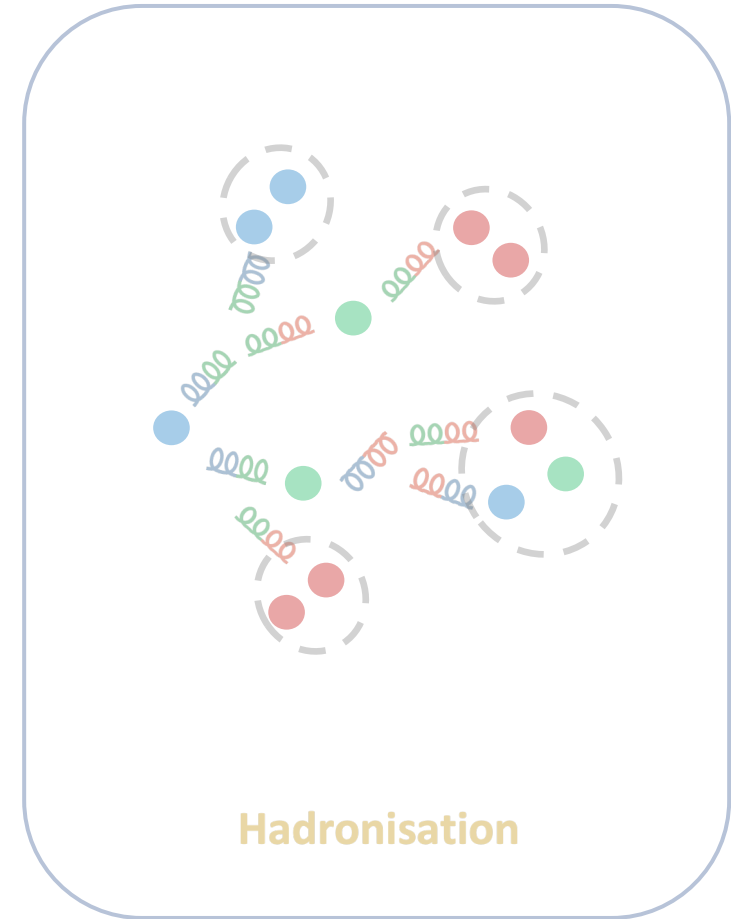
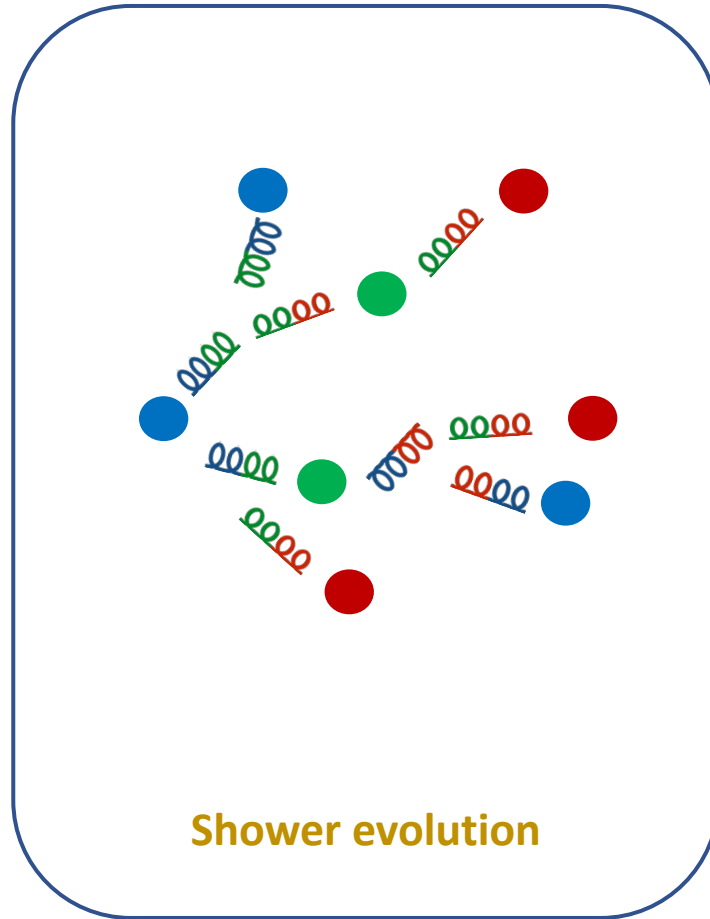
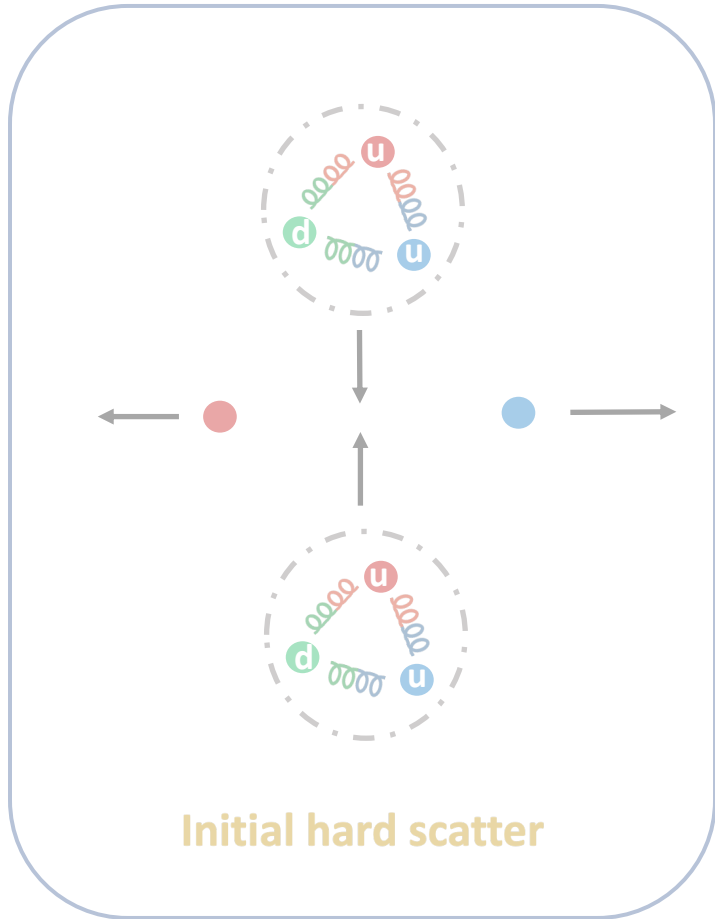
Tracing heavy-flavour quarks through the parton shower

Nima Zardoshti

Heavy-flavours at high p_T workshop
Edinburgh
29/11/2023



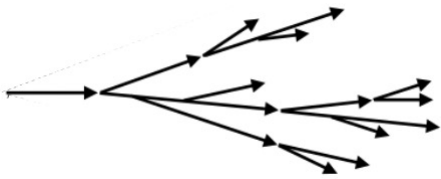




A wealth of partonic interactions to explore QCD
How can we access this region from final state hadrons?

Gluon-initiated shower

Broader shower profile
Higher number of emissions



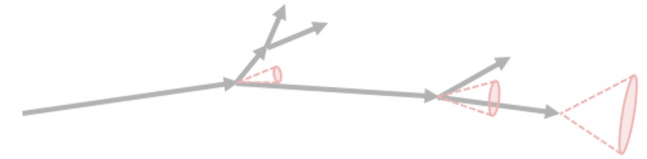
Quark-initiated shower

narrower shower profile
Fewer emissions in the shower



Heavy-quark-initiated shower

Suppression of small angle emissions
Harder fragmentation



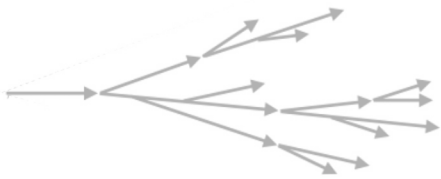
Casimir Colour factors

Different emission properties due to the different amount of colour charge carried by quarks and gluons

$$\frac{C_A}{C_F} = \frac{9}{4}$$

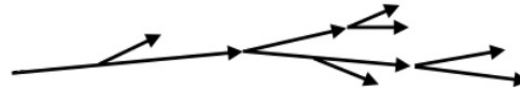
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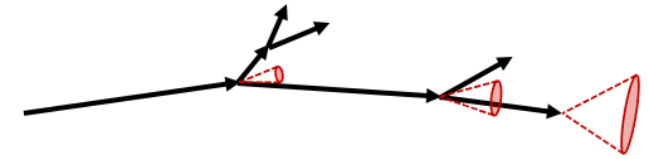
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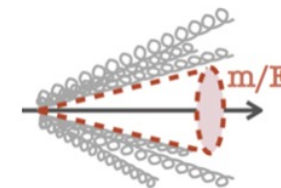
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The dead-cone effect

A suppression of emissions in a cone of size m/E around the direction of the emitter

Sizeable effect for low energy heavy quarks

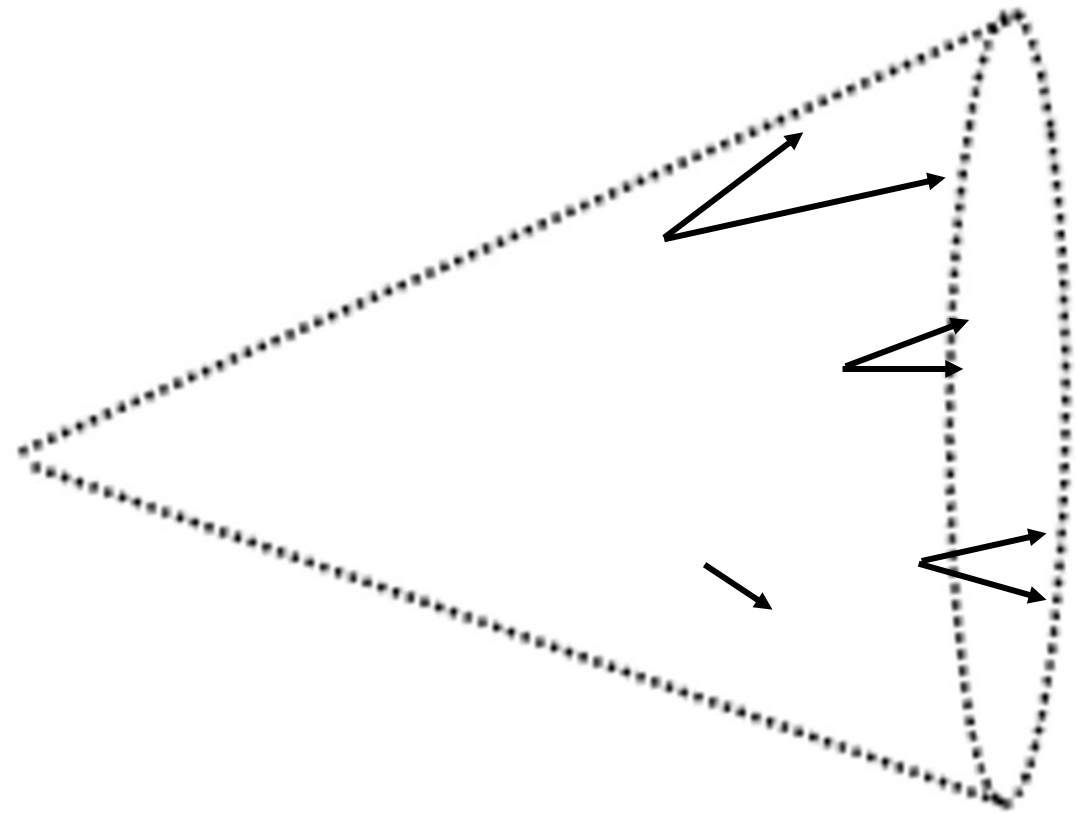


Use the anti- k_T algorithm to cluster jets and identify the final state particles from the shower

Reconstructing the shower

Assume the evolution of the shower followed a given ordering

The jet is reclustered with an algorithm that respects that ordering
Angular ordering \rightarrow C/A



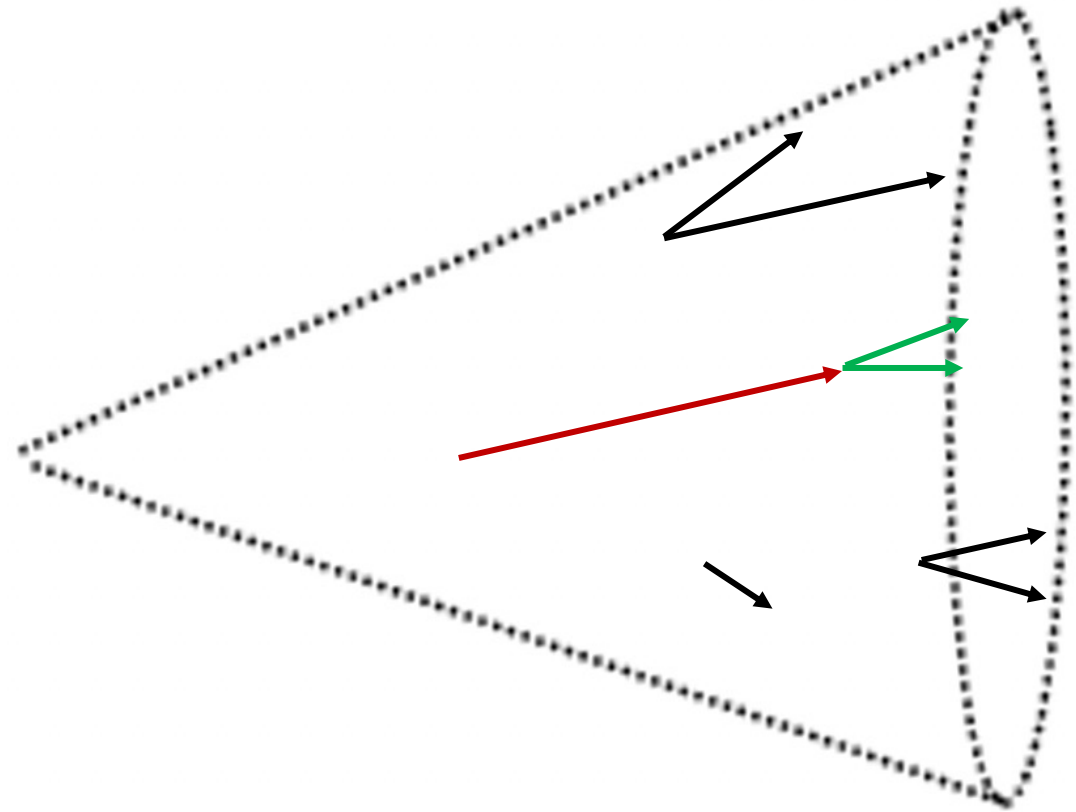
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The shower is then built up by bringing the constituents closest in angle together



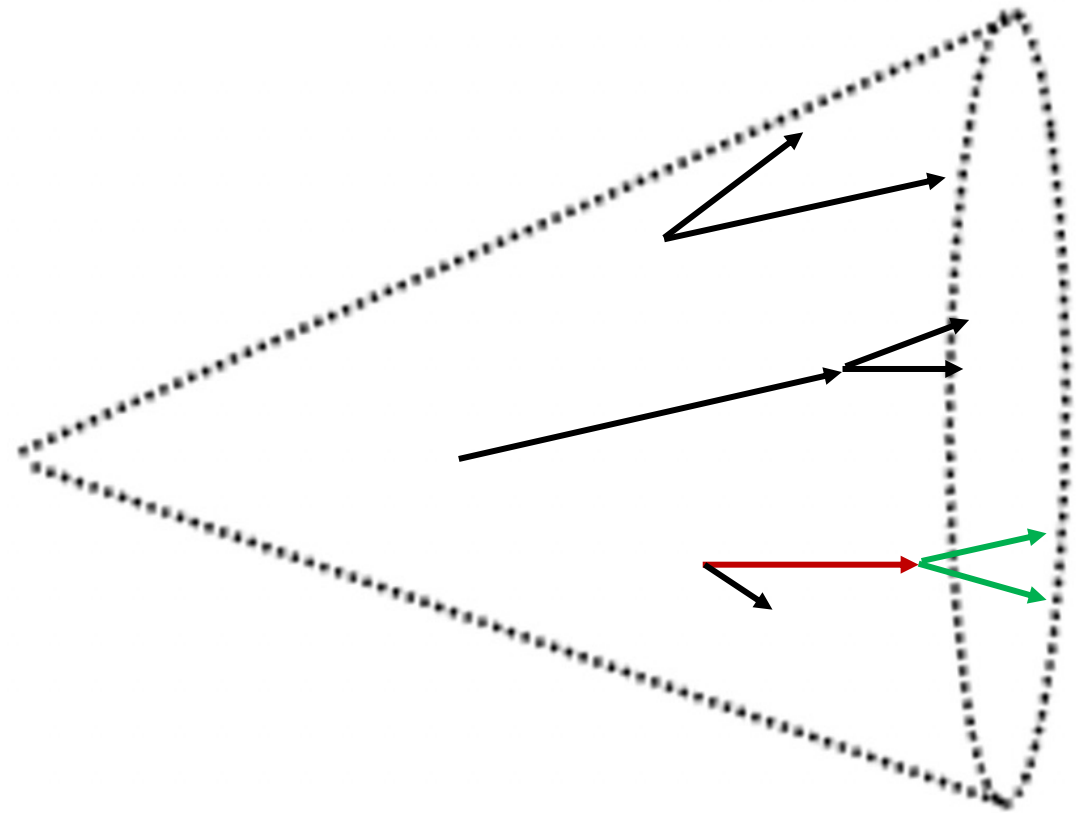
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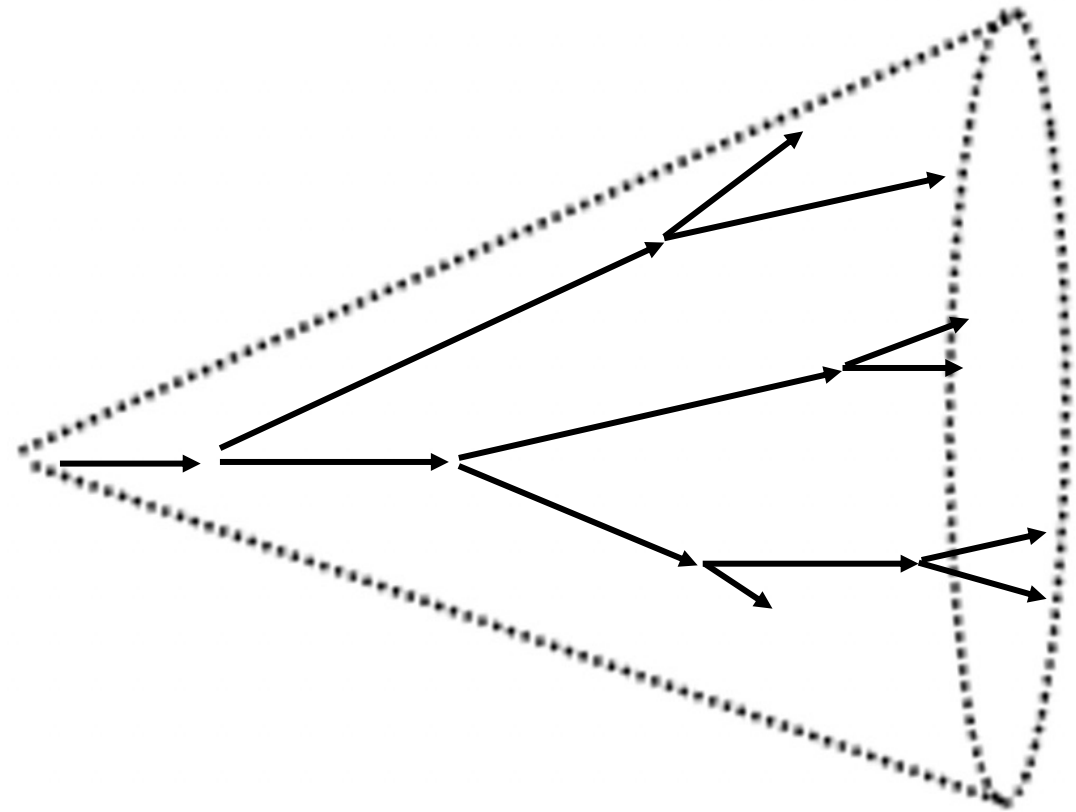
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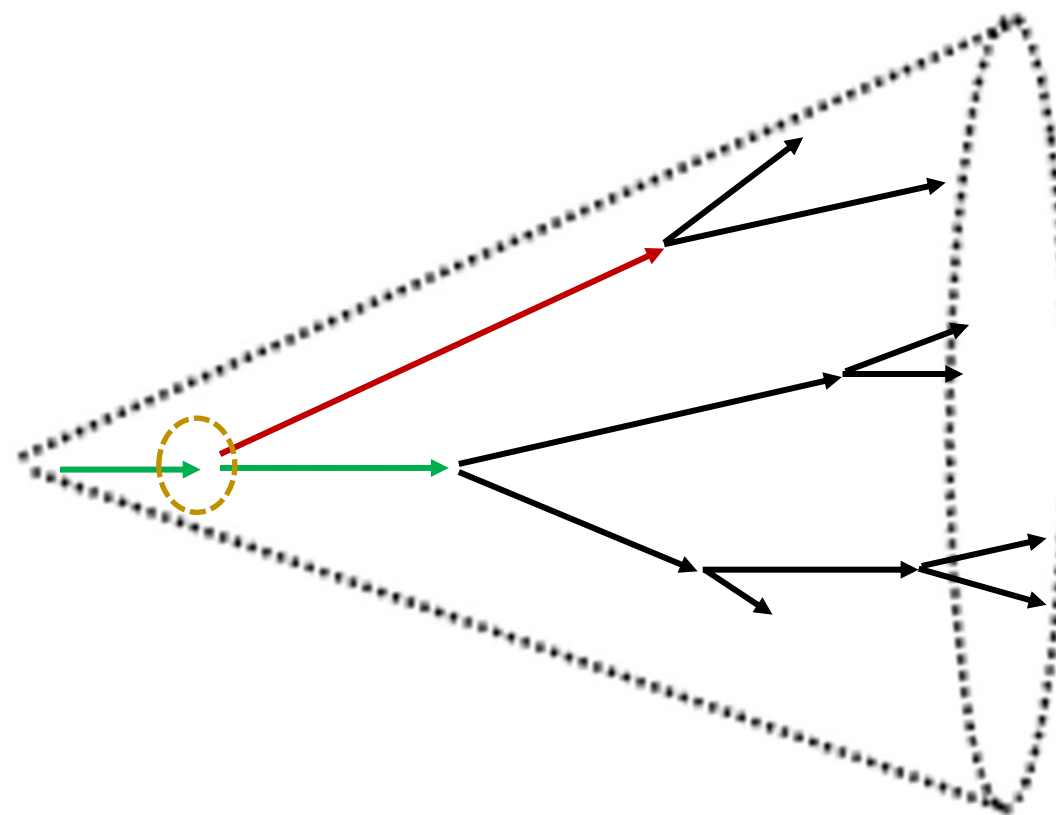


The idea is to follow the evolution of a particular parton through the shower

Requirements for tracing

Access the structure of the shower

Make a choice at each splitting **vertex** of which **branch** to follow

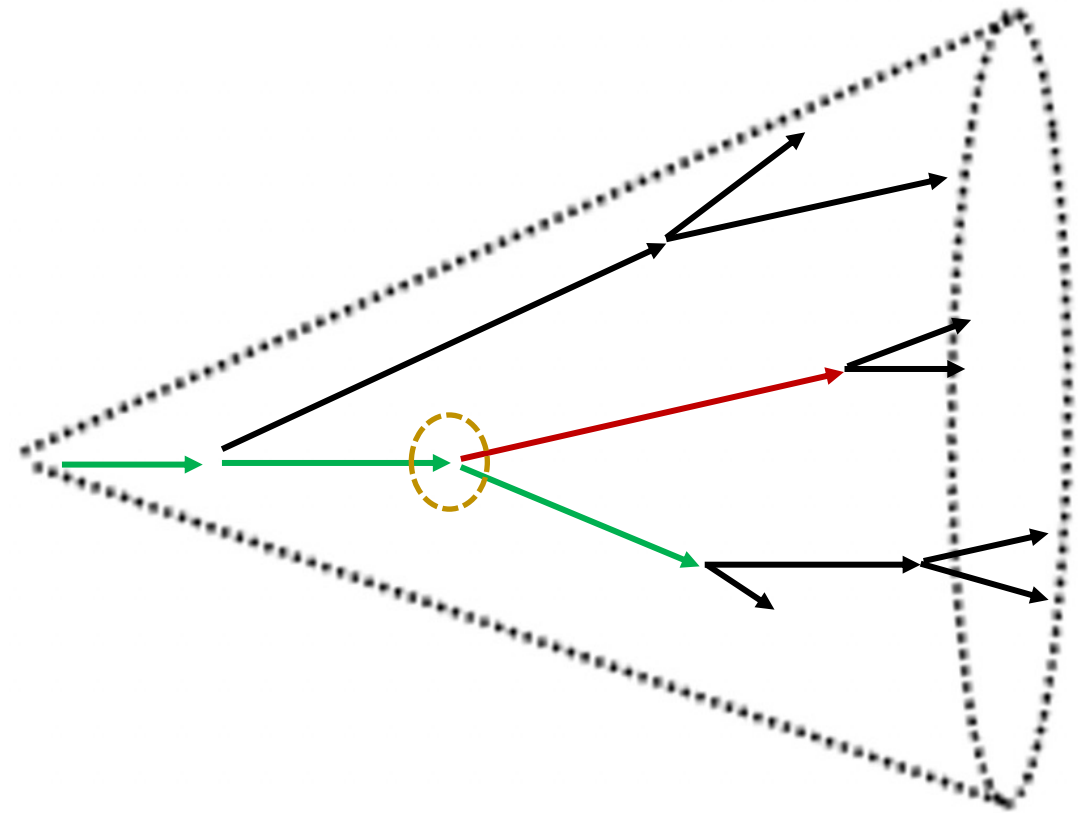


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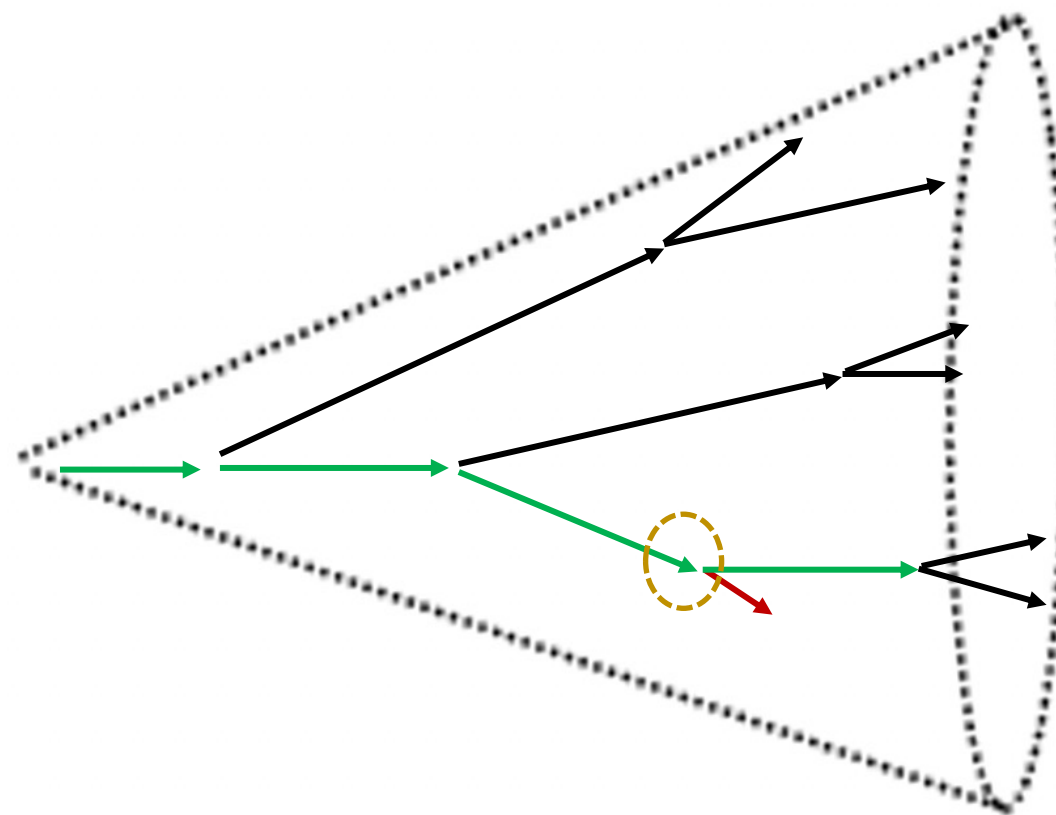


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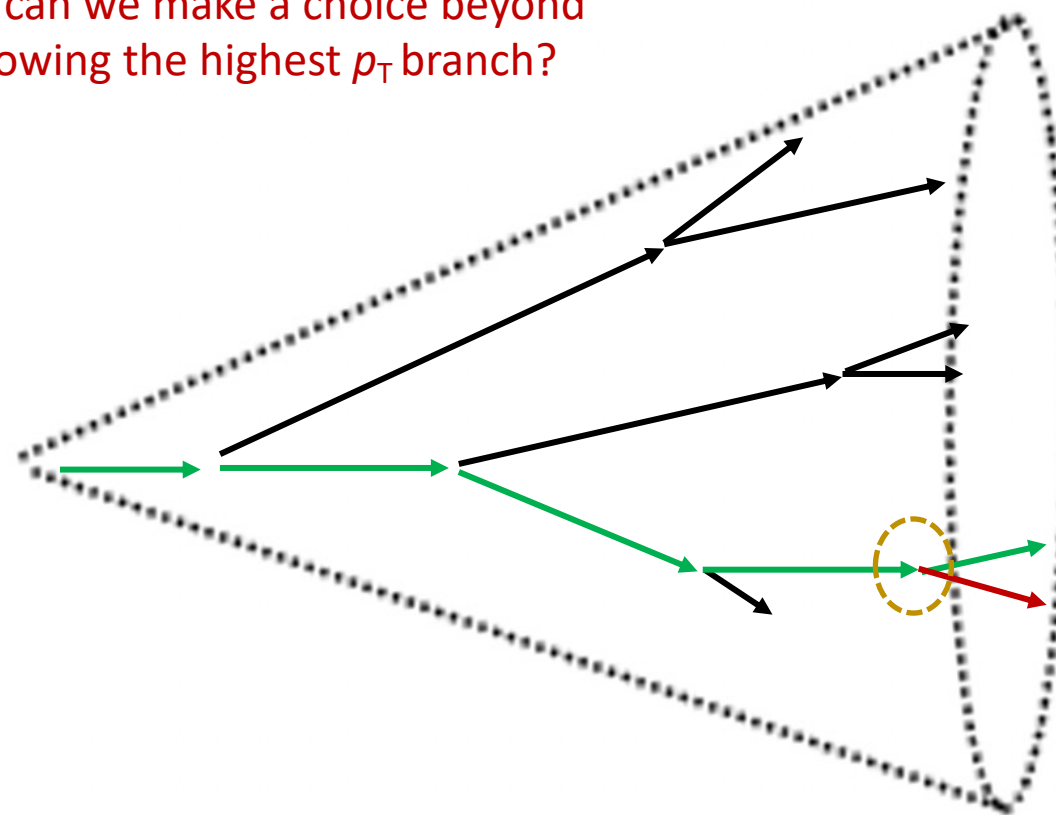
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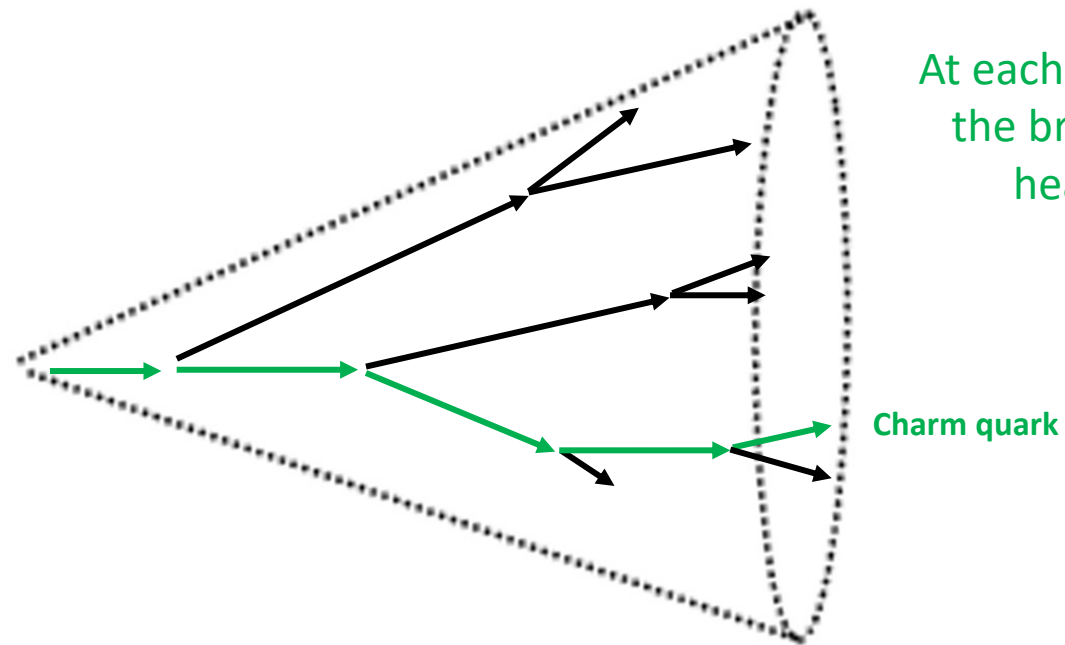
Access the structure of the shower

Make a choice at each splitting **vertex** of which **branch** to follow

The key to tracing is to make the correct choice at each vertex

How can we make a choice beyond following the highest p_T branch?





Hadronisation

Heavy-quark production through string breaking is suppressed during hadronisation

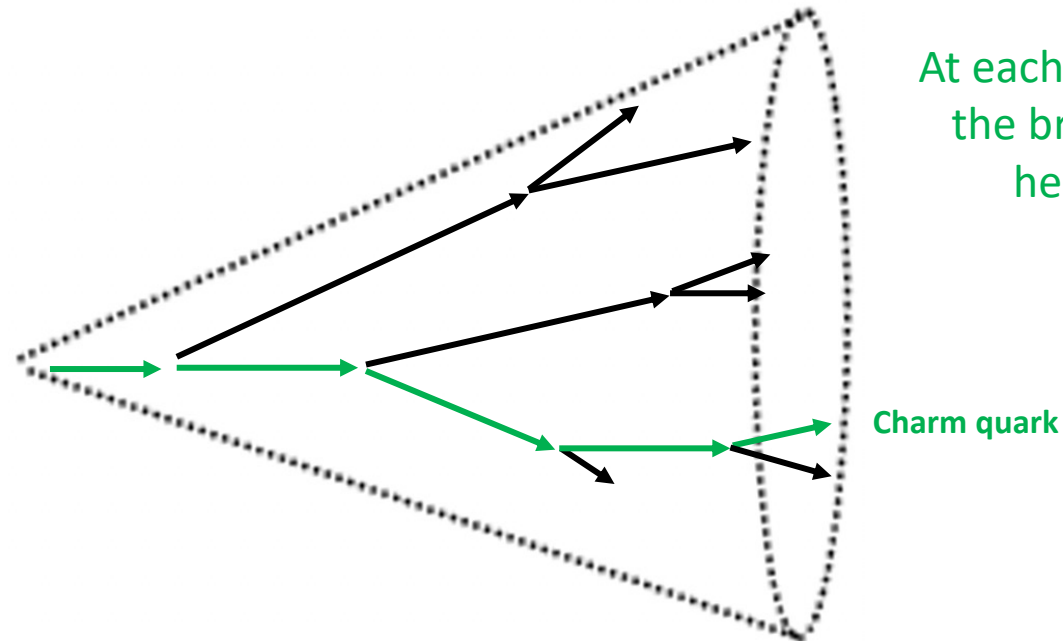
Factor of 10^{-11} suppression compared to light quarks

Single emission channel

Once a quark is produced in the shower it can only undergo $q \rightarrow qg$ emissions

$c \rightarrow cg$ or $b \rightarrow bg$

Once a charm quark has been identified in the final state we can guarantee that it participated in the shower



At each splitting vertex follow the branch that contains a heavy-flavour quark

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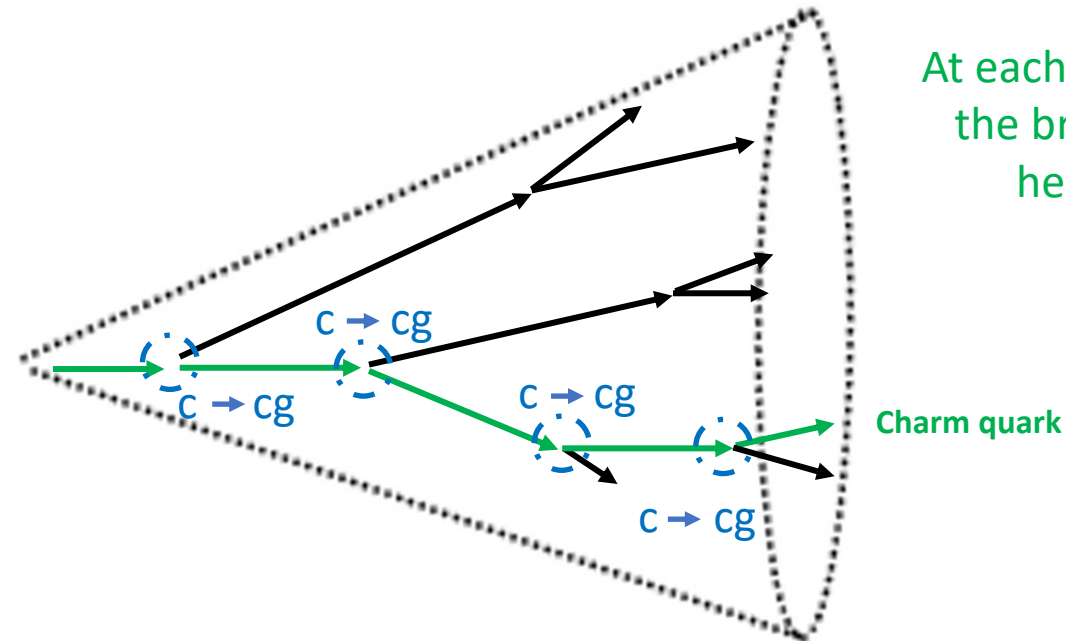
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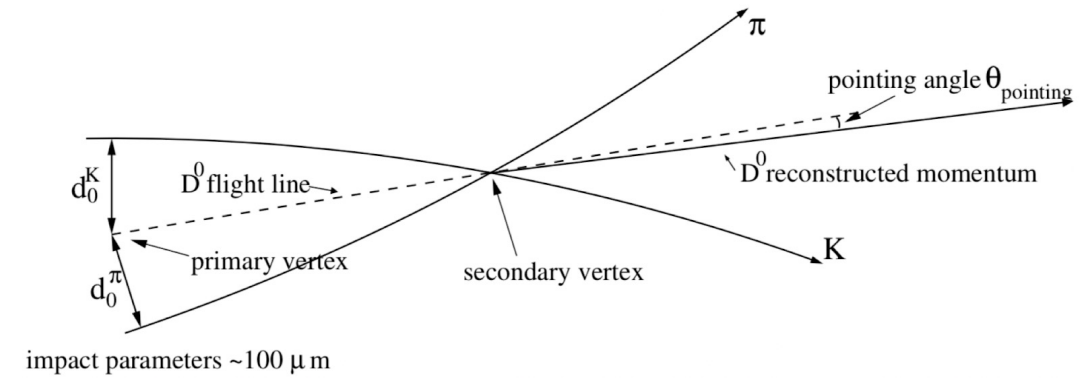
Once a charm quark has been identified in the final state we can guarantee that it participated in the shower

Following the charm quark through the shower gives access to a well controlled splitting flavour by only requiring its presence



At each splitting vertex follow the branch that contains a heavy-flavour quark

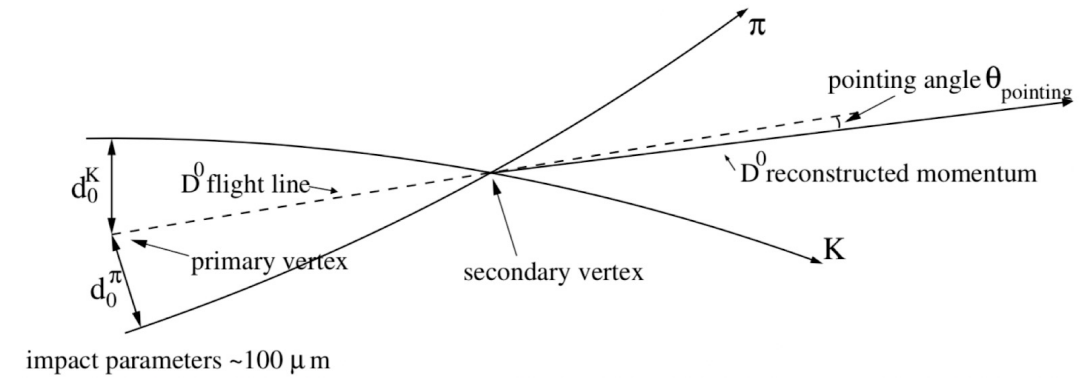
Methodology



The heavy-flavour hadron is a proxy for the final state of the heavy-quark in the shower

Methodology

Heavy-flavour hadrons are identified from their decay products

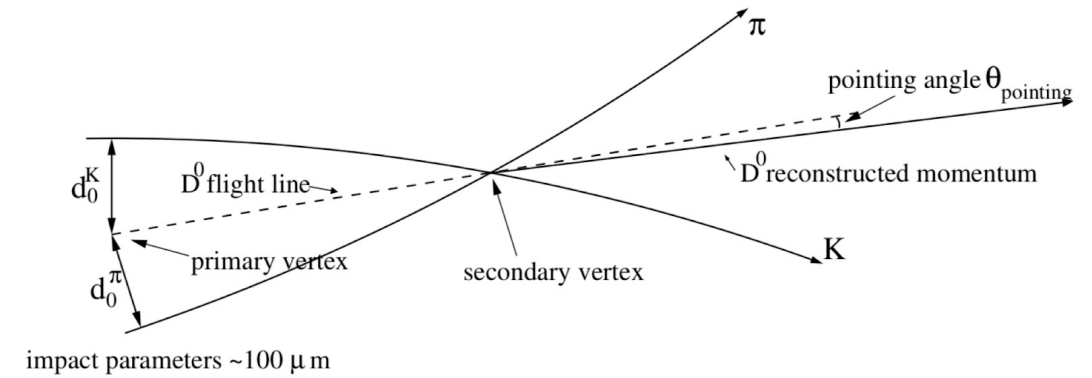


Decay products

Methodology

Heavy-flavour hadrons are identified from their decay products

Replace the heavy-flavour hadron daughters with the parent's four-momentum

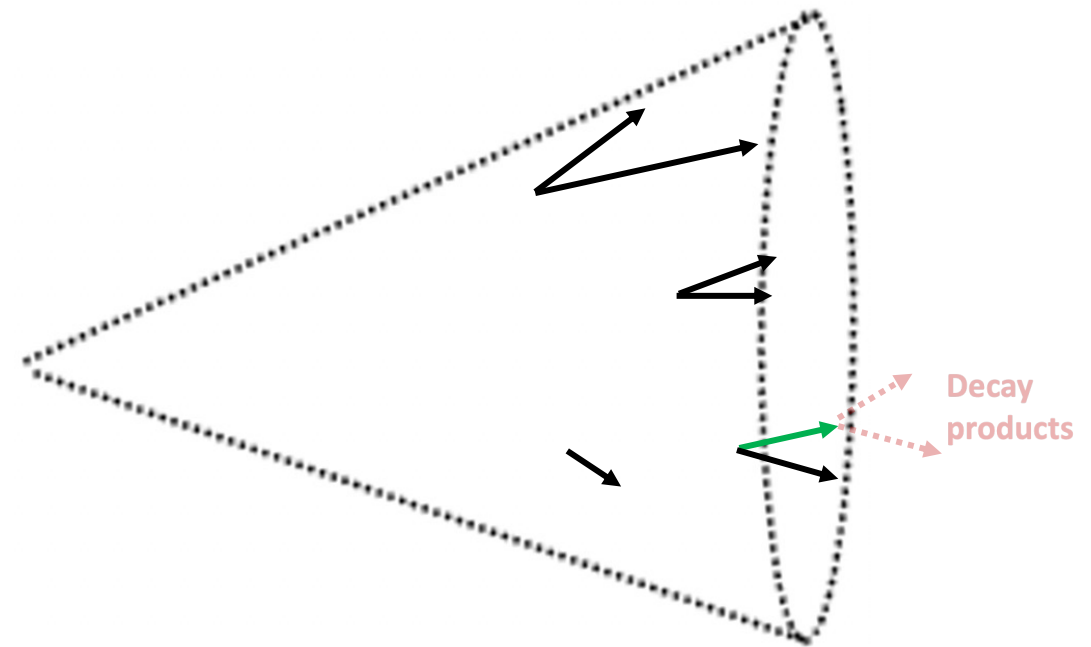
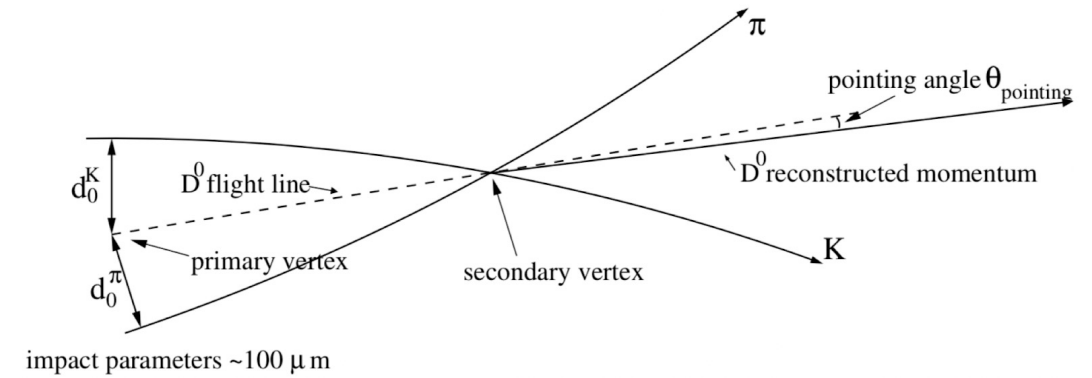


Methodology

Heavy-flavour hadrons are identified from their decay products

Replace the heavy-flavour hadron daughters with the parent's four-momentum

Perform jet finding and tag the jet with the heavy-flavour hadron



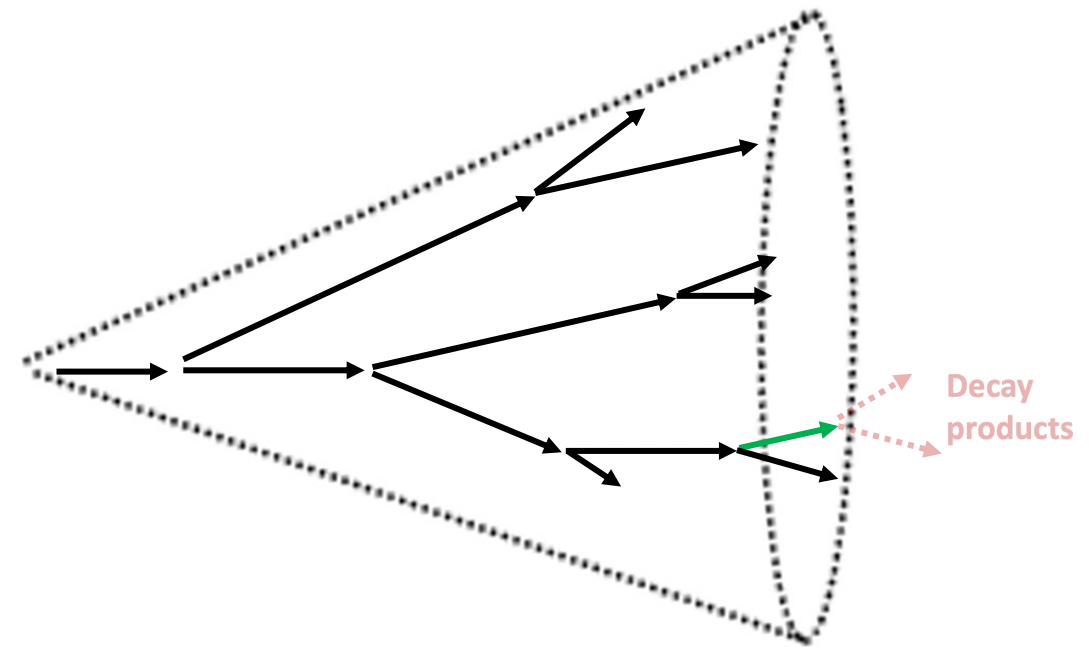
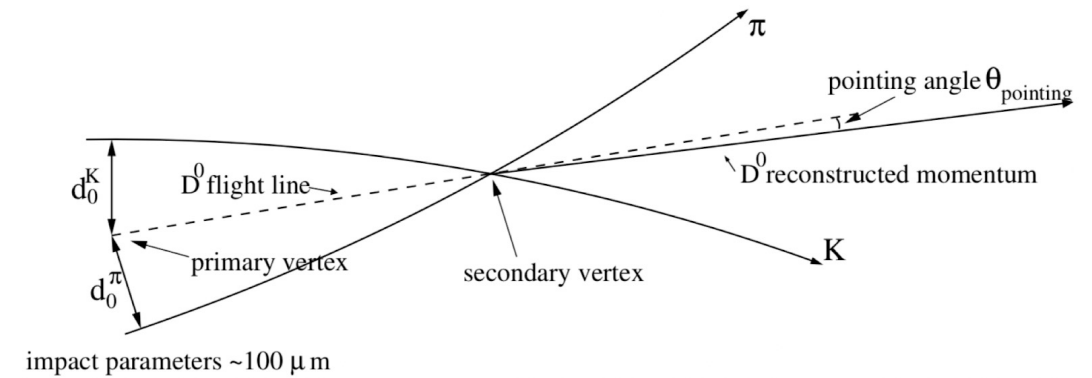
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Recluster the jet to access the splitting tree



Methodology

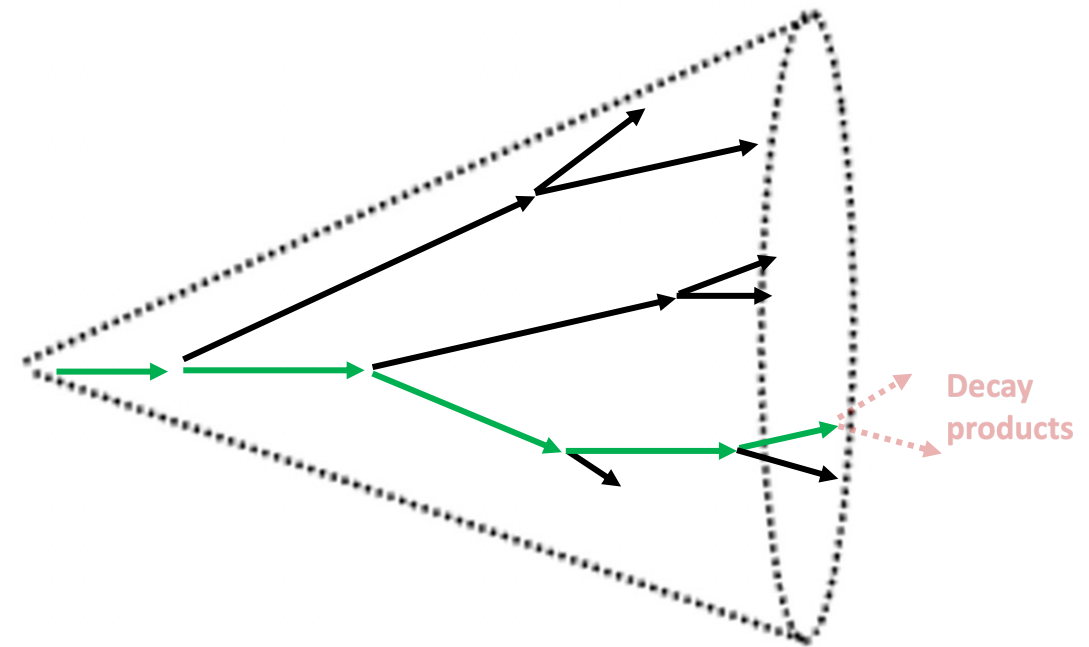
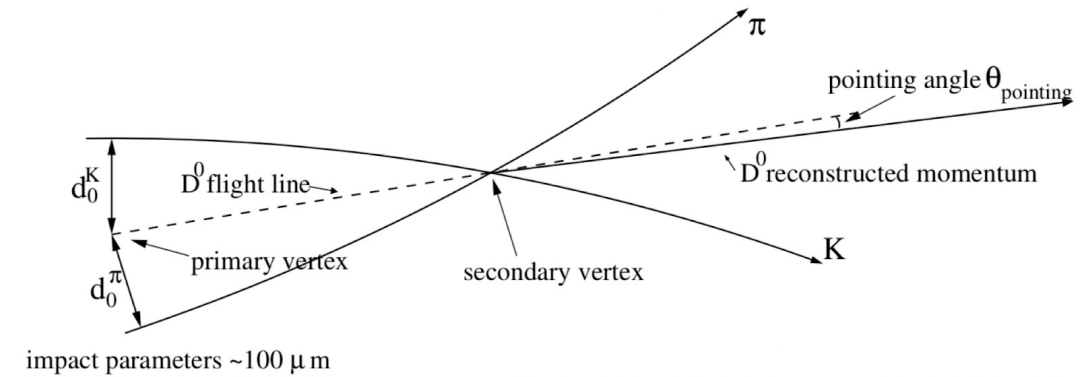
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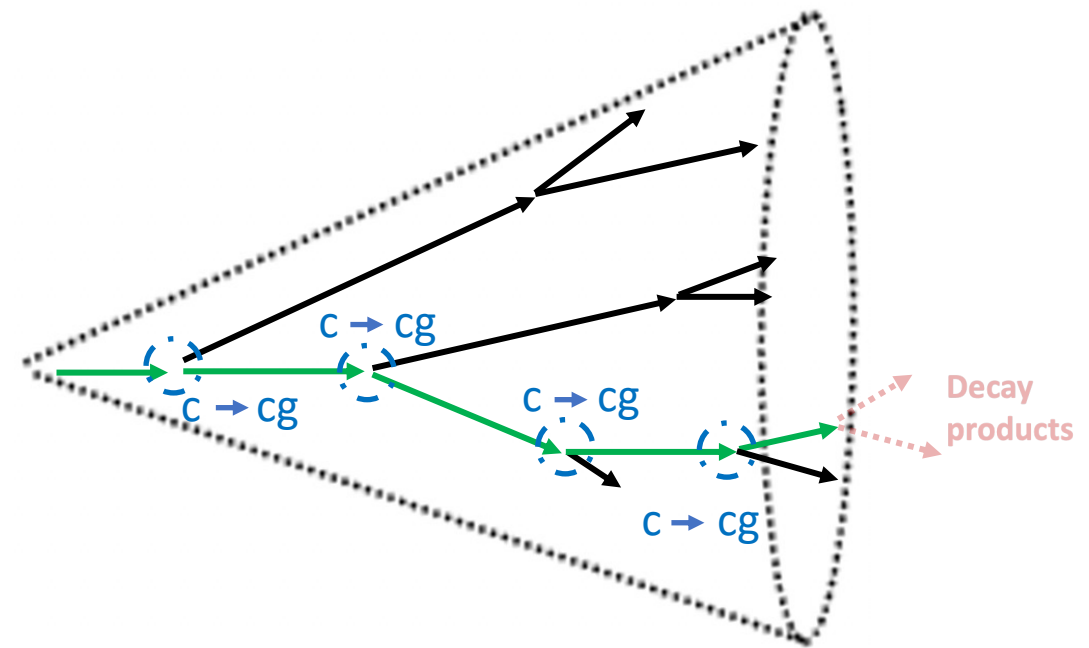
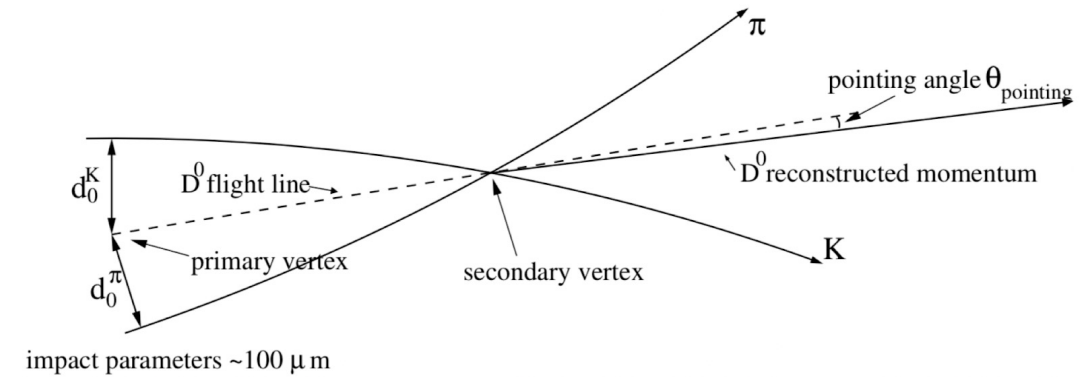
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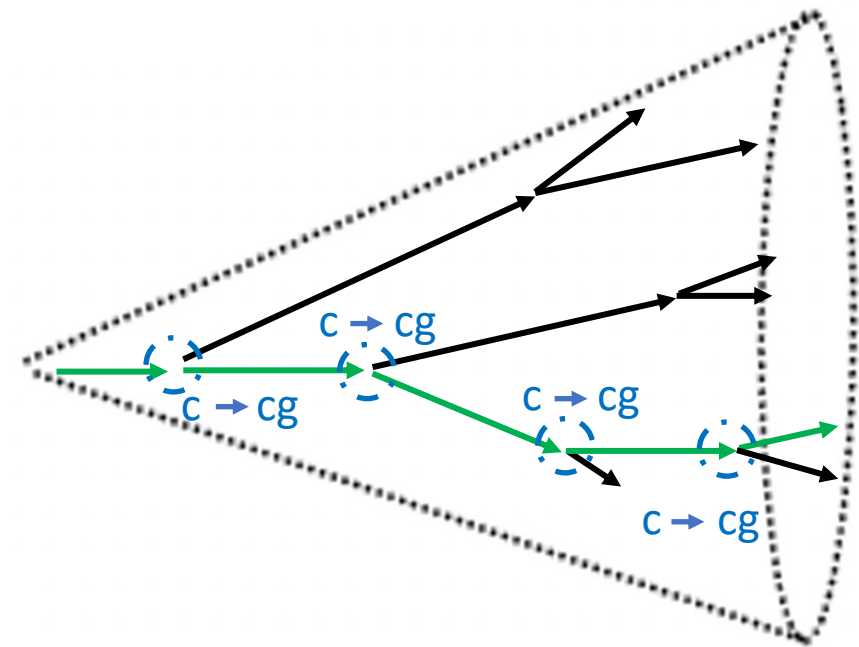
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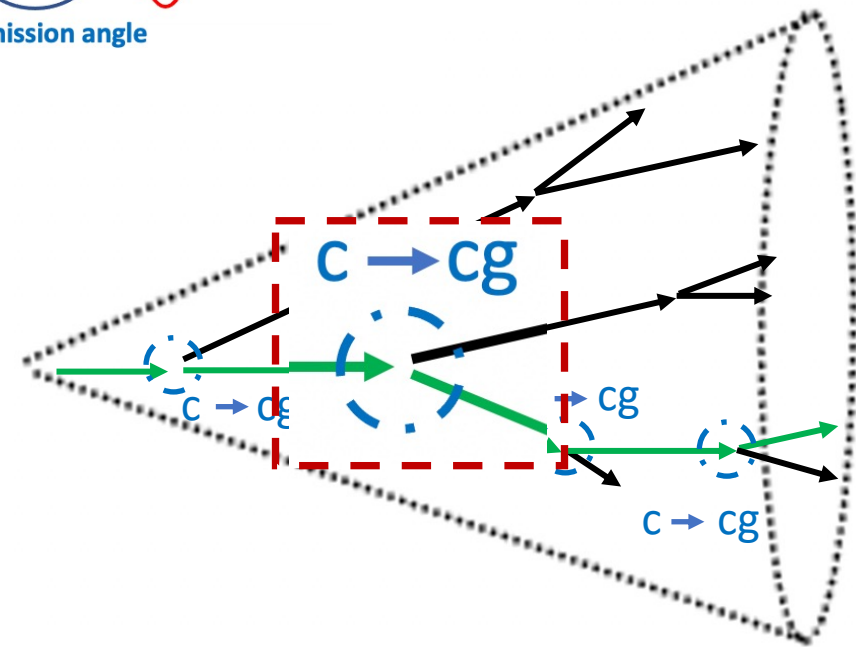
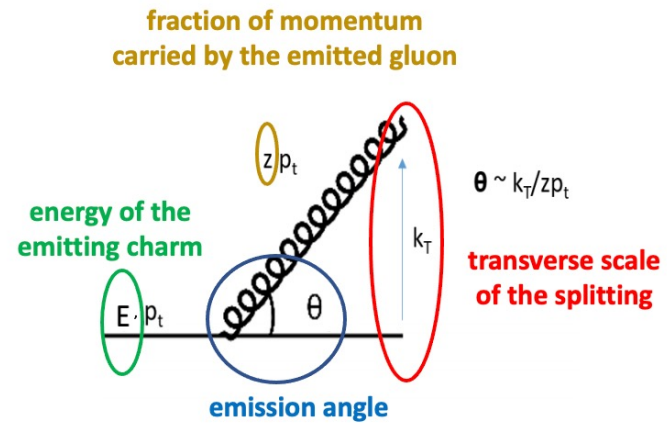
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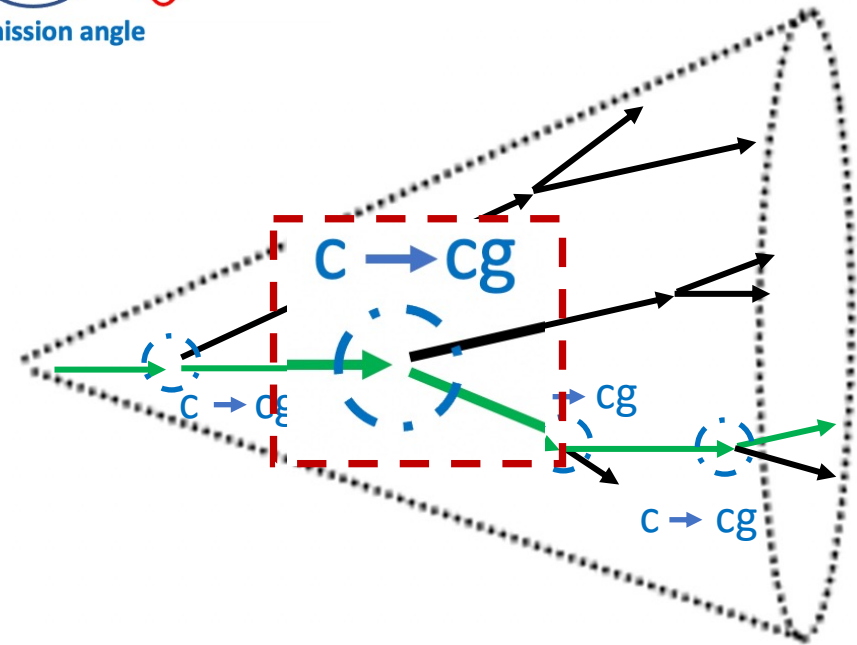
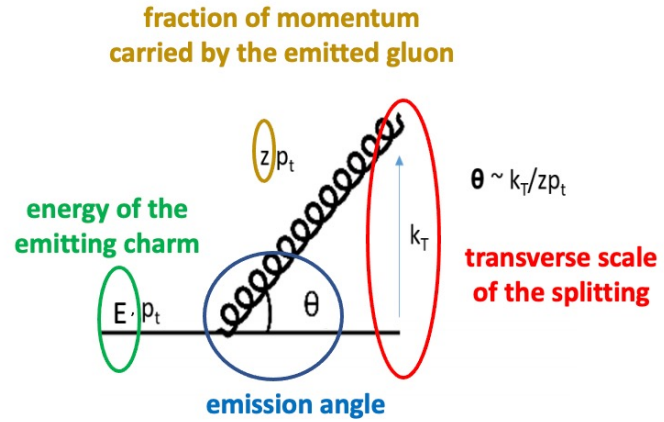
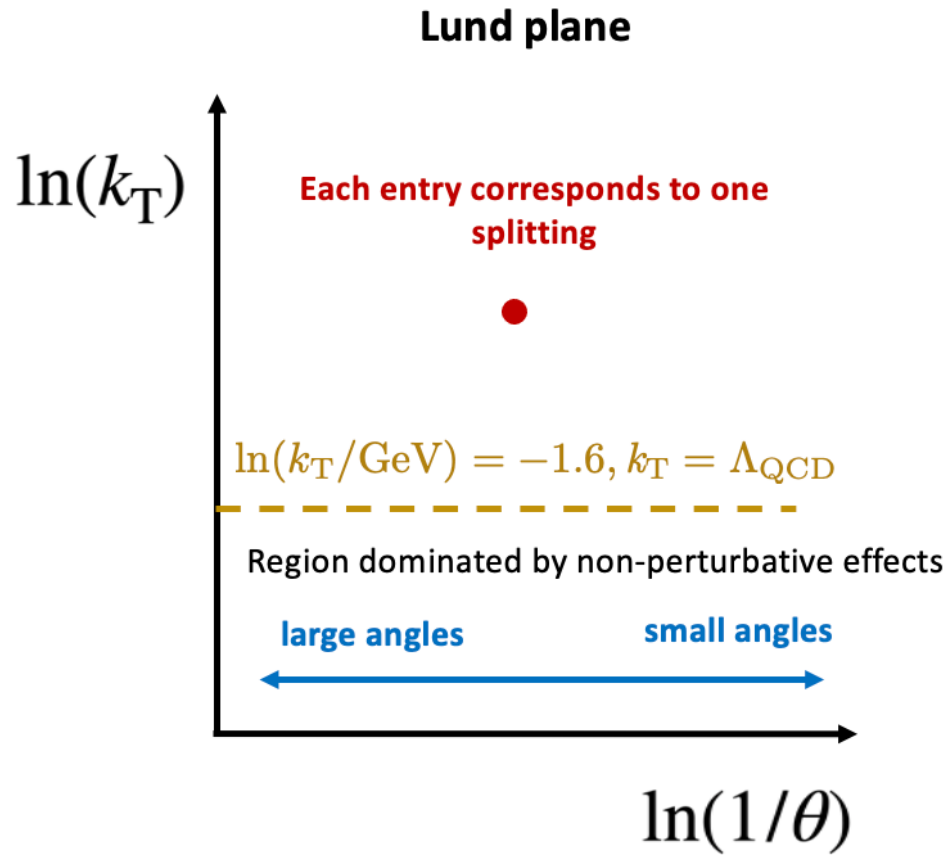
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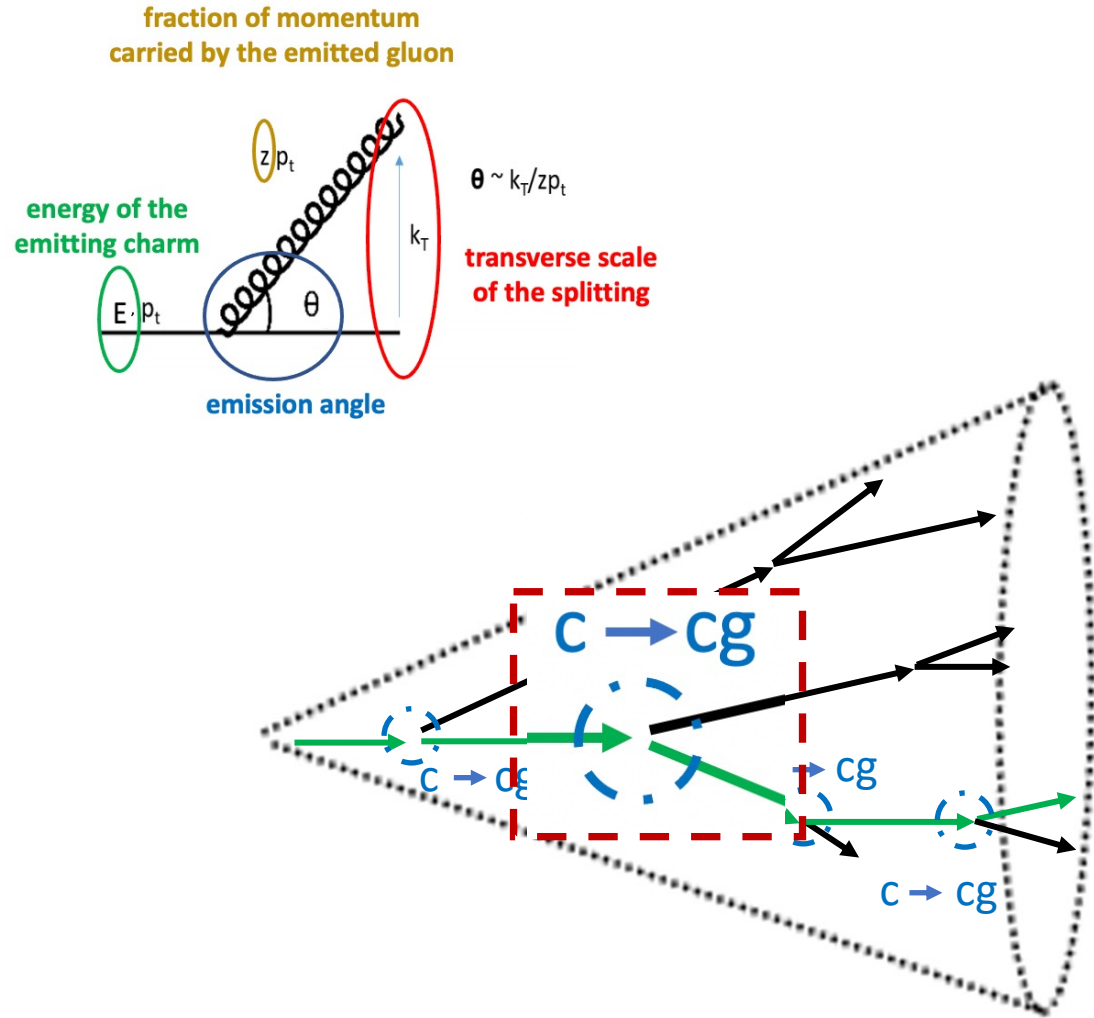
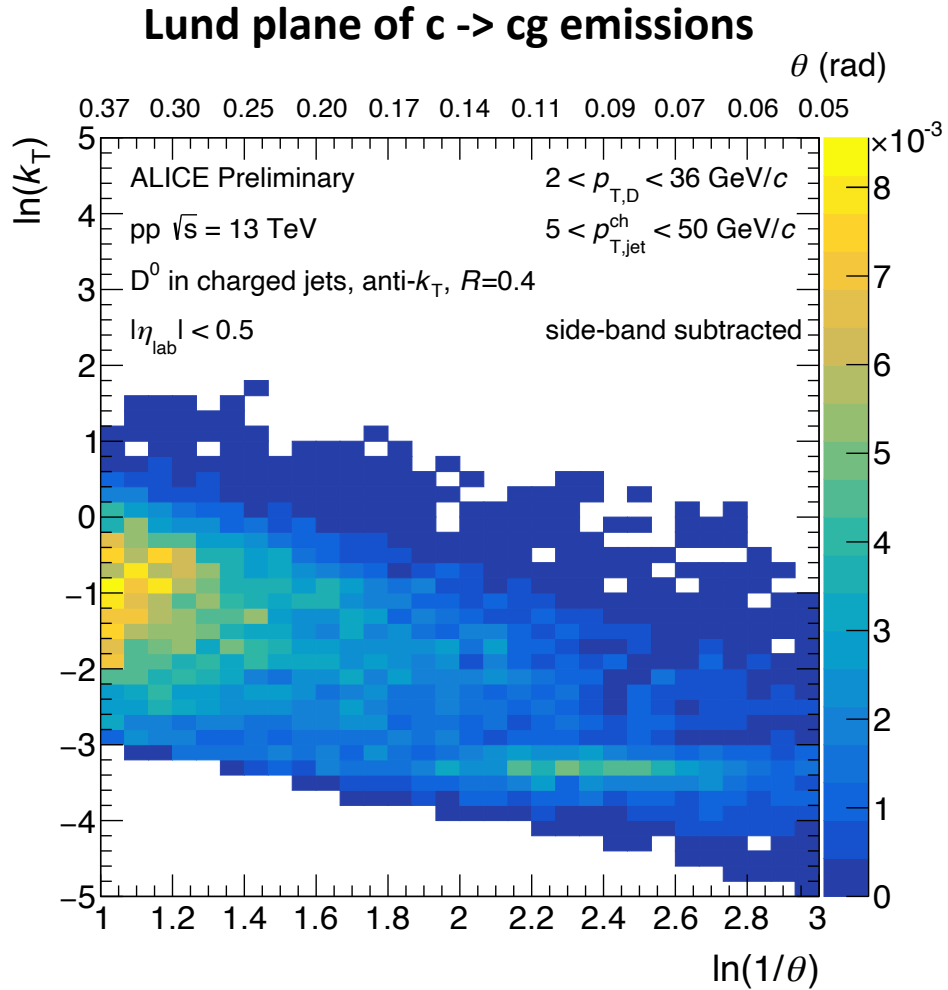
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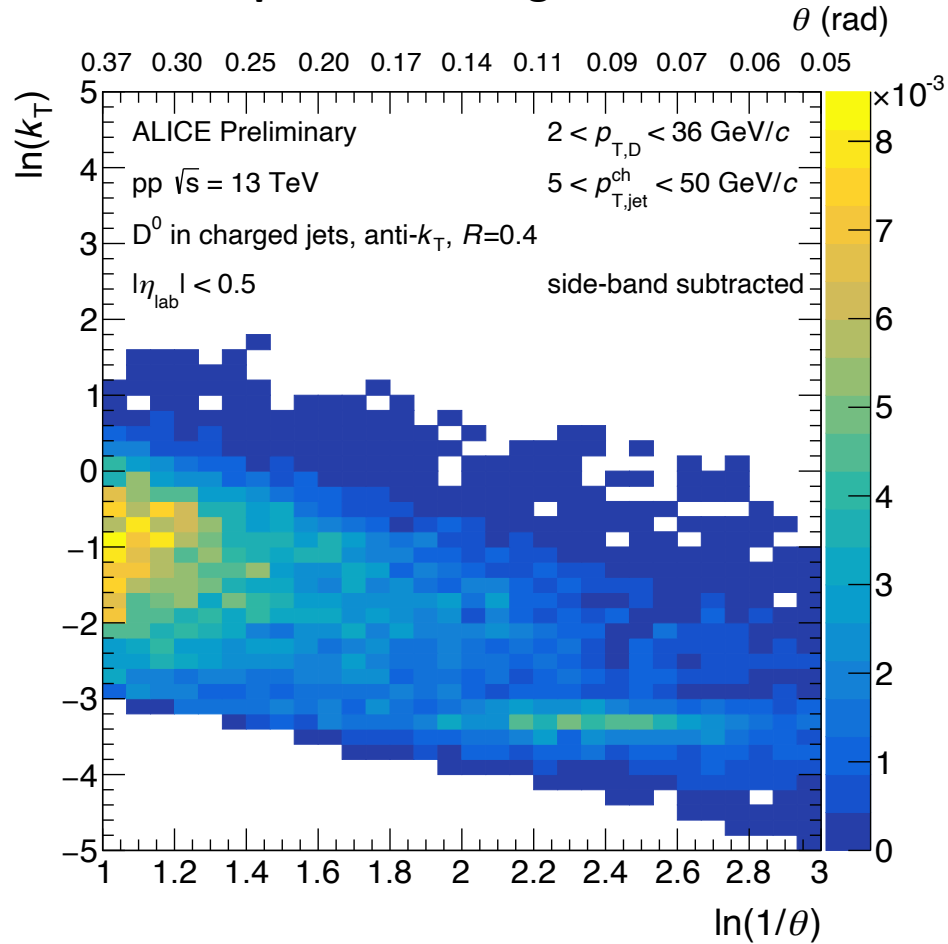




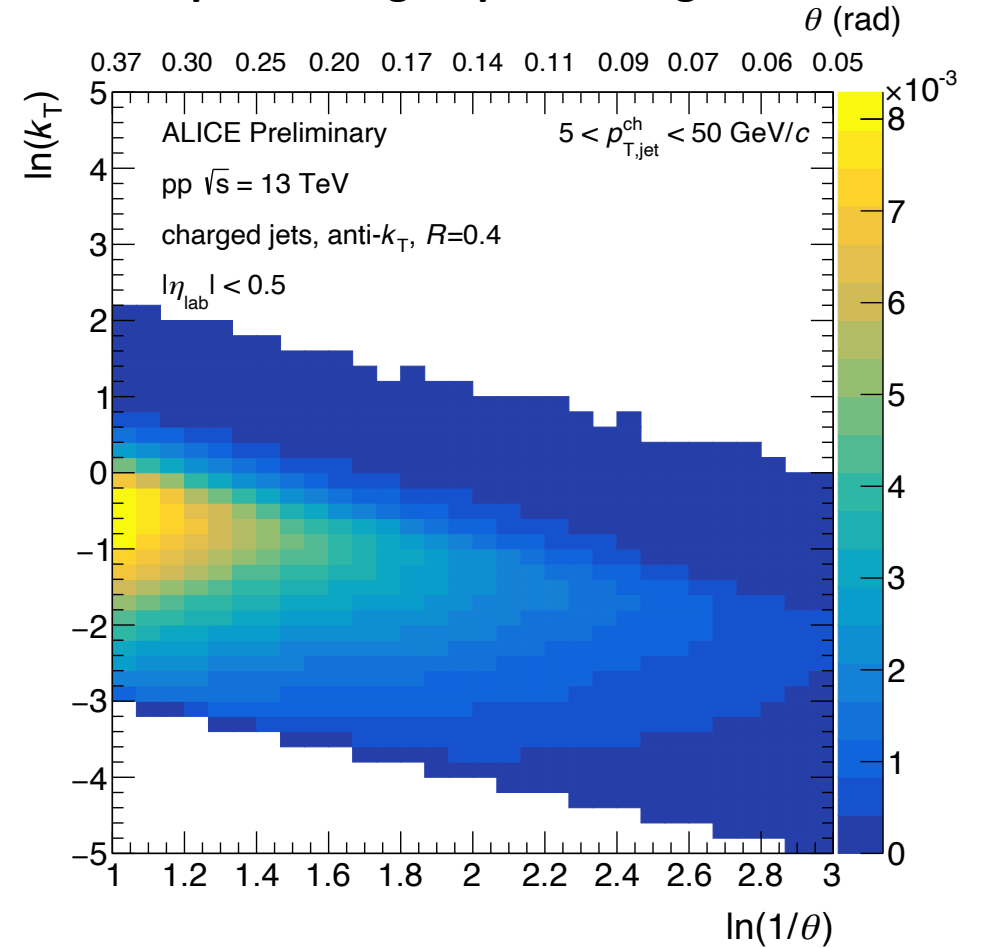




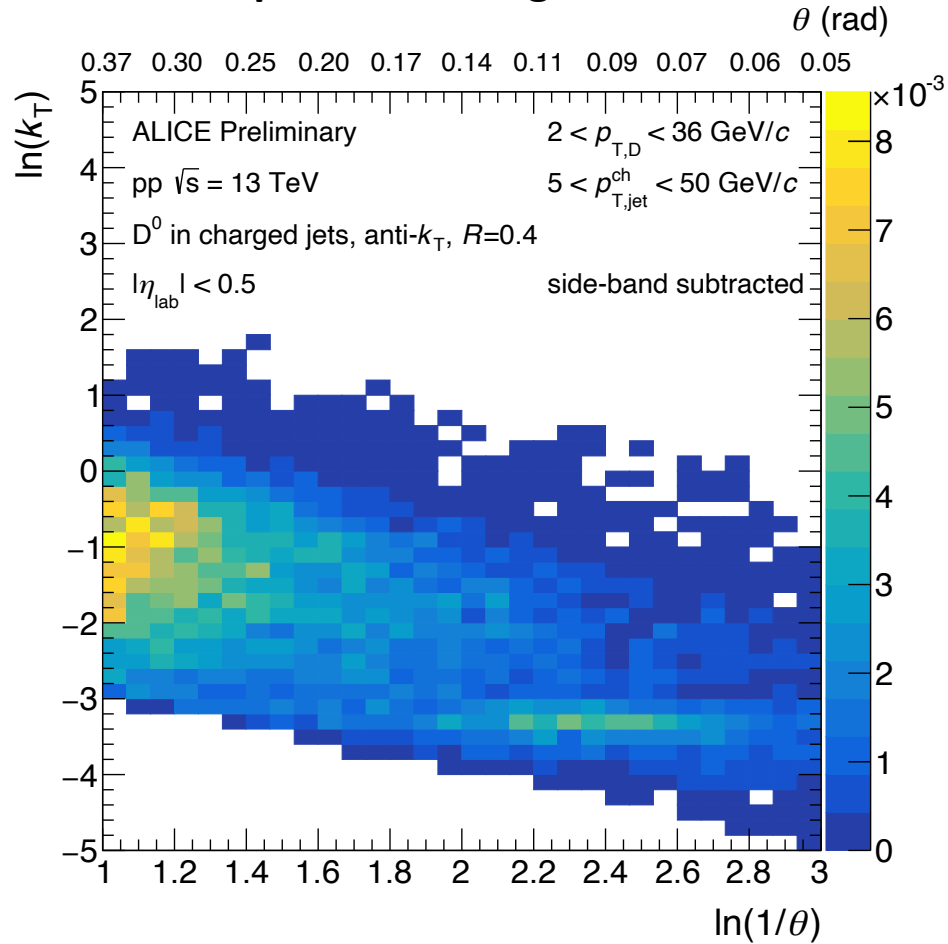
Lund plane of $c \rightarrow cg$ emissions



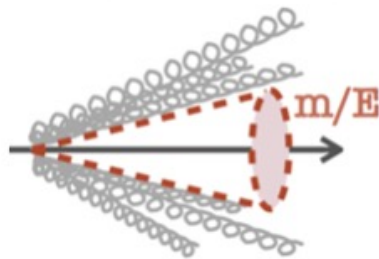
Lund plane of light quark and gluon emissions



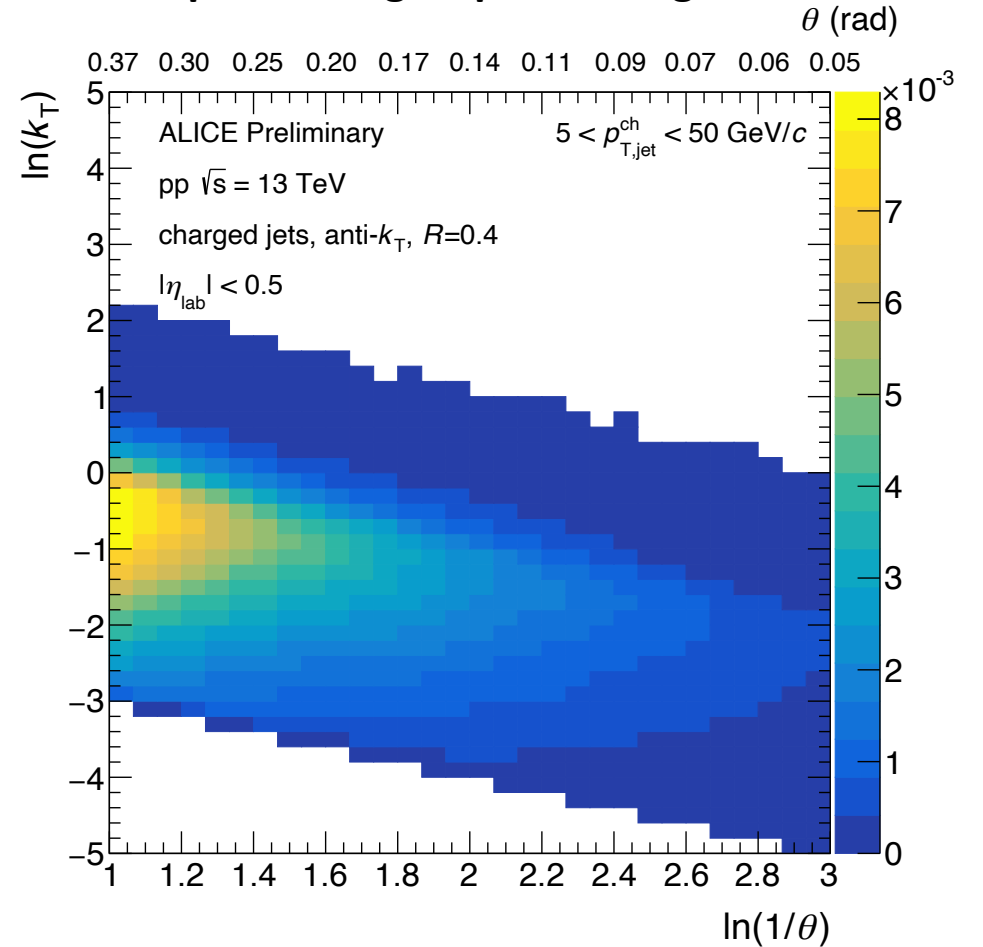
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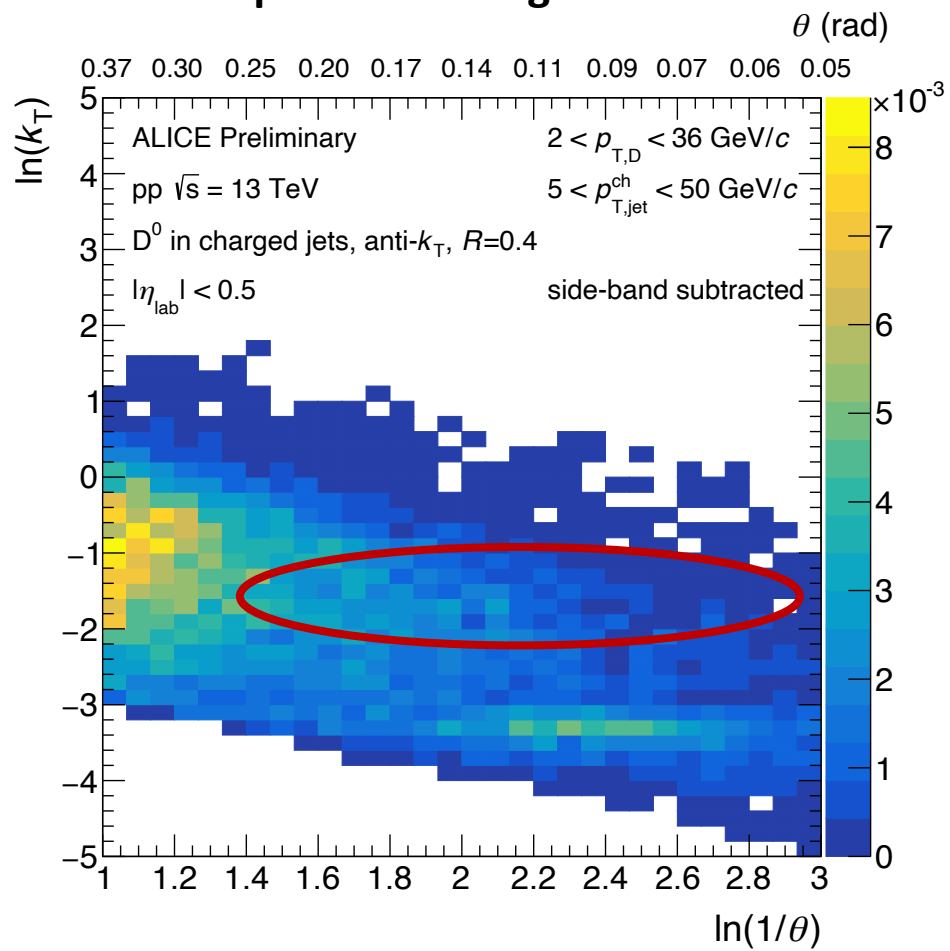
Are we sensitive to the dead-cone effect?



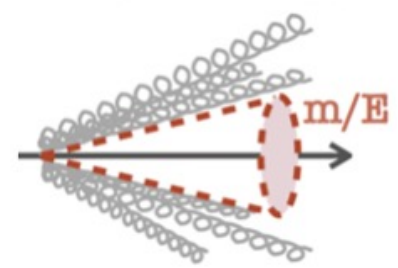
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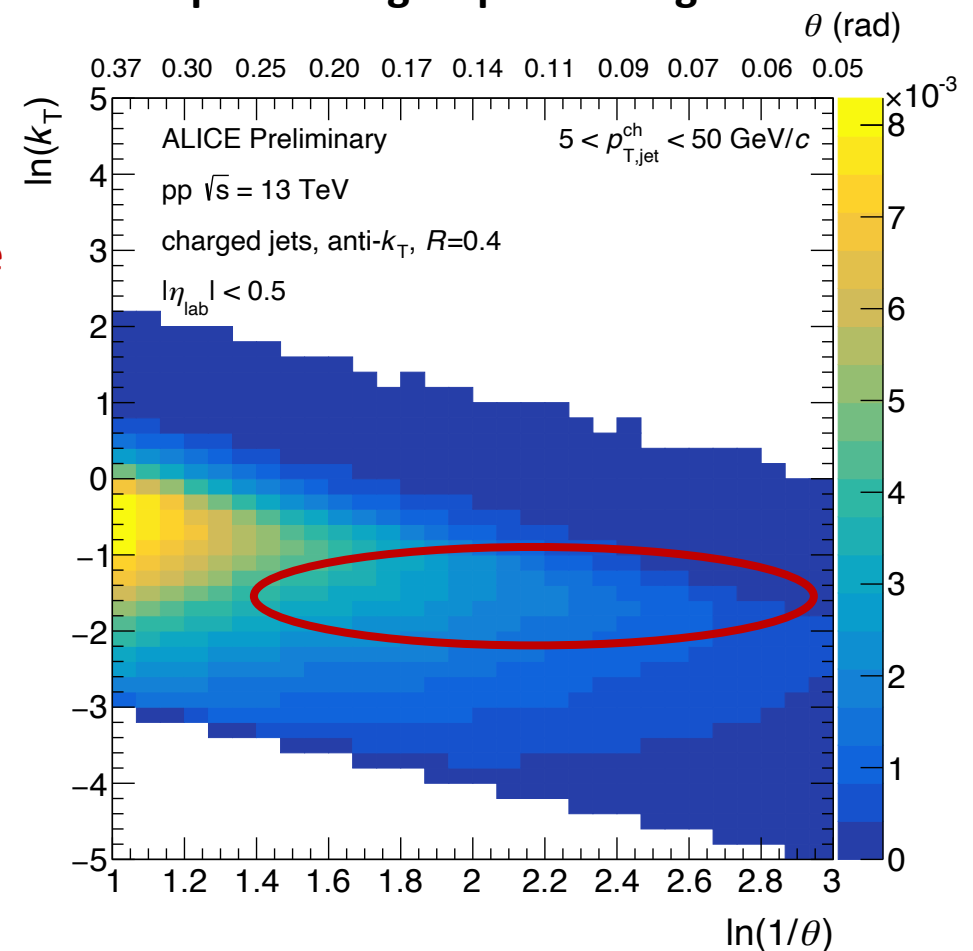
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Are we sensitive to the dead-cone effect?



Lund plane of light quark and gluon emissions



$$R(\theta) = \frac{1}{N^{\text{D}^0 \text{ jets}}} \frac{dn^{\text{D}^0 \text{ jets}}}{d\ln(1/\theta)} \bigg/ \frac{1}{N^{\text{inclusive jets}}} \frac{dn^{\text{inclusive jets}}}{d\ln(1/\theta)} \bigg|_{k_T, E_{\text{Radiator}}}$$

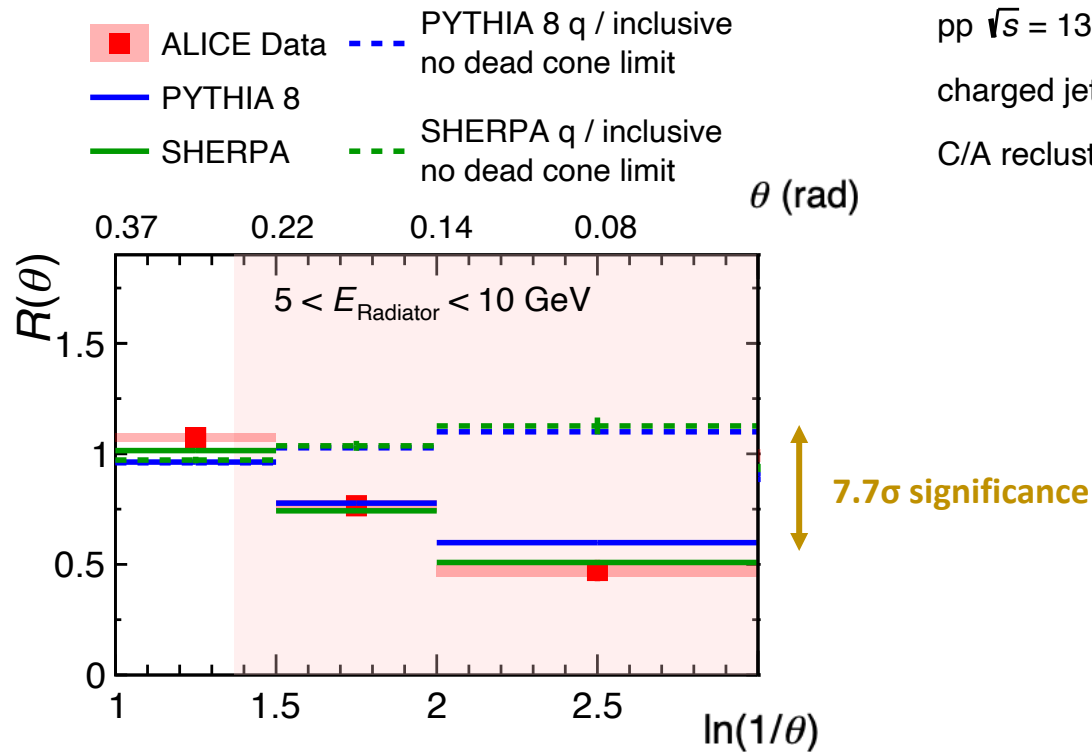
Compare the angular distribution of charm-quark emissions to those of light quarks and gluons

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Compare the angular distribution of charm-quark emissions to those of light quarks and gluons

Nature 605 (2022) 440-446

Observation of the QCD dead cone

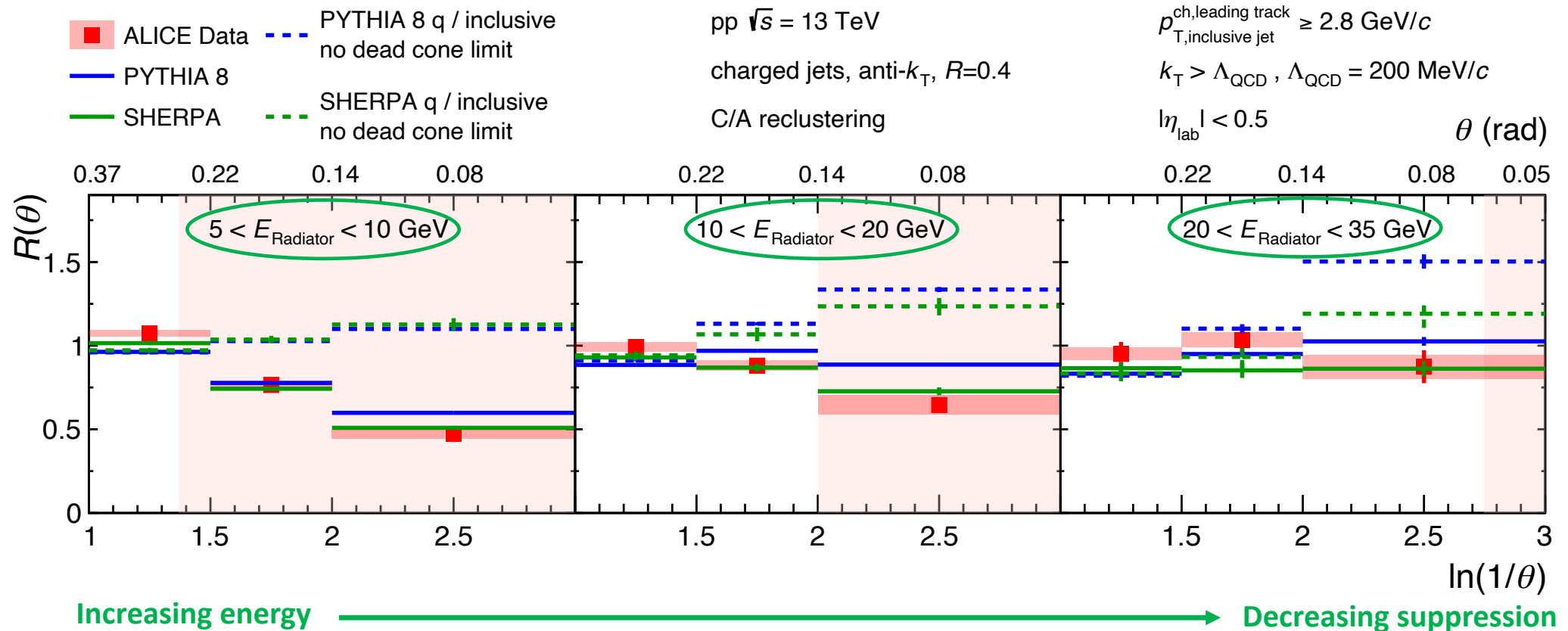


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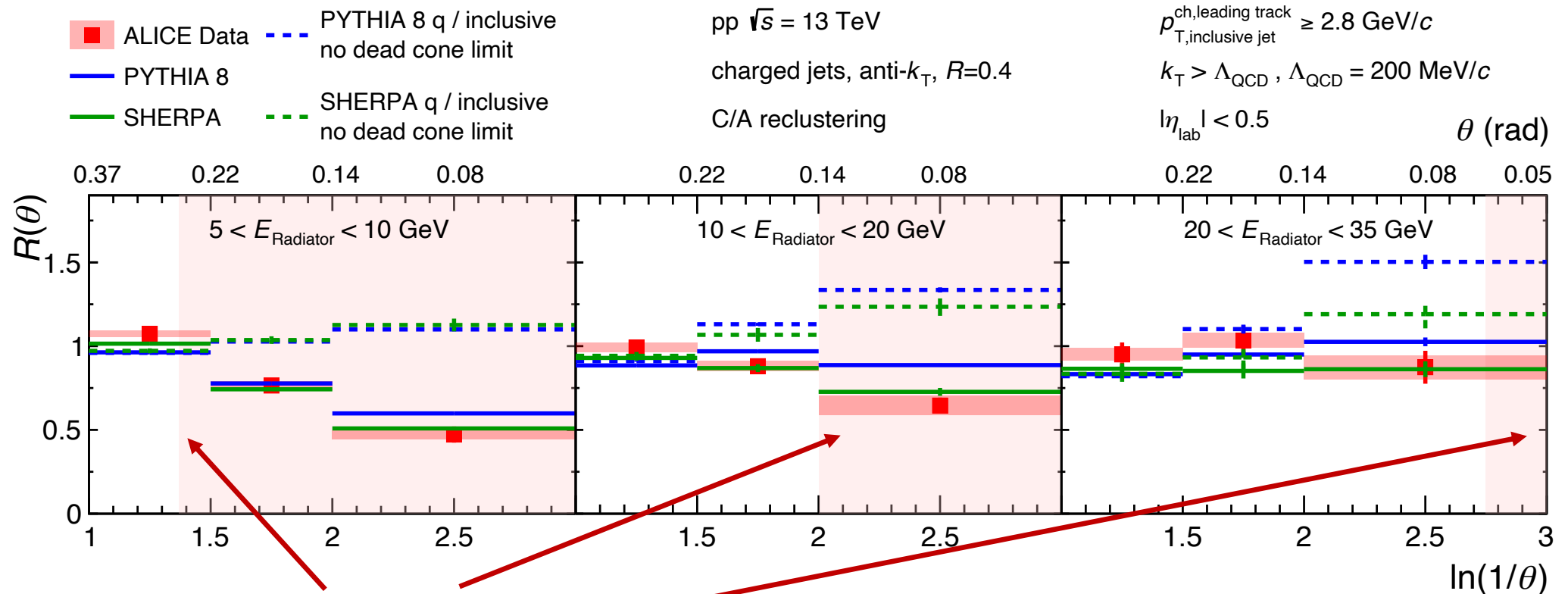


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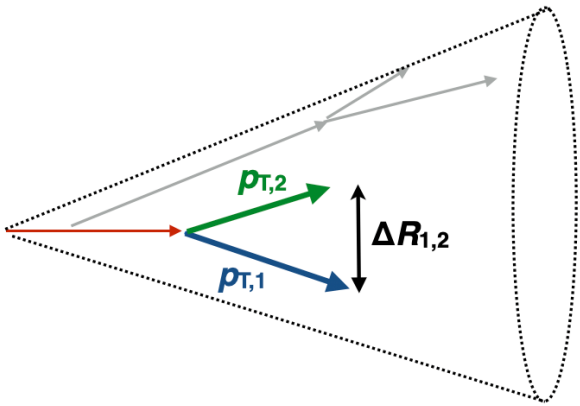
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Observation of the QCD dead cone



Shaded region corresponds to the dead-cone of a charm quark with a mass of 1.275 GeV/c

$$dP_{i \rightarrow jk} = \frac{d\theta}{\theta} dz P_{i \rightarrow jk}(z)$$



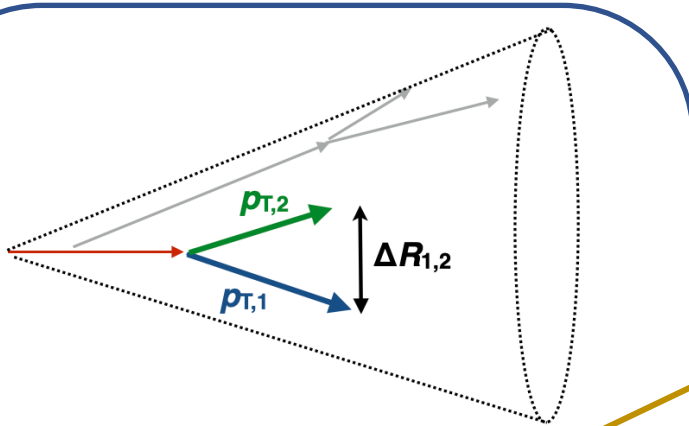
Soft Drop grooming condition

$$z = \frac{p_{T,2}}{p_{T,1} + p_{T,2}} > z_{\text{cut}} \left(\frac{\Delta R_{1,2}}{R} \right)^\beta$$

$$z = 0.1, \beta = 0$$

A. J. Larkoski et al. , JHEP 1405 (2014) 146

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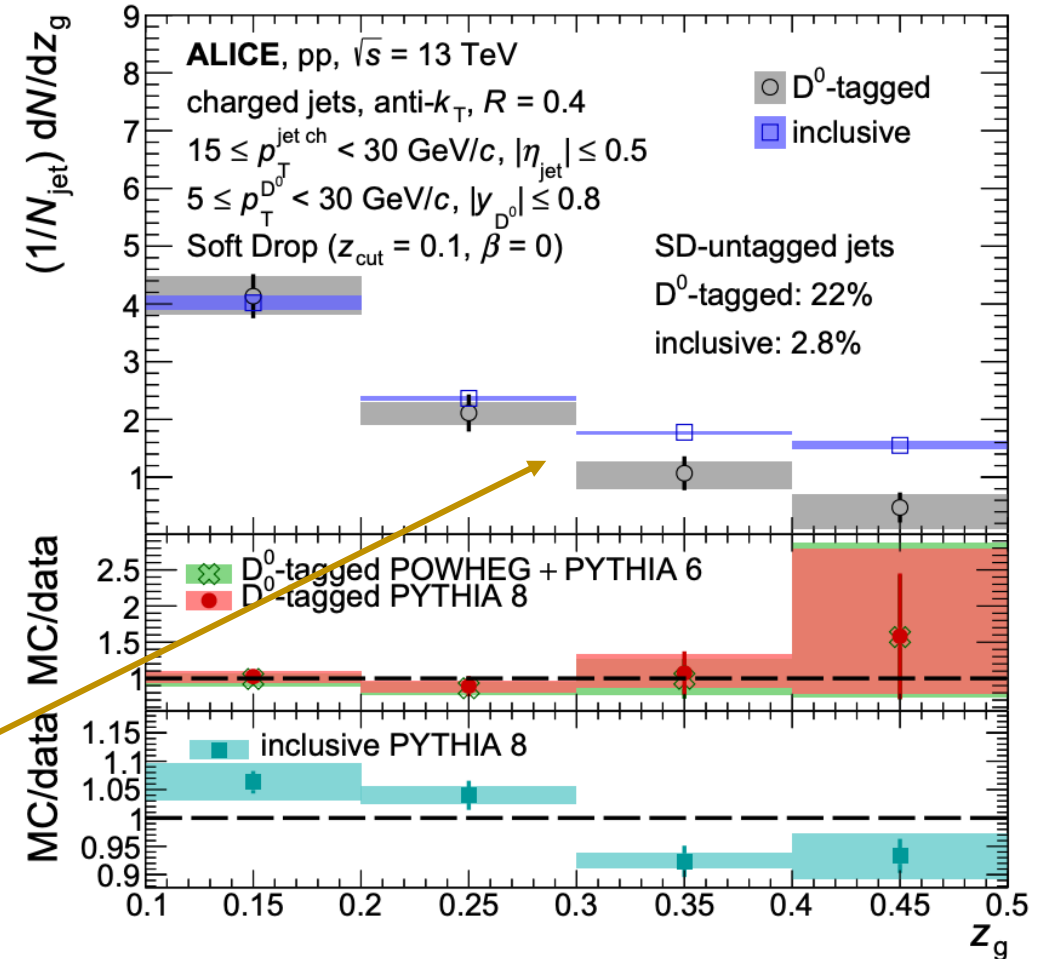
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A. J. Larkoski et al. , JHEP 1405 (2014) 146

Converges onto the QCD splitting function for the first splitting that passes Soft Drop

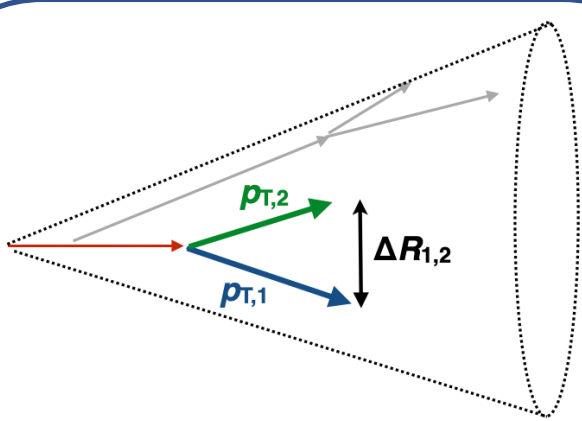
Emissions from charm-quarks have a steeper splitting probability than light quarks and gluons

Fewer symmetric splittings



PRL 131.192301

$$dP_{i \rightarrow jk} = \frac{d\theta}{\theta} dz P_{i \rightarrow jk}(z)$$



Soft Drop grooming condition

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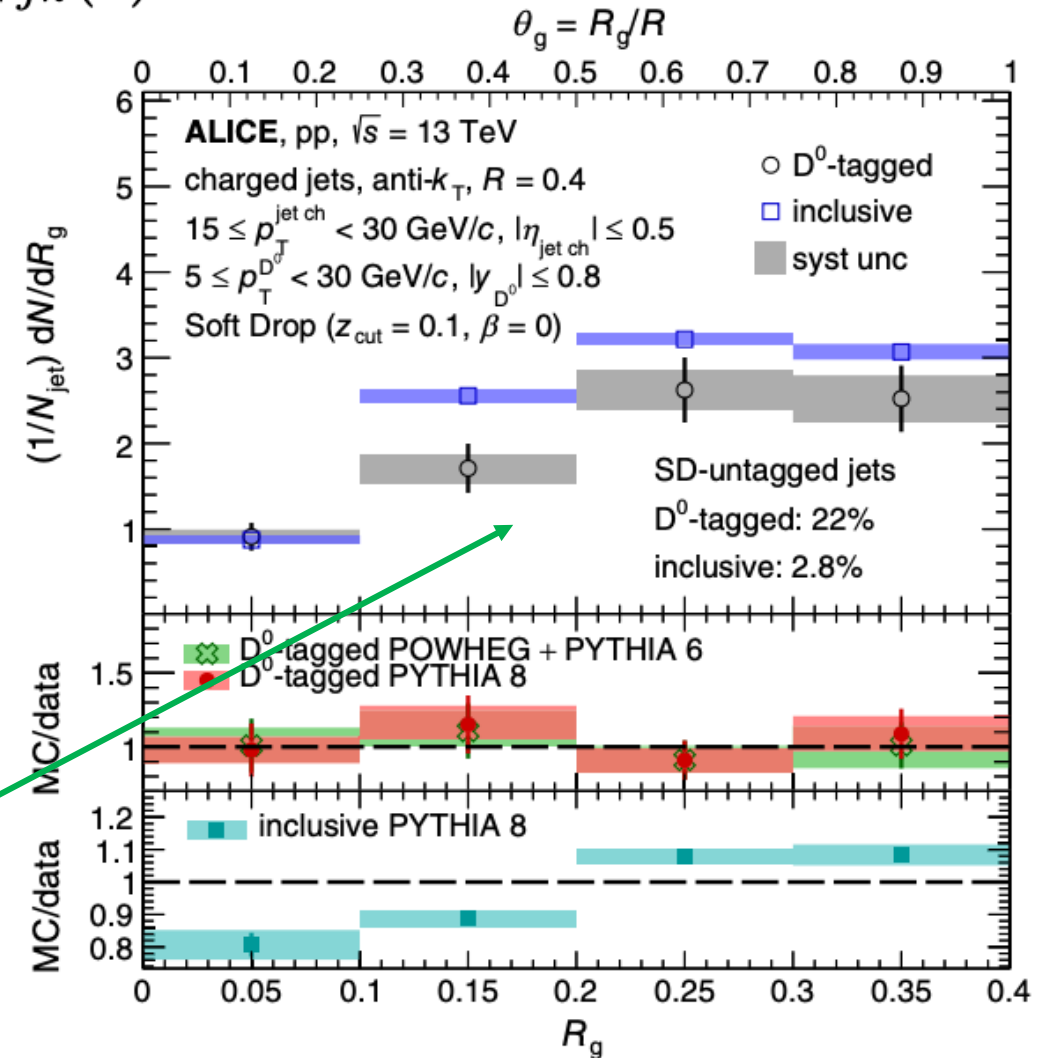
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A. J. Larkoski et al. , JHEP 1405 (2014) 146

Opening angle of the first emission passing Soft Drop

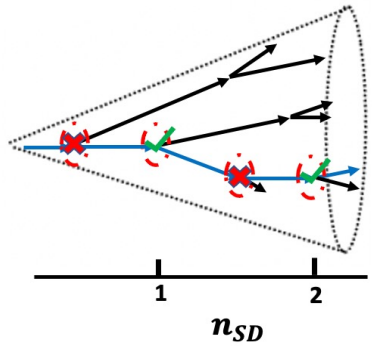
Gluon jets have a broader shower profile than quark jets

Competing effects between the dead cone and the increased quark emissions at small angles



PRL 131.192301

Towards isolating the perturbative physics of heavy-flavour fragmentation functions



- ✗ Emission is groomed away
- ✓ Emission satisfies Soft Drop

Soft Drop grooming condition

$$z = \frac{p_{T,2}}{p_{T,1} + p_{T,2}} > z_{\text{cut}} \left(\frac{\Delta R_{1,2}}{R} \right)^\beta$$

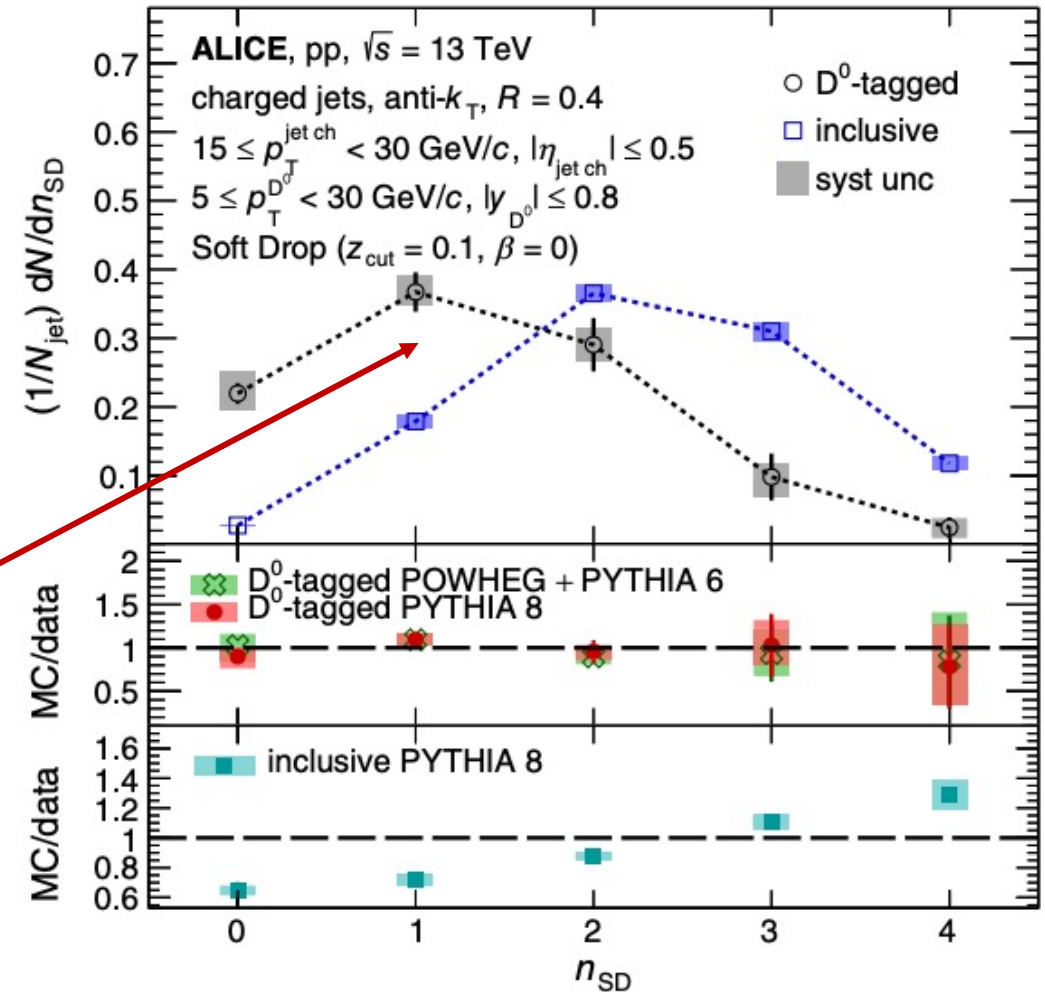
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A. J. Larkoski et al. , JHEP 1405 (2014) 146

Strongly correlated to the number of perturbative emissions in the shower

Charm quarks on average have fewer hard emissions

Hardening of the fragmentation function from the dead-cone



PRL 131.192301

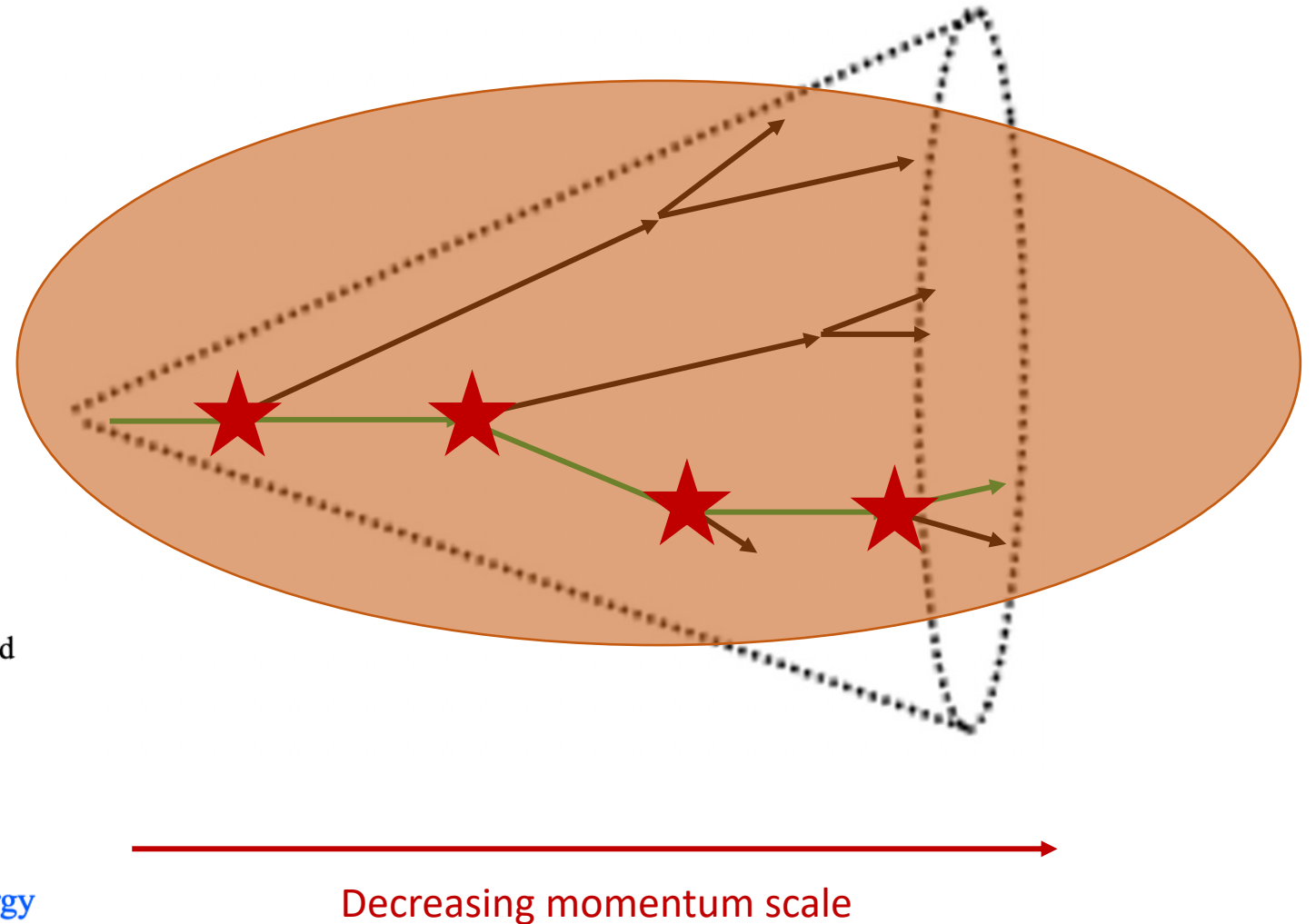
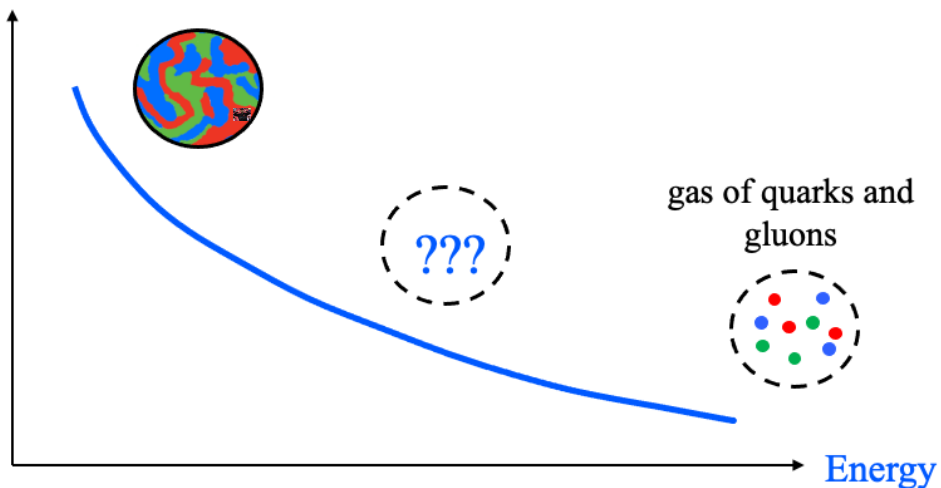
Allows to access QCD at all momentum scales whilst starting with a perturbatively well controlled object

In the presence of the medium it allows us to probe the scale dependent features of the medium

State of the art

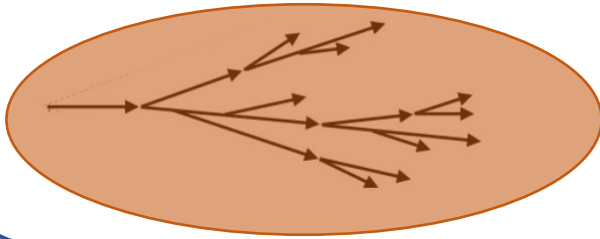
most strongly-coupled liquid ever observed

QCD coupling



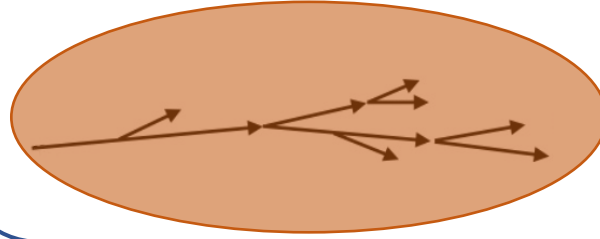
Gluon-initiated shower

Broader shower profile
Higher number of emissions



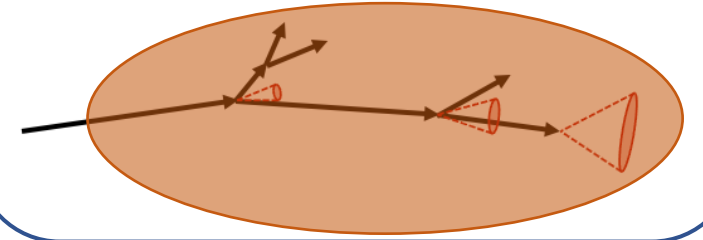
Quark-initiated shower

narrower shower profile
Fewer emissions in the shower



Heavy-quark-initiated shower

Suppression of small angle emissions
Harder fragmentation



Casimir Colour factors

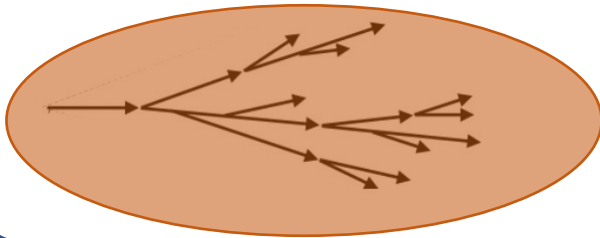
The medium couples differently
to quarks and gluons

The dead-cone effect

How does the dead-cone interplay
with medium emissions?

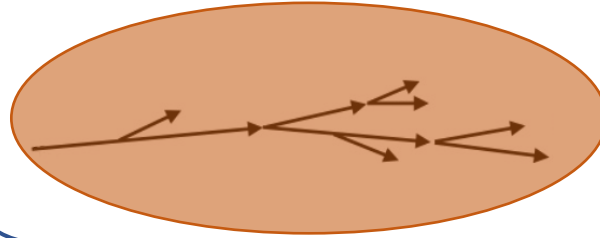
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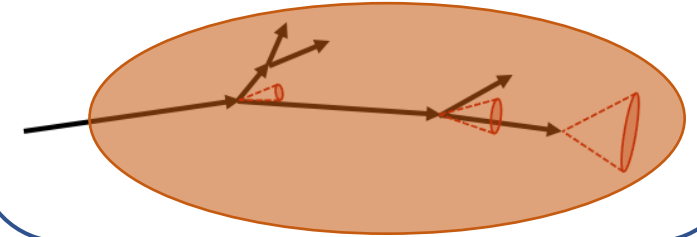
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Casimir Colour factors

The medium couples differently to quarks and gluons

Theoretical frameworks describe medium interactions as a modification of individual splittings

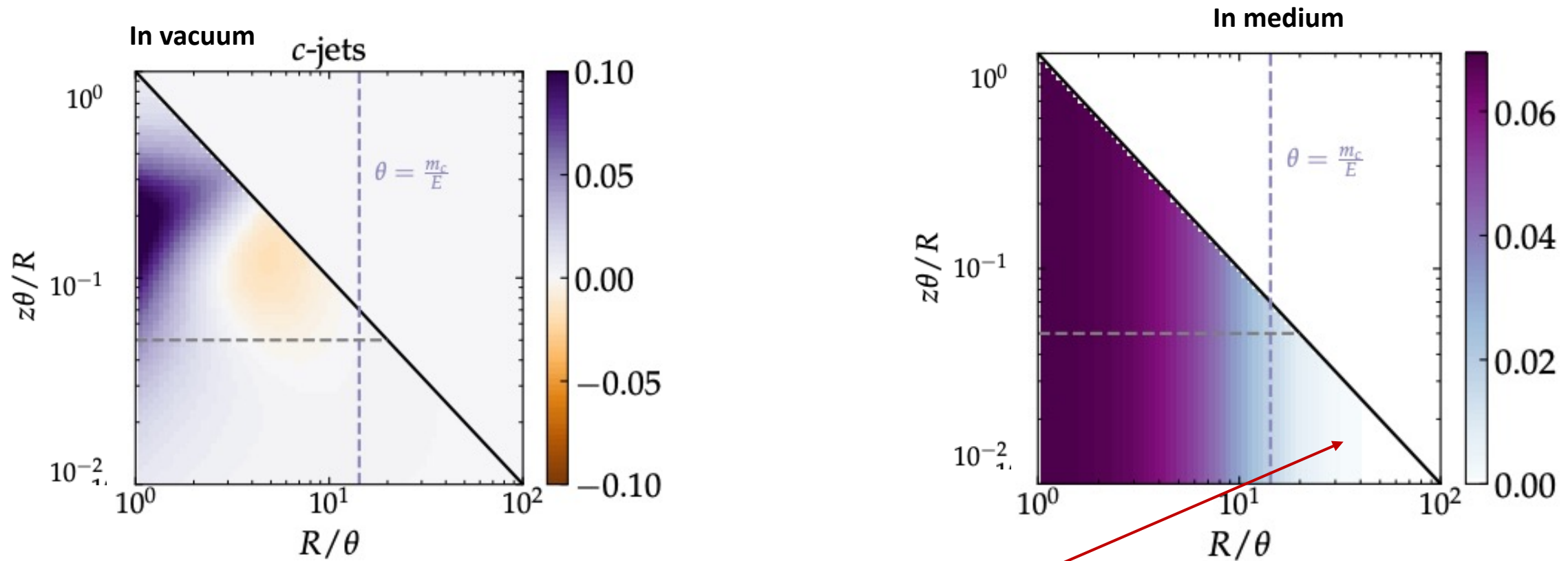
$$P_{splitting}(z, \theta) = P_{vacuum}(z, \theta) + P_{medium}(z, \theta, E)$$

The dead-cone effect

How does the dead-cone interplay with medium emissions?

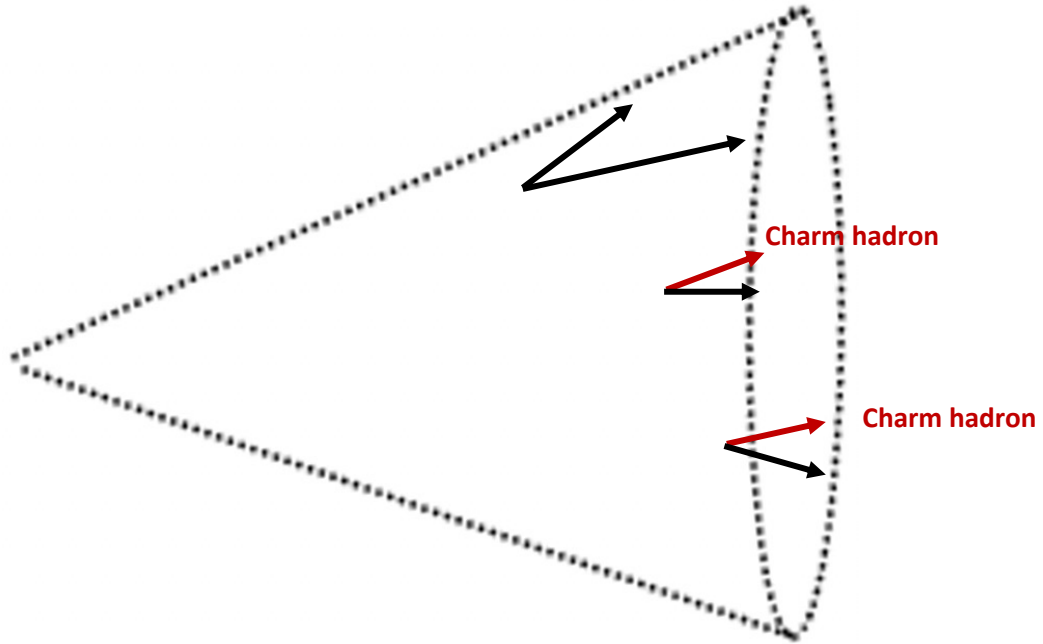
Different splitting flavours at the same scale will be modified differently by the same medium

The fractions of splitting flavours are not known after quenching



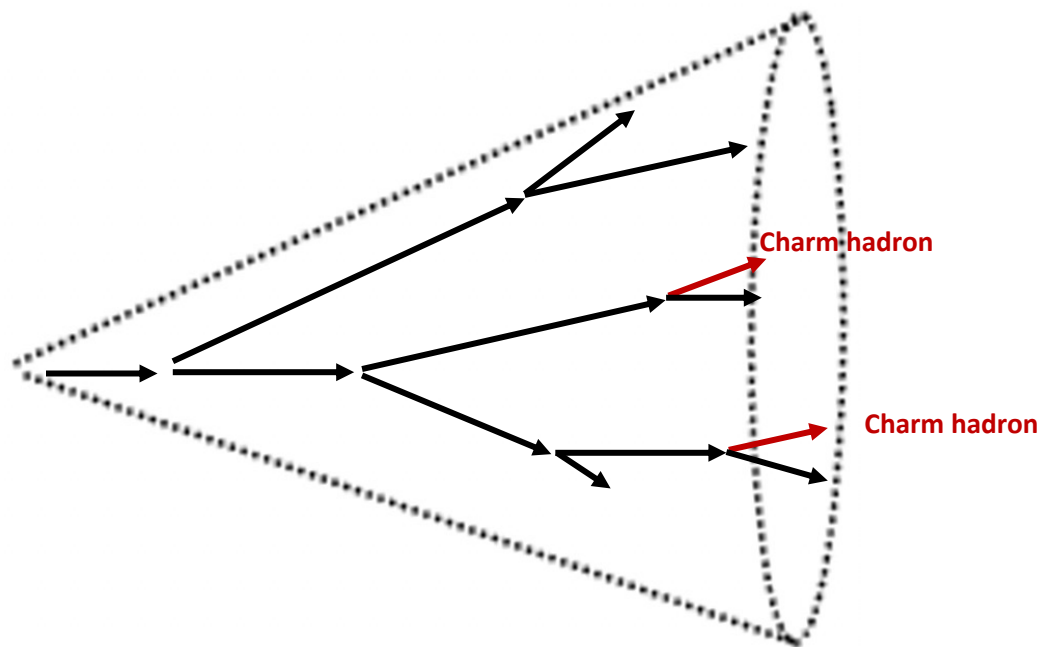
How do medium induced emissions interplay with the dead-cone region?
 Opportunity to isolate medium emissions?

Splittings deep in the shower are less sensitive to background effects



Methodology

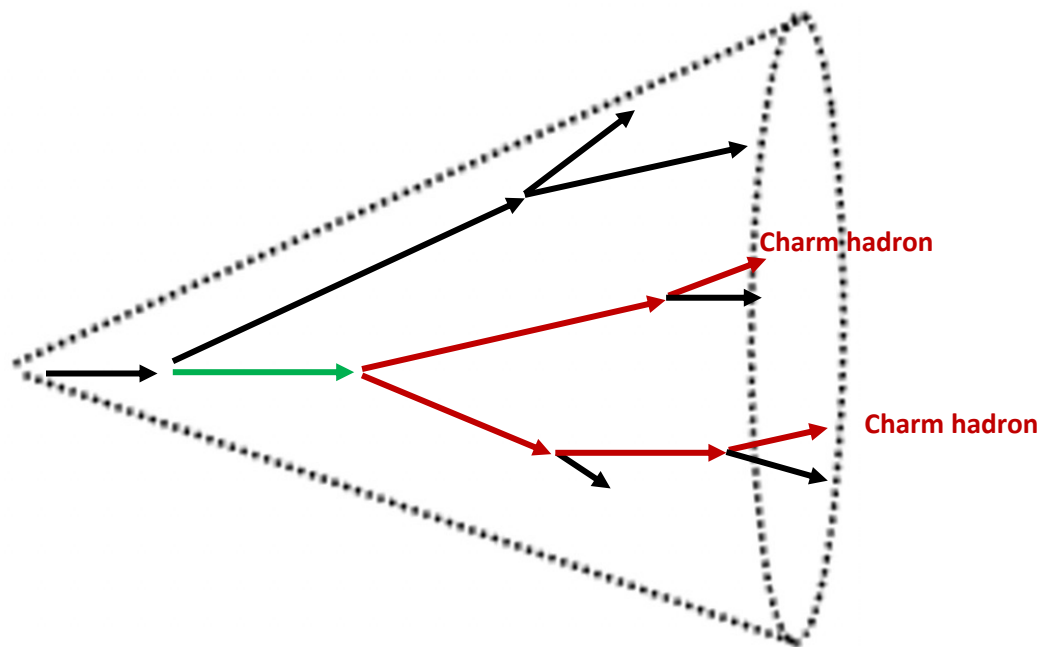
A jet containing two heavy-flavour hadrons is tagged



Methodology

A jet containing two heavy-flavour hadrons is tagged

Recluster the jet to access the splitting tree

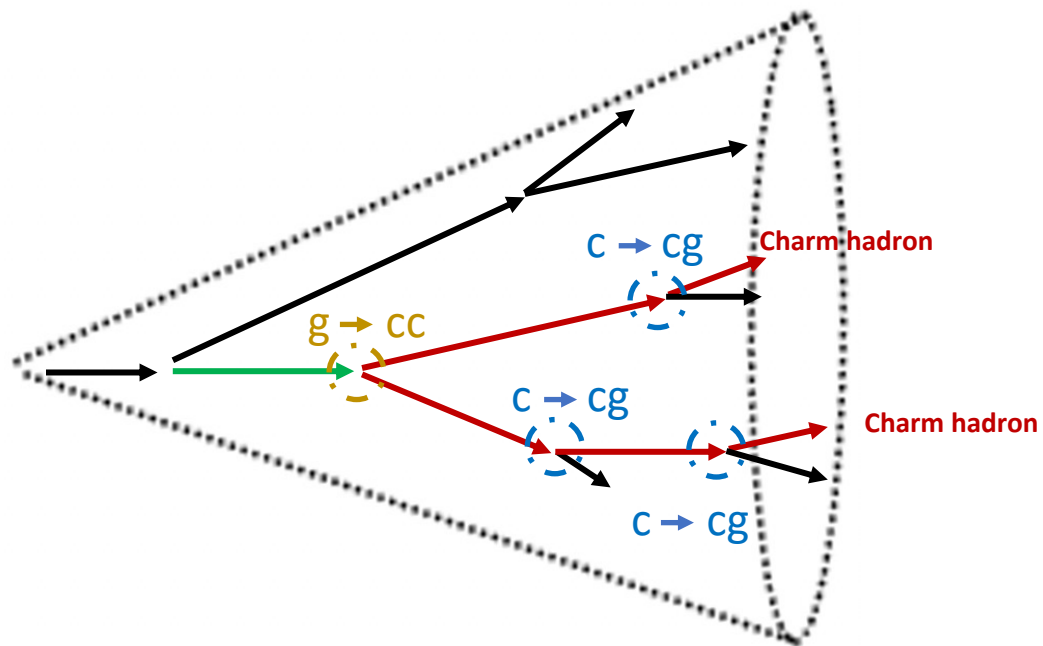


Methodology

A jet containing two heavy-flavour hadrons is tagged

Recluster the jet to access the splitting tree

Trace the heavy-flavour hadrons until the deepest splitting containing both is found

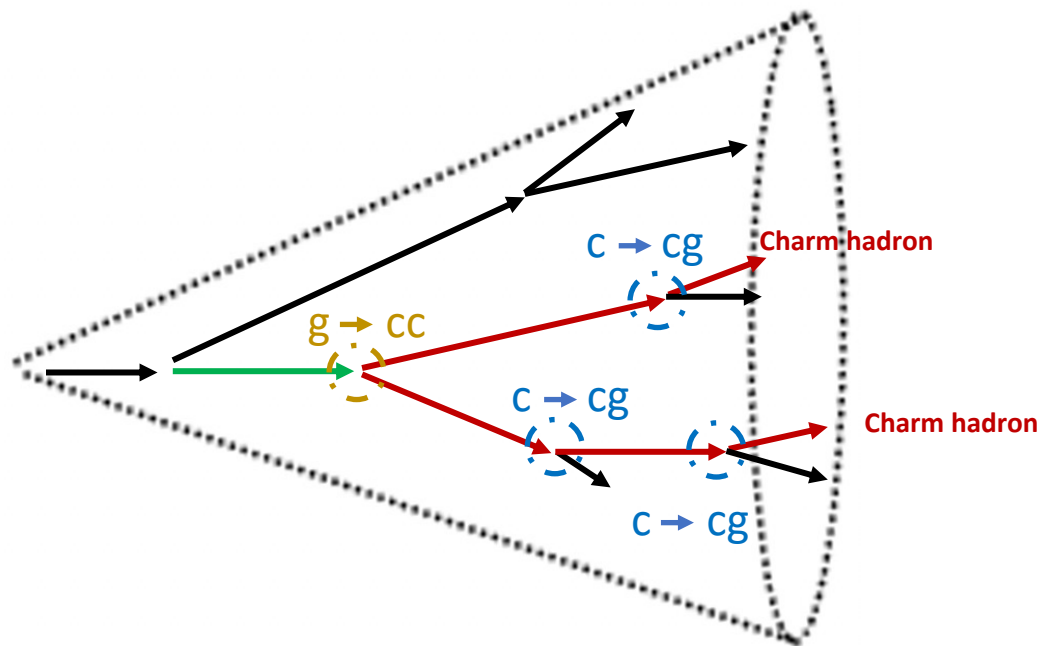


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Attems et al. , JHEP 01(2023)080
 Attems et al. , arXiv: 2209.13600

Methodology

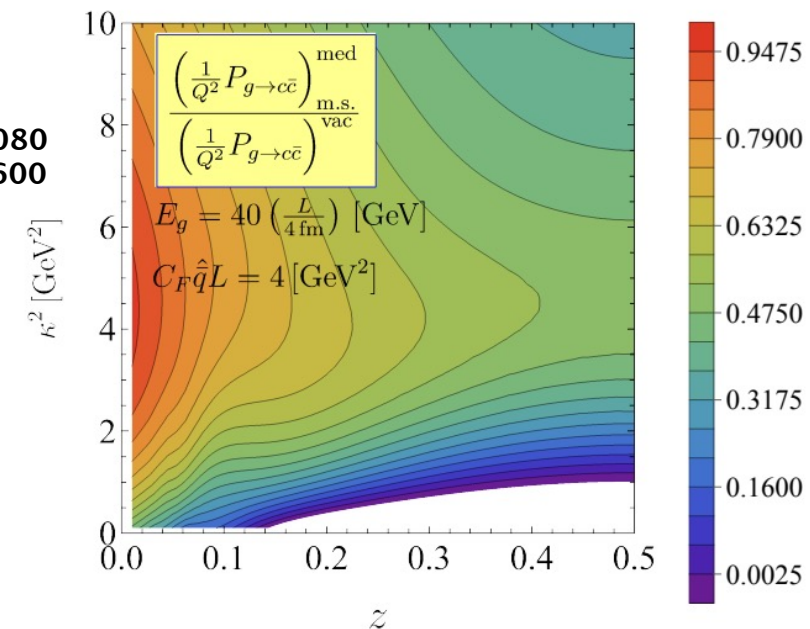
A jet containing two heavy-flavour hadrons is tagged

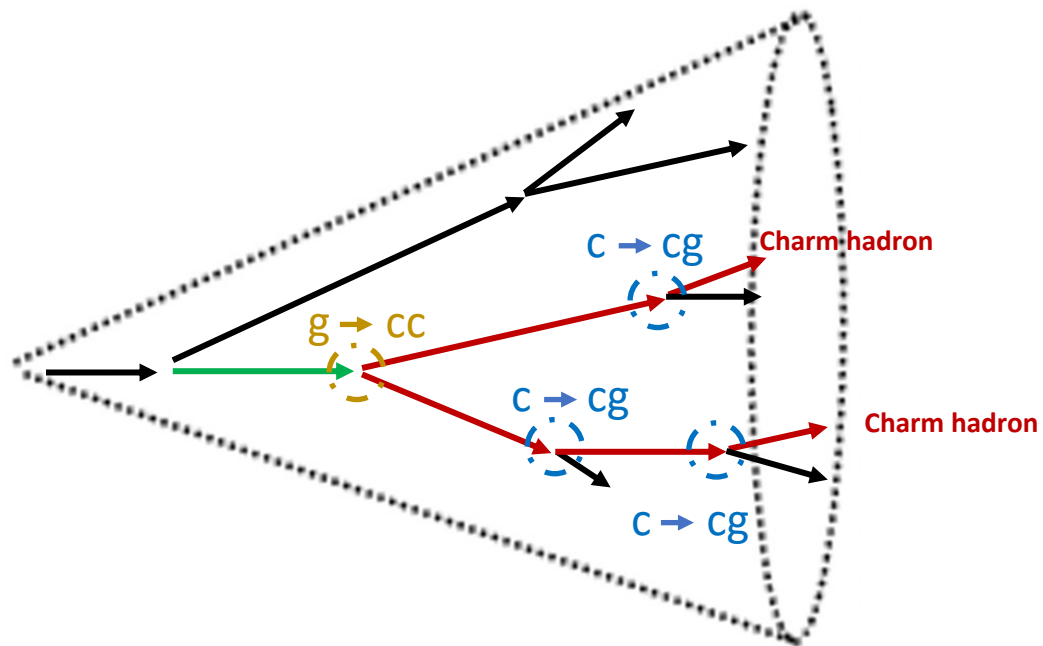
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Controlled access to features of the $g \rightarrow QQ$ splitting

Next step of precision in accessing medium modification of splittings



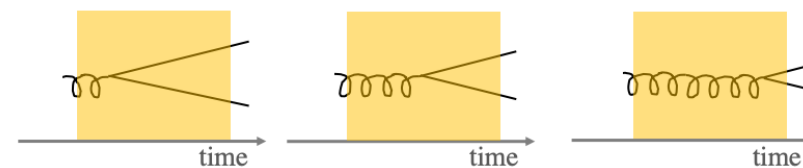


Methodology

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Increasing gluon energy

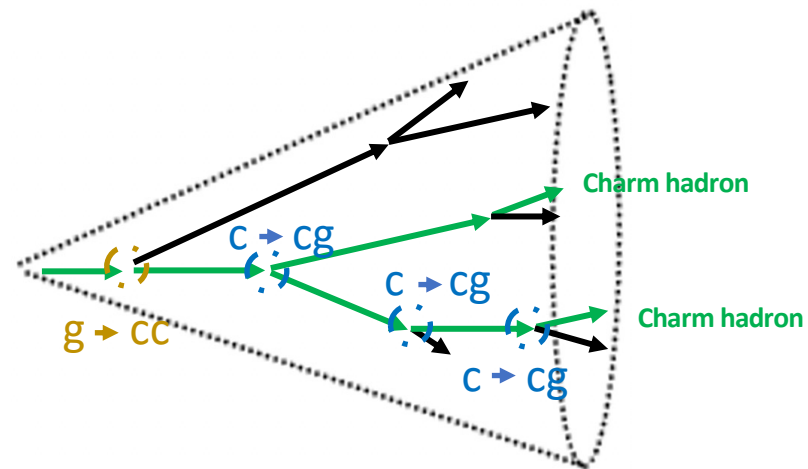
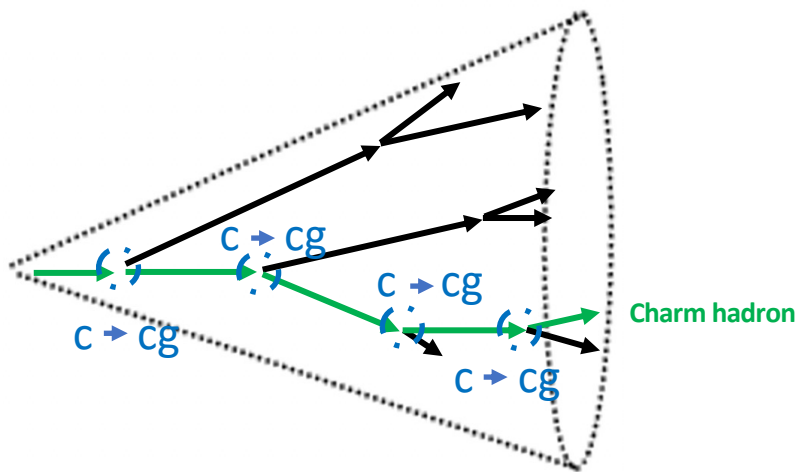
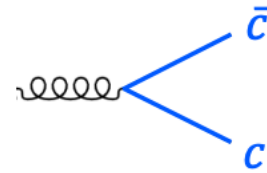
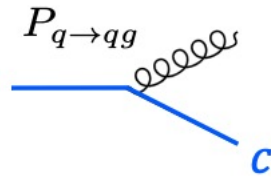
Attems et al. , arXiv: 2209.13600

Controlled access to features of the $g \rightarrow QQ$ splitting

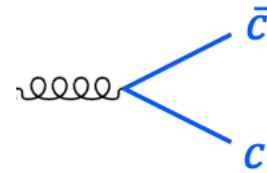
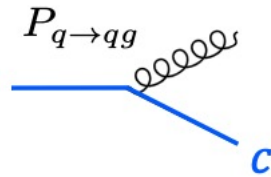
Next step of precision in accessing medium modification of splittings

Can access features of the shower in a time and space dependent way

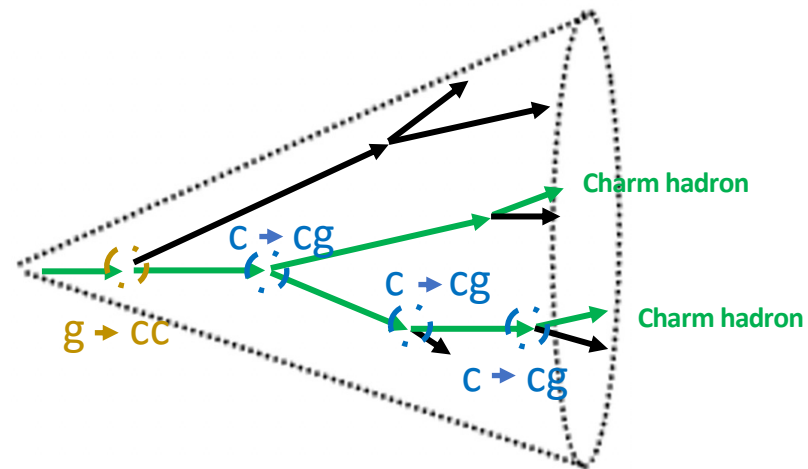
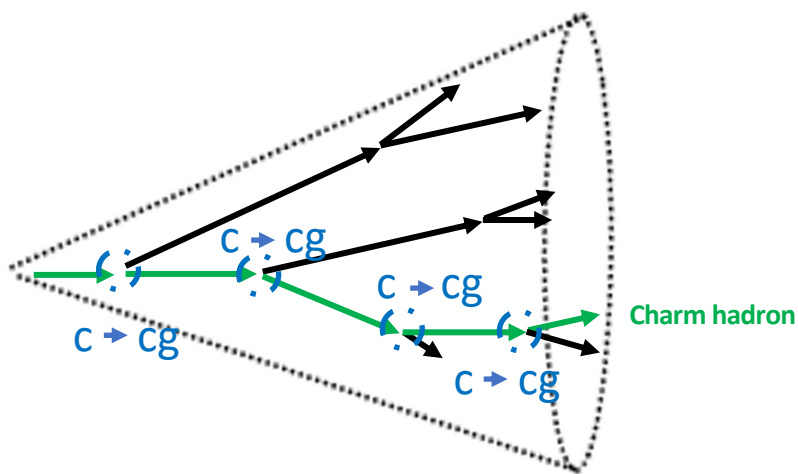
Using heavy-flavour tracing to access quark-initiated splittings



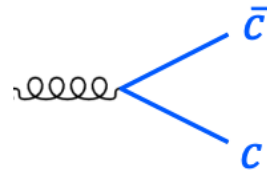
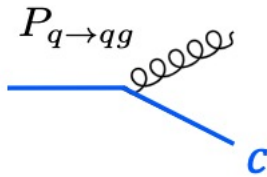
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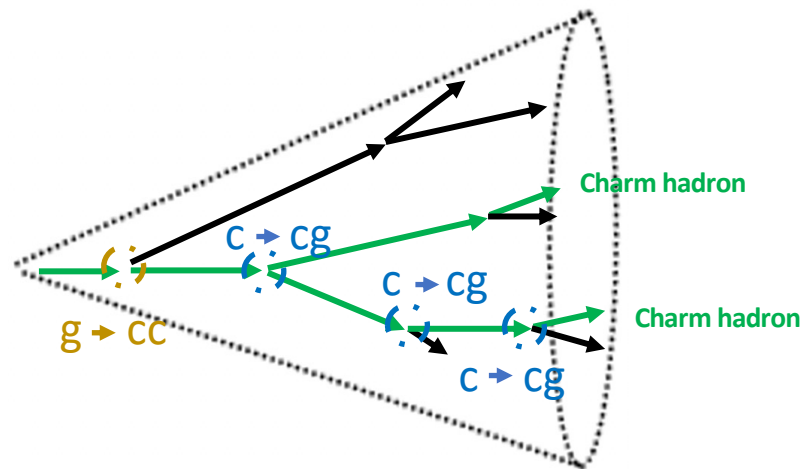
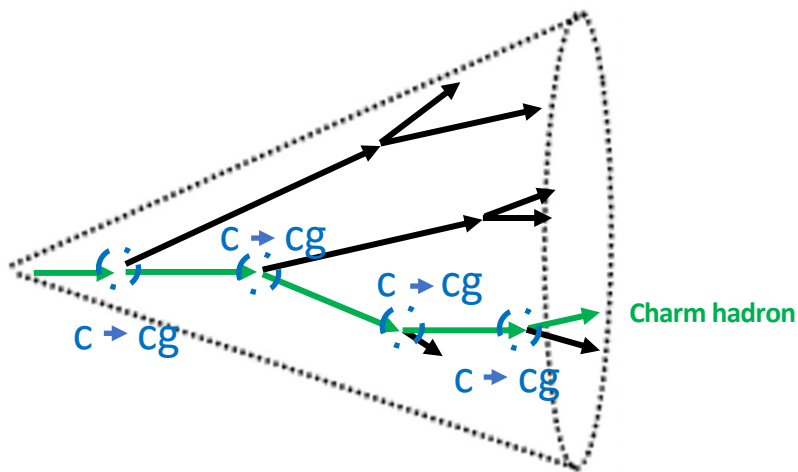
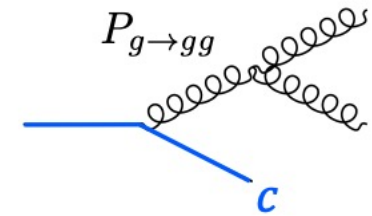
What about the remaining QCD splitting?



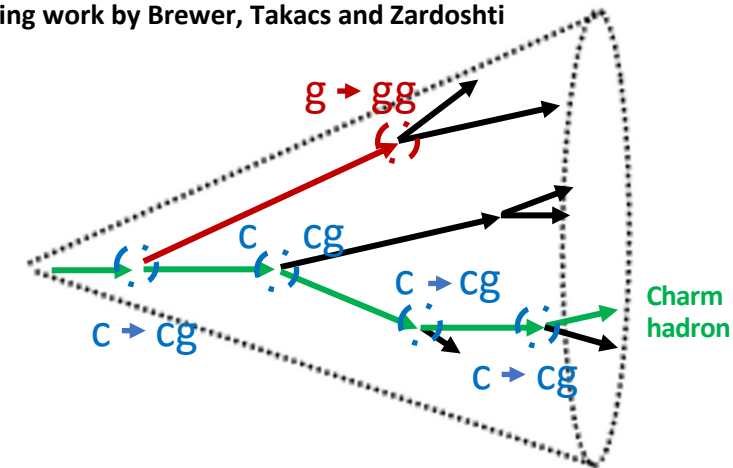
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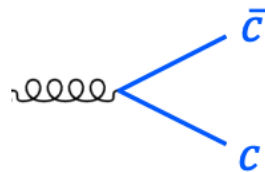
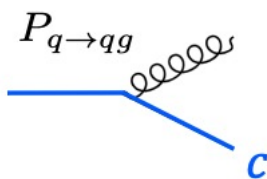
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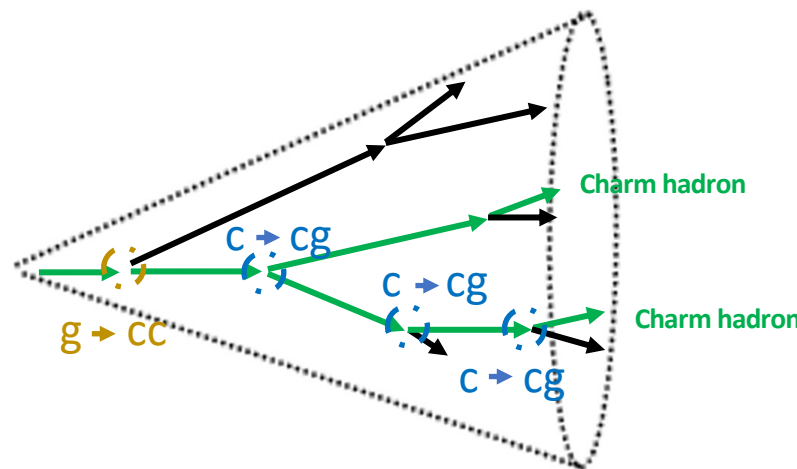
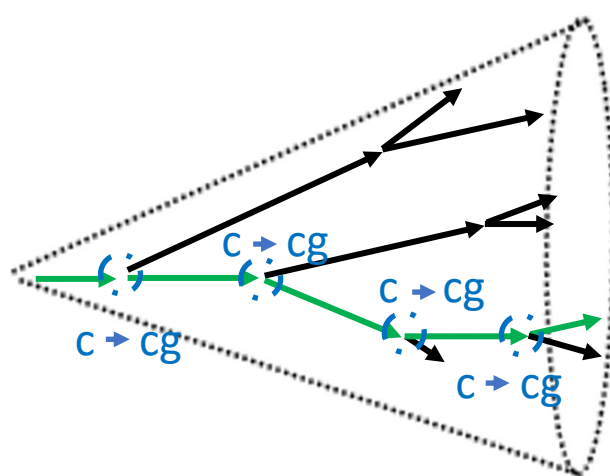
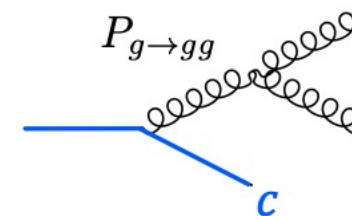
Ongoing work by Brewer, Takacs and Zardoshti



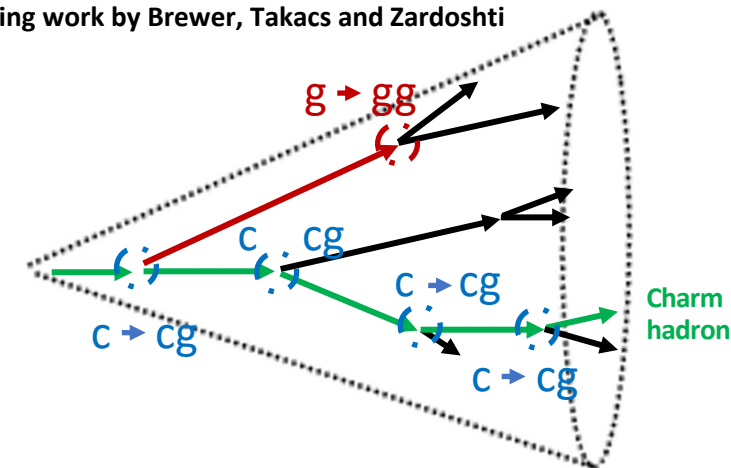
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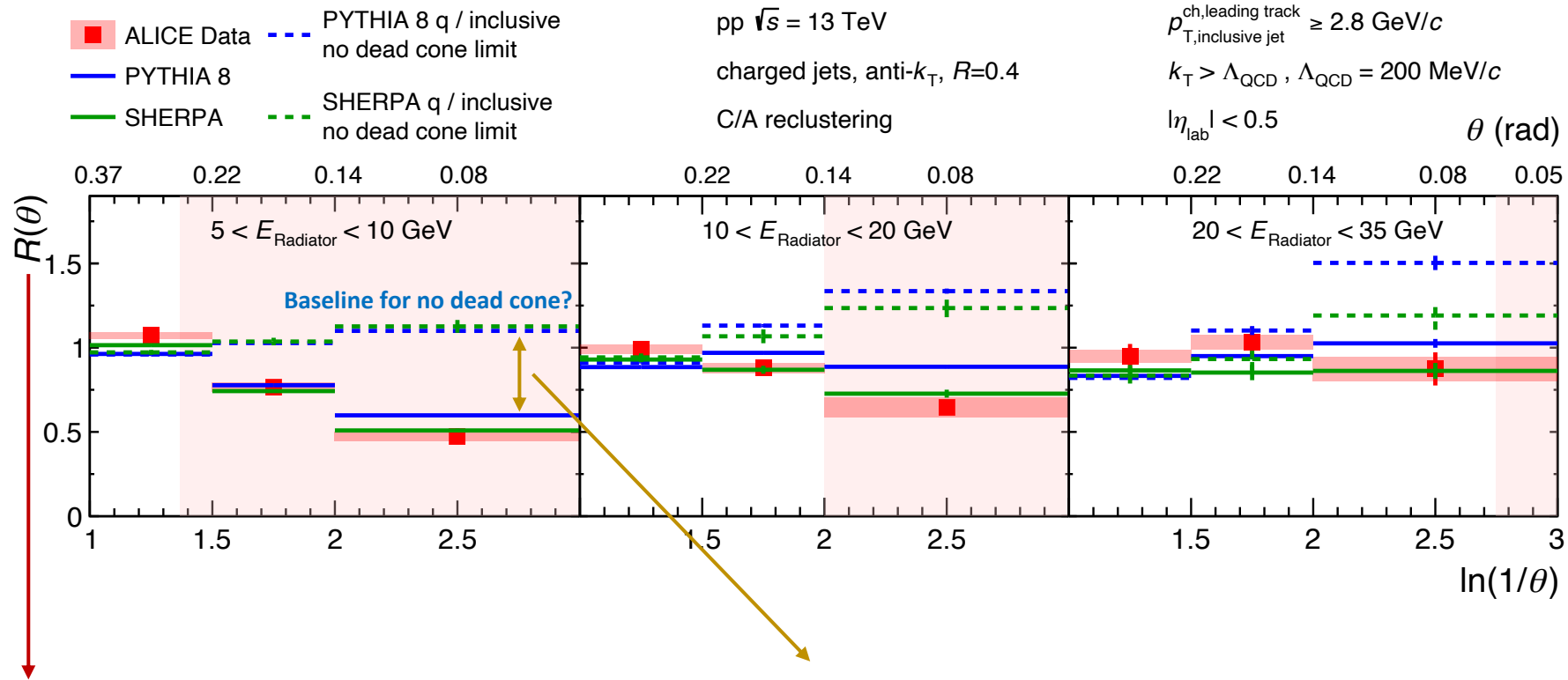
Ongoing work by Brewer, Takacs and Zardoshti



Heavy-flavour tracing tests our ability to calculate secondary splitting dynamics and beyond with control over all splitting flavours along the chain

Important in both pp and HI collisions

Observation of the QCD dead cone



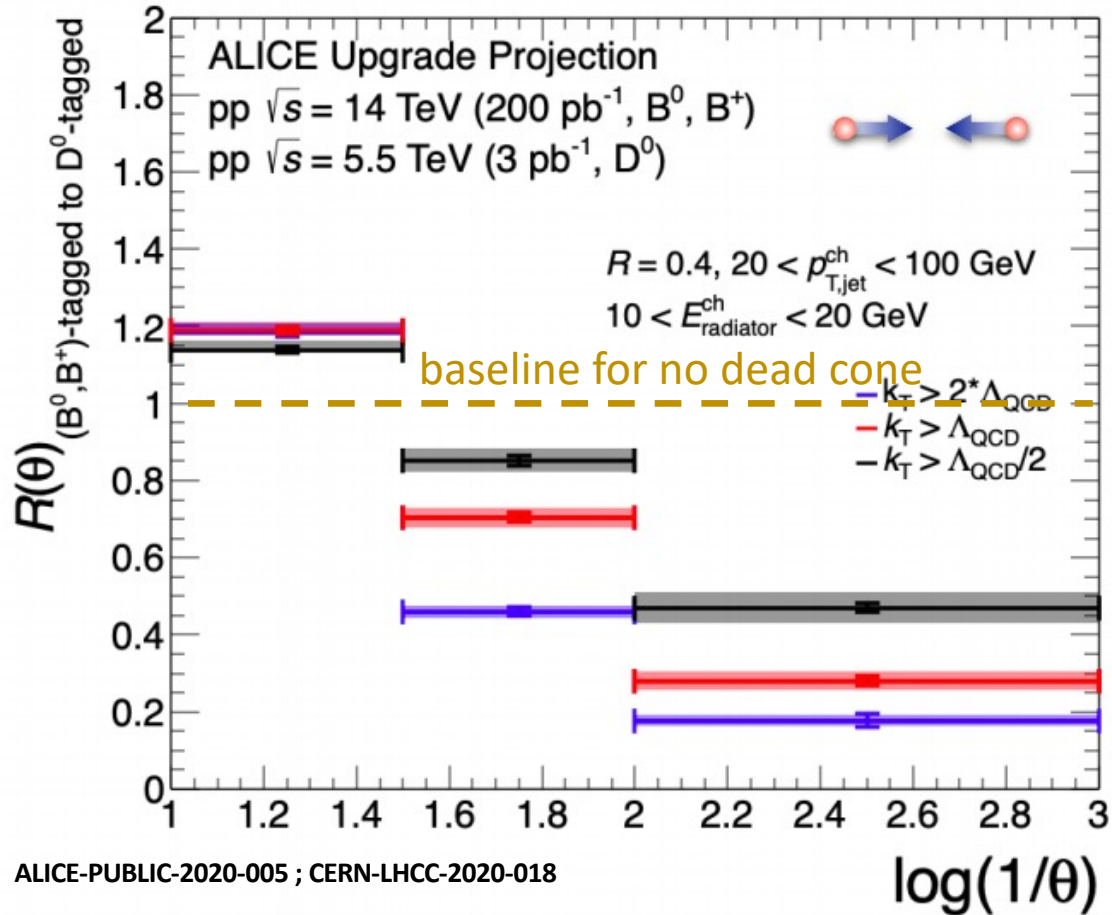
angular distribution of charm emissions

Sensitive to both Casimir colour factors and mass effects

angular distribution of gluon + light quark emissions

How can we separate flavour effects?

Dead cone of B^+ - tagged jets
 Dead cone of D^0 - tagged jets



ALICE-PUBLIC-2020-005 ; CERN-LHCC-2020-018

Run 3 projection from ALICE

Accessing Mass Effects

Jets tagged with a charm or beauty hadron represent a sample of enhanced quark jets

Comparison of $b \rightarrow bg$ and $c \rightarrow cg$ emissions is only sensitive to mass effects

Accessing Casimir Effects

At high energies mass effects die out

Comparison of $Q \rightarrow Qg$ and inclusive emissions are only sensitive to Casimir colour effects at high p_T

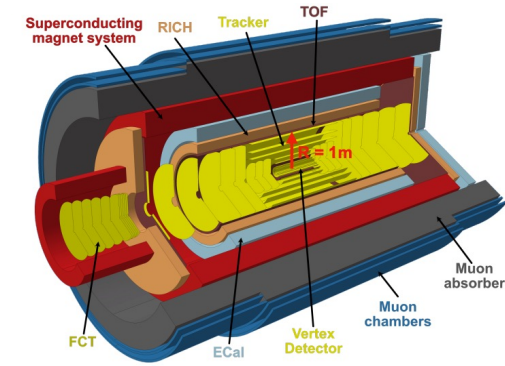
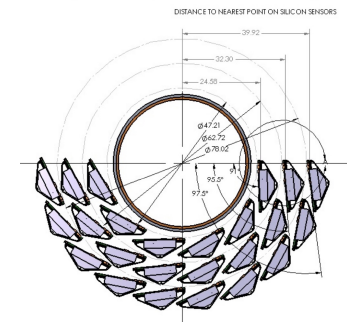
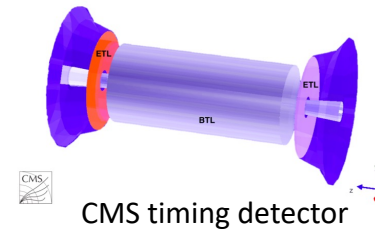
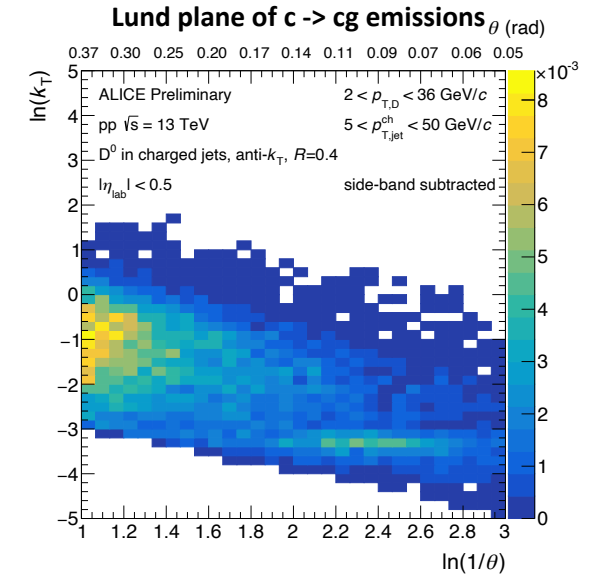
Heavy-flavour tracing is a powerful tool to take the next step in precision understanding of parton showers

Heavy-flavour tracing can provide access to all three types of QCD splittings in pp and HI collisions

Full control over the flavour dynamics is necessary to connect experiment and theory in pp and HI collisions

Many challenges accompanied by many opportunities

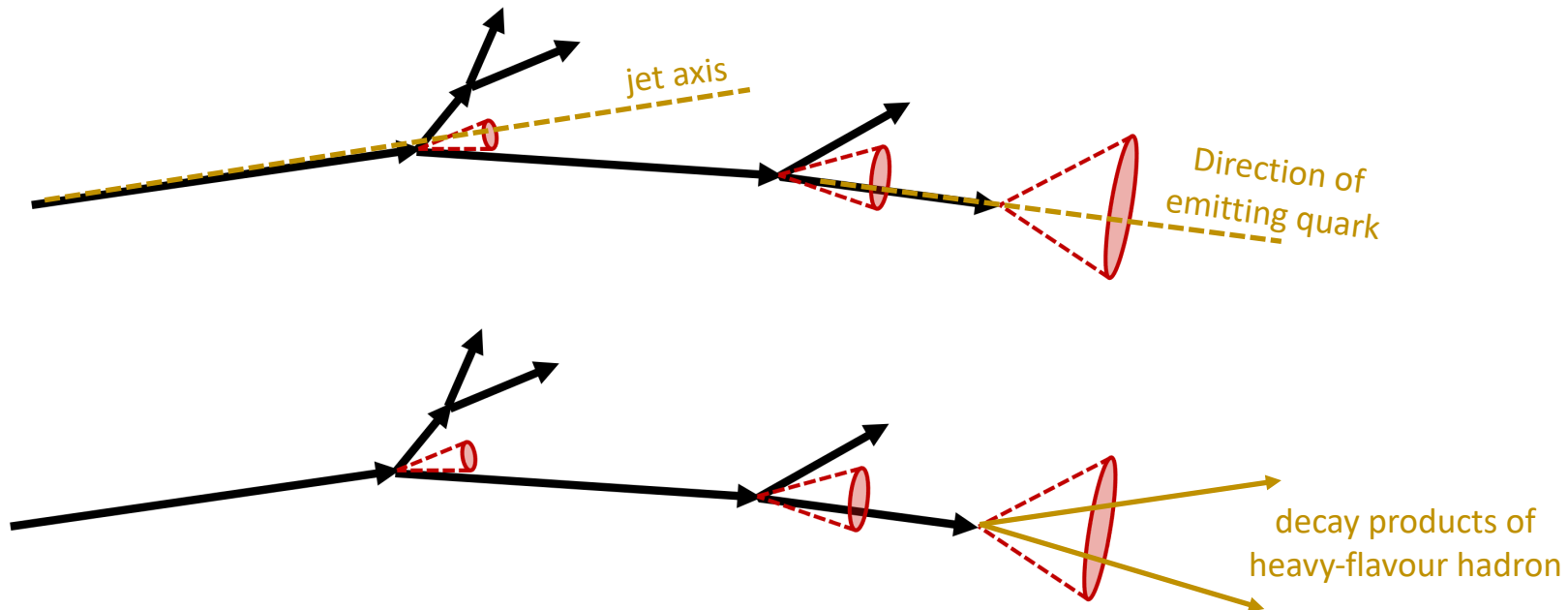
Run 3 and beyond promise to be fruitful and exciting times with experimental upgrades targeting improved heavy-flavour capabilities



Full heavy-flavour hadron reconstruction

Jets contain information on the kinematics of the final state heavy-flavour quark

Significant statistical penalties due to small branching fractions and reconstruction efficiencies



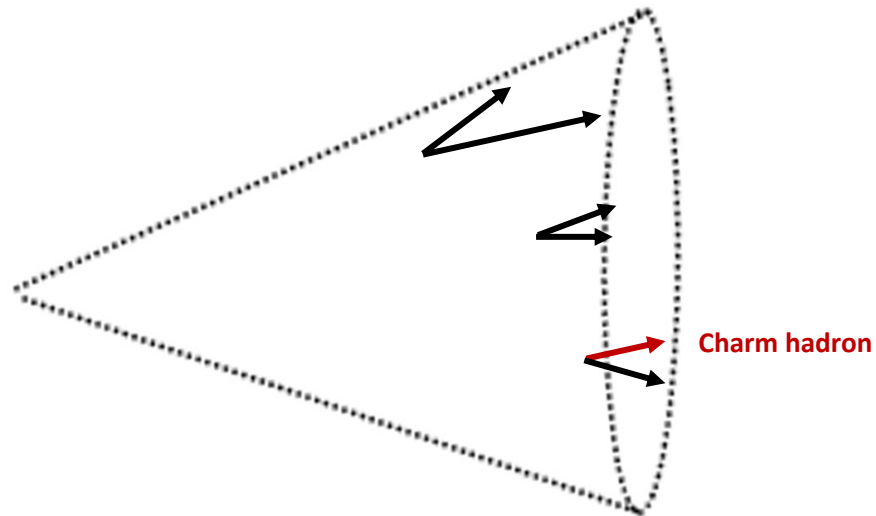
Kinematics are updated at each vertex

Decay products do not smear the shower reconstruction

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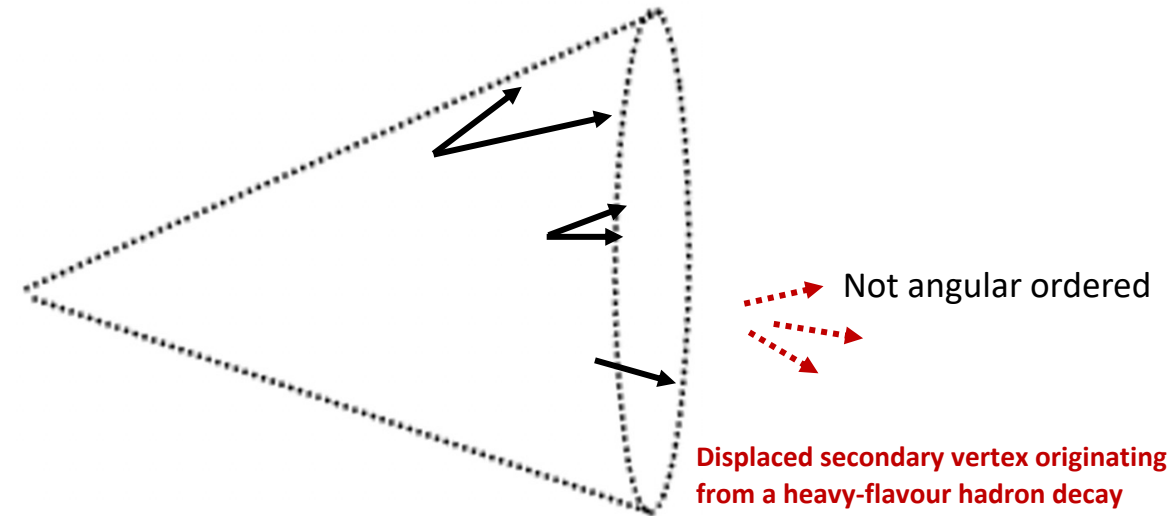


Jets with a displaced secondary vertex

Much better statistical precision

Jets lack full information on the kinematics of the final state heavy-flavour quark

How important is this?



Full heavy-flavour hadron reconstruction

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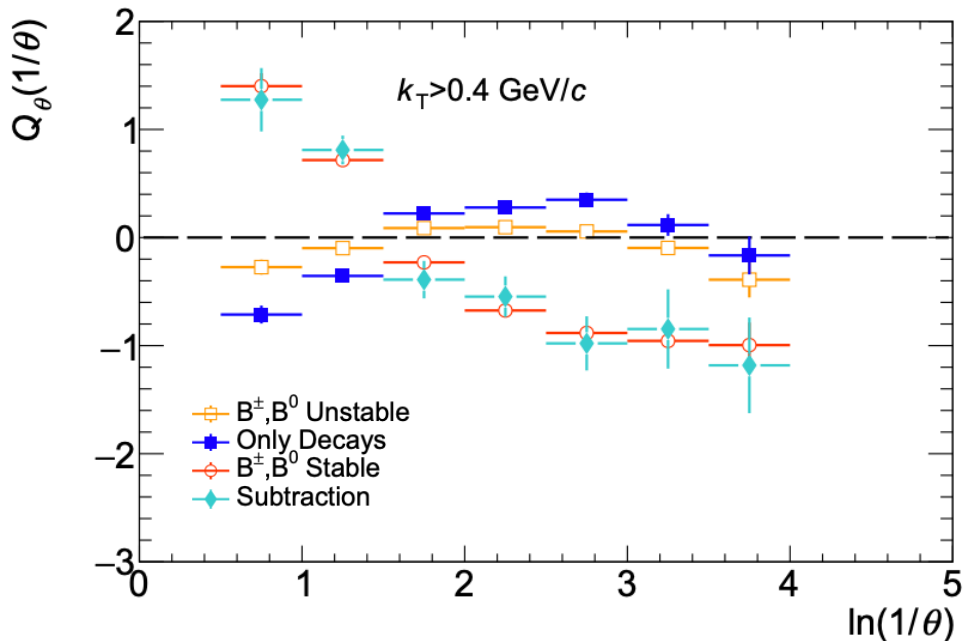
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Substructure measurements with full heavy-flavour hadrons are much more sensitive to flavour effects

Decay particles of the heavy-flavour hadron and the partial jet information can wash out differences due to flavour

Fully reconstructing hadrons is key to tracing measurements as well as substructure

Is it possible to try to estimate the heavy-flavour hadron kinematics from topology of the secondary vertex?

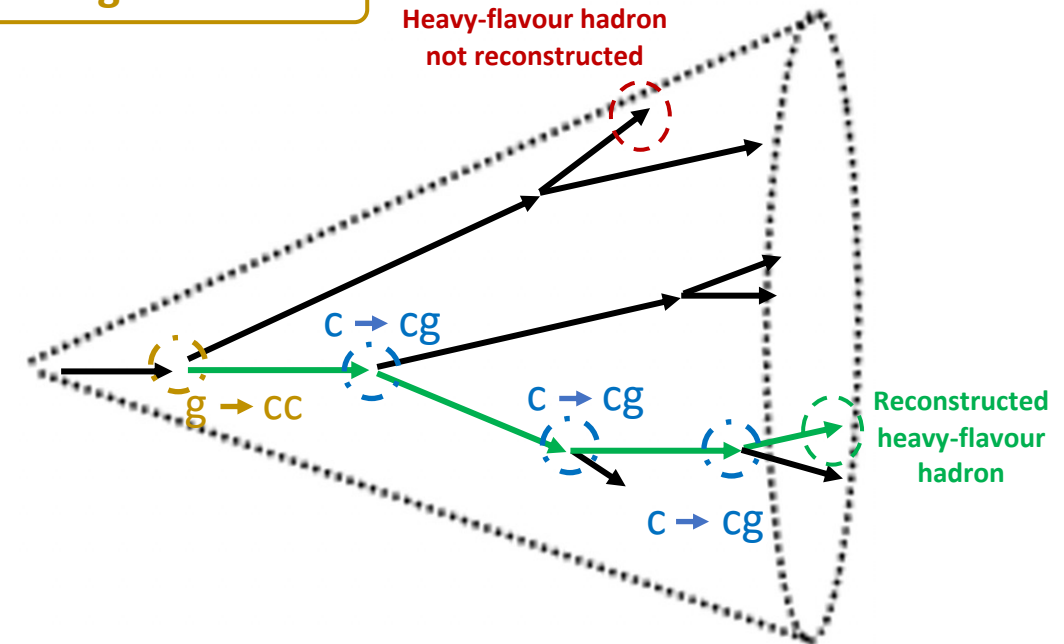
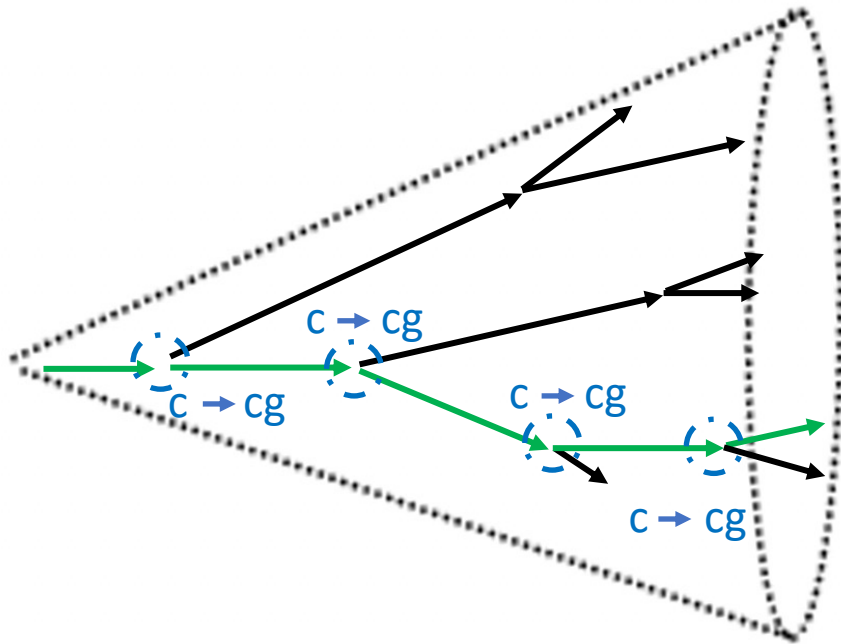
The picture presented so far assumes the heavy-flavour jet was initiated by a heavy-quark

$g \rightarrow QQ$ processes or initial state radiation can reduce control over splitting flavours

Impact of gluon-splitting reduces deeper into the tree

Can we remove gluon-splitting processes with jet clustering algorithms, substructure cuts or cuts on the secondary vertex of the non-reconstructed heavy-flavour hadron?

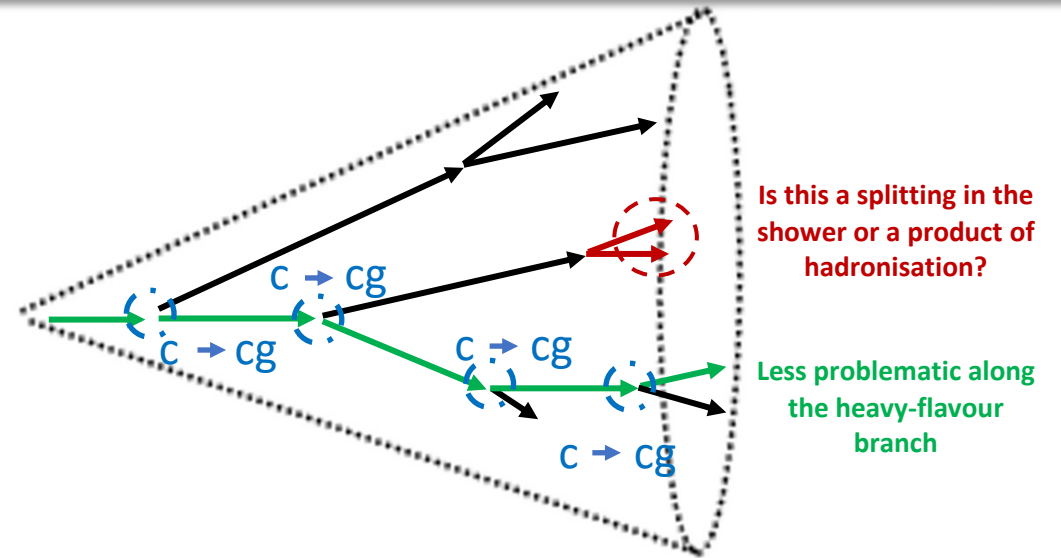
Largest challenge for tracing methods



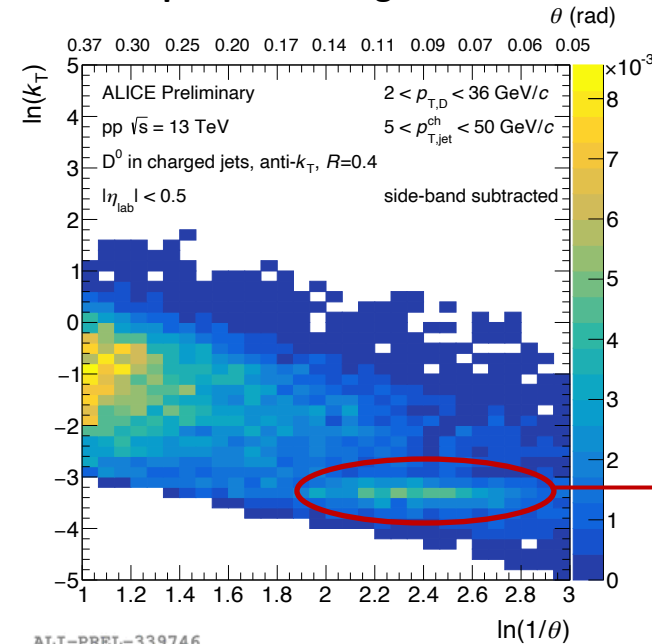
Increased non-perturbative effects

Splittings deep in the shower are more sensitive to contamination from non-perturbative sources

Strict cuts such as k_T required



Lund plane of $c \rightarrow cg$ emissions



Contamination of soft pions from $D^* \rightarrow D^0 \pi$
 Removed with a k_T cut

Increased non-perturbative effects

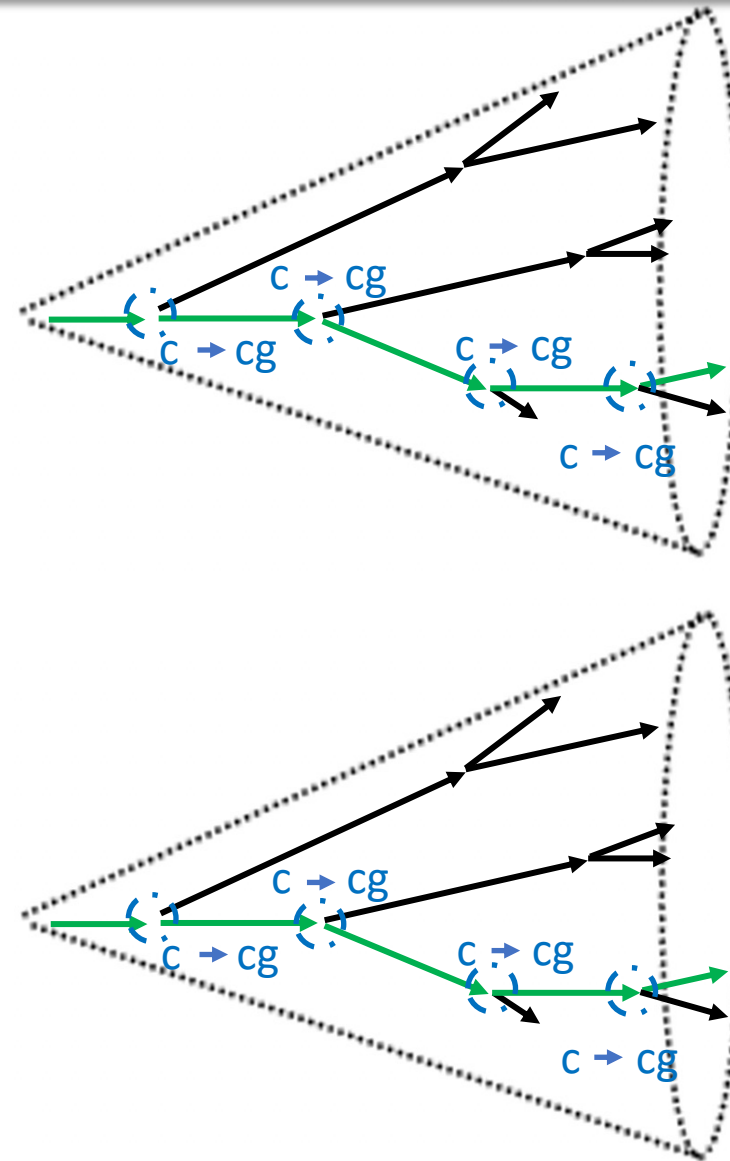
Splittings deep in the shower are more sensitive to contamination from non-perturbative sources

Strict cuts such as k_T required

Greater impact of mistagging

Is mistagging due to track losses or the underlying event more significant for deeper splittings?

Enhanced protection in heavy-flavour case as the heavy-flavour hadron cannot be lost



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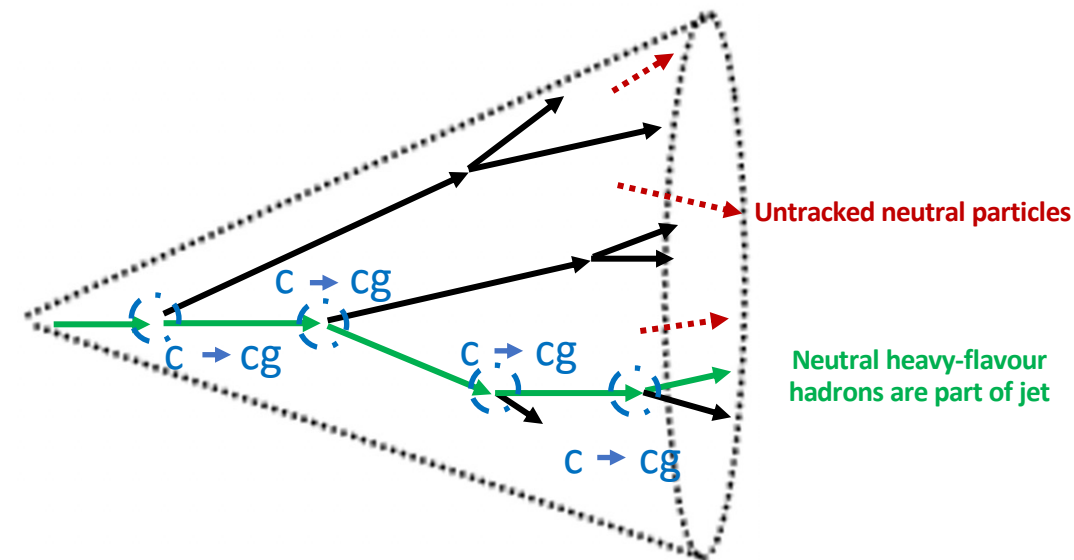
Enhanced protection in heavy-flavour case as the heavy-flavour hadron cannot be lost

Impact of neutral component

Do the missing neutral particles impact deeper splittings more?

Can we treat this as tracking losses and correct with unfolding?

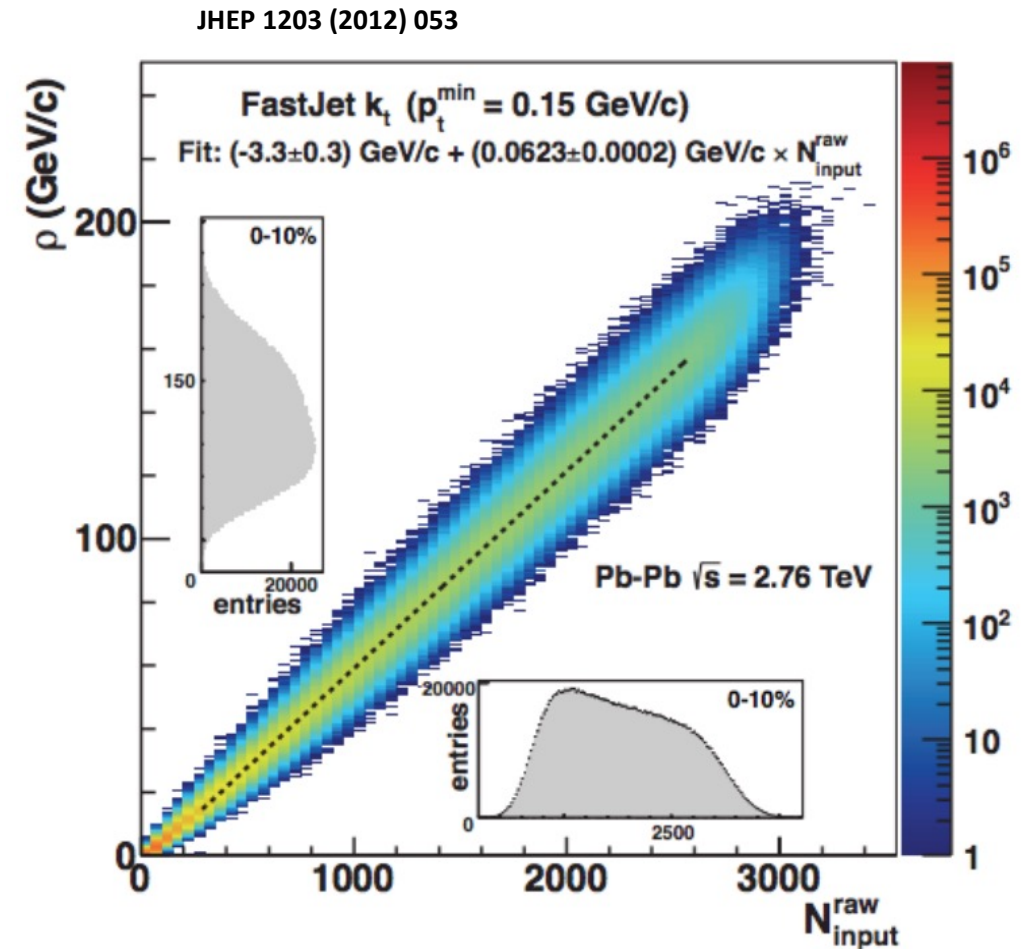
Tracing measurements often performed with track-based jets



The heavy-ion background poses a large challenge to tracing measurements

Background effects are less significant deeper into the tree (at small angles)

However if present can they have a larger impact?



The heavy-ion background poses a large challenge to tracing measurements

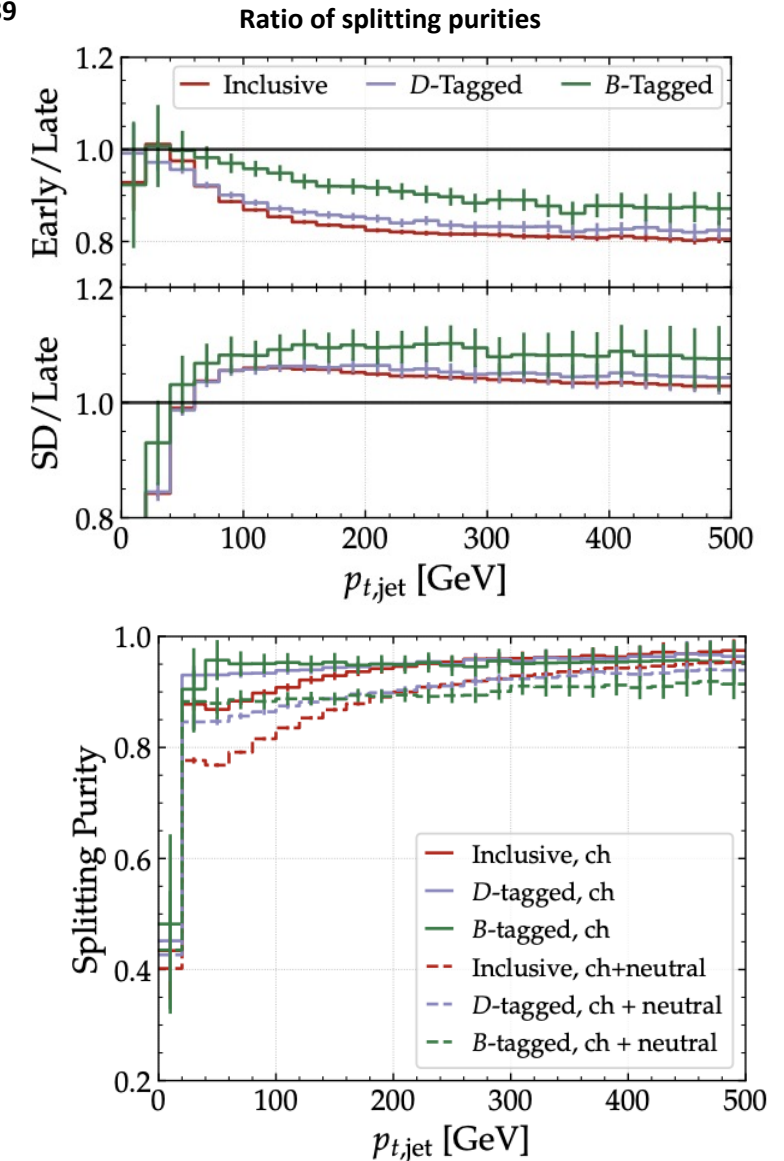
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Studies show that the combination of late splittings with grooming selections have a higher resilience to the background

Jets tagged with a heavy-flavour hadron show less sensitivity to the background than inclusive jets

arXiv: 2211.11789



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Heavy-flavour hadrons are guaranteed to be non-background

Need to modify background estimation and subtraction techniques accordingly

Opportunity to push to lower p_T jets?

