

# Searches for Lepton Number Violation and resonances in the $K^\pm \rightarrow \pi\mu\mu$ decays by NA48/2 at CERN

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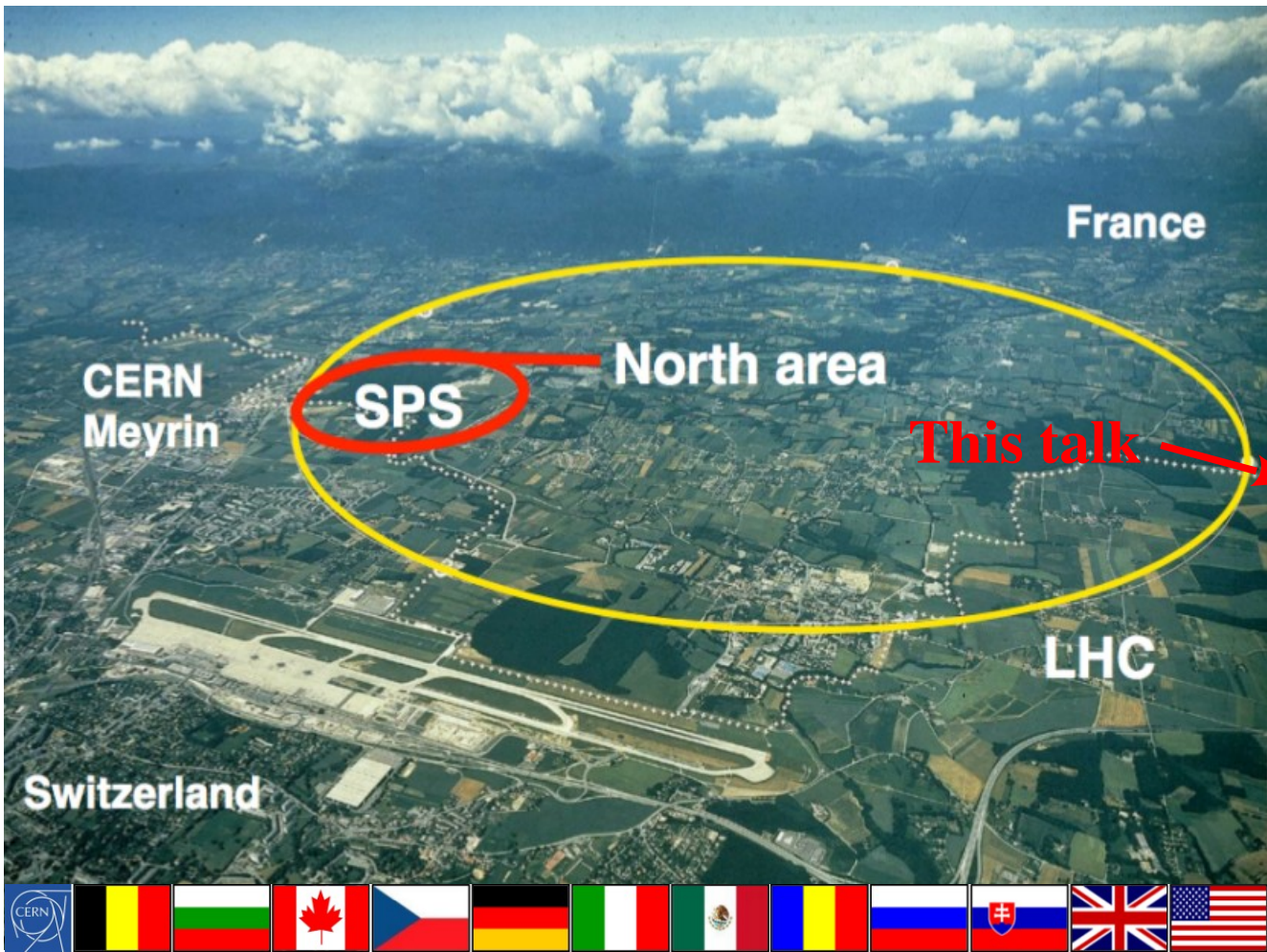


## Outline:

- The NA48/2 experiment
- Theoretical Motivations
- Search for LNV  $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$  decay – Majorana neutrinos
- Search for resonances in  $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$  decays
- Prospects for the NA62 experiment

*1<sup>st</sup> Forum on Rare Kaon Decays – Edinburgh, UK – 22/02/2018*

# The NA48/NA62 experiments @ CERN



1997 ↓ 2001	NA48 ( $K_S/K_L$ )	Re $\epsilon'/\epsilon$ <b>Discovery of direct CPV</b>
2002	NA48/1 ( $K_S$ /hyperons)	Rare $K_S$ and hyperon decays
<b>2003</b> ↓ <b>2004</b>	<b>NA48/2 (<math>K^+/K^-</math>)</b>	Direct CPV, <b>Rare <math>K^+/K^-</math> decays</b>
2007 ↓ 2008	NA62- $R_K$ ( $K^+/K^-$ )	$R_K = K_{e2}^{\pm}/K_{\mu 2}^{\pm}$
2015 ↓ -	NA62 ( $K^+$ )	$K^+ \rightarrow \pi^+ \nu \bar{\nu}$ , Rare $K^+$ and $\pi^0$ decays

**Main NA48/2 physics goal:** Search for direct CPV in  $K^{\pm} \rightarrow \pi^{\pm} \pi^+ \pi^-$  and  $K^{\pm} \rightarrow \pi^{\pm} \pi^0 \pi^0$  decays

**Main triggers:** 3-track vertex,  $K^{\pm} \rightarrow \pi^{\pm} \pi^0 \pi^0$

World largest  $K^{\pm} \rightarrow 3$ -tracks sample: **Ideal environment for  $K^{\pm} \rightarrow \pi \ell \ell$  studies**

# The NA48/2 detector

## Narrow momentum band $K^\pm$ beams:

$$P_K = 60 \text{ GeV}/c, \delta P_K/P_K \sim 4\% \text{ (rms)}$$

Nominal  $K^\pm$  decay rate:  $\sim 100 \text{ kHz}$

Simultaneous  $K^+/K^-$  beams

22% of kaons decay in  
114m-long vacuum tank  
upstream the detector



## Principal sub-detectors:

- **Spectrometer (4 DCHs)**

$$\sigma_p/p = 1.02\% \oplus 0.044\% p(\text{GeV})$$

4 views/DCH: redundancy  $\rightarrow$  efficiency

- **Scintillator Hodoscope**

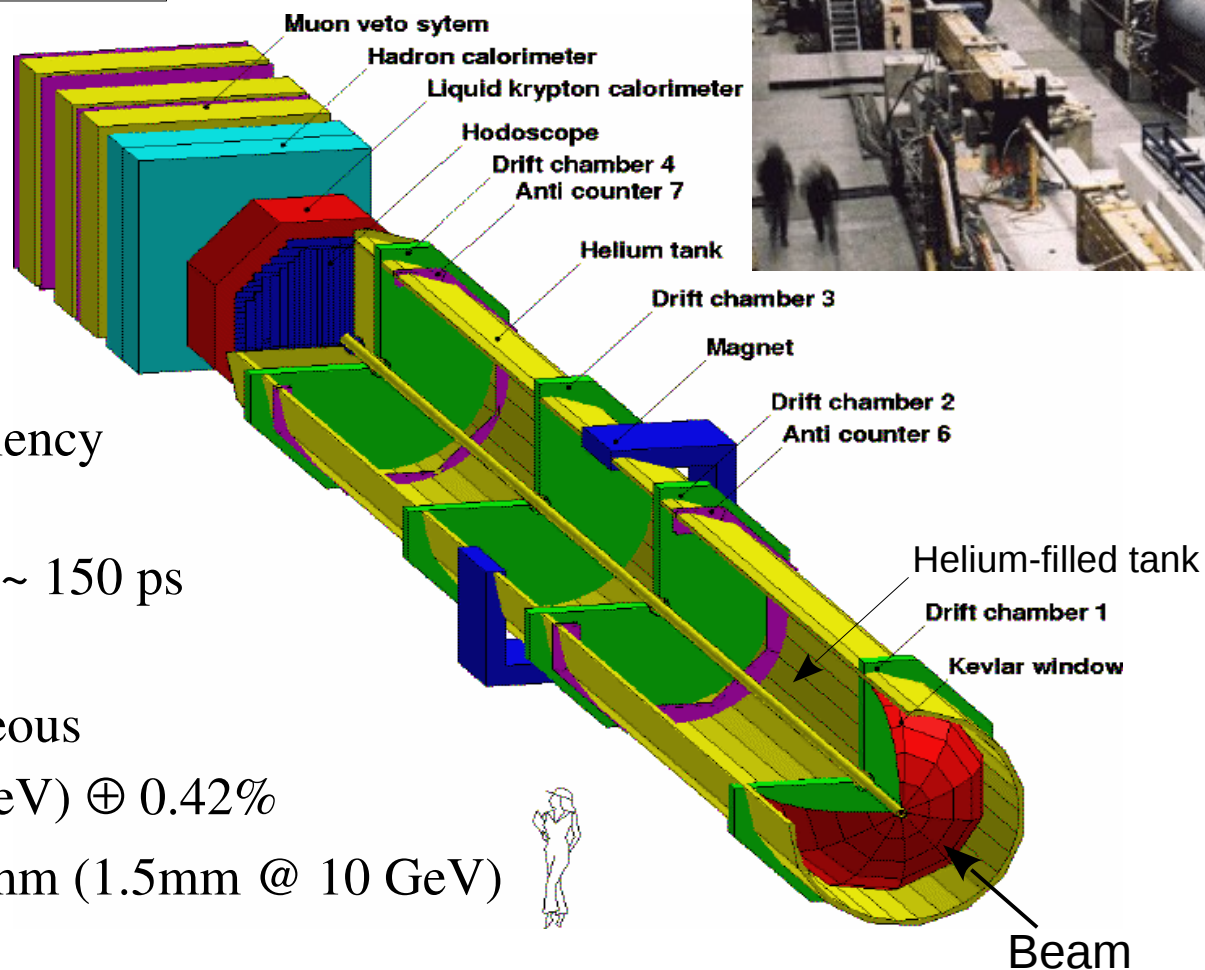
Fast trigger, time measurement  $\sigma_t \sim 150 \text{ ps}$

- **LKr EM calorimeter**

High-granularity, quasi-homogeneous

$$\sigma_E/E = 3.2\%/\sqrt{E(\text{GeV})} \oplus 9\%/E(\text{GeV}) \oplus 0.42\%$$

$$\sigma_x = \sigma_y = 4.2\text{mm}/\sqrt{E(\text{GeV})} \oplus 0.6\text{mm} \text{ (1.5mm @ 10 GeV)}$$



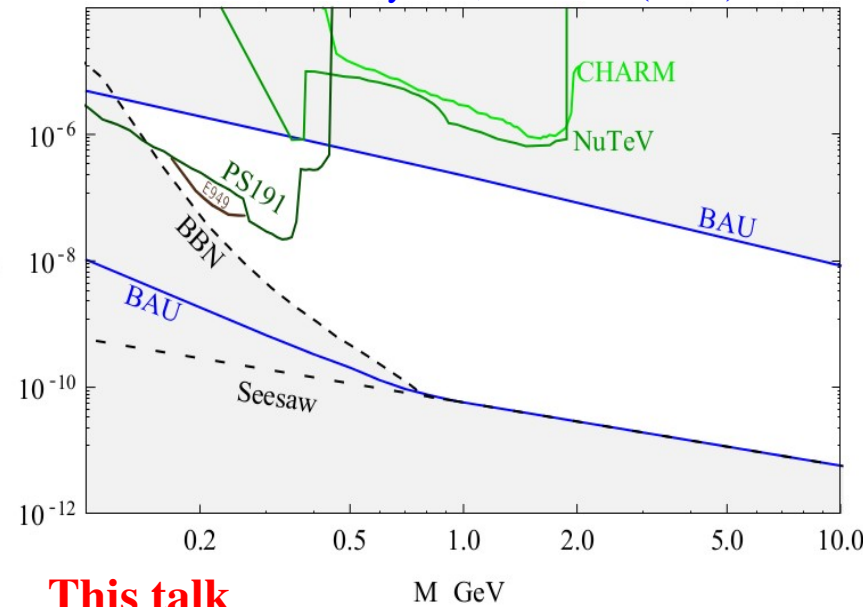
# Majorana Neutrinos

**Asaka-Shaposhnikov model (vMSM)** [[Asaka and Shaposhnikov, PLB 620 \(2005\) 17](#)]:

Dark Matter + Baryon Asymmetry of the Universe (BAU) + low mass of SM  $\nu$  can be explained by adding three sterile Majorana neutrinos  $N_i$  to the SM

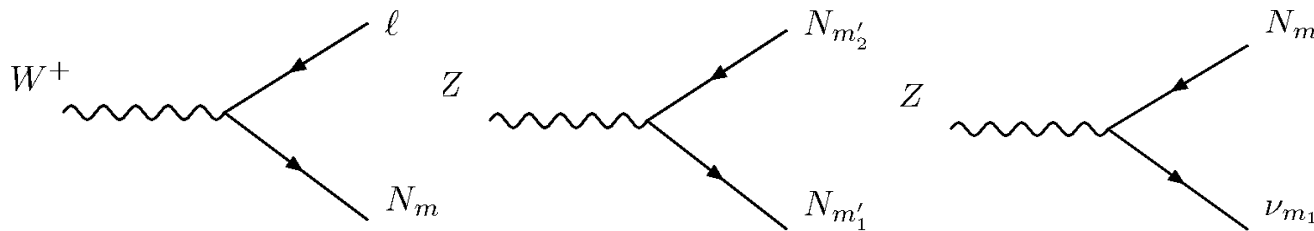
- $N_1$  is the lightest  $O(\text{keV}) \rightarrow$  Dark Matter candidate
- $N_2, N_3$  are nearly degenerate (100 MeV to few GeV) to tune CPV-phases and extra-CKM sources of baryon asymmetry.  $N_2, N_3$  produce standard neutrino masses through seesaw with a Yukawa coupling of  $\sim 10^{-8}$

Gorbunov & Timiryasov, PLB 745 (2015) 29



## Active-sterile neutrino mixing (U-matrix):

Effective vertices involving the sterile neutrinos  $N_i$ , the  $W^\pm, Z$  bosons and SM leptons



$$\text{BR}(K^\pm \rightarrow \mu^\pm N) \times \text{BR}(N \rightarrow \pi^\mp \mu^\pm) \sim |U_{\mu 4}|^4$$

**This talk**

**[ $\ell = \mu$ ]**

**$N_{2,3}$  production in  $K^\pm$  decays:**

$K^\pm \rightarrow \ell^\pm N, K^\pm \rightarrow \pi^0 \ell N, \dots$

**$N_{2,3}$  decays for  $m_{2,3} < m_K - m_\ell$ :**

$N \rightarrow \pi^\pm \ell^\mp, N \rightarrow \pi^0 \nu$

$N \rightarrow \ell_1^\pm \ell_2^\mp \nu_2, N \rightarrow \nu_1 \ell_2^+ \ell_2^-$

$N \rightarrow \nu_\ell \bar{\nu} \bar{\nu}$

# Inflatons

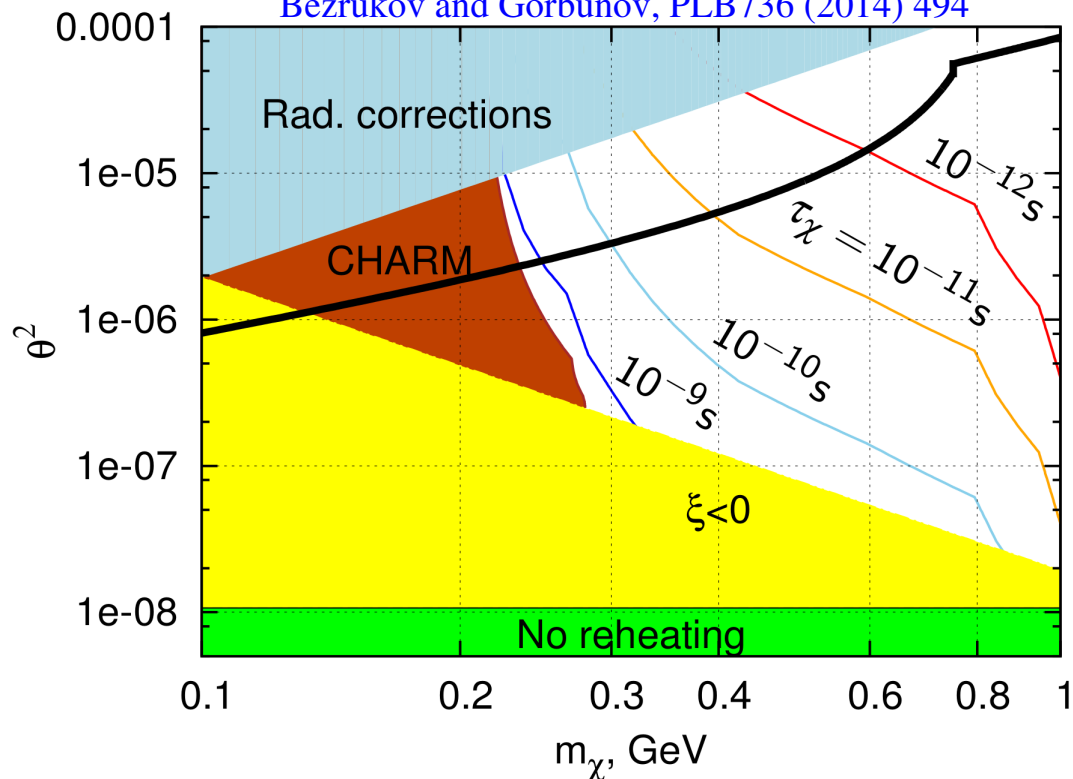
**Shaposhnikov-Tkachev model** [Shaposhnikov and Tkachev, PLB 639 (2006) 414]:

vMSM + a real scalar field (inflaton  $\chi$ ) with scale-invariant couplings

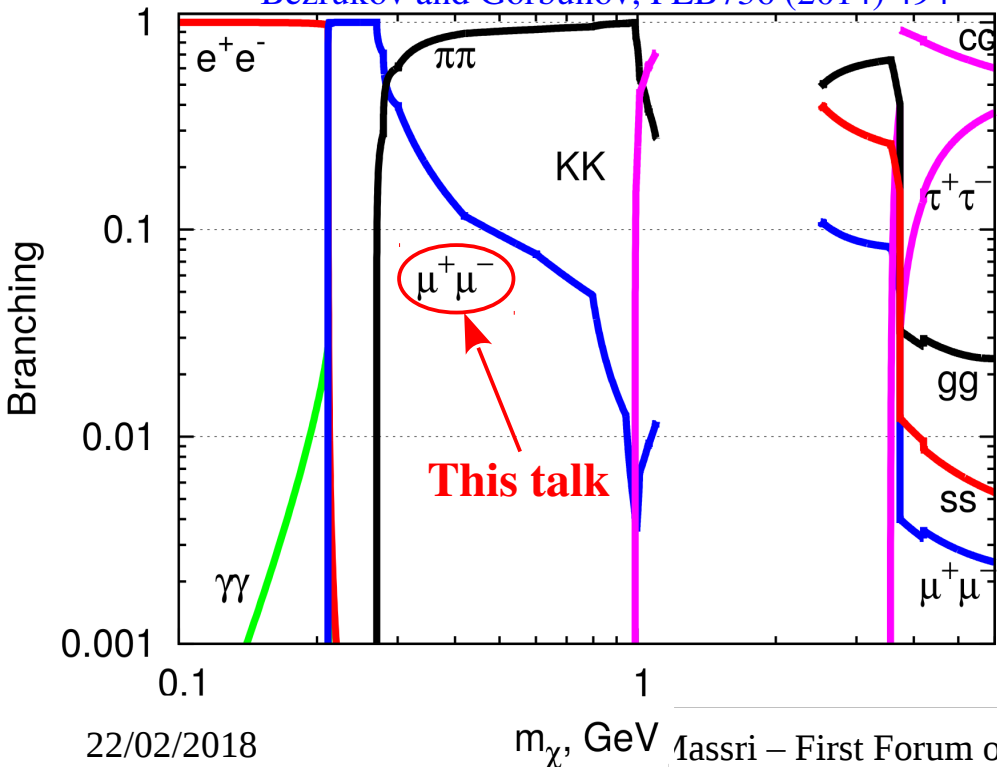
Explains Universe homogeneity and isotropy on large scales/structures on smaller scales

- $\chi$ -Higgs mixing with mixing angle  $\theta$
- $\chi$ -Higgs coupling  $\rightarrow$  Universe reheating
- $\chi$  is unstable:  $\tau \sim (10^{-8}-10^{-12})$  s

Bezrukov and Gorbunov, PLB736 (2014) 494



Bezrukov and Gorbunov, PLB736 (2014) 494



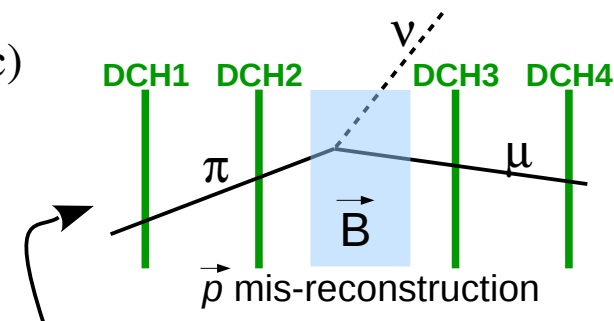
$\chi$  in Kaon decays [ $m_\chi < 354 \text{ MeV}/c^2$ ]

$$BR(K^\pm \rightarrow \pi^\pm \chi) = 1.3 \times 10^{-3} \left( \frac{2|\vec{p}_\chi|}{M_K} \right) \theta^2$$

# The NA48/2 same-sign muons sample (LNV)

## Basic principles of the searches:

- Fully reconstructed final states, 3-track vertex topology
- Similar topology to normalisation channel  $K^\pm \rightarrow \pi^\pm\pi^+\pi^-$   
 → First-order cancellation of systematic effects (trigger inefficiency, etc)



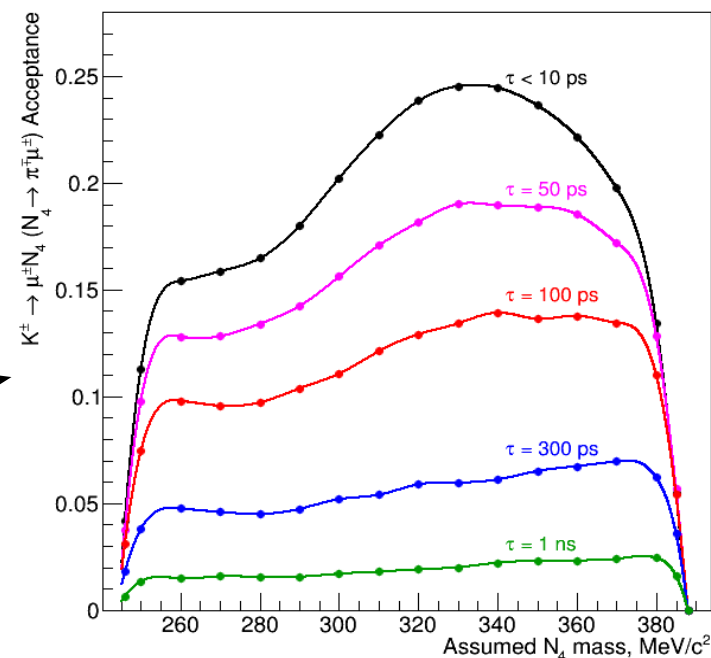
## Search for Lepton Number Violation – Majorana neutrinos

- Method: exclusive search for the  $K^\pm \rightarrow \pi^\mp\mu^\pm\mu^\pm$  decay
- Main background:  $K^\pm \rightarrow \pi^\pm\pi^+\pi^-$  with 2  $\pi^\pm \rightarrow \mu^\pm\nu$  decays (one within the Spectrometer)

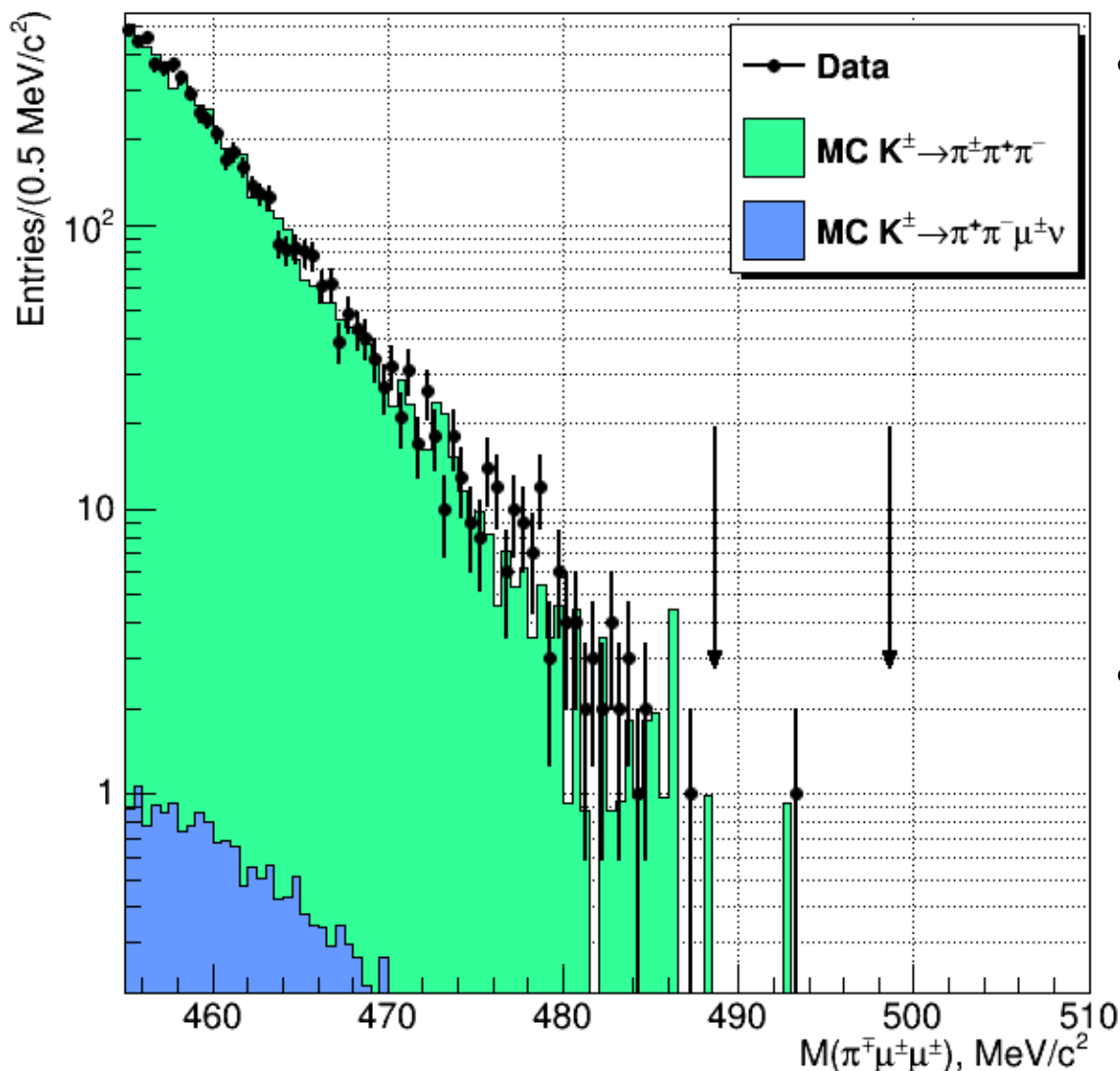
## Sensitivity:

$$\left. \begin{array}{l} \text{UL on BR}(K^\pm \rightarrow \pi^\mp\mu^\pm\mu^\pm) \\ \text{UL on BR}(K^\pm \rightarrow \mu^\pm N_4) \times \text{BR}(N_4 \rightarrow \pi^\mp\mu^\pm) \end{array} \right\} \sim \frac{1}{N_K * \text{Acceptance}}$$

Mass and lifetime dependence of the signal acceptance from dedicated MC simulation of the signal



# The same-sign muons selection (LNV)



## • Blind analysis:

$K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$  selection based on

- $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$  MC simulation
  - Uniform phase-space ( $|M_{fi}|^2 = 1$ )
  - Resonant Majorana neutrino model
- $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  MC simulation ( $10^{10}$  events)
- Control Region:

$$M(\pi^\mp \mu^\pm \mu^\pm) < 480 \text{ MeV}/c^2$$

## • Event selection:

- One well-reconstructed 3-track vertex
- 2 same-sign muons, 1 odd-sign pion
- Total  $P_T$  consistent with zero
- Signal Region:

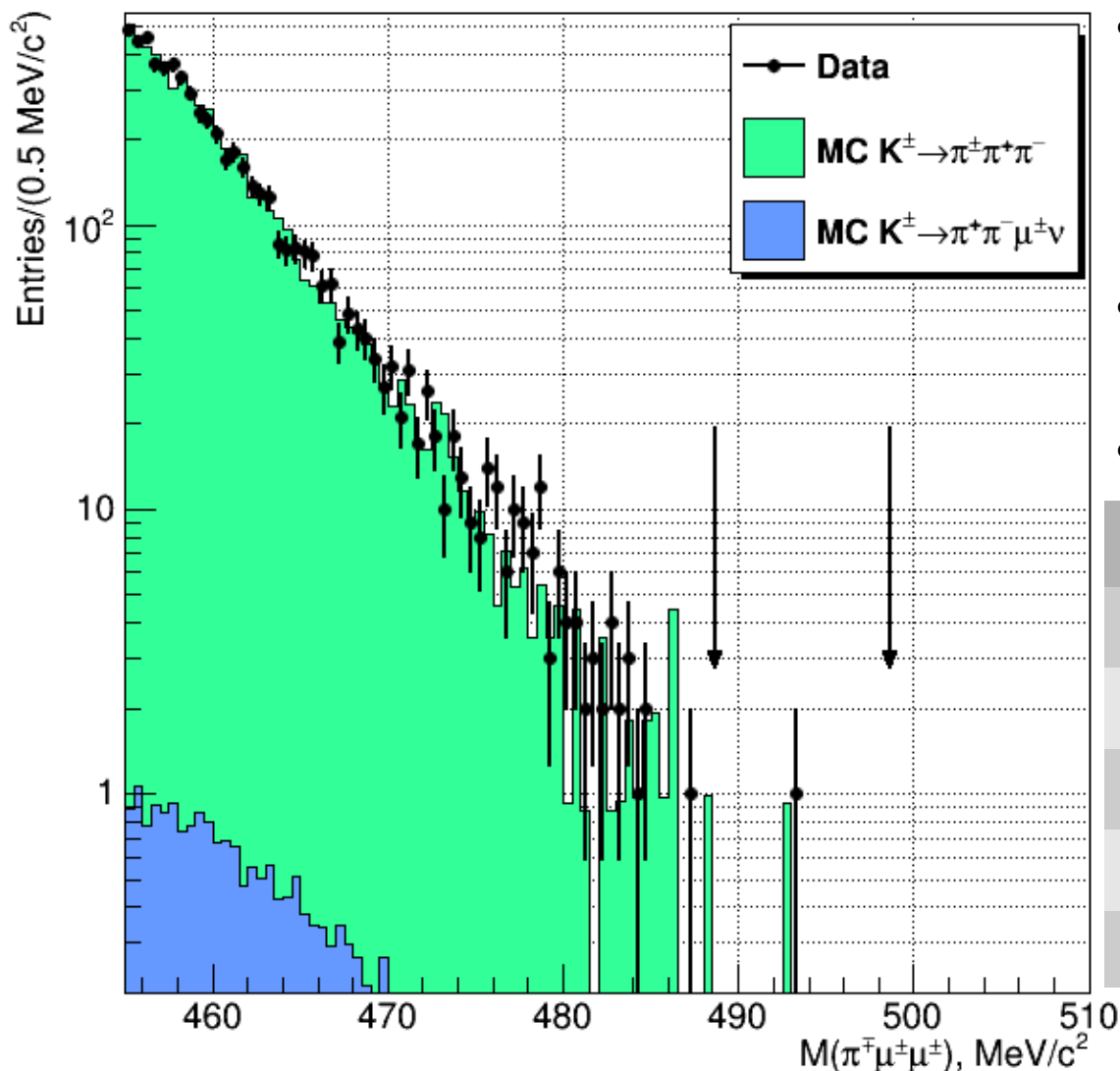
$$|M(\pi^\mp \mu^\pm \mu^\pm) - M_K| < 5 \text{ MeV}/c^2$$

## • Expected background:

Additional  $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  MC sample ( $10^{10}$  events)

dedicated to evaluation of number of expected  $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  events in Signal Region

# Upper Limit on $\text{BR}(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm)$



• Kaon decays in the fiducial volume:

$$N_K \sim 2 \times 10^{11}$$

(from reconstructed  $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  decays)

• Events in Signal Region observed:

$$N_{\text{obs}} = 1$$

• Expected background: (from MC)

Decay	BR	$N_{\text{exp}}$ (LNV)
$K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$	$(5.583 \pm 0.024)\%$	$0.864 \pm 0.864$
$K^\pm \rightarrow \pi^+ \pi^- \mu^\pm \nu$	$(4.5 \pm 0.2) \times 10^{-6}$	$0.027 \pm 0.015$
$K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$	$(9.4 \pm 0.6) \times 10^{-8}$	$0.257 \pm 0.027$
$K^\pm \rightarrow \mu^\pm \mu^+ \mu^- \nu$	$1.35 \times 10^{-8}$	$0.012 \pm 0.001$
Total	–	$1.160 \pm 0.865$

Acceptance( $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$ ) =  $(20.62 \pm 0.01)\%$

Rolke-Lopez statistical treatment to get  $\text{UL}(N_{\text{sig}})$ :

$$\text{BR}(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) < 8.6 \times 10^{-11} \text{ @ } 90\% \text{ CL}$$



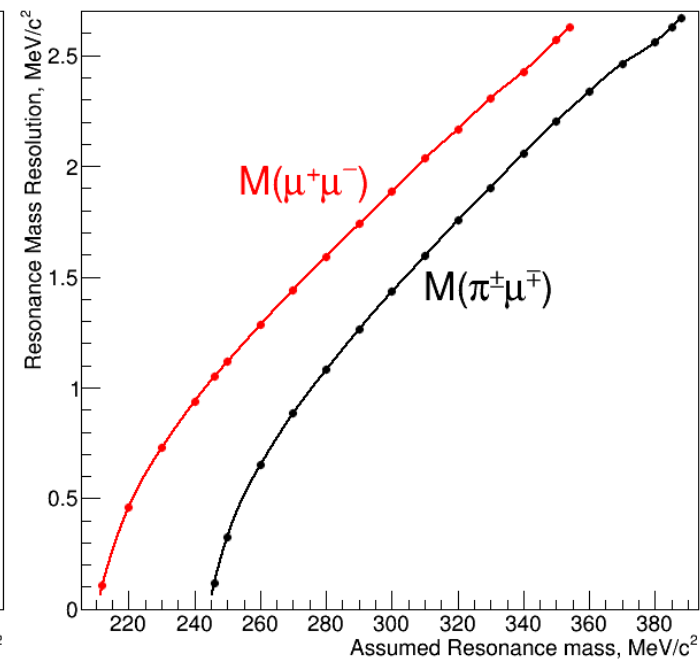
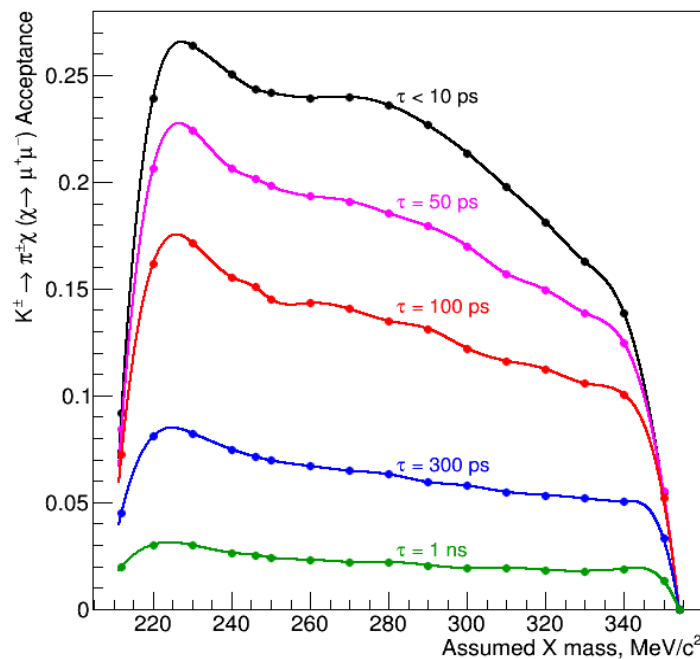
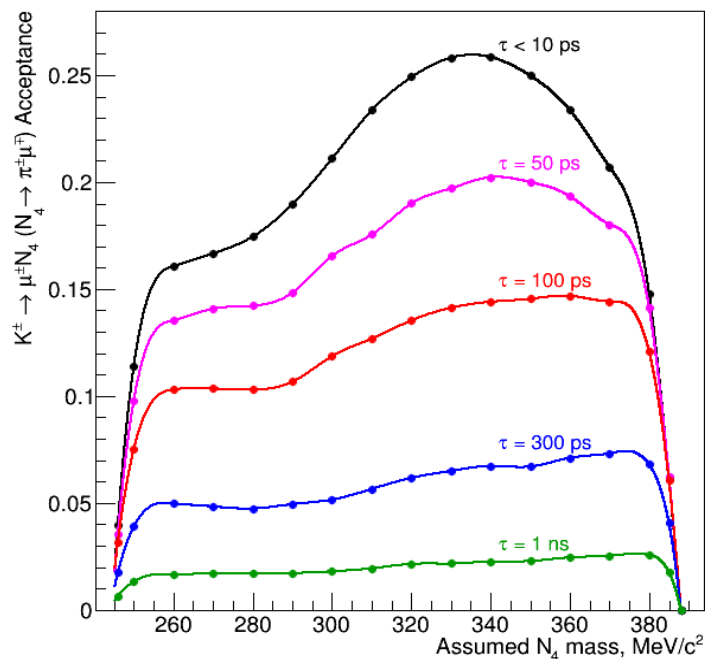
# The NA48/2 opposite-sign muons sample (LNC)

## Basic principles of the searches:

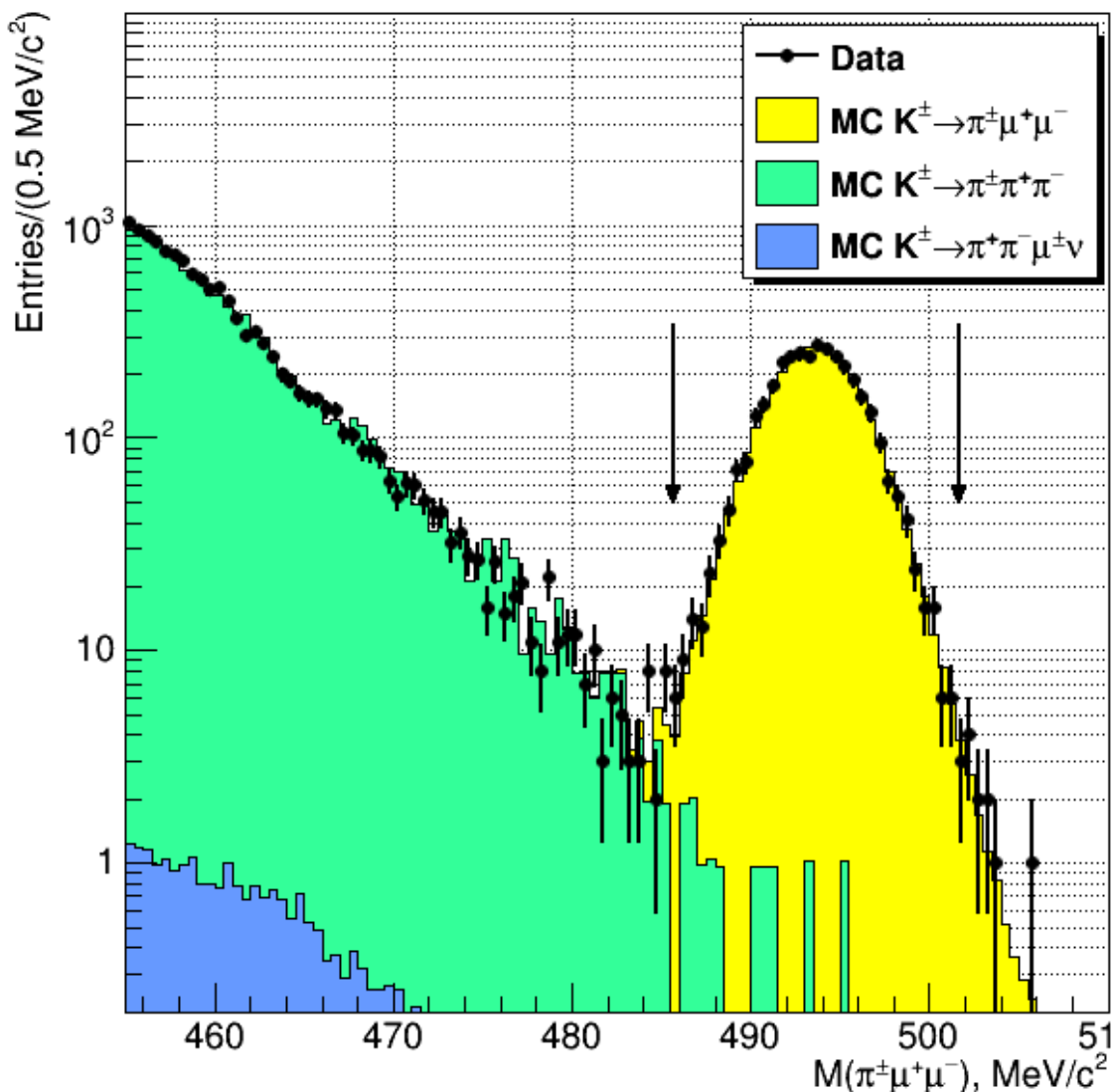
- Fully reconstructed final states, 3-track vertex topology
- Similar topology to normalisation channel  $K^\pm \rightarrow \pi^\pm\pi^+\pi^-$   
→ First-order cancellation of systematic effects (trigger inefficiency, etc)

## Search for resonances in $K^\pm \rightarrow \pi^\pm\mu^+\mu^-$ decays

- Method: exclusive search for the decay chains  $K^\pm \rightarrow \mu^\pm N_4 (N_4 \rightarrow \pi^\pm\mu^\mp)$ ,  $K^\pm \rightarrow \pi^\pm X (X \rightarrow \mu^+\mu^-)$
- Main background:  $K^\pm \rightarrow \pi^\pm\mu^+\mu^-$  (irreducible) → Limited sensitivity
- Sensitivity: UL on  $BR(K^\pm \rightarrow \mu^\pm N_4) \times BR(N_4 \rightarrow \pi^\pm\mu^\mp)$   
UL on  $BR(K^\pm \rightarrow \pi^\pm X) \times BR(X \rightarrow \mu^+\mu^-)$  }  $\sim \frac{\sqrt{BR(K^\pm \rightarrow \pi^\pm\mu^+\mu^-)}}{\sqrt{N_K * Acceptance}} \sqrt{\frac{\sigma(M_{res})}{m_K - (m_\pi + 2m_\mu)}}$



# The opposite-sign muons selection (LNC)



## • Event selection:

- Minimal changes wrt LNV selection
- One well-reconstructed 3-track vertex
- 2 opposite-sign muons, 1 pion
- Total  $P_T$  consistent with zero
- Signal Region:

$$|M(\pi^\pm\mu^+\mu^-) - M_K| < 8 \text{ MeV}/c^2$$

## • Expected background: (from MC)

Decay	BR	$N_{\text{exp}}$ (LNC)
$K^\pm \rightarrow \pi^\pm\pi^+\pi^-$	$(5.583 \pm 0.024)\%$	$10.85 \pm 3.06$
$K^\pm \rightarrow \pi^+\pi^-\mu^\pm\nu$	$(4.5 \pm 0.2) \times 10^{-6}$	$0.018 \pm 0.012$
$K^\pm \rightarrow \pi^\pm\mu^+\mu^-$	$(9.4 \pm 0.6) \times 10^{-8}$	$3422 \pm 219$
$K^\pm \rightarrow \mu^\pm\mu^+\mu^-\nu$	$1.35 \times 10^{-8}$	$0.037 \pm 0.003$
Total	–	$3433 \pm 219$

3489  $K^\pm \rightarrow \pi^\pm\mu^+\mu^-$  candidates in Signal Region\*

→ To be scanned searching for peaks in  $M(\pi^\pm\mu^\mp)$  and  $M(\mu^+\mu^-)$  invariant masses

\*: Improved selection wrt previous NA48/2  $K^\pm \rightarrow \pi^\pm\mu^+\mu^-$  analysis [PLB 697 (2011) 107]

# The mass scan framework

## Basic principles:

- Based on selected  $K^\pm \rightarrow \pi\mu\mu$  candidates. Variable step =  $0.5\sigma(M_{res})$  and window =  $\pm 2\sigma(M_{res})$
- For each  $M_{res}$ : Observed events in data ( $N_{obs}$ ) vs Expected events from MC ( $N_{exp}$ )  $\rightarrow$  UL( $N_{sig}$ )
- Rolke-Lopez statistical treatment used in each mass hypothesis  $M_{res}$  to get UL( $N_{sig}$ )

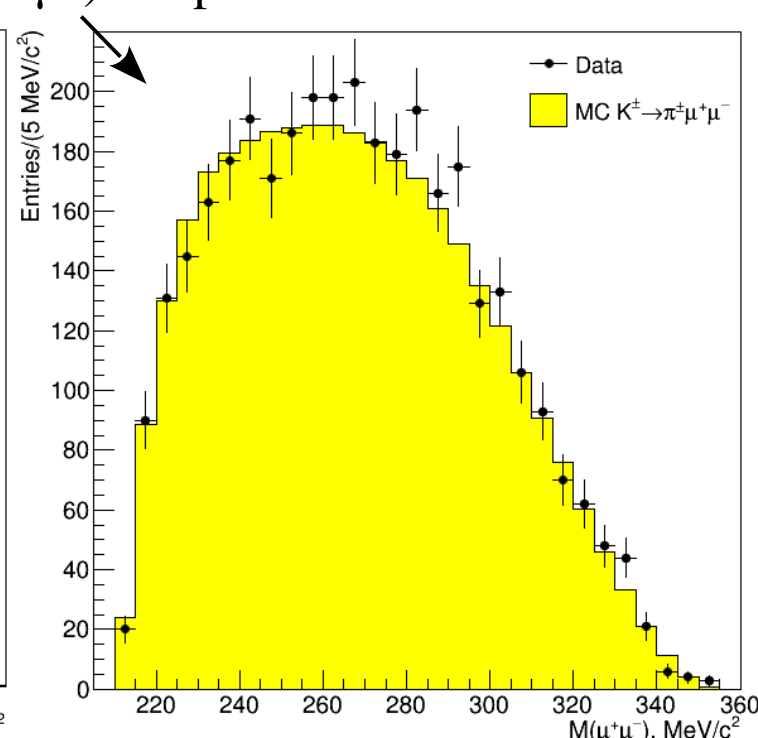
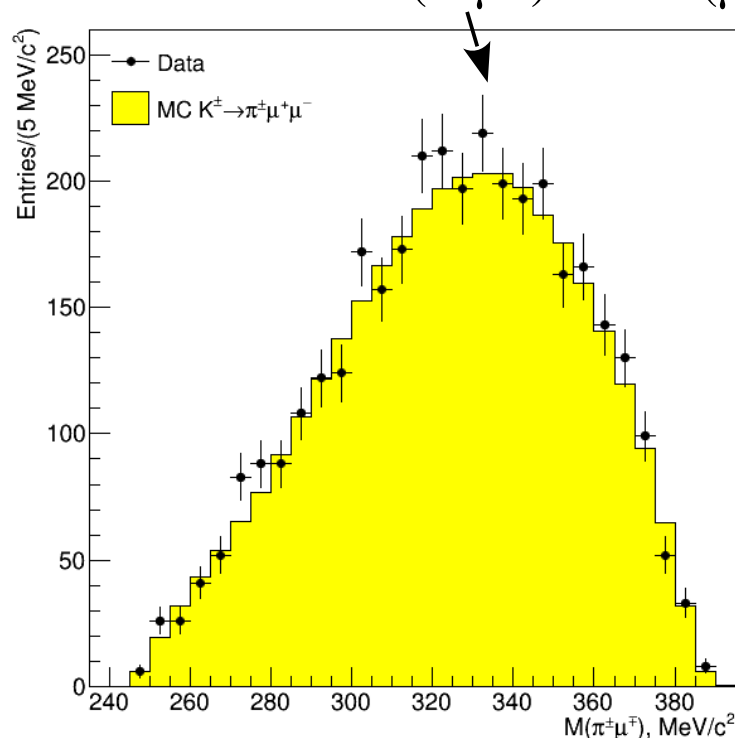
## Search for Lepton Number Violation/Majorana neutrinos [284 mass hypotheses $M_{res}$ tested]

- 2 possibilities in building  $M(\pi^\mp\mu^\pm)$  [same-sign  $\mu$ s]: closest invariant mass to  $M_{res}$  considered

## Search for resonances in $K^\pm \rightarrow \pi^\pm\mu^+\mu^-$ decays [267 hypotheses for $M(\pi^\pm\mu^\mp)$ , 280 for $M(\mu^+\mu^-)$ ]

- The distributions of both invariant masses  $M(\pi^\pm\mu^\mp)$  and  $M(\mu^+\mu^-)$  are probed

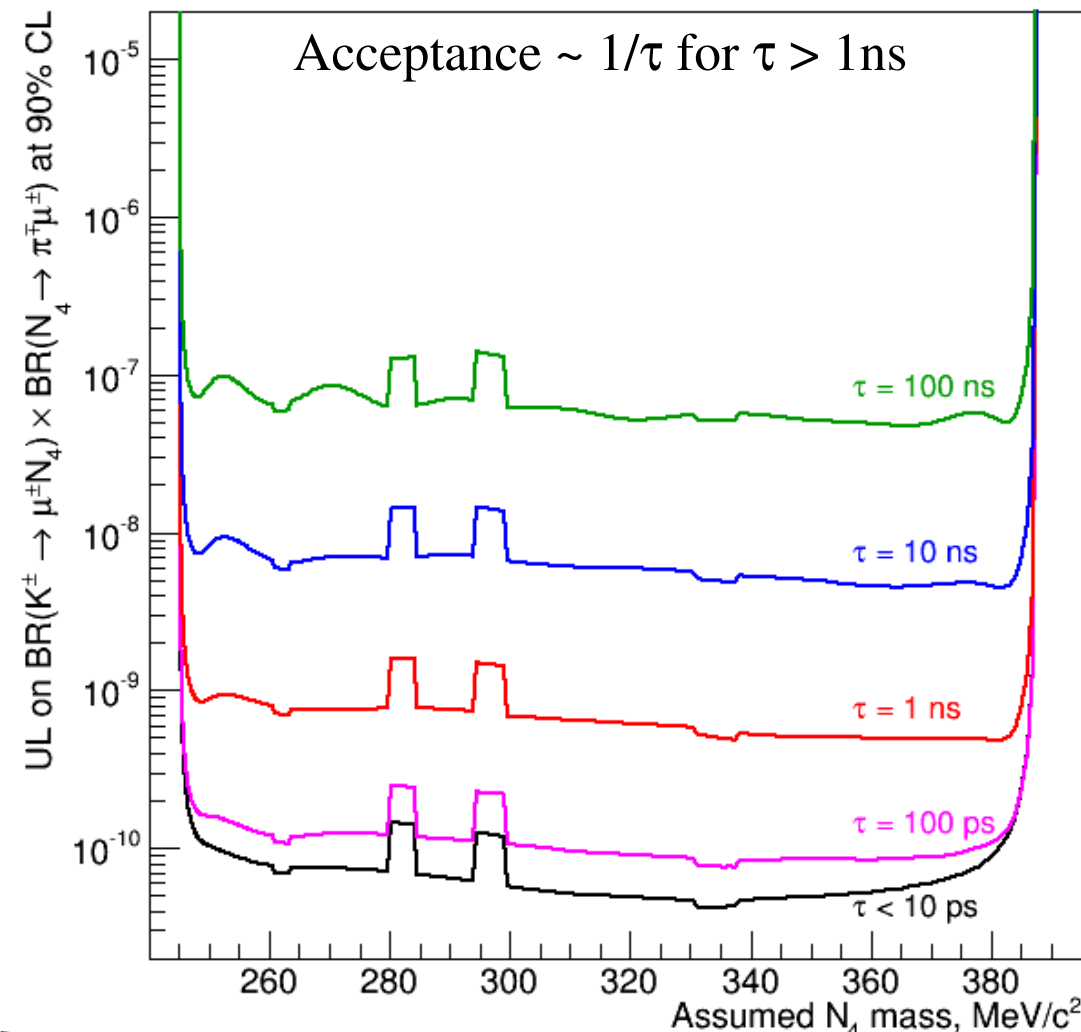
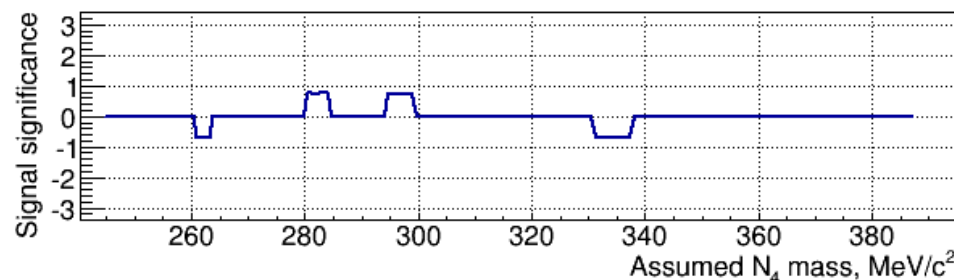
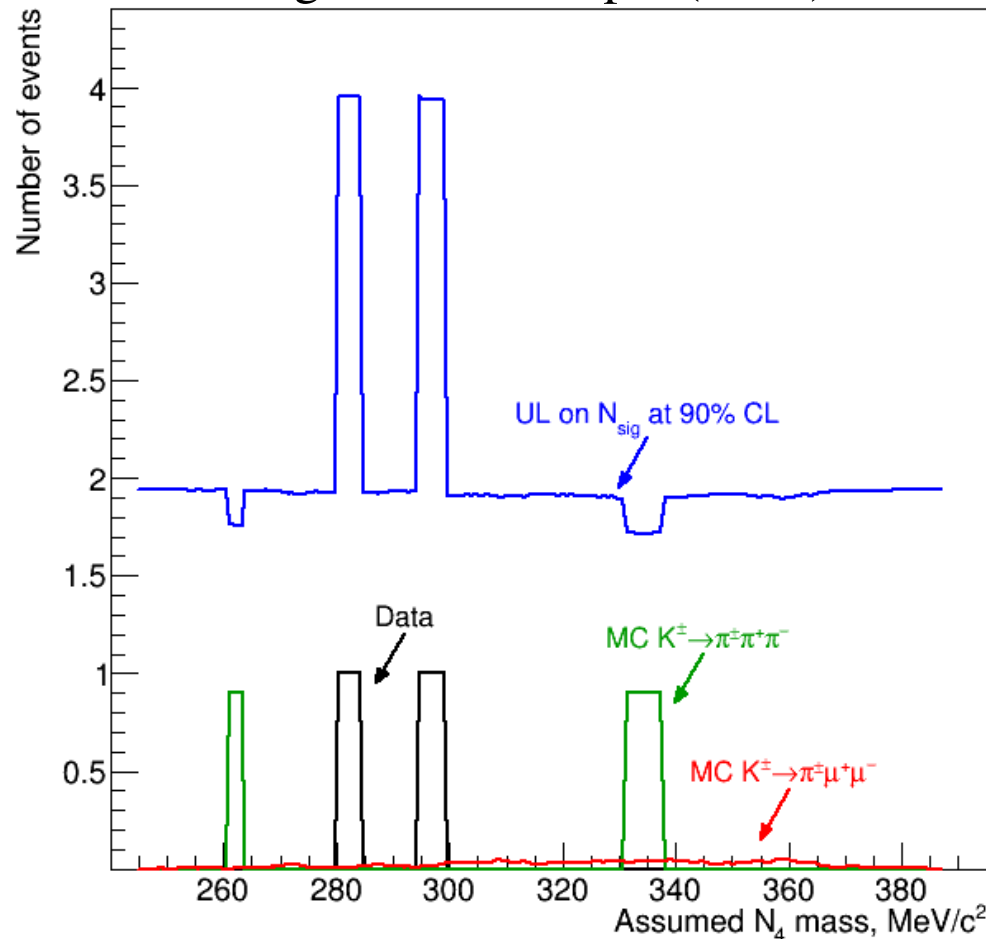
$K^\pm \rightarrow \pi^\pm\mu^+\mu^-$  MC uses form factors extracted from the selected data sample to obtain best data/MC agreement



# Search for $K^\pm \rightarrow \mu^\pm N_4 (N_4 \rightarrow \pi^\mp \mu^\pm)$ decays

Same-sign muons sample (LNV)

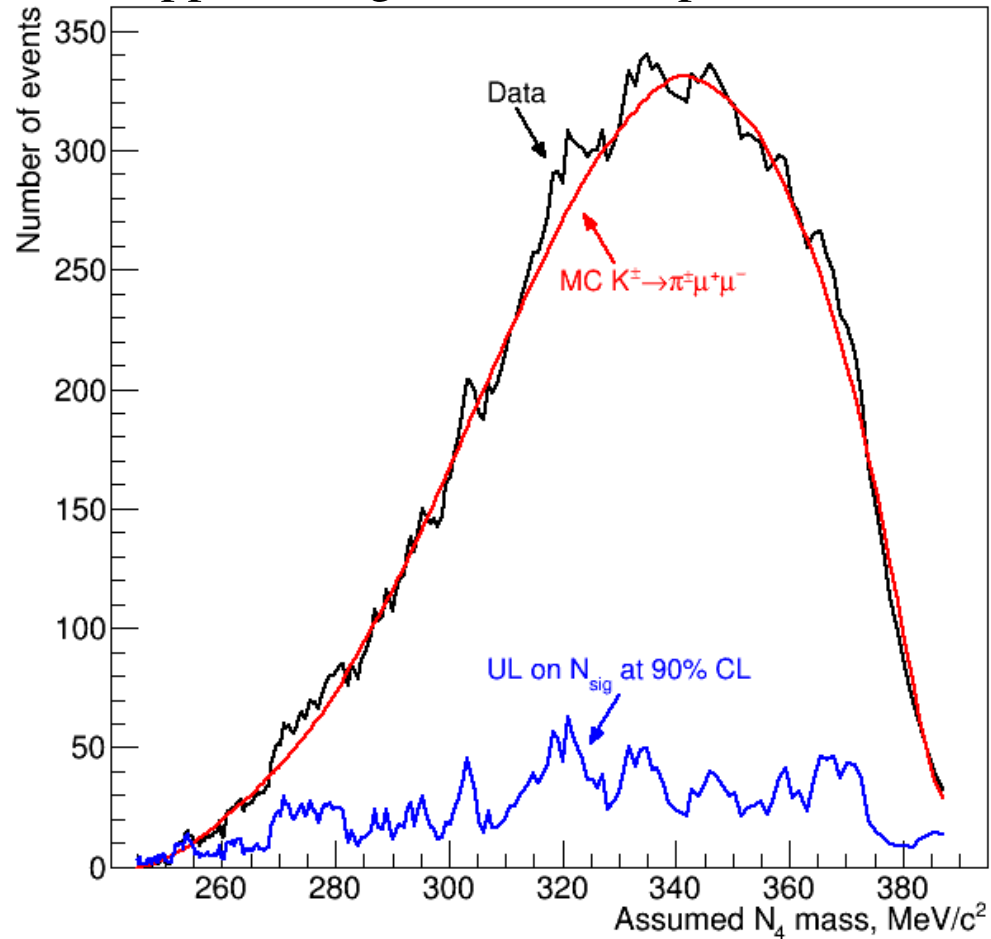
$$UL(BR(K^\pm \rightarrow \mu^\pm N_4) BR(N_4 \rightarrow \pi^\mp \mu^\pm)) = \frac{UL(N_{sig})}{N_K * Acceptance}$$



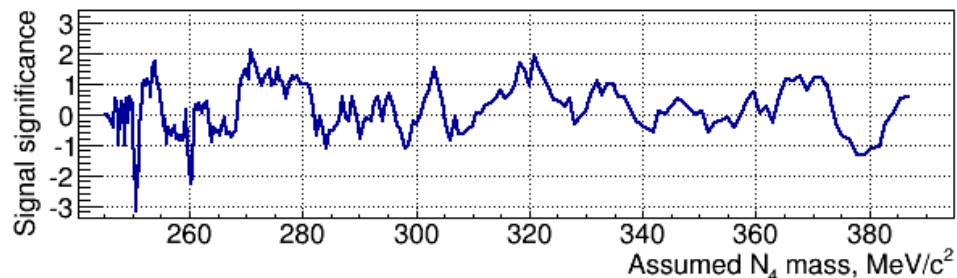
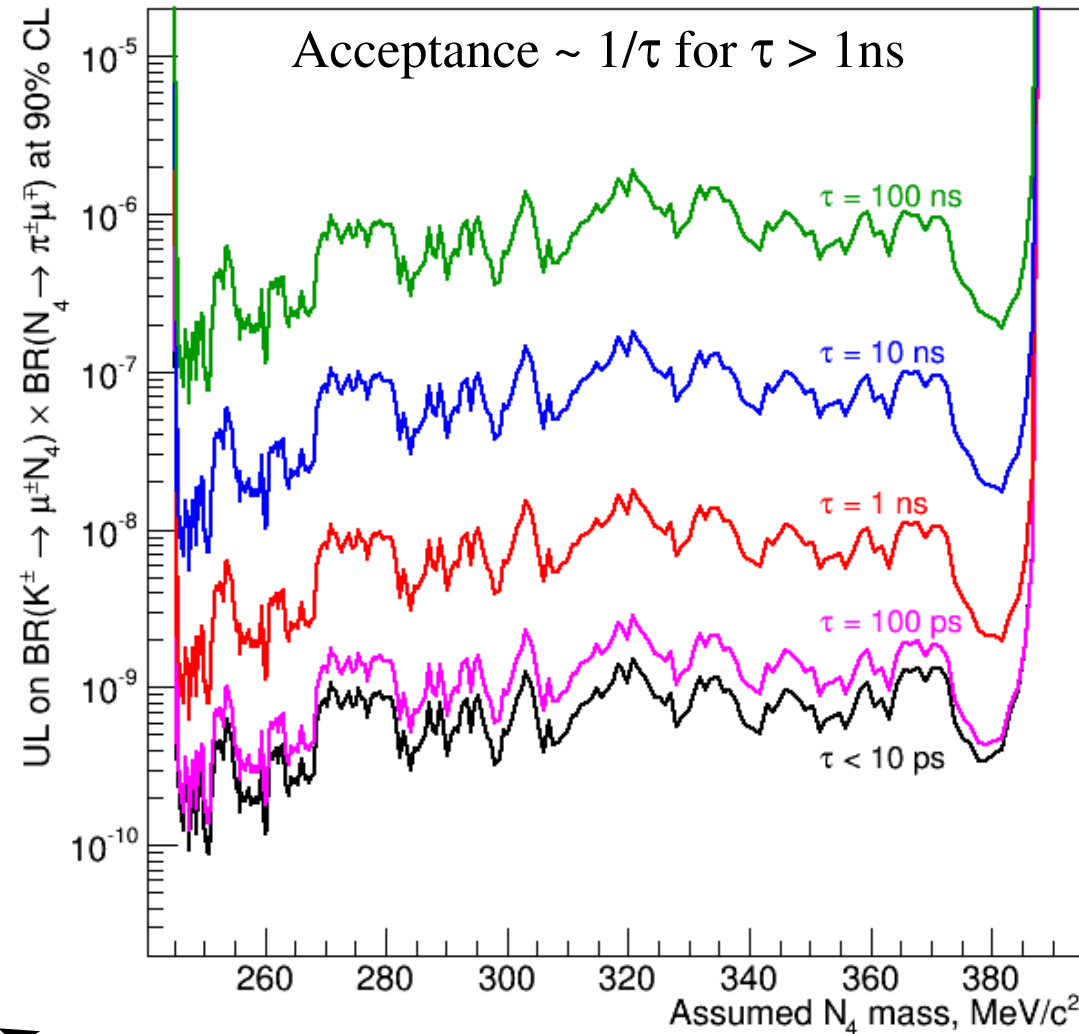
Statistical significance  $z = \frac{N_{obs} - N_{exp}}{\sigma(N_{obs}) \oplus \sigma(N_{exp})}$   
 never exceeds  $+3\sigma$ : no signal observed

# Search for $K^\pm \rightarrow \mu^\pm N_4 (N_4 \rightarrow \pi^\pm \mu^\mp)$ decays

Opposite-sign muons sample (LNC)



$$UL(BR(K^\pm \rightarrow \mu^\pm N_4) BR(N_4 \rightarrow \pi^\pm \mu^\mp)) = \frac{UL(N_{sig})}{N_K * Acceptance}$$



Statistical significance  $z = \frac{N_{obs} - N_{exp}}{\sigma(N_{obs}) \oplus \sigma(N_{exp})}$

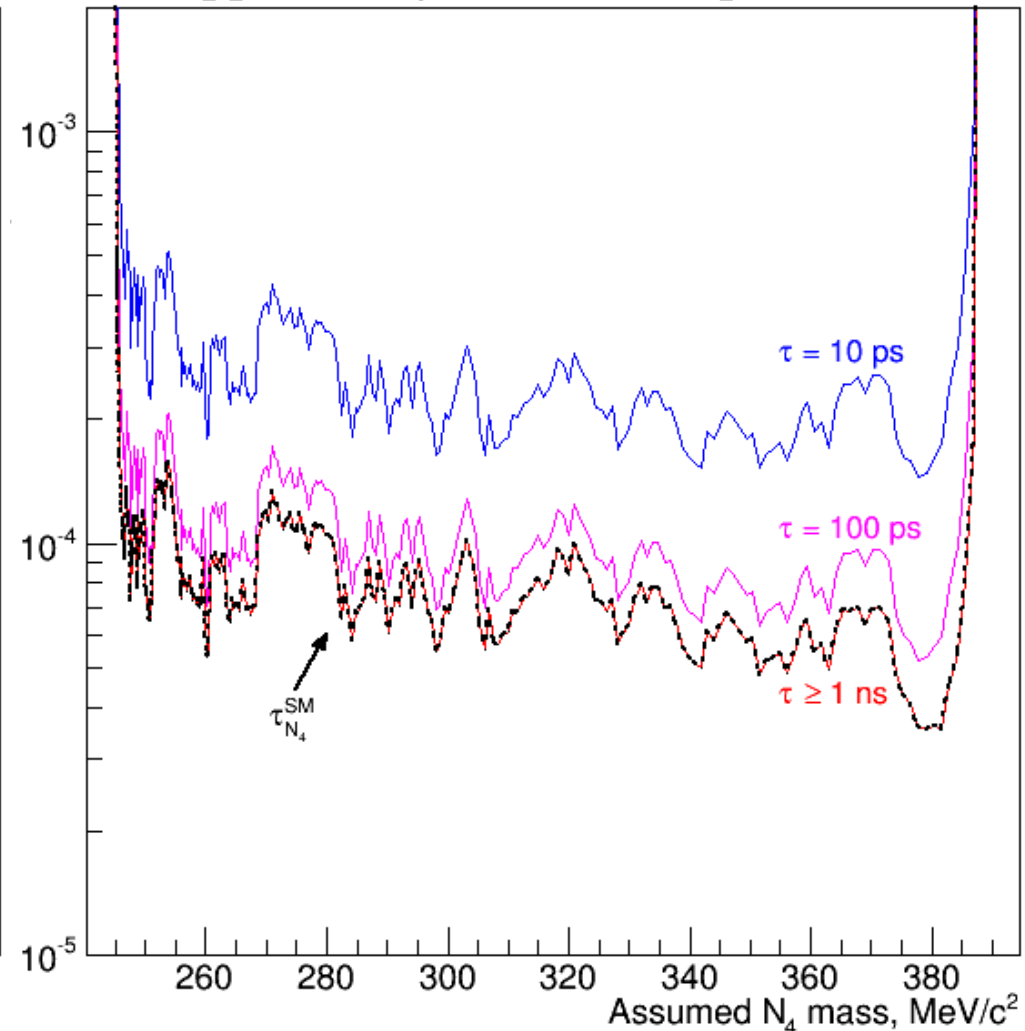
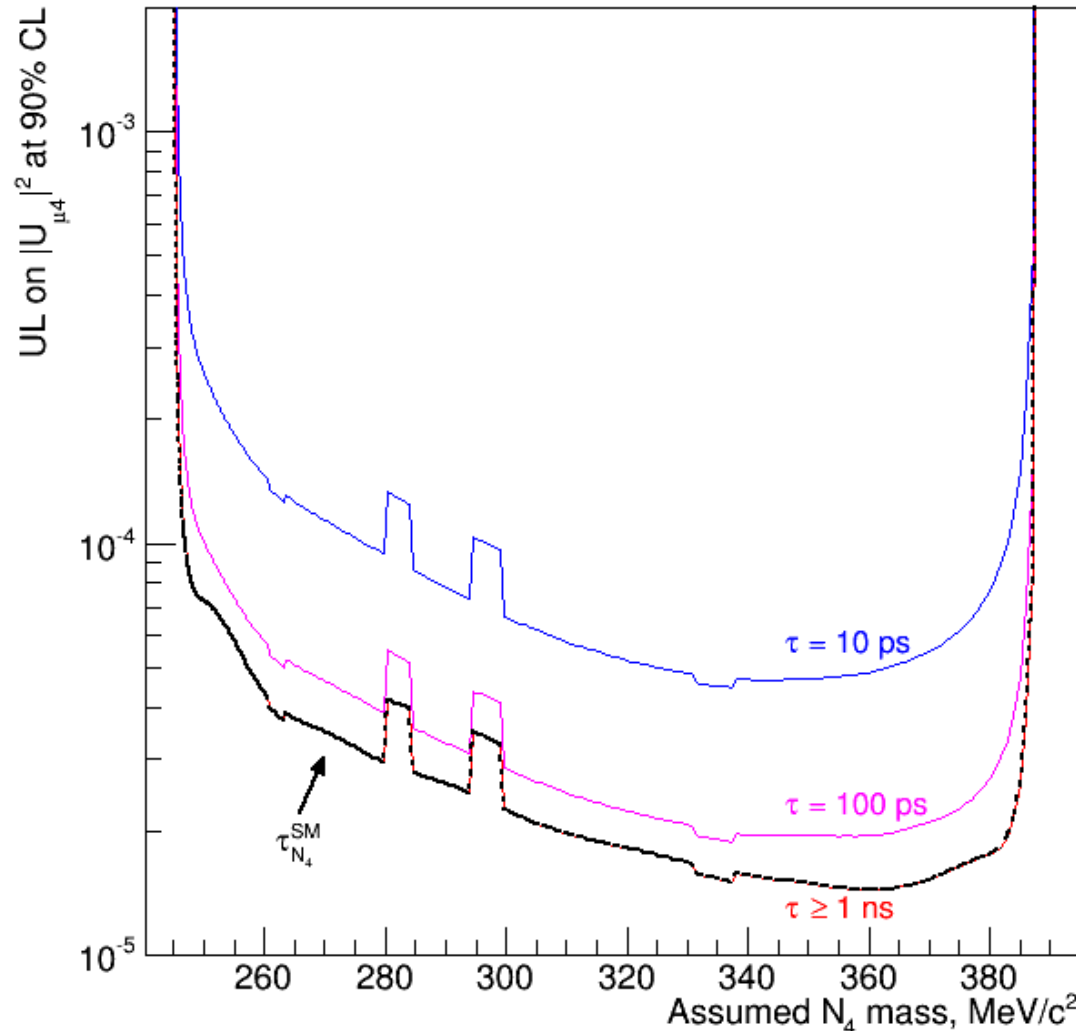
never exceeds  $+3\sigma$ : no signal observed

# Limits on $|U_{\mu 4}|^2$ from $K^\pm \rightarrow \mu^\pm N_4 (N_4 \rightarrow \pi\mu)$

$$|U_{\mu 4}|^2 = \frac{8\sqrt{2}\pi\hbar}{G_F^2 \sqrt{M_K \tau_K} f_K f_\pi |V_{us} V_{ud}|} \sqrt{\frac{\mathcal{B}(K^\pm \rightarrow \mu^\pm N_4) \mathcal{B}(N_4 \rightarrow \pi\mu)}{\tau_{N_4} M_{N_4}^5 \lambda^{\frac{1}{2}}(1, r_\mu^2, r_{N_4}^2) \lambda^{\frac{1}{2}}(1, \rho_\pi^2, \rho_\mu^2) \chi_{\mu\mu}}}$$

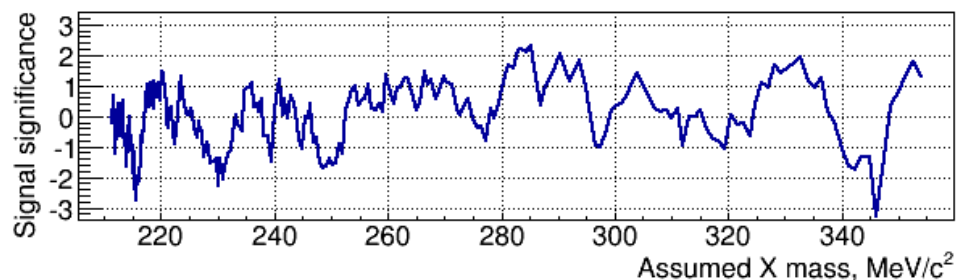
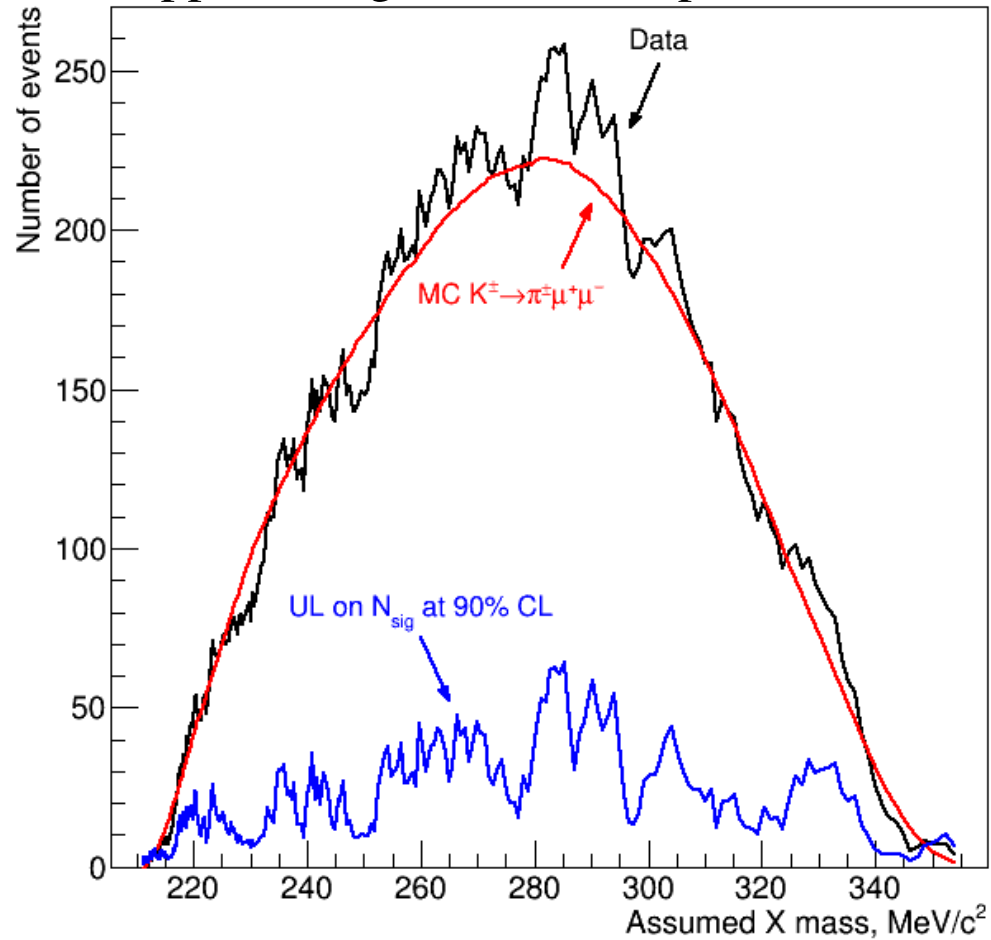
Same-sign muons sample (LNV)

Opposite-sign muons sample (LNC)

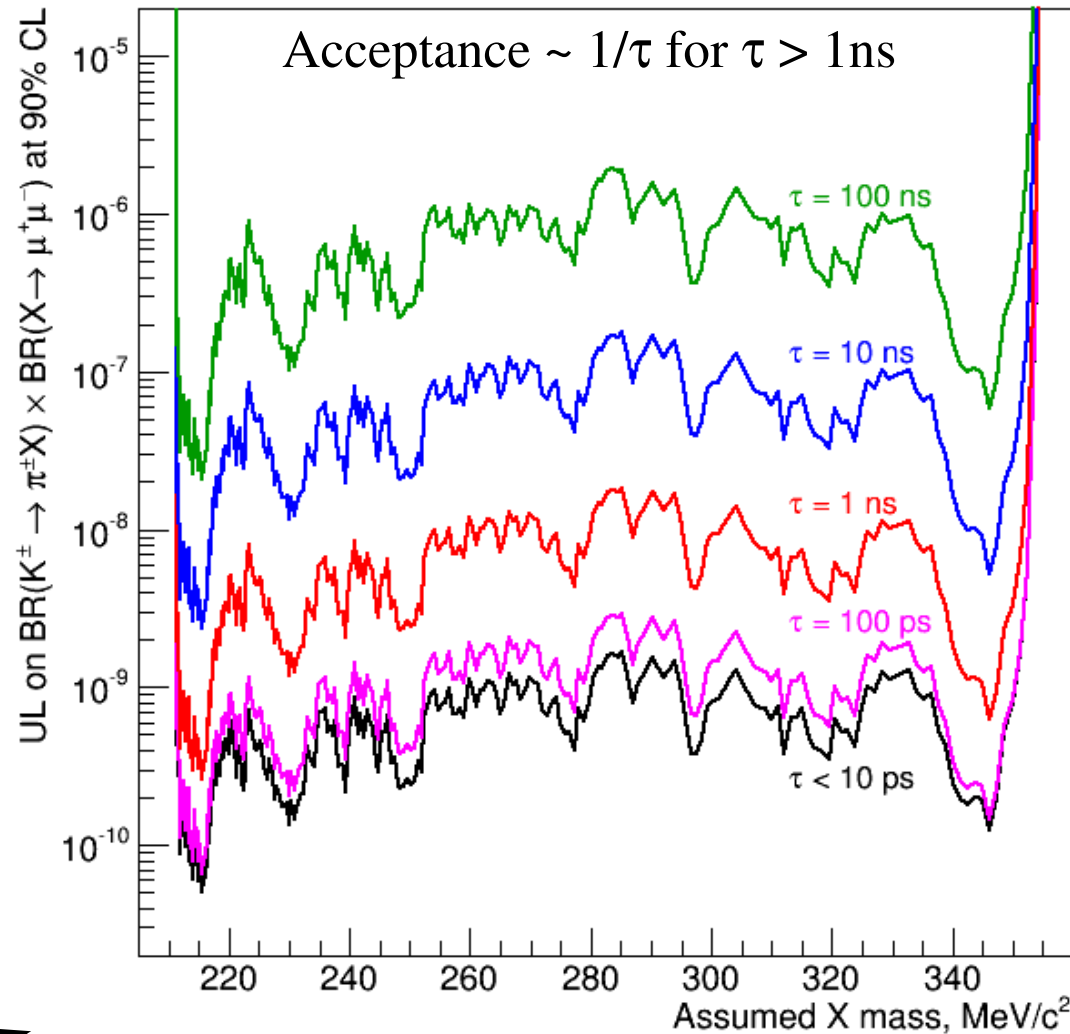


# Search for $K \rightarrow \pi^\pm X (X \rightarrow \mu^+ \mu^-)$ decays

Opposite-sign muons sample (LNC)



$$UL(BR(K^\pm \rightarrow \pi^\pm X) BR(X \rightarrow \mu^+ \mu^-)) = \frac{UL(N_{sig})}{N_K * Acceptance}$$

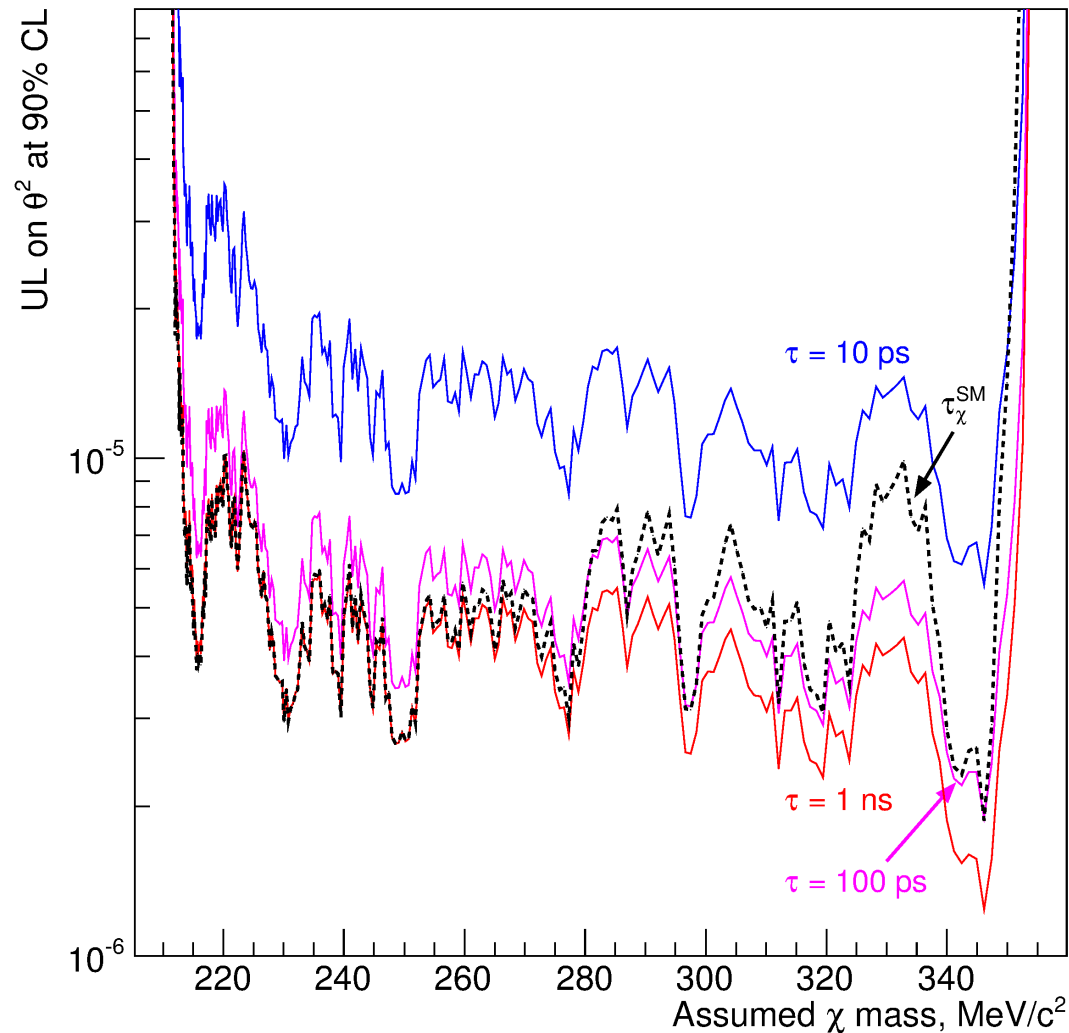


Statistical significance  $z = \frac{N_{obs} - N_{exp}}{\sigma(N_{obs}) \oplus \sigma(N_{exp})}$

never exceeds  $+3\sigma$ : no signal observed

# Limits on $\theta^2$ from $K^\pm \rightarrow \pi^\pm X (X \rightarrow \mu^+ \mu^-)$

$$\theta^2 = \sqrt{\frac{8\pi \hbar v^2}{\alpha_\chi}} \sqrt{\frac{\mathcal{B}(K^\pm \rightarrow \pi^\pm \chi) \mathcal{B}(\chi \rightarrow \mu^+ \mu^-)}{\tau_\chi M_\chi^3 \lambda^{\frac{1}{2}}(1, r_\pi^2, r_\chi^2) \lambda^{\frac{1}{2}}(1, \tilde{\rho}_\mu^2, \tilde{\rho}_\mu^2) \tilde{\chi}_{\mu\mu}}}$$





# Prospects for the NA62 experiment

## Search for Lepton Number Violation – Majorana neutrinos

- Main background:  $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$  with 2  $\pi^\pm \rightarrow \mu^\pm \nu$  decays (one within the Spectrometer)

- Sensitivity:

$$\left. \begin{array}{l} \text{UL on BR}(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) \\ \text{UL on BR}(K^\pm \rightarrow \mu^\pm N_4) \times \text{BR}(N_4 \rightarrow \pi^\mp \mu^\pm) \end{array} \right\} \sim \frac{1}{N_K * \text{Acceptance}}$$

## Search for resonances in $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$ decays

- Main background:  $K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$  (irreducible)  $\rightarrow$  Limited sensitivity

$$\left. \begin{array}{l} \text{UL on BR}(K^\pm \rightarrow \mu^\pm N_4) \times \text{BR}(N_4 \rightarrow \pi^\pm \mu^\mp) \\ \text{UL on BR}(K^\pm \rightarrow \pi^\pm X) \times \text{BR}(X \rightarrow \mu^+ \mu^-) \end{array} \right\} \sim \frac{\sqrt{\text{BR}(K^\pm \rightarrow \pi^\pm \mu^+ \mu^-)}}{\sqrt{N_K * \text{Acceptance}}} \sqrt{\frac{\sigma(M_{res})}{m_K - (m_\pi + 2m_\mu)}}$$

## NA62 expectations (from C. Parkinson numbers):

$$\left. \begin{array}{l} N_{NA62}(K_{\pi\mu\mu}) \sim 7 \times N_{NA48/2}(K_{\pi\mu\mu}) \\ \text{Acc}_{NA62}(K_{\pi\mu\mu}) \sim 0.8 \times \text{Acc}_{NA48/2}(K_{\pi\mu\mu}) \\ \sigma_{NA62}(M_{\pi\mu\mu}) \sim 0.5 \times \sigma_{NA48/2}(M_{\pi\mu\mu}) \end{array} \right\} \begin{array}{l} \text{SES}_{NA62}(\text{LNV}) \sim 0.2 \times \text{SES}_{NA48/2}(\text{LNV}) \\ \text{SES}_{NA62}(\text{LNC}) \sim 0.3 \times \text{SES}_{NA48/2}(\text{LNC}) \end{array}$$

# Conclusions

The NA48/2 experiment at CERN was exposed to  $\sim 2 \times 10^{11}$   $K^\pm$  decays in 2003-2004

• **NA48/2 results presented:** [[Batley et al., PLB 769 \(2017\) 67](#)]

- **Search for LNV  $K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm$  decay:**

•  **$BR(K^\pm \rightarrow \pi^\mp \mu^\pm \mu^\pm) < 8.6 \times 10^{-11}$  @ 90% CL [World Best Limit]**

• Factor of 10 improvement with respect to previous best limit [ $1.1 \times 10^{-9}$  @ 90% CL]

- **Search for  $K^\pm \rightarrow \mu^\pm N_4 (N_4 \rightarrow \pi^\mp \mu^\pm)$  decays [Majorana neutrinos]**

• Limits on BR products of the order of  $10^{-10}$  for neutrino lifetimes  $< 100$  ps

- **Search for  $K^\pm \rightarrow \mu^\pm N_4 (N_4 \rightarrow \pi^\pm \mu^\mp)$  decays [LNC heavy neutrinos]**

• Limits on BR products of the order of  $10^{-9}$  for neutrino lifetimes  $< 100$  ps

- **Search for  $K \rightarrow \pi^\pm X (X \rightarrow \mu^+ \mu^-)$  decays [Inflatons, ...]**

• Limits on BR products of the order of  $10^{-9}$  for resonance lifetimes  $< 100$  ps

• **Prospects for the new NA62 experiment (See next talk by C. Parkinson):**

• NA62 will collect the world-largest  $K^+$  decay sample ( $\sim 10^{13}$ ) in 3 years of data taking

• Major beam and detector upgrades for  $K^+ \rightarrow \pi^+ \bar{\nu} \nu$ : improved performances

• Possible improvements to the present limits by a factor  $\sim \times 3-5$