

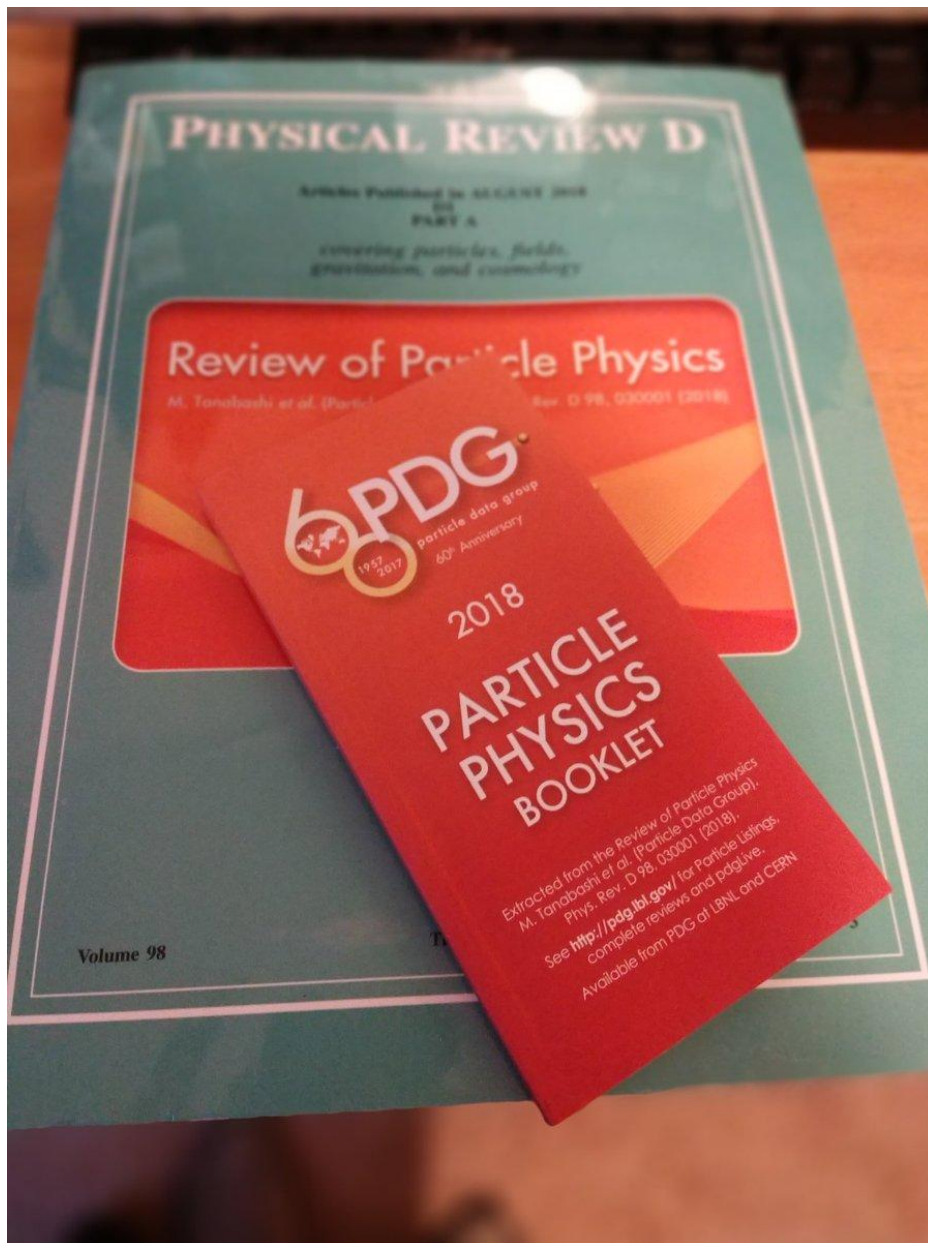
Spectroscopy

Hadron physics

Outline

- Lecture 1: Baryon spectroscopy
- Lecture 2: Meson spectroscopy
- Lecture 3: How to discover a particle

The Bible

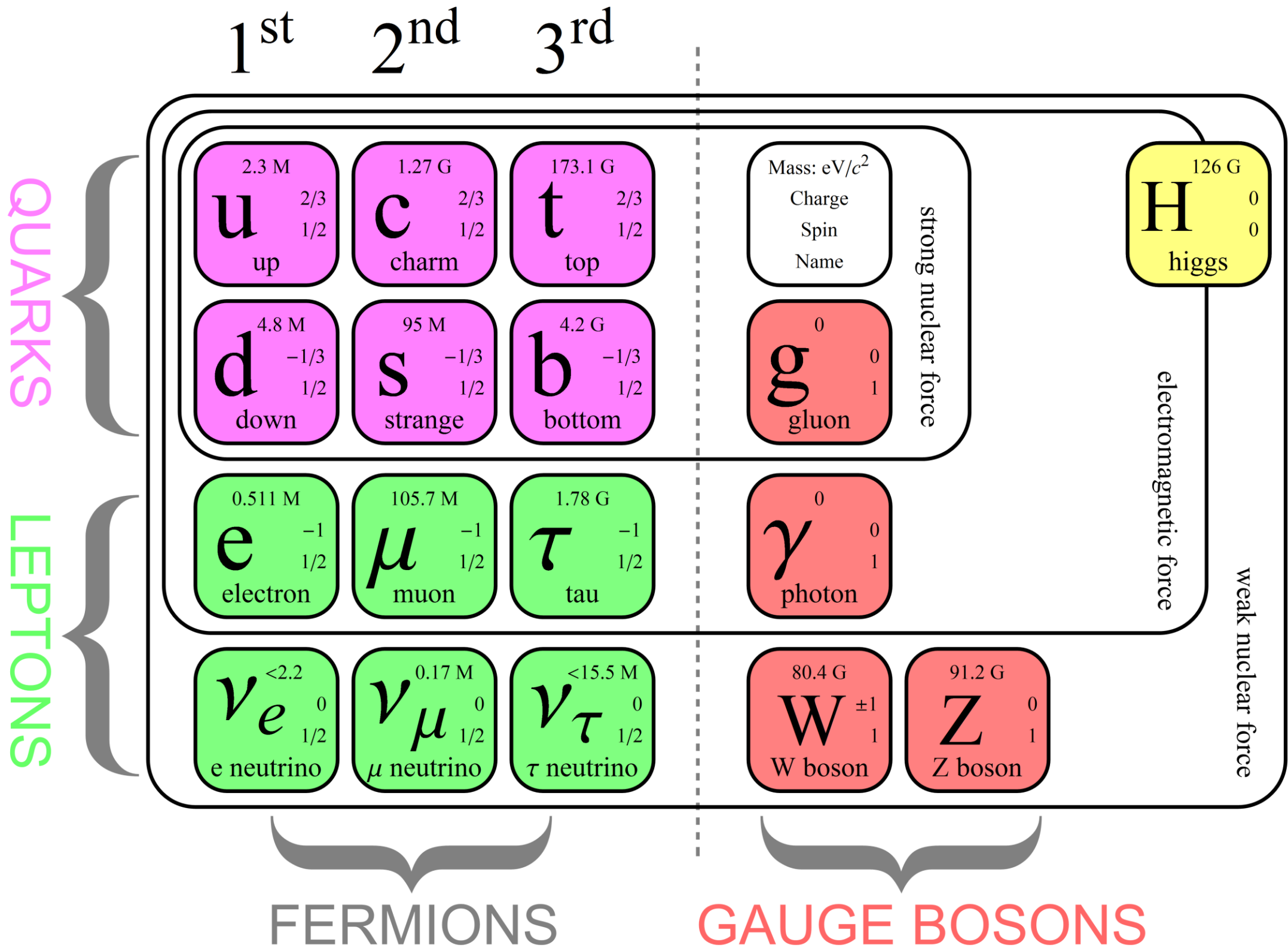


<http://pdg.lbl.gov/>

Reviews, Tables & Plots	
R.L. Workman <i>et al.</i> (Particle Data Group), <i>Prog. Theor. Exp. Phys.</i> 2022 , 083C01 (2022) and 2023 update	
Files can be downloaded directly by clicking on the icon: 	
Expand/Collapse All	
Introduction, History plots, Online information	
Introduction	
History plots (rev.)	
Authors	
Online particle physics information (rev.)	Interactive version 
Constants, Units, Atomic and Nuclear Properties	
Standard Model and Related Topics	
9 Quantum chromodynamics (rev.)	
10 Electroweak model and constraints on new physics	
11 Higgs boson physics, status of (rev.)	
12 CKM quark-mixing matrix	
13 CP violation in the quark sector (rev.)	
14 Neutrino masses, mixing, and oscillations (rev.)	
15 Quark model (rev.)	
16 Heavy-quark and soft-collinear effective theory	
17 Lattice quantum chromodynamics (rev.)	
18 Structure functions (rev.)	
19 Fragmentation functions in e^+e^- , ep, and pp collisions	
20 High energy soft QCD and diffraction (rev.)	
Tests of conservation laws (rev.)	
Astrophysics and Cosmology	
21 Experimental tests of gravitational theory (rev.)	
22 Big-Bang cosmology (rev.)	
23 Inflation (rev.)	
24 Big-Bang nucleosynthesis (rev.)	
25 Cosmological parameters (rev.)	
26 Neutrinos in cosmology (rev.)	
27 Dark matter (rev.)	
28 Dark energy (rev.)	
29 Cosmic microwave background (rev.)	
30 Cosmic rays (rev.)	

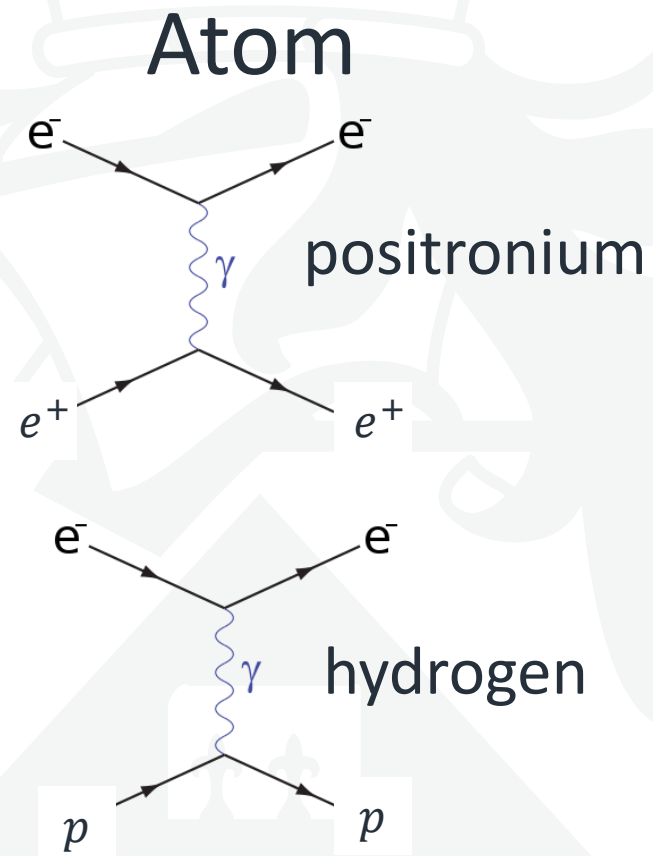
Latest information about particles (masses, widths, decays)
Common information

Standard Model



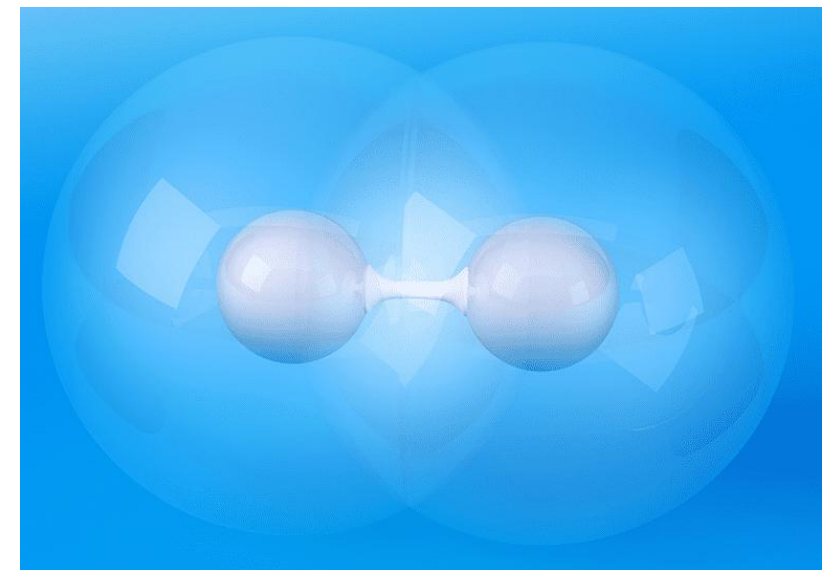
States in Standard model

Electromagnetic force



Photon couples to charge

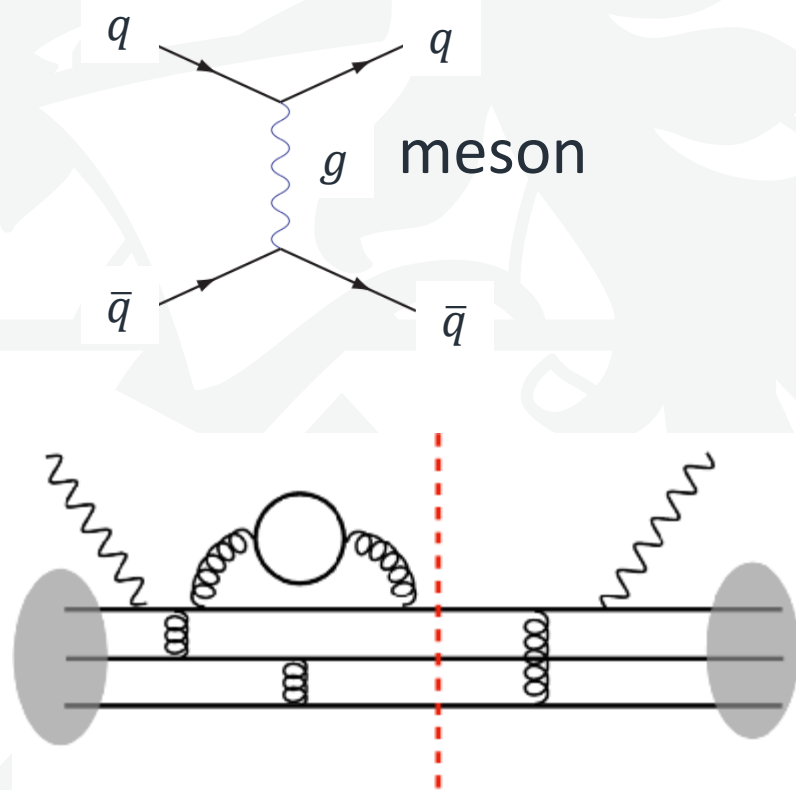
Molecule



Two charge neutral objects
Residual force

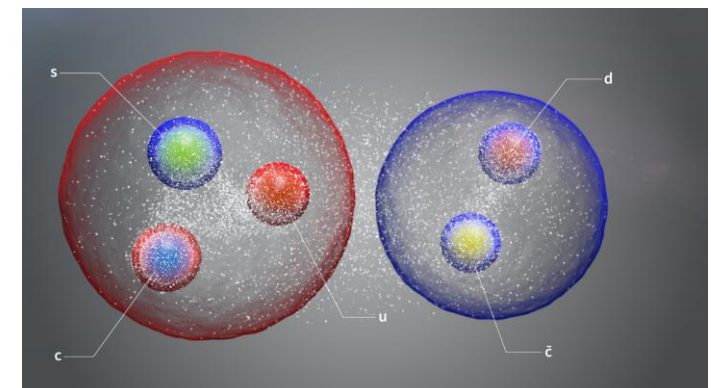
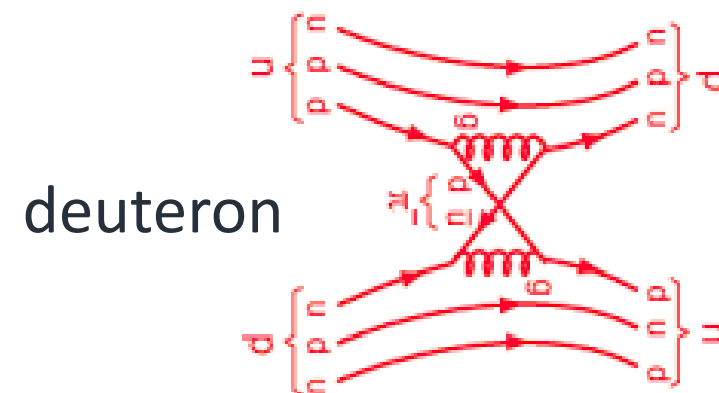
Strong force

“Atom” analogue



Gluon couples to charge
Mesons, baryons....
Colour components bound
by colour force

Molecule analogue



Two colour-neutral objects
Residual force
(meson-meson, meson baryon, baryon-
baryon molecules)
All nuclei are molecules

Force	Strength	Theory	Mediator
Strong	10	Chromodynamics	Gluon
Electromagnetic	10^{-2}	Electrodynamics	Photon
Weak	10^{-13}	Flavordynamics	W and Z
Gravitational	10^{-42}	Geometrodynamics	Graviton

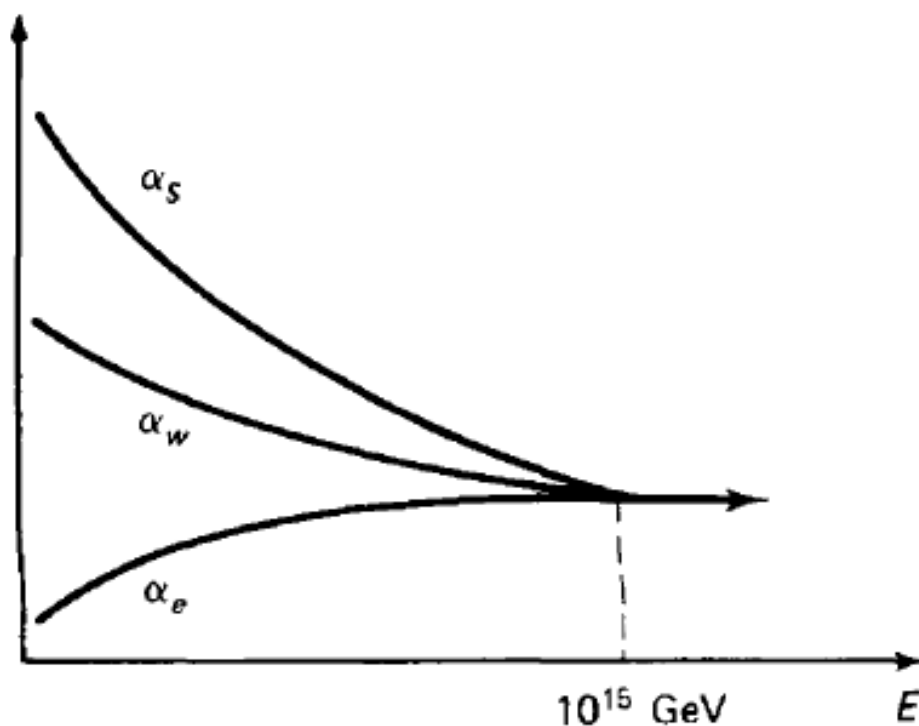
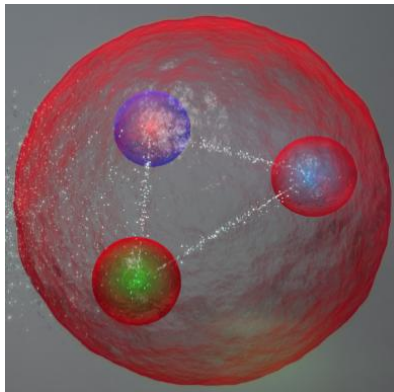


Figure 2.5 Evolution of the three fundamental coupling constants.

Spin

- Particles have spin – consequences for how they can assemble

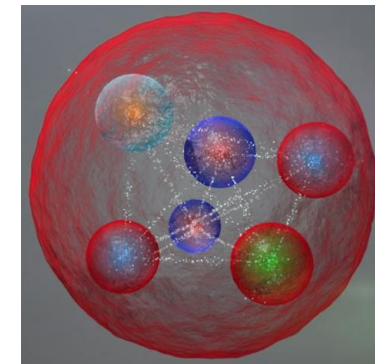


Half-integer spin (Fermion)

e.g. Proton, neutron, electron,...

Pauli exclusion principle:

Identical Fermions **cannot** occupy the same quantum state



Integer spin (Boson)

e.g. Photon, pi-meson, d^*

Bose-Einstein Condensate:

Identical Bosons **want to** occupy same quantum state !!

Spin

Fermions
(Half-integer spin)



UNIVERSITY
of York

Bosons
Integer spin



Particles and antiparticles

$$\text{Quark } J^P = \frac{1}{2}^+ \quad \text{Antiquark } J^P = ?$$

Spin^{Parity}

Particles and antiparticles

$$\text{Quark } J^P = \frac{1}{2}^+$$

$$\text{Antiquark } J^P = \frac{1}{2}^-$$

Spin^{Parity}

$$\text{Lepton } J^P = \frac{1}{2}^+$$

$$\text{Antilepton } J^P = \frac{1}{2}^-$$

$$\text{Electron } (e^-) J^P = \frac{1}{2}^+$$

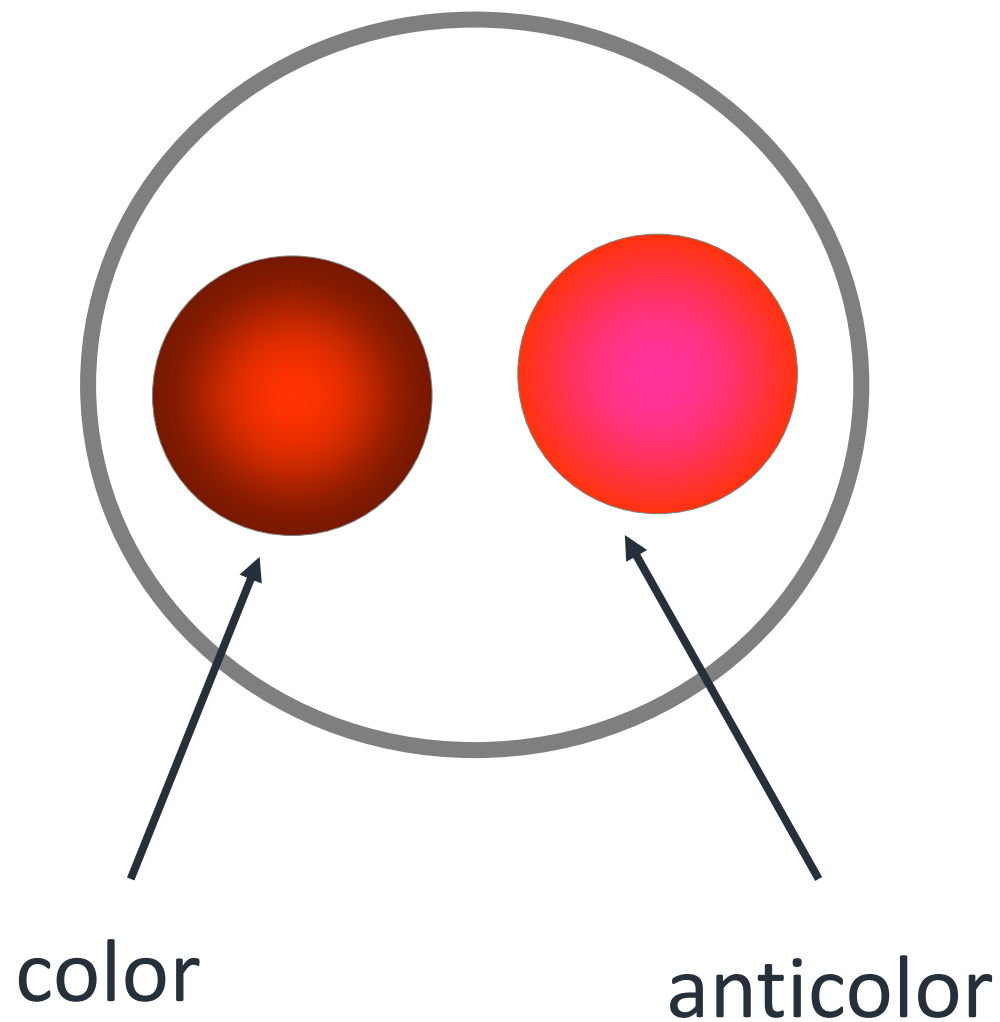
$$\text{Positron } (e^+) J^P = \frac{1}{2}^-$$

Mass(particle)=Mass(antiparticle)

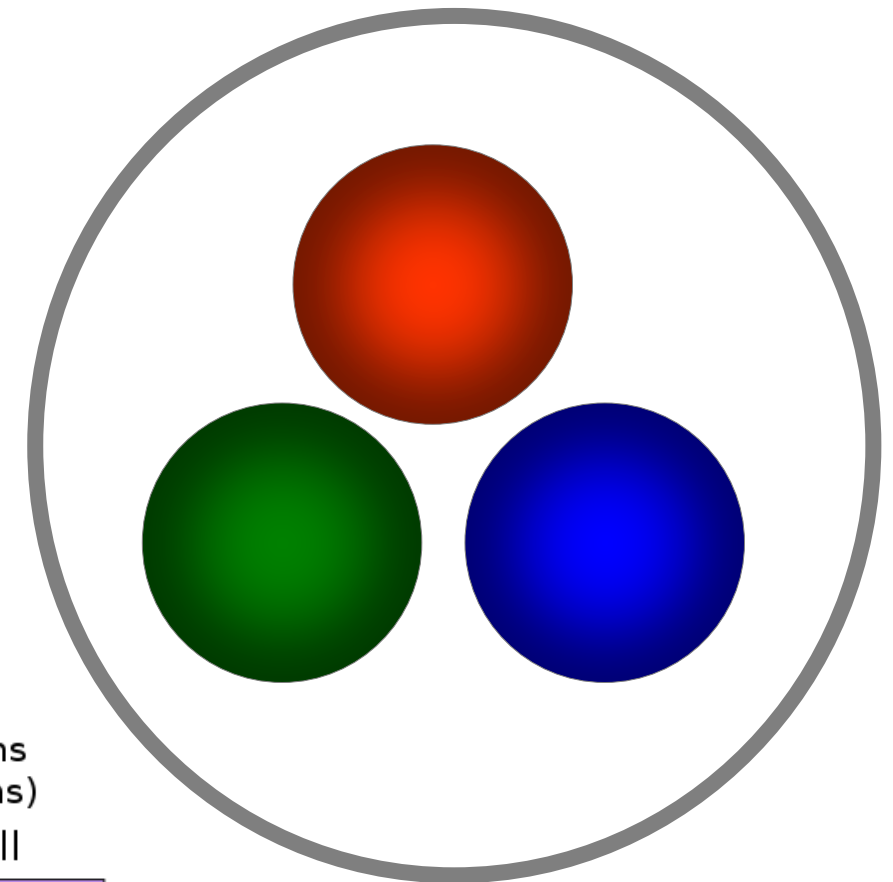
Baryon spectroscopy

Types of particles/resonances

Meson



Baryon



Three Generations
of Matter (Fermions)

	I	II	III
mass→	3 MeV	1.24 GeV	172.5 GeV
charge→	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$
spin→	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
name→	u up	c charm	t top
Quarks	6 MeV	95 MeV	4.2 GeV
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	d down	s strange	b bottom

Quarks

- fermions
- 3 colors
- Parity +1
- Constituent quarks:
 - $M_{u/d} \sim 300 \text{ MeV}$
 - $M_s \sim 500 \text{ MeV}$

Three Generations of Matter (Fermions)			
	I	II	III
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	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	down	strange	bottom

Constituent quarks

Flavour	B	J	I	I_3	s	Q/e
u	1/3	1/2	1/2	$+\frac{1}{2}$	0	$+\frac{2}{3}$
d	1/3	1/2	1/2	$-\frac{1}{2}$	0	$-\frac{1}{3}$
s	1/3	1/2	0	0	-1	$-\frac{1}{3}$

B – baryon number

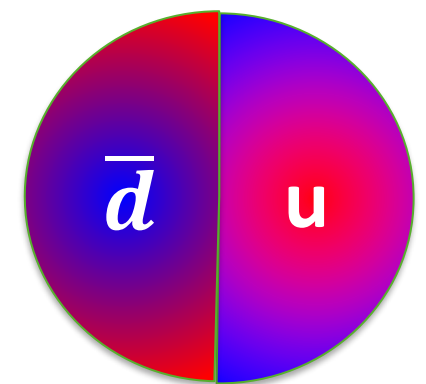
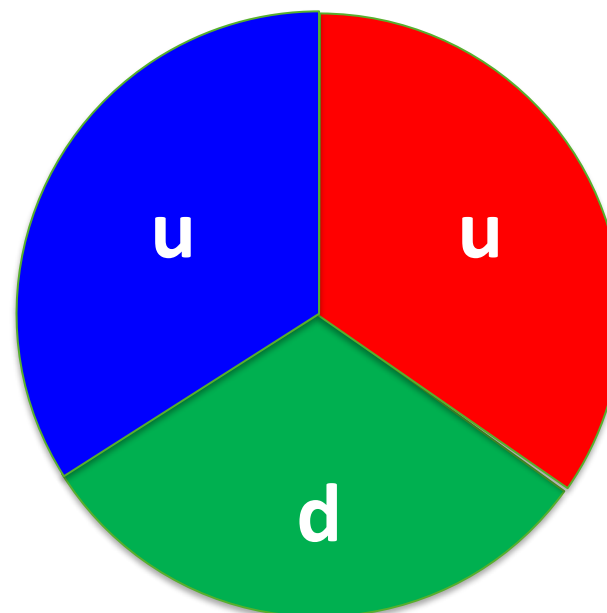
J – spin

I – isospin

I_3 - z-projection of isospin

s- strangeness

Q - charge



Quark states in SU(3) symmetry

$$\begin{pmatrix} u \\ d \\ s \end{pmatrix}$$

$$\text{Baryons: } 3 \otimes 3 \otimes 3 = 3 \otimes (6 \oplus \bar{3}) = \\ = 10_S \oplus 8_{M,S} \oplus 8_{M,A} \oplus 1_A$$

$$3 \otimes 3 = (6 \oplus \bar{3}):$$

6	$\bar{3}$
uu	
$\frac{1}{\sqrt{2}}(ud + du)$	$\frac{1}{\sqrt{2}}(ud - du)$
dd	
$\frac{1}{\sqrt{2}}(us + su)$	$\frac{1}{\sqrt{2}}(us - su)$
ss	
$\frac{1}{\sqrt{2}}(ds + sd)$	$\frac{1}{\sqrt{2}}(ds - sd)$

symmetric

antisymmetric

Quark states in SU(3) symmetry

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6	$\bar{3}$
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ss	
$\frac{1}{\sqrt{2}}(ds + sd)$	$\frac{1}{\sqrt{2}}(ds - sd)$

symmetric

antisymmetric

Quark states in SU(3) symmetry



$\begin{pmatrix} u \\ d \\ s \end{pmatrix}$

Baryons: $3 \otimes 3 \otimes 3 = 3 \otimes (6 \oplus \bar{3}) = 10_S \oplus 8_{M,S} \oplus 8_{M,A} \oplus 1_A$

$6 \otimes 3 = (10 \oplus 8):$

symmetric

mixed

10
uuu
$\frac{1}{\sqrt{3}}(uud + udu + duu)$
$\frac{1}{\sqrt{3}}(udd + dud + ddu)$
ddd
$\frac{1}{\sqrt{3}}(uus + usu + suu)$
$\frac{1}{\sqrt{3}}(uss + sus + ssu)$
sss
$\frac{1}{\sqrt{3}}(dds + dsd + sdd)$
$\frac{1}{\sqrt{3}}(dss + sds + ssd)$
$\frac{1}{\sqrt{6}}(uds + usd + dus + sud + sdu + dsu)$

8
$\frac{1}{\sqrt{6}}((ud + du)u - 2uud)$
$\frac{1}{\sqrt{6}}((ud + du)d - 2ddu)$
$\frac{1}{\sqrt{6}}((us + su)u - 2uus)$
$\frac{1}{\sqrt{6}}((ds + sd)d - 2dds)$
$\frac{1}{\sqrt{6}}((us + su)s - 2ssu)$
$\frac{1}{\sqrt{6}}((ds + sd)s - 2ssd)$
$\frac{1}{2}((ds - sd)u + (us - su)d)$
$\frac{1}{\sqrt{12}}(2(ud - du)s + (us - su)d + (sd - ds)u)$

Quark states in SU(3) symmetry

$$\begin{pmatrix} u \\ d \\ s \end{pmatrix}$$

Baryons: $3 \otimes 3 \otimes 3 = 3 \otimes (6 \oplus \bar{3}) =$
 $= 10_S \oplus 8_{M,S} \oplus 8_{M,A} \oplus 1_A$

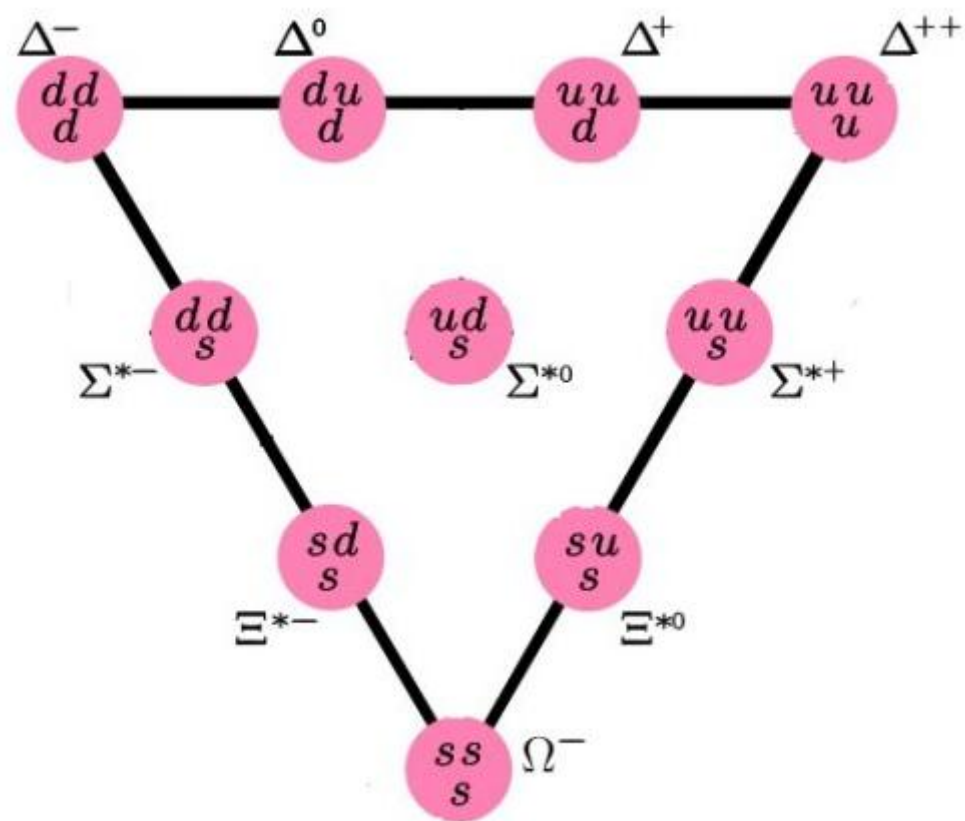
Decuplet

$\uparrow\uparrow\uparrow$

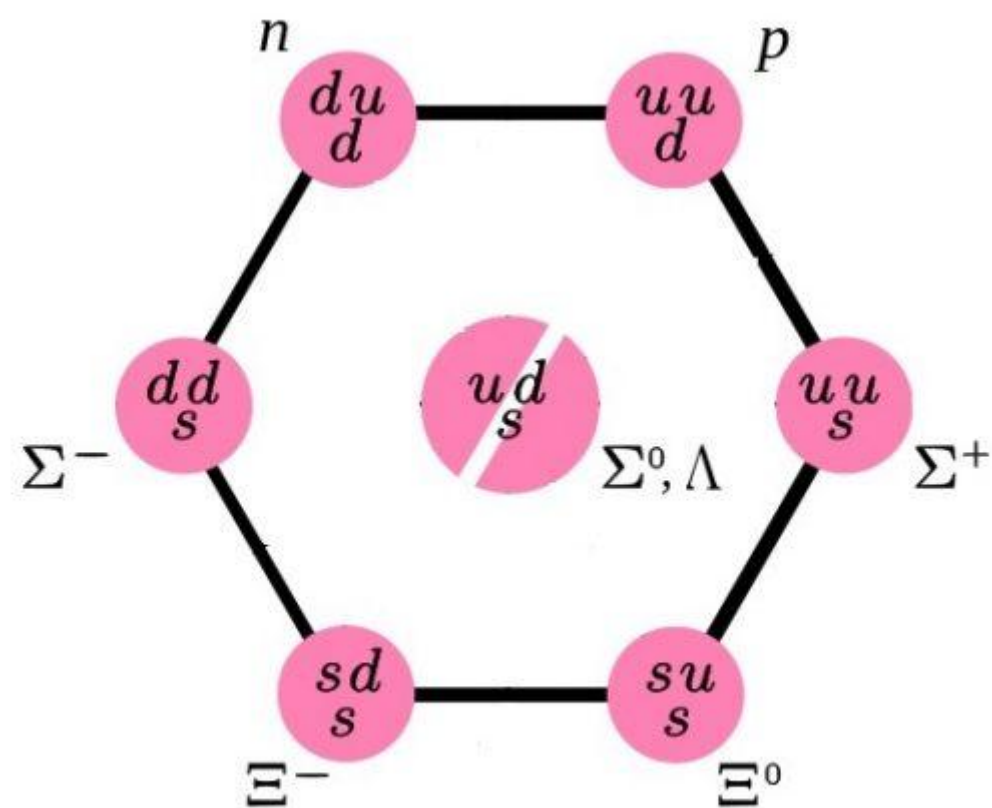
Octet

$\uparrow\uparrow\downarrow + \uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow$

$$J^P = \frac{3}{2}^+$$



$$J^P = \frac{1}{2}^+$$



Hyperfine splitting, $\uparrow\downarrow$ vs $\uparrow\uparrow$

- E-M force, magnetic moment interaction: $\Delta E = \mu \cdot B$
 $= \frac{2}{3} \mu_i \mu_j |\Psi(0)|^2 = \frac{2\pi}{3} \cdot \frac{\alpha}{m_i m_j} |\Psi(0)|^2 \sigma_i \sigma_j$



Pauli matrixes, spin

Hyperfine splitting, $\uparrow\downarrow$ vs $\uparrow\uparrow$

- E-M force, magnetic moment interaction: $\Delta E = \mu \cdot B$

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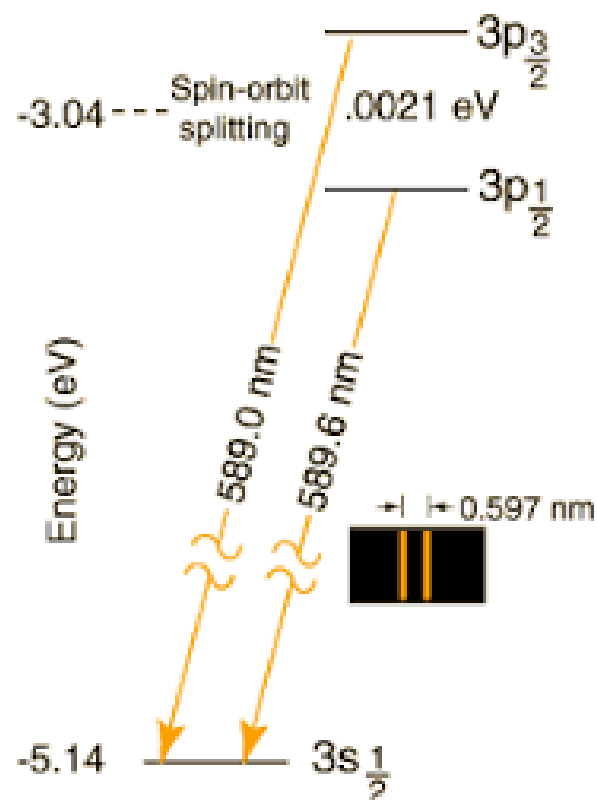


Pauli matrixes, spin

Nuclear



Atoms (Na doublet)

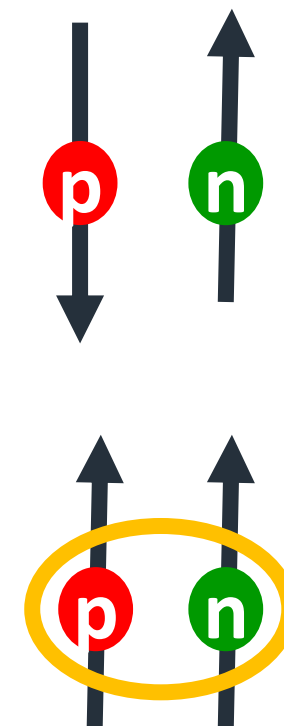


"Demon deuteron"

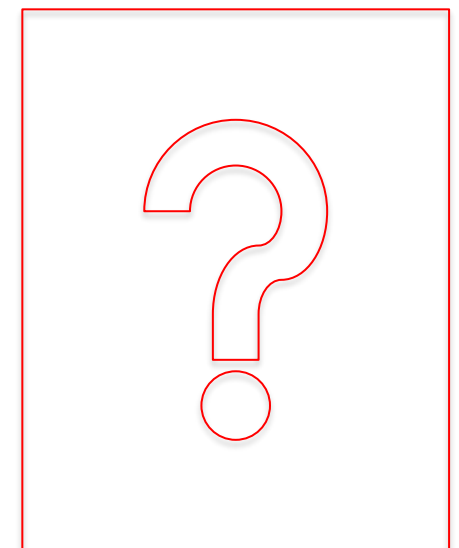
Threshold

2.2 MeV

deuteron



Quarks

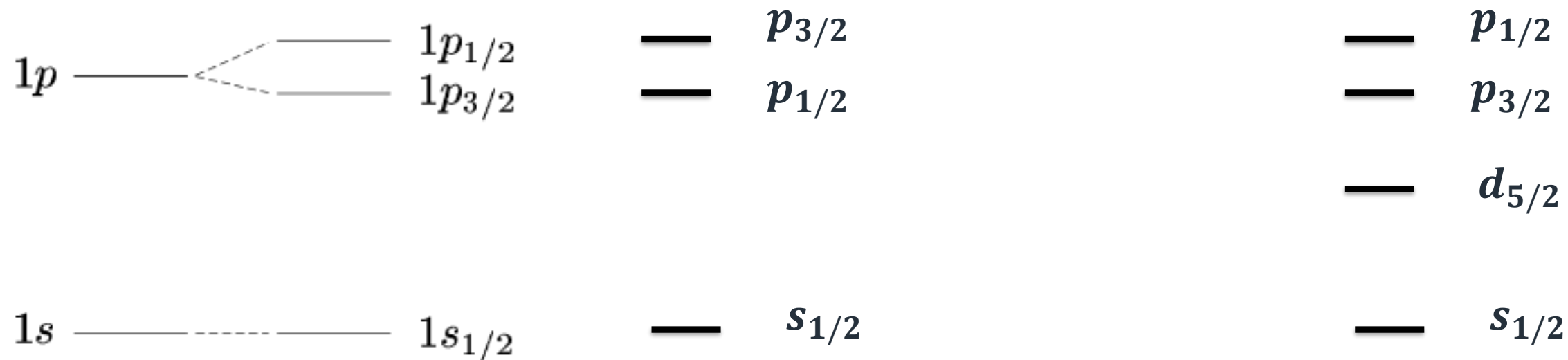


Hyperfine splitting, $\uparrow\downarrow$ vs $\uparrow\uparrow$

Nuclear

Photon/Gluon

Pion exchange $J^P = 0^-$



Same for $J^P = 0^-, J^P = 1^+$

$J^P = 0^+, J^P = 1^-$

$J^P = 2^+$

Hyperfine splitting, $\uparrow\downarrow$ vs $\uparrow\uparrow$

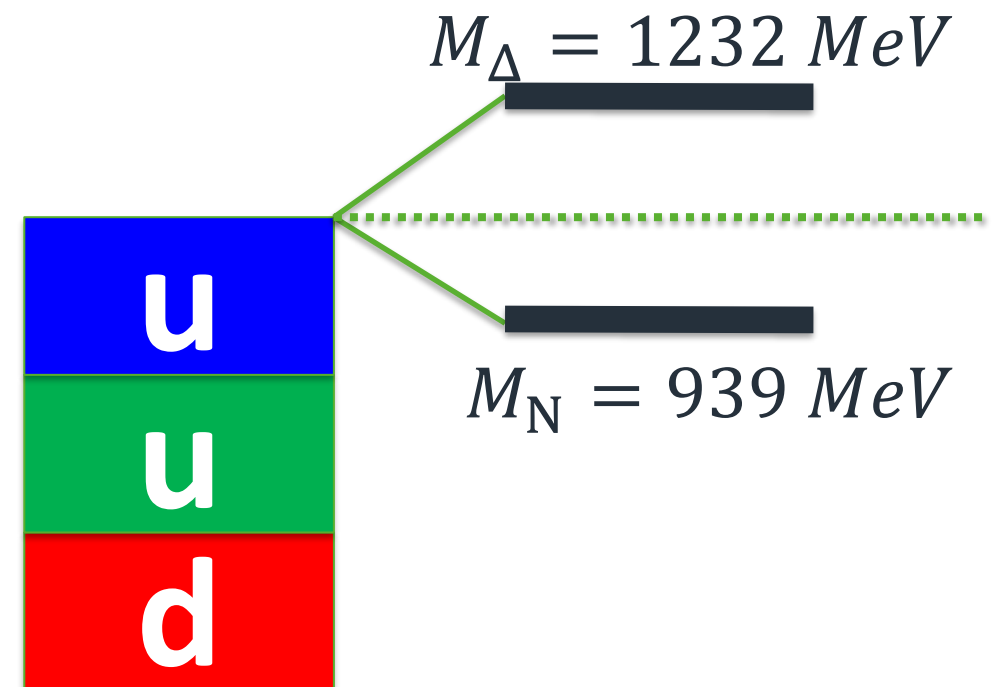
- $m_u \approx m_d = m_n = 363 \text{ MeV}$

- $m_s = 538 \text{ MeV}$

- $\frac{K}{m_n^2} = 50 \text{ MeV}$

- $\Delta E_\Delta = +3 \frac{K}{m_n^2}$
 $\Delta E_N = -3 \frac{K}{m_n^2}$

1089 MeV

- $\Delta^+(u \uparrow u \uparrow d \uparrow), M = 1232 \text{ MeV}$
- $p(u \uparrow u \downarrow d \uparrow), M = 939 \text{ MeV}$

Scales and interactions

Three Generations of Matter (Fermions)

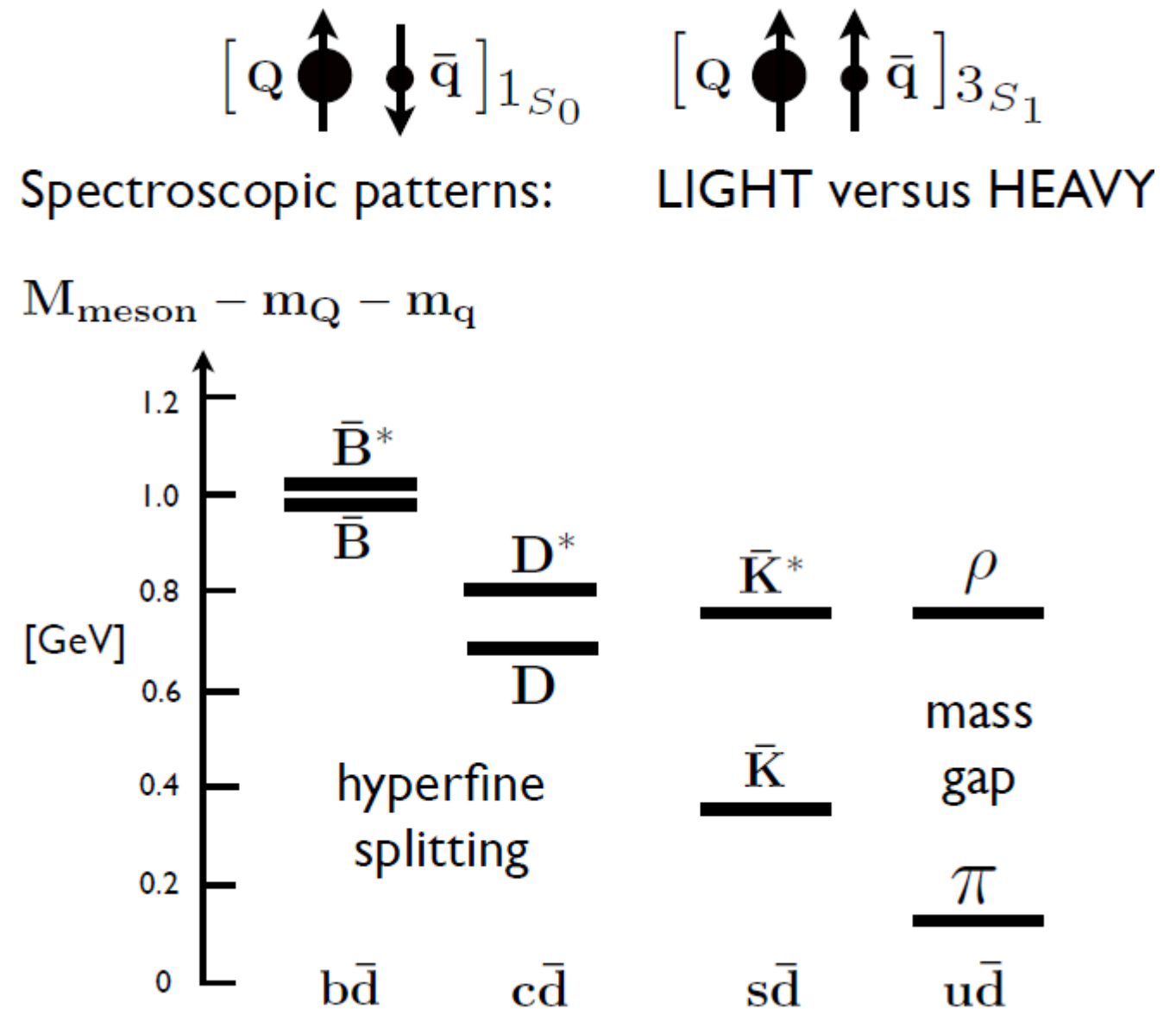
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name→	u up	c charm	t top
Quarks	6 MeV	95 MeV	4.2 GeV
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$
	d down	s strange	b bottom

$$M_B = 5279 \text{ MeV}$$

$$M_D = 1870 \text{ MeV}$$

$$M_K = 494 \text{ MeV}$$

$$M_\pi = 140 \text{ MeV}$$



Baryon summary table, PDG

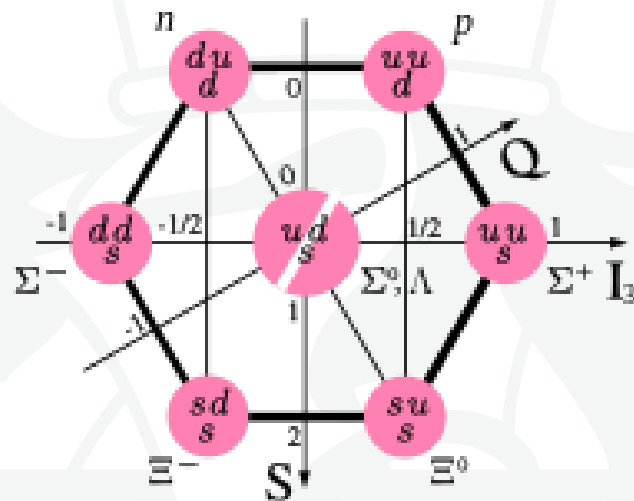
Number of 3- and 4- star Resonances

p	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	Σ^+	$1/2^+$	****	Ξ^0	$1/2^+$	****	Λ_c^+	$1/2^+$	****
n	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	***	Σ^0	$1/2^+$	****	Ξ^-	$1/2^+$	****	$\Lambda_c(2595)^+$	$1/2^-$	***
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	****	Σ^-	$1/2^+$	****	$\Xi(1530)$	$3/2^+$	****	$\Lambda_c(2625)^+$	$3/2^-$	***
$N(1520)$	$3/2^-$	****	$\Delta(1700)$	$3/2^-$	****	$\Sigma(1385)$	$3/2^+$	****	$\Xi(1620)$	*		$\Lambda_c(2765)^+$	*	
$N(1535)$	$1/2^-$	****	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1480)$	*		$\Xi(1690)$	***		$\Lambda_c(2880)^+$	$5/2^+$	***
$N(1650)$	$1/2^-$	****	$\Delta(1900)$	$1/2^-$	**	$\Sigma(1560)$	**		$\Xi(1820)$	$3/2^-$	***	$\Lambda_c(2940)^+$	***	
$N(1675)$	$5/2^-$	****	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1580)$	$3/2^-$	*	$\Xi(1950)$	***		$\Sigma_c(2455)$	$1/2^+$	****
$N(1680)$	$5/2^+$	****	$\Delta(1910)$	$1/2^+$	****	$\Sigma(1620)$	$1/2^-$	*	$\Xi(2030)$	$\geq \frac{5}{2}?$	***	$\Sigma_c(2520)$	$3/2^+$	***
$N(1685)$	*		$\Delta(1920)$	$3/2^+$	***	$\Sigma(1660)$	$1/2^+$	***	$\Xi(2120)$	*		$\Sigma_c(2800)$	***	
$N(1700)$	$3/2^-$	***	$\Delta(1930)$	$5/2^-$	***	$\Sigma(1670)$	$3/2^-$	****	$\Xi(2250)$	**		Ξ_c^+	$1/2^+$	***
$N(1710)$	$1/2^+$	***	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1690)$	**		$\Xi(2370)$	**		Ξ_c^0	$1/2^+$	***
$N(1720)$	$3/2^+$	****	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1730)$	$3/2^+$	*	$\Xi(2500)$	*		$\Xi_c^{'+}$	$1/2^+$	***
$N(1860)$	$5/2^+$	**	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1750)$	$1/2^-$	***				Ξ_c^0	$1/2^+$	***
$N(1875)$	$3/2^-$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1770)$	$1/2^+$	*	Ω^-	$3/2^+$	****	$\Xi_c(2645)$	$3/2^+$	***
$N(1880)$	$1/2^+$	**	$\Delta(2200)$	$7/2^-$	*	$\Sigma(1775)$	$5/2^-$	****	$\Omega(2250)^-$	***		$\Xi_c(2790)$	$1/2^-$	***
$N(1895)$	$1/2^-$	**	$\Delta(2300)$	$9/2^+$	**	$\Sigma(1840)$	$3/2^+$	*	$\Omega(2380)^-$	**		$\Xi_c(2815)$	$3/2^-$	***
$N(1900)$	$3/2^+$	***	$\Delta(2350)$	$5/2^-$	*	$\Sigma(1880)$	$1/2^+$	**	$\Omega(2470)^-$	**		$\Xi_c(2930)$	*	
$N(1990)$	$7/2^+$	**	$\Delta(2390)$	$7/2^+$	*	$\Sigma(1900)$	$1/2^-$	*				$\Xi_c(2980)$	***	
$N(2000)$	$5/2^+$	**	$\Delta(2400)$	$9/2^-$	**	$\Sigma(1915)$	$5/2^+$	****				$\Xi_c(3055)$	**	
$N(2040)$	$3/2^+$	*	$\Delta(2420)$	$11/2^+$	****	$\Sigma(1940)$	$3/2^+$	*				$\Xi_c(3080)$	***	
$N(2060)$	$5/2^-$	**	$\Delta(2750)$	$13/2^-$	**	$\Sigma(1940)$	$3/2^-$	***				$\Xi_c(3123)$	*	
$N(2100)$	$1/2^+$	*	$\Delta(2950)$	$15/2^+$	**	$\Sigma(2000)$	$1/2^-$	*				Ω_c^0	$1/2^+$	***
$N(2120)$	$3/2^-$	**				$\Sigma(2030)$	$7/2^+$	****				$\Omega_c(2770)^0$	$3/2^+$	***
$N(2190)$	$7/2^-$	****	Λ	$1/2^+$	****	$\Sigma(2070)$	$5/2^+$	*				Ξ_{cc}^+	*	
$N(2220)$	$9/2^+$	****	$\Lambda(1405)$	$1/2^-$	****	$\Sigma(2080)$	$3/2^+$	**				Λ_b^0	$1/2^+$	***
$N(2250)$	$9/2^-$	****	$\Lambda(1520)$	$3/2^-$	****	$\Sigma(2100)$	$7/2^-$	*				$\Lambda_b(5912)^0$	$1/2^-$	***
$N(2300)$	$1/2^+$	**	$\Lambda(1600)$	$1/2^+$	***	$\Sigma(2250)$		***				$\Lambda_b(5920)^0$	$3/2^-$	***
$N(2570)$	$5/2^-$	**	$\Lambda(1670)$	$1/2^-$	****	$\Sigma(2455)$		**				Σ_b	$1/2^+$	***
$N(2600)$	$11/2^-$	***	$\Lambda(1690)$	$3/2^-$	****	$\Sigma(2620)$		**				Σ_b^+	$3/2^+$	***
$N(2700)$	$13/2^+$	**	$\Lambda(1710)$	$1/2^+$	*	$\Sigma(3000)$		*				Ξ_b^0, Ξ_b^-	$1/2^+$	***
			$\Lambda(1800)$	$1/2^-$	***	$\Sigma(3170)$		*				$\Xi_b(5945)^0$	$3/2^+$	***
			$\Lambda(1810)$	$1/2^+$	***							Ω_b^-	$1/2^+$	***
			$\Lambda(1820)$	$5/2^+$	****									
			$\Lambda(1830)$	$5/2^-$	****									
			$\Lambda(1890)$	$3/2^+$	****									
			$\Lambda(2000)$	*										
			$\Lambda(2020)$	$7/2^+$	*									
			$\Lambda(2050)$	$3/2^-$	*									
			$\Lambda(2100)$	$7/2^-$	****									
			$\Lambda(2110)$	$5/2^+$	***									
			$\Lambda(2325)$	$3/2^-$	*									
			$\Lambda(2350)$	$9/2^+$	***									
			$\Lambda(2585)$	**										

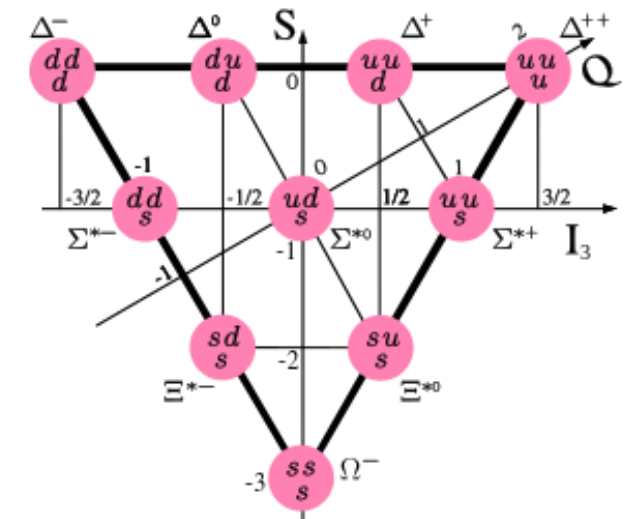
Baryon	2004	2020
N^*	15	21
Δ	10	12
Λ	14	14
Σ	10	9*
Ξ	6	6
Ω	2	2

* $\Sigma(2250)$ was downgraded

Baryons



Octet: N^* , Λ^* , Σ^* , Ξ^*
Decuplet: Δ^* , Σ^* , Ξ^* , Ω^*



	LQCD* ($M < 2M_\Omega$)	“Observed”, PDG	Counting based on N^* 's
N^*	62	21	21
Δ^*	38	12	21
Λ^*	71	14	21
Σ^*	66	9	42
Ξ^*	73	6	42
Ω^*	36	2	21

*R.G. Edwards et al, Phys.Rev.D 87 (2013) 5, 054506

Baryon Spectroscopy

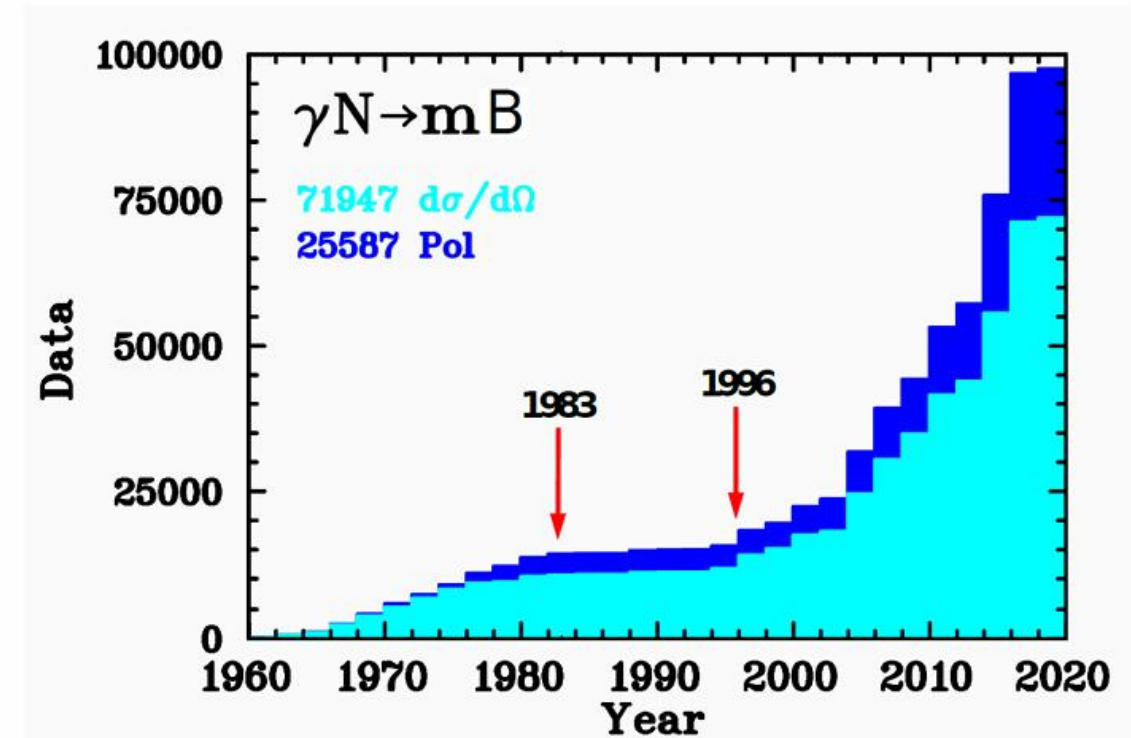
⇒ **Good understanding of the spectrum and properties of baryon resonances**

Experimentally:

Broad and strongly overlapping resonances

Important:

- Investigation of different final states
- Investigation of different production processes: πN , γN , $\gamma^* N$, Ψ , Ψ' -decays, ...
- Measurement of polarization observables (unambiguous PWA)



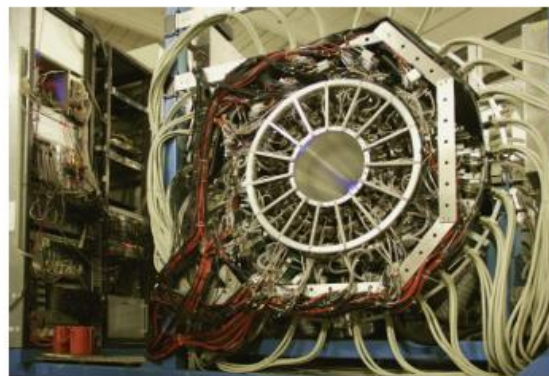
D. Ireland et al., Prog. Part. Nucl. Phys. 111 (2020) 103752

Recently: a lot of progress from photoproduction experiments:

CLAS (JLab),



CBELSA/TAPS (ELSA),



CBALL (MAMI),



LEPS (Spring-8), BGOOD (ELSA),
GlueX (JLab), ...

⇔ **polarized beam,
polarized target**

Double Polarization Experiments - Selected Results -

Circularly polarized photons, longitudinally polarized target

CBELSA/TAPS



PWAs:

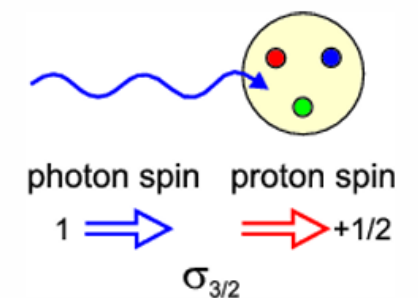
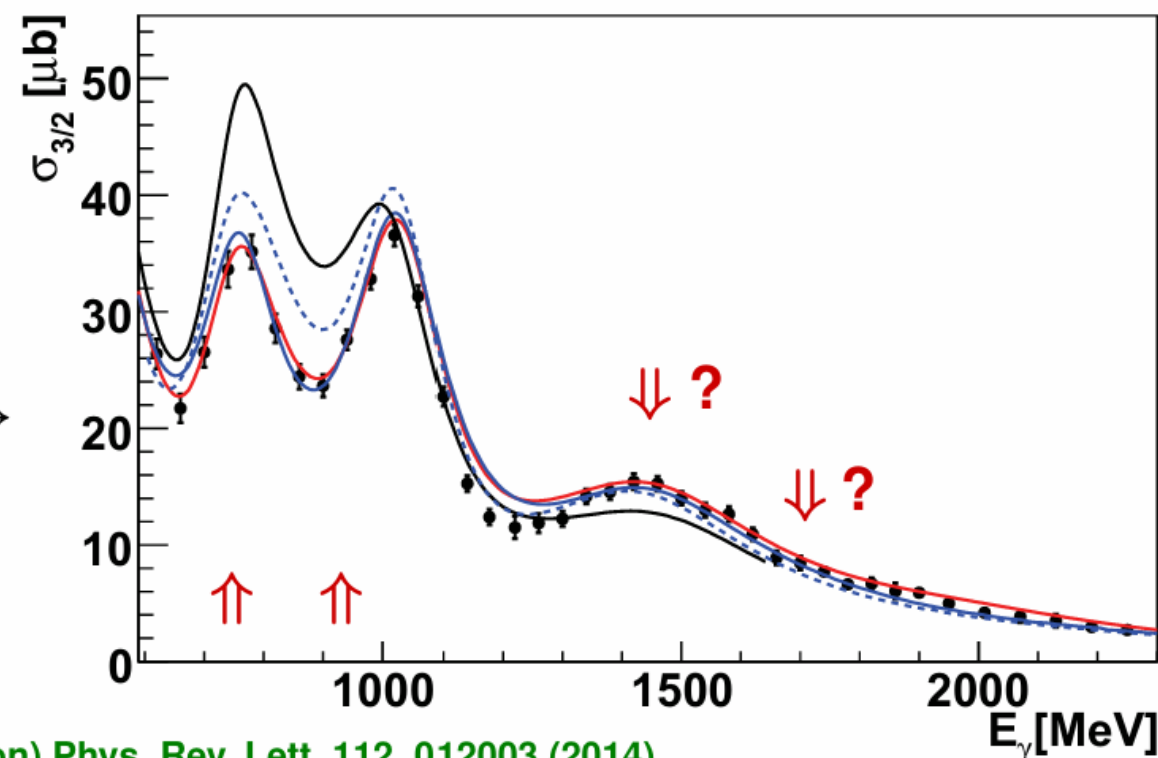
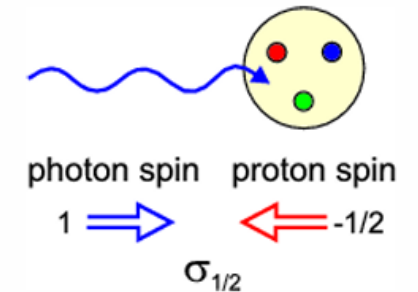
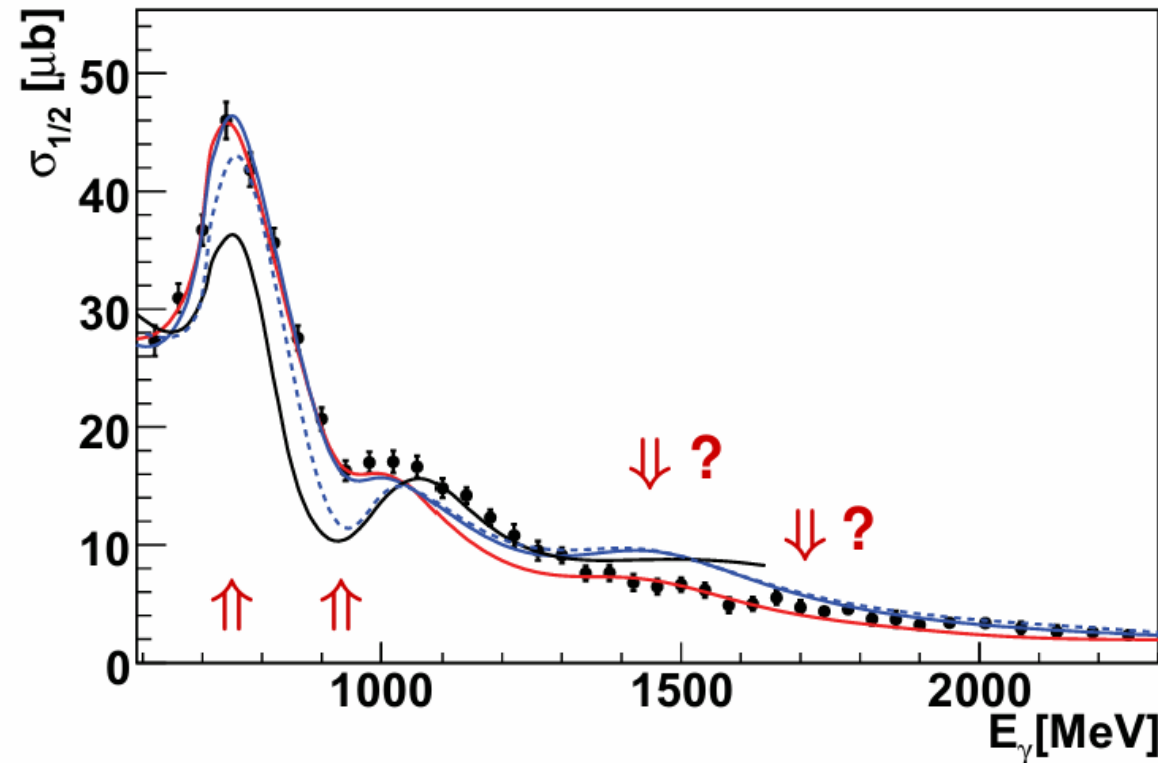
SAID (SN11, CM12), **MAID**

BnGa (2011-2)

↔ describe the
so far existing
photoproduction
data, but ...

large deviations
observed →

Differences even at low
energies where everything
was thought to be well
understood ... →



⇒
**Sensitivity
on high mass
resonances !**

M. Gottschall et al. (CBELSA/TAPS-collaboration) Phys. Rev. Lett. 112, 012003 (2014)

Results: The Spectrum of Baryon Resonances

Multi-channel Bonn-Gatchina PWA:

- ⇒ **Confirmation known resonances, better determination of their properties**
- ⇒ **New resonances observed**

	RPP 2010	our analyses	RPP'22 (2018-22)
N(1710)1/2 ⁺	***	*****	*****
N(1860)5/2⁺		*	**
N(1875)3/2⁻		***	***
N(1880)1/2⁺		***	***
N(1895)1/2⁻		*****	*****
N(1900)3/2⁺	**	*****	*****
N(2060)5/2⁻		***	***
N(2100)1/2 ⁺	*	***	***
N(2120)3/2⁻		***	***
Δ(1600)3/2⁺	***	***	*****
Δ(1900)1/2⁻	*	***	***
Δ(1940)3/2⁻	*	**	**
Δ(2200)7/2⁻	*	***	***

only examples shown

from 2000-2010 not one new baryon resonance was considered by the PDG

↔ **Results from photoproduction do enter the PDG and determine the properties of baryon resonances!**

before: almost entirely πN -elastic scattering and some π -photoproduction

At higher $\sqrt{s}$:

⇒ elastic cross section decreases

⇒ more and more inelastic channels open

Photoproduction provides access to the “inelastic channels”

⇒ **resonance properties**

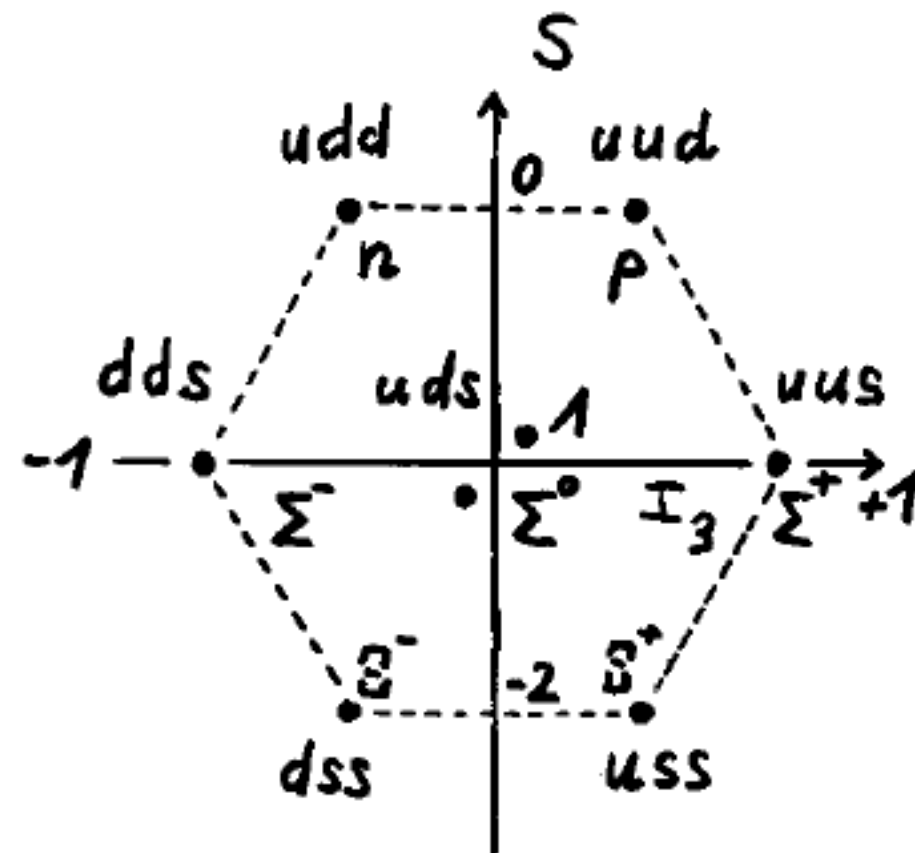
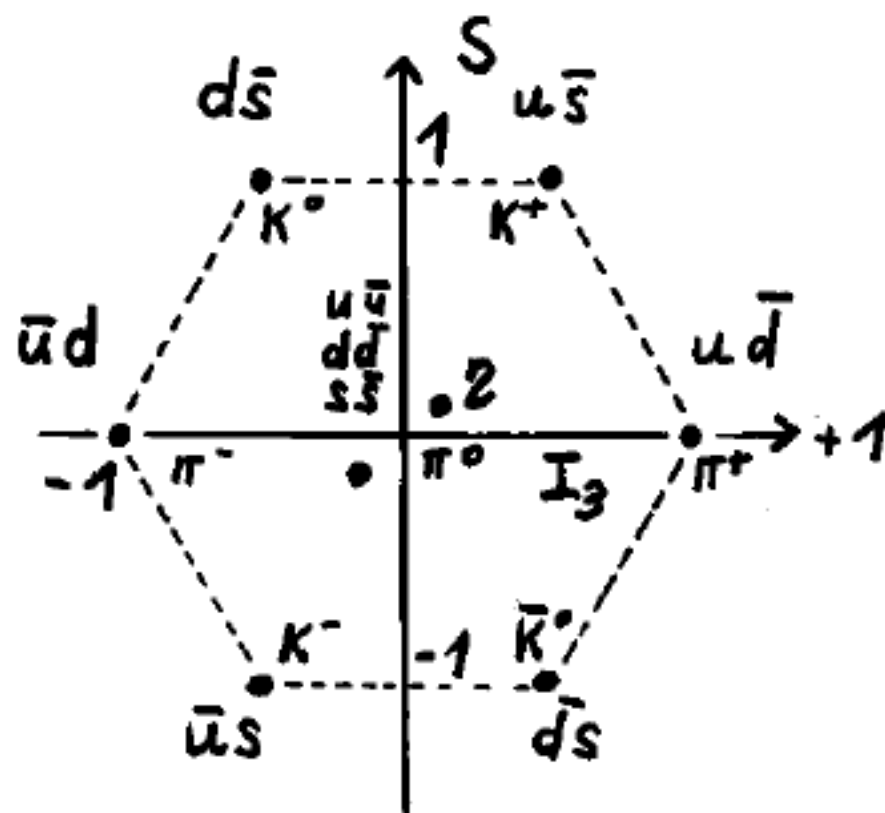
Excitations

The early days

Murray Gell Mann 1964

“A schematic model of baryons and mesons”

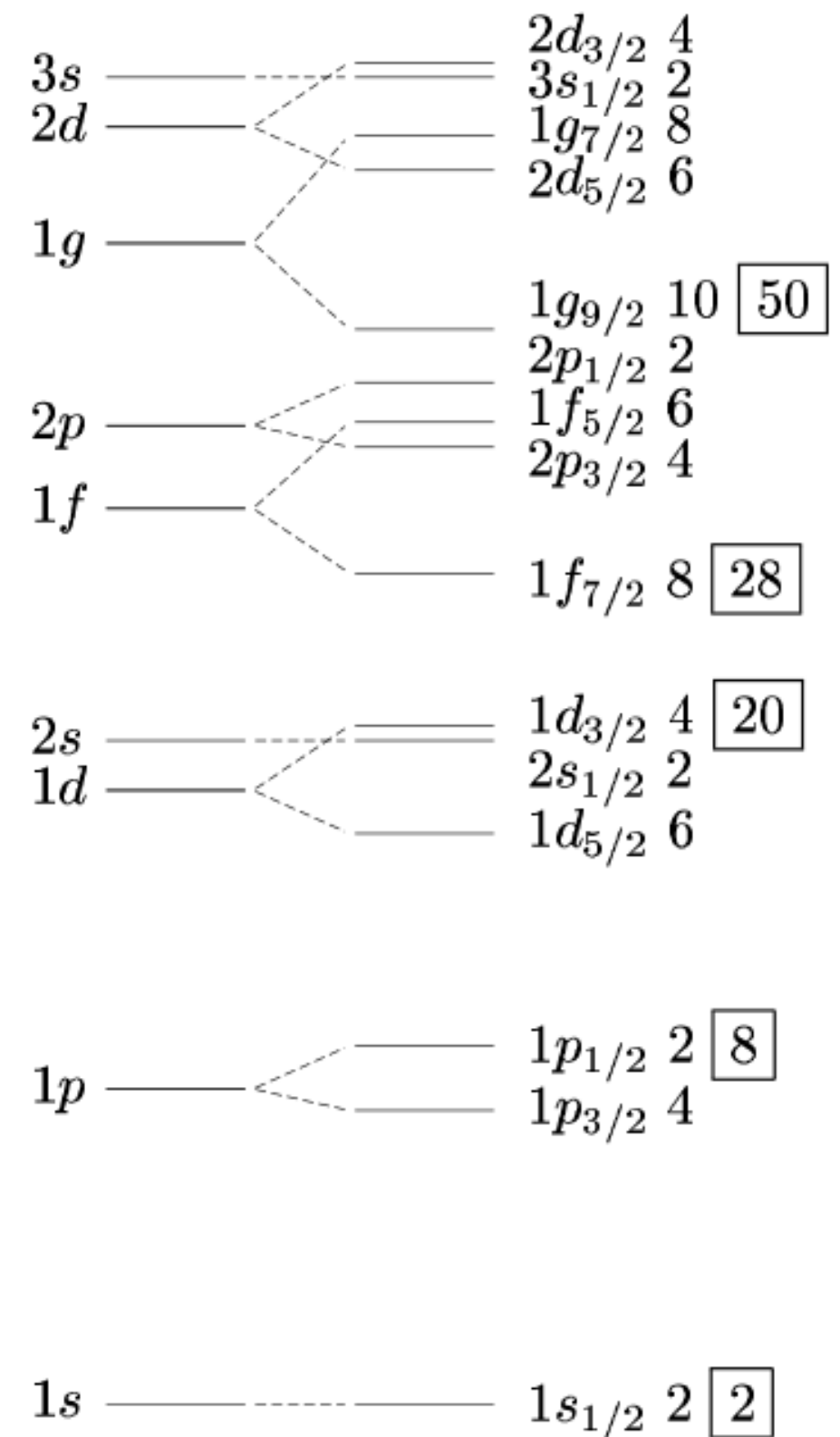
- ground state octets:



- Baryons are 3 quark systems
- Mesons are quark-antiquark systems

UNIVERSITY
of York

The diagram illustrates the potential wells for a proton and a neutron within a nucleus. A central vertical dashed line represents the axis of symmetry. The **Proton potential well** is shown as a black curve that is deep in the center and rises sharply at the edges. A dashed line above it, labeled "Coulomb repulsion adds to proton well potential", shows the additional energy barrier for protons. The **Neutron potential well** is shown as a red curve that is deeper than the proton well in the center and also rises at the edges. The area between the two wells is shaded pink.



Nucleon excited states?

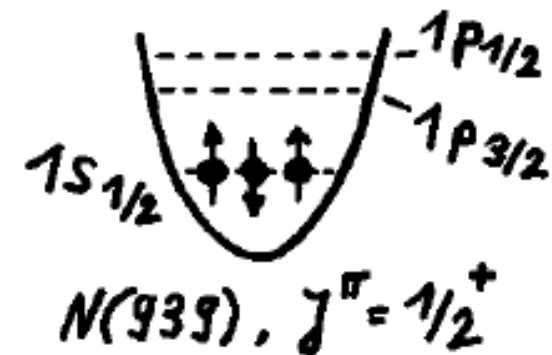
- the nucleon

$$P = (-1)^L$$

P – parity

L – angular momentum

ground state



excited states



$\Delta(1232)$
 $J^P = 3/2^+$



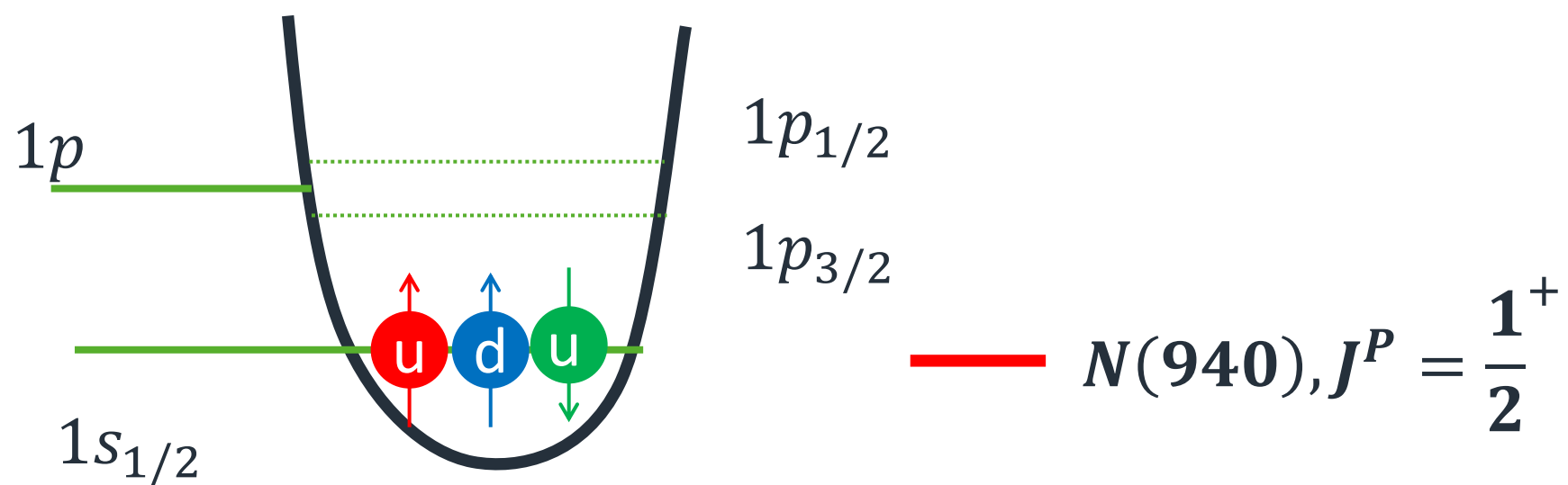
$D_{13}(1520)$
 $J^P = 3/2^-$



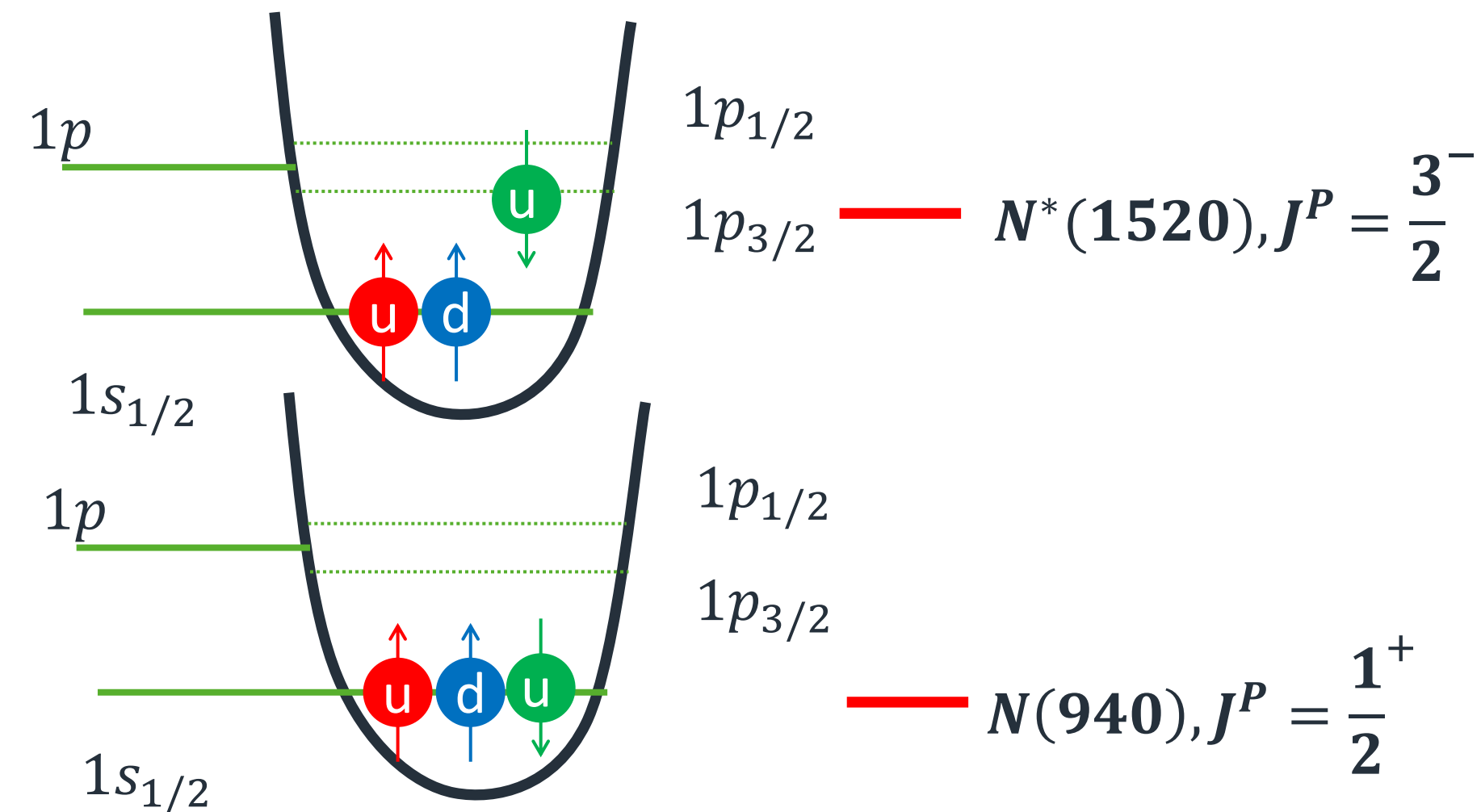
$S_{11}(1535)$
 $J^P = 1/2^-$

"N" baryons $I=1/2$, "Δ" baryons $I=3/2$

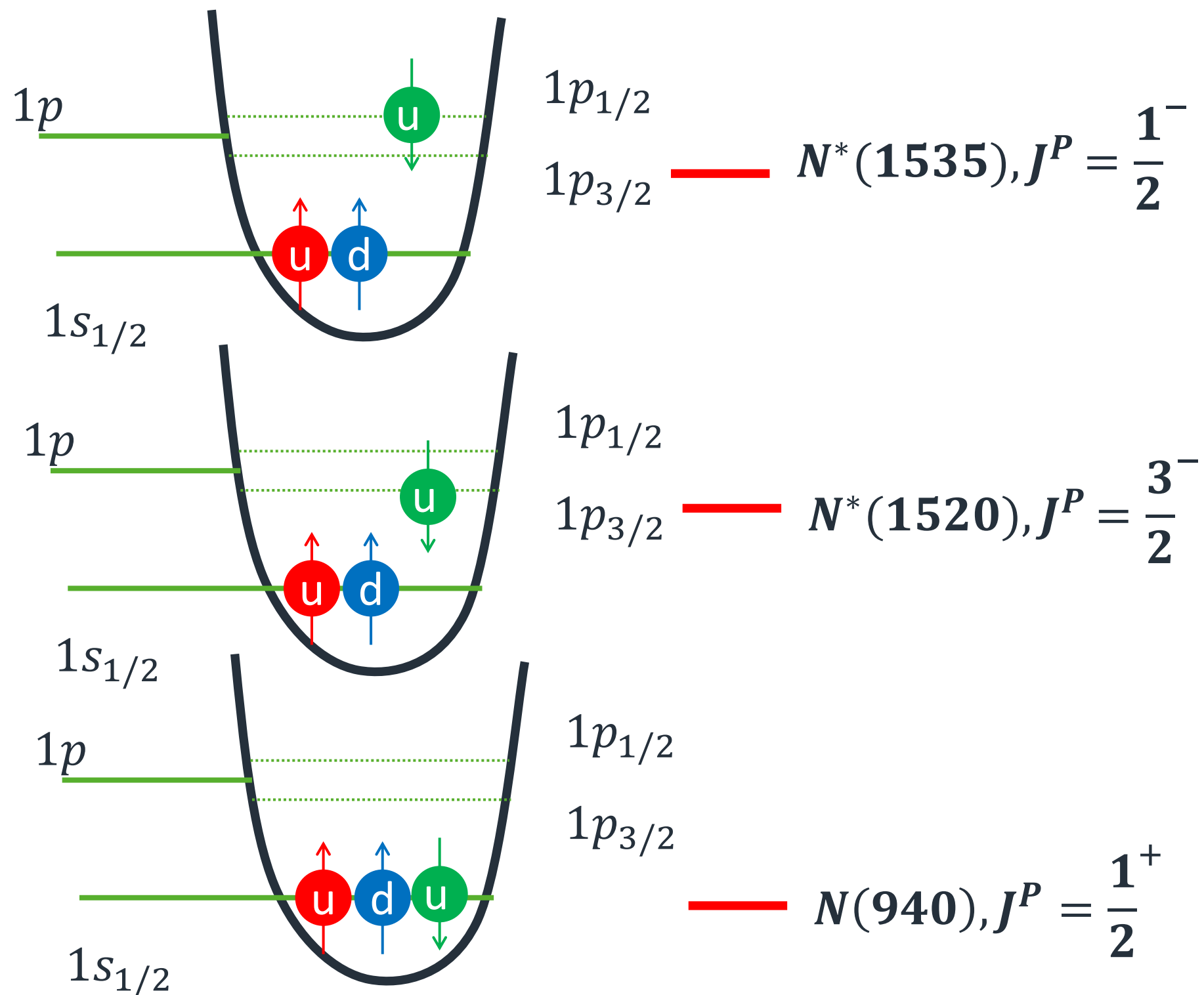
Excited states - expectation



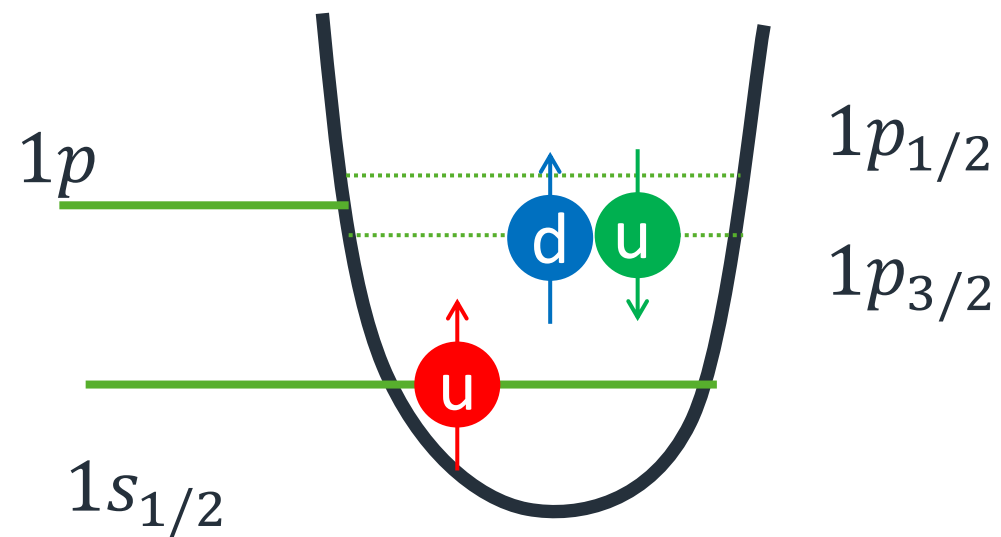
Excited states - expectation



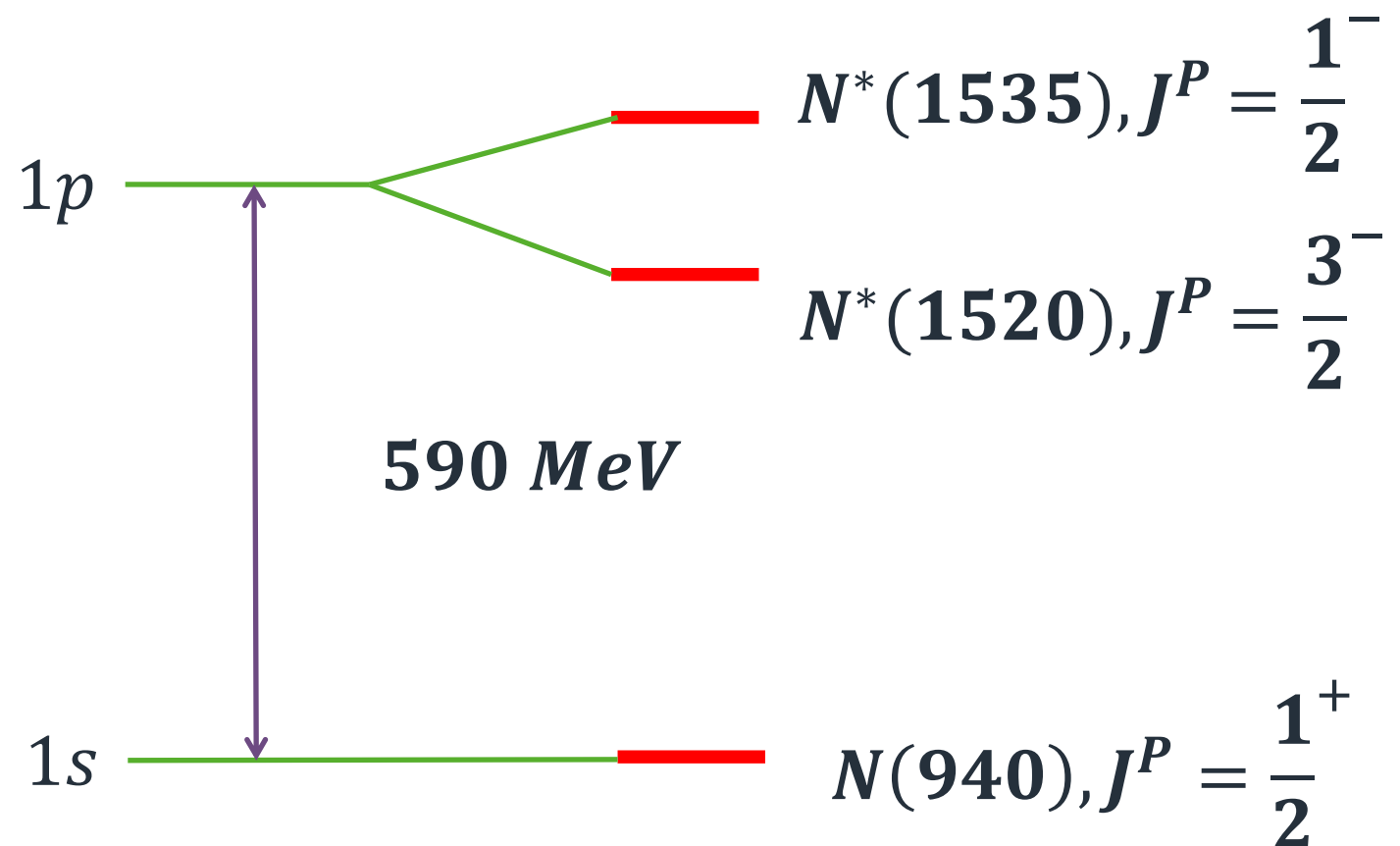
Excited states - expectation



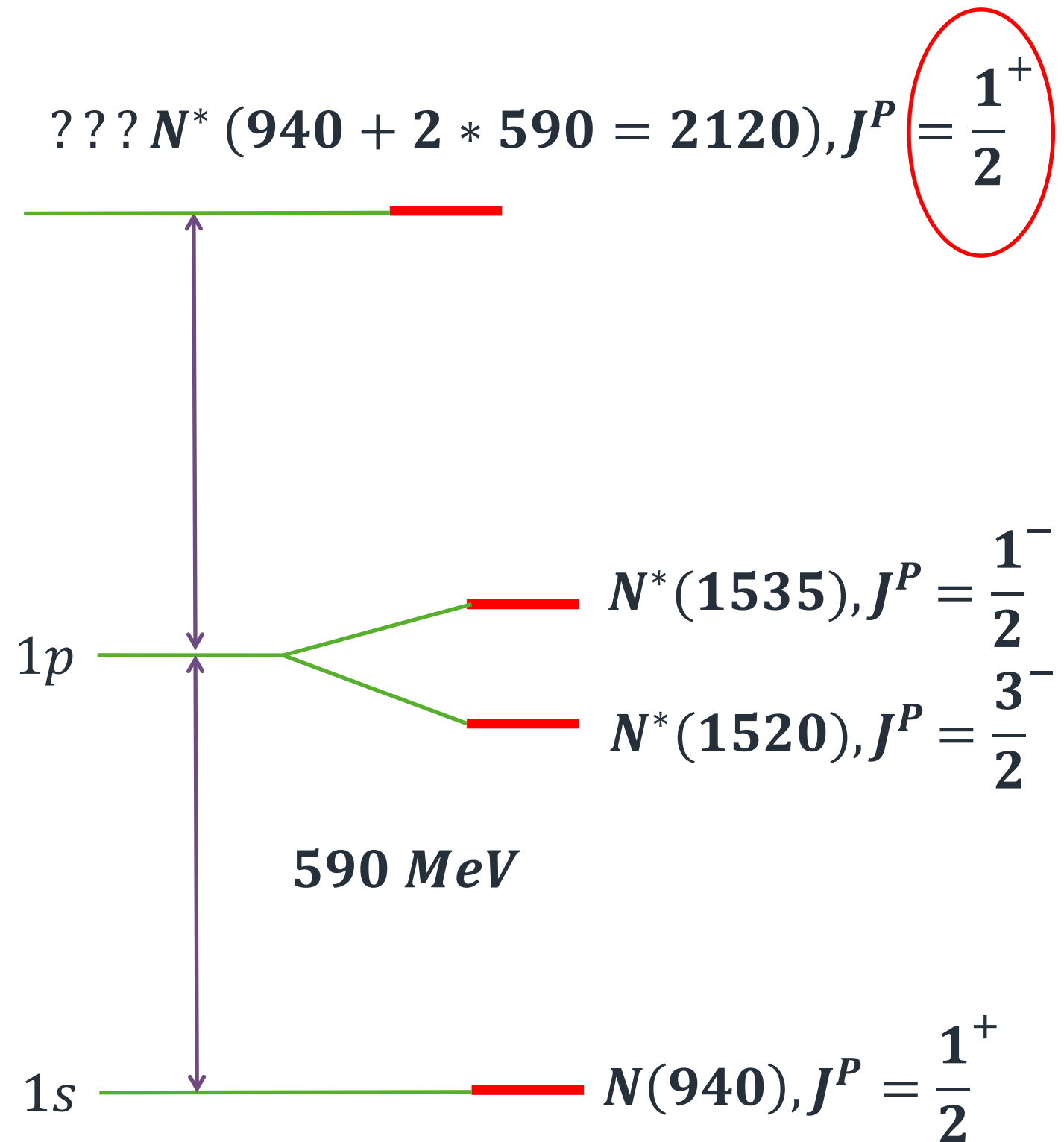
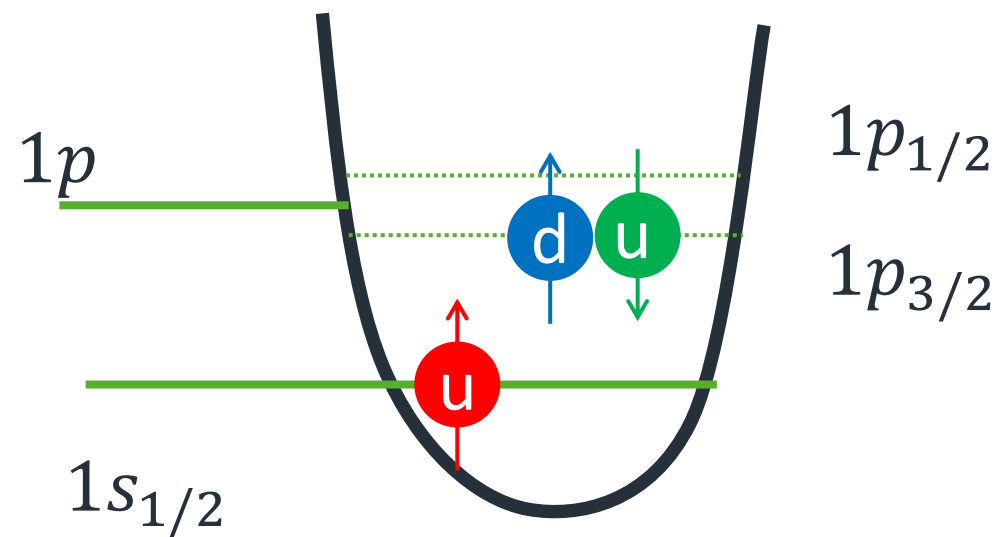
Excited states - expectation



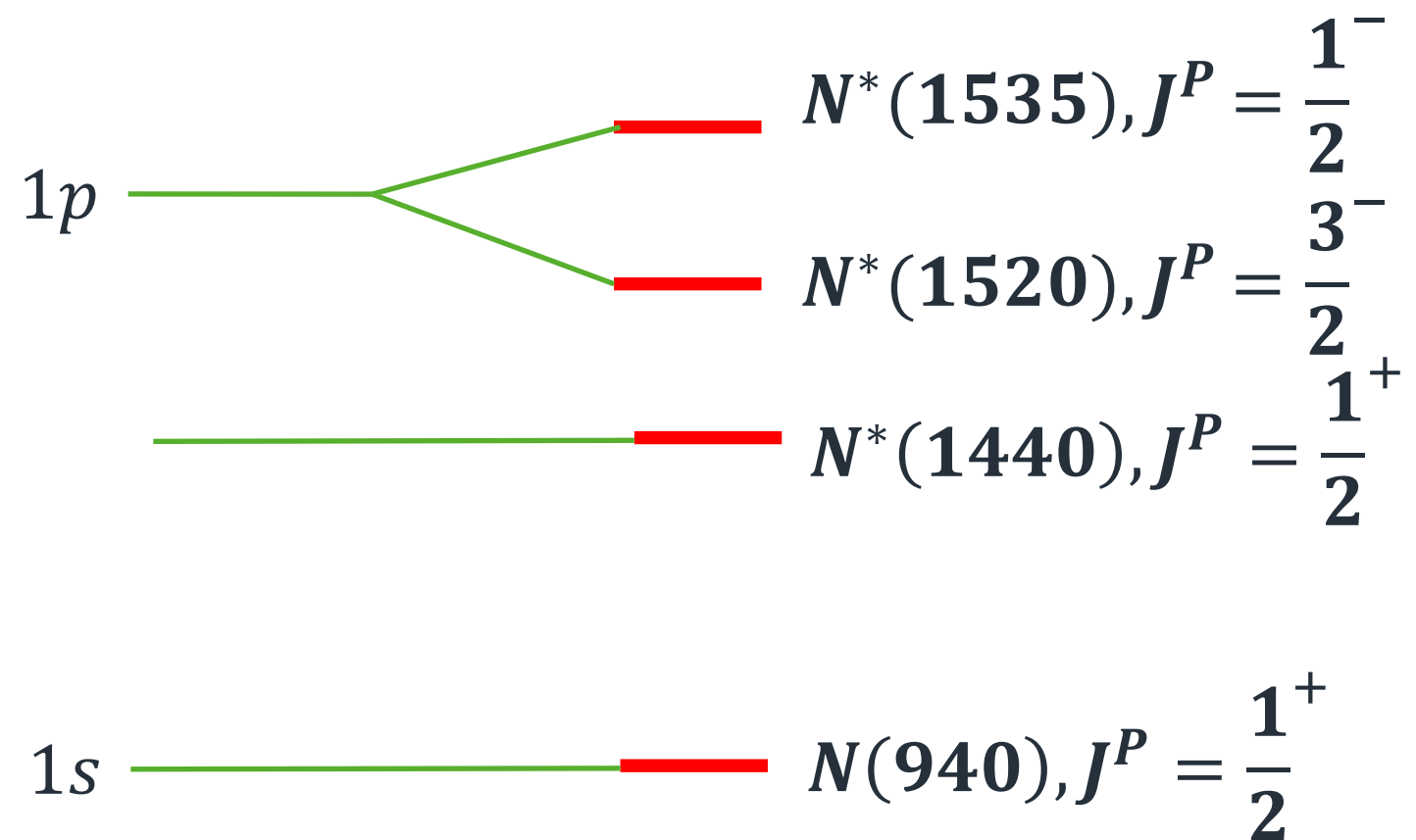
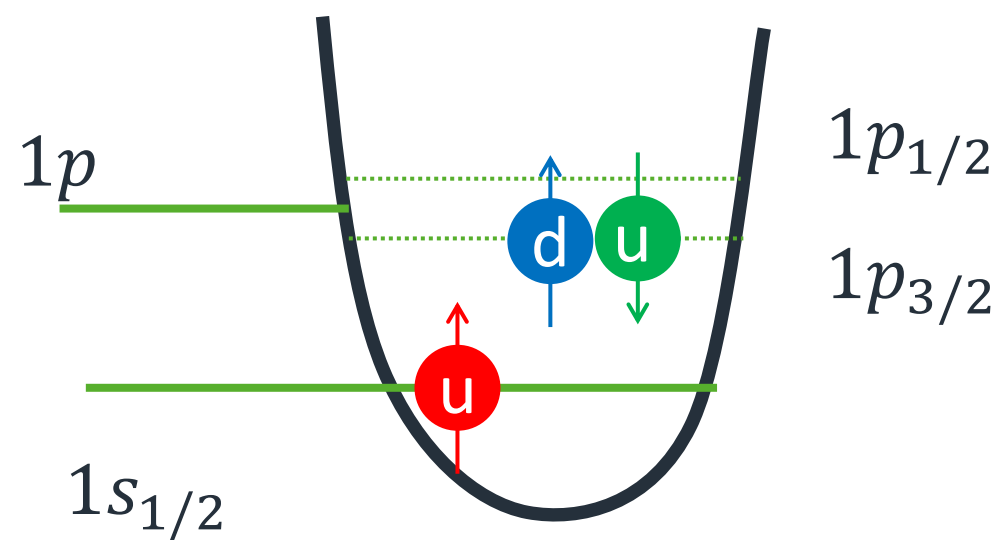
$$N^*(???), J^P = \frac{1}{2}^+$$



Excited states - expectation



Excited states - reality



Hyperons

— $N^*(1535), J^P = \frac{1}{2}^-$

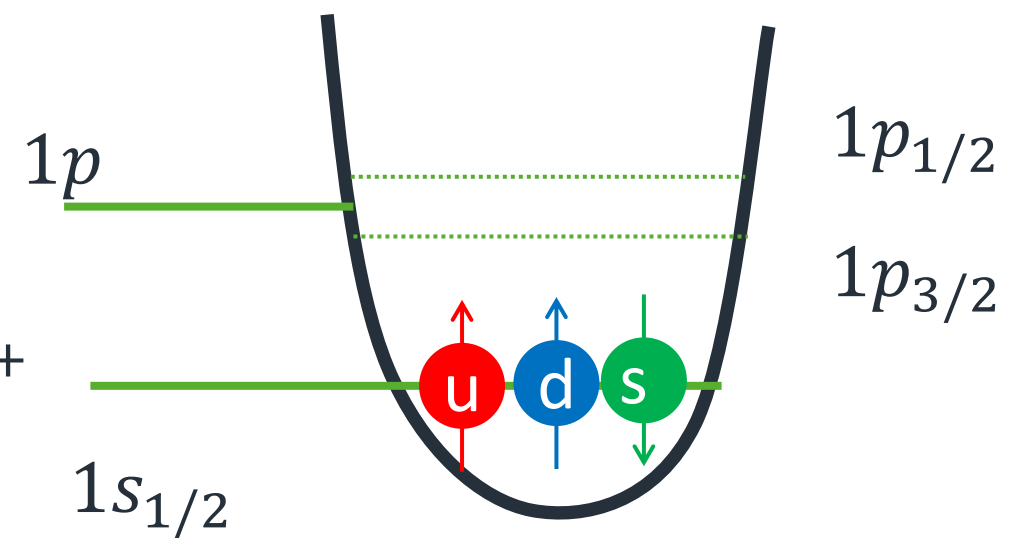
— $N^*(1520), J^P = \frac{3}{2}^-$

— $N^*(1440), J^P = \frac{1}{2}^+$

— $N(940), J^P = \frac{1}{2}^+$

176 MeV

— $\Lambda(1116), J^P = \frac{1}{2}^+$



Excited hyperons?

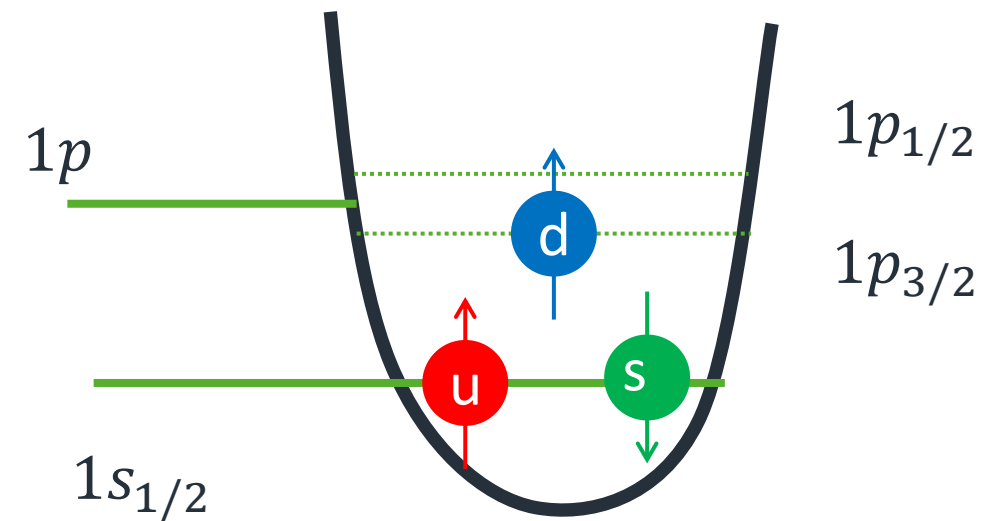
$$\text{---} N^*(1535), J^P = \frac{1}{2}^-$$

$$\text{---} N^*(1520), J^P = \frac{3}{2}^-$$

$$\text{---} N^*(1440), J^P = \frac{1}{2}^+$$

$$\text{---} \Lambda^*(1700?), J^P = \frac{3}{2}^-$$

$$1700 = 1520 + 176$$



$$\text{---} \Lambda(1116), J^P = \frac{1}{2}^+$$

176 MeV

$$\text{---} N(940), J^P = \frac{1}{2}^+$$

Excited hyperons - reality

— $N^*(1535), J^P = \frac{1}{2}^-$

— $N^*(1520), J^P = \frac{3}{2}^-$

— $N^*(1440), J^P = \frac{1}{2}^+$

— $\Lambda(1520), J^P = \frac{3}{2}^-$

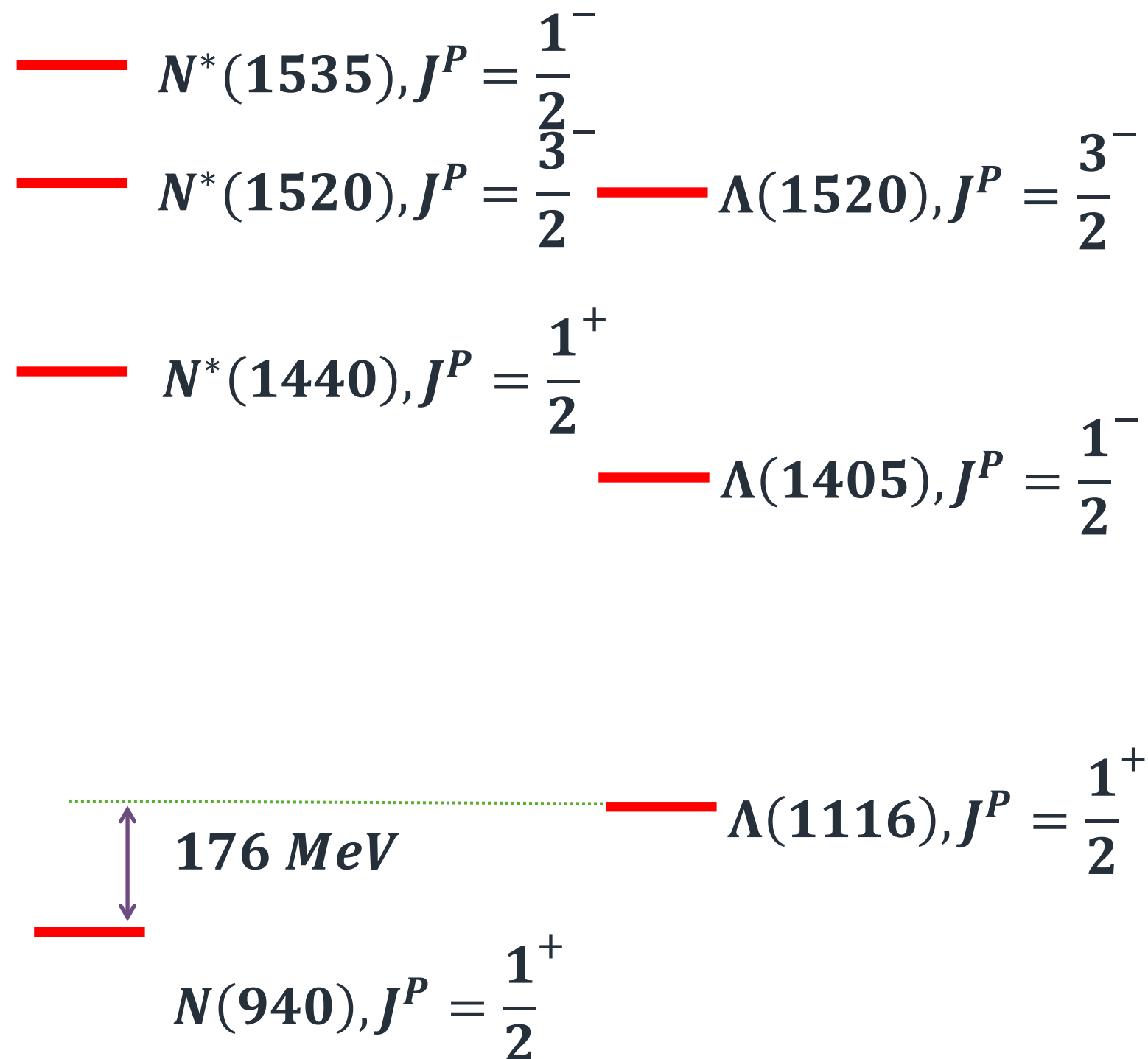
— $\Lambda(1405), J^P = \frac{1}{2}^-$

— $\Lambda(1116), J^P = \frac{1}{2}^+$

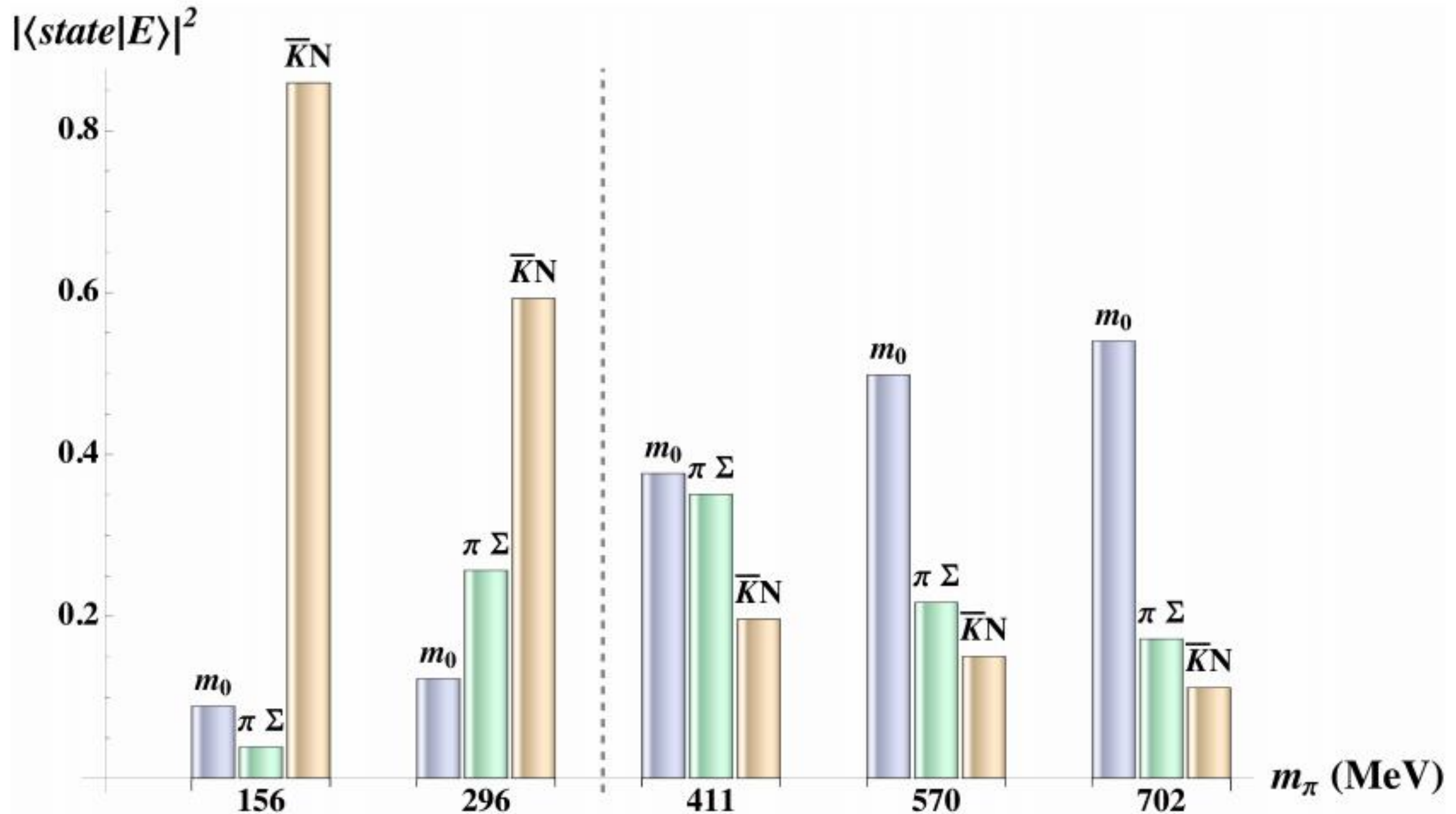
176 MeV

— $N(940), J^P = \frac{1}{2}^+$

Excited hyperons - reality



$\Lambda(1405)$ from Lattice QCD



Molecular states

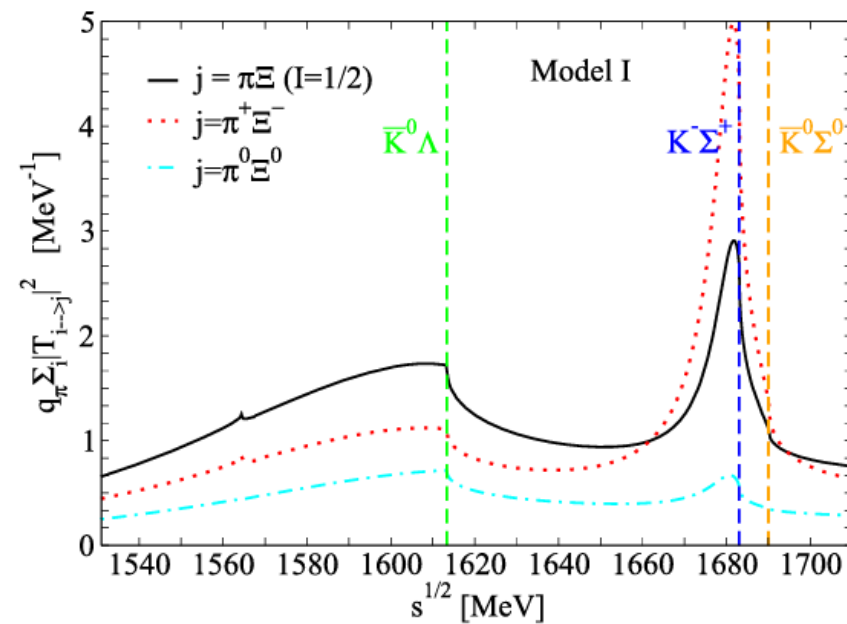
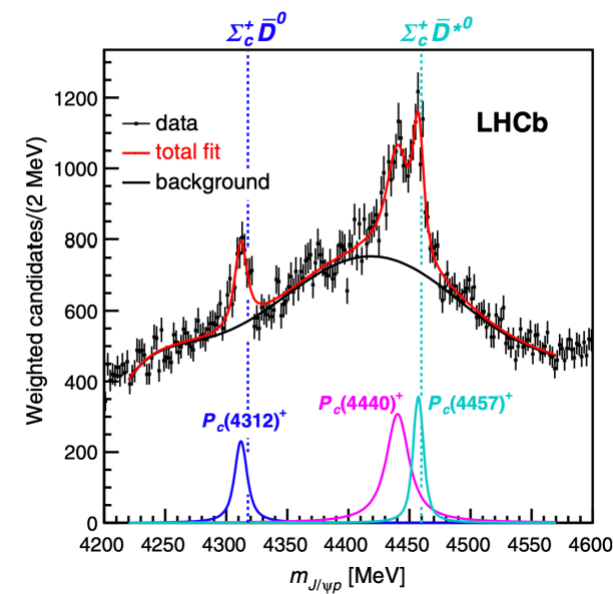


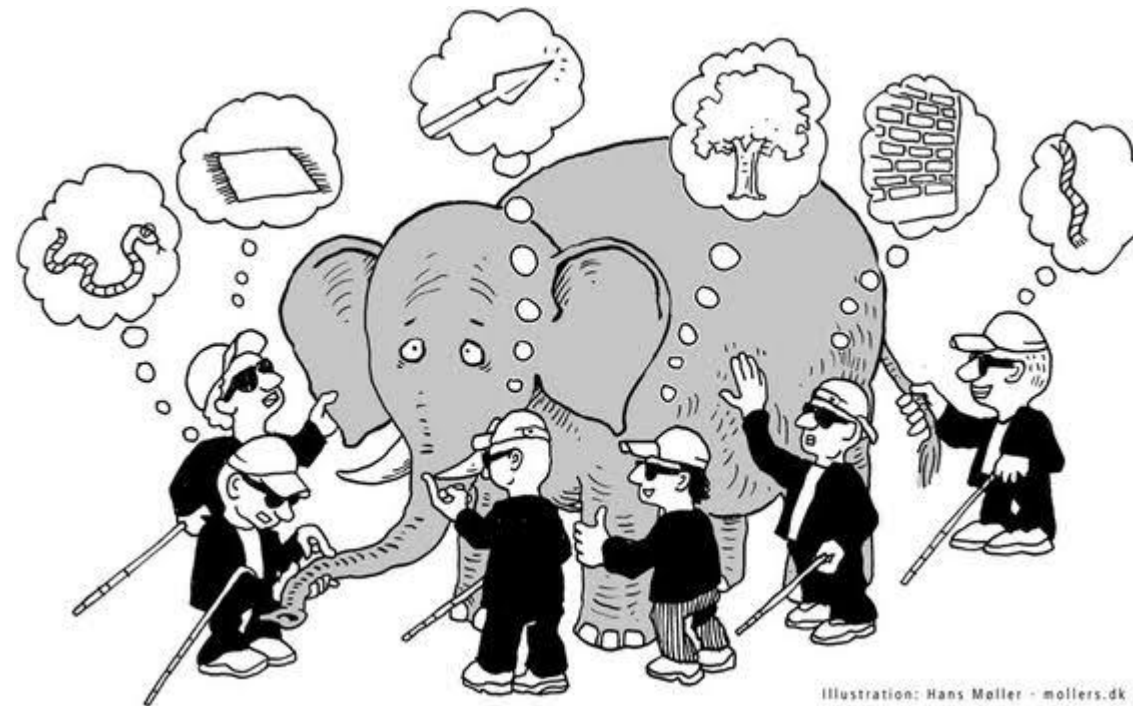
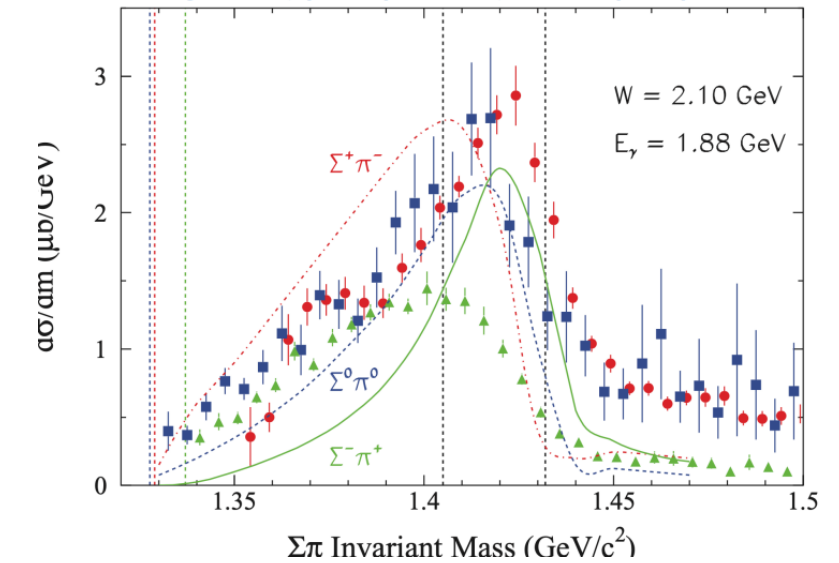
Fig. 2. Sum of amplitudes squared times a phase space factor. The vertical dashed lines represent the channel threshold locations.

Pentaquarks at LHCb

PRL 155, 072001 (2015), PRL 112, 222001 (2019)



Moriya et al., (CLAS) PRC 87, 035206 (2013)



Molecular states. Mesons

$\sigma(500)$: $\pi - \pi$ molecule

$f_0/a_0(980)$: $K - K$ molecule

$\kappa(700)$: $K - \pi$ molecule

Molecular states. Baryons

$N^*(1440)$: $N - \sigma$ molecule: $|uud + \bar{u}d + u\bar{d}\rangle$

$\Lambda(1405)$: $N - \bar{K}$ molecule: $|udd + s\bar{d}\rangle$

$N^*(1535)$: $\Sigma - K$ molecule: $|uds + d\bar{s}\rangle$

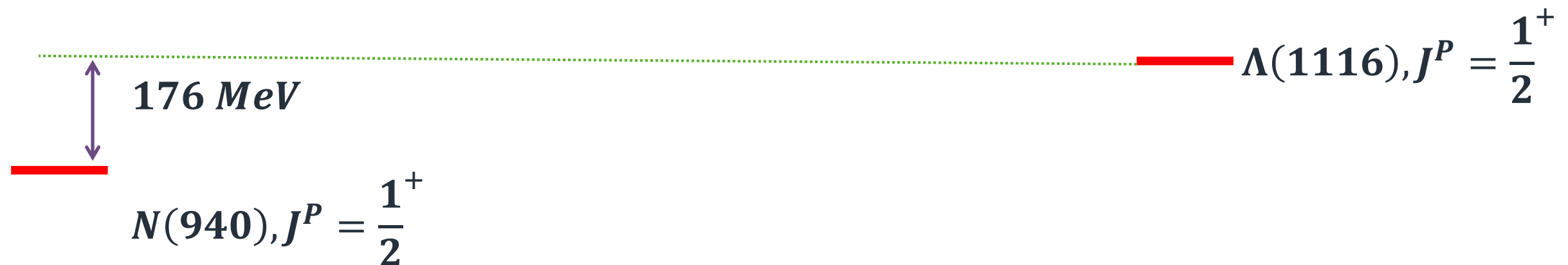
Excited hyperons - reality

$N^*(1535)$: $\Sigma - K$ molecule: $|uds + d\bar{s}\rangle$

— $N^*(1535), J^P = \frac{1}{2}^-$

$\Lambda(1405)$: $N - K$ molecule: $|uud + s\bar{d}\rangle$

— $\Lambda(1405), J^P = \frac{1}{2}^-$



Excited hyperons - reality

$$M_{N^*(1535)} - M_{\Lambda(1405)} = 130 \text{ MeV}$$

$N^*(1535)$: $\Sigma - K$ molecule: $|uds + d\bar{s}\rangle$

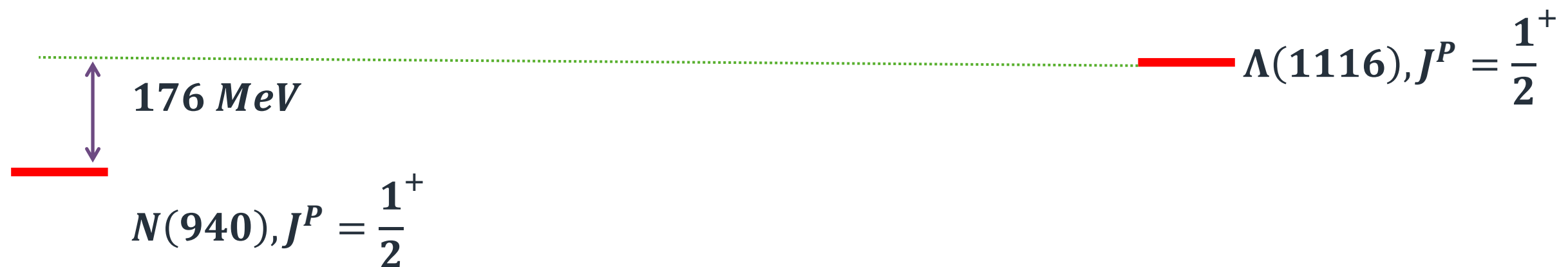
— $N^*(1535), J^P = \frac{1}{2}^-$

2 s-quarks

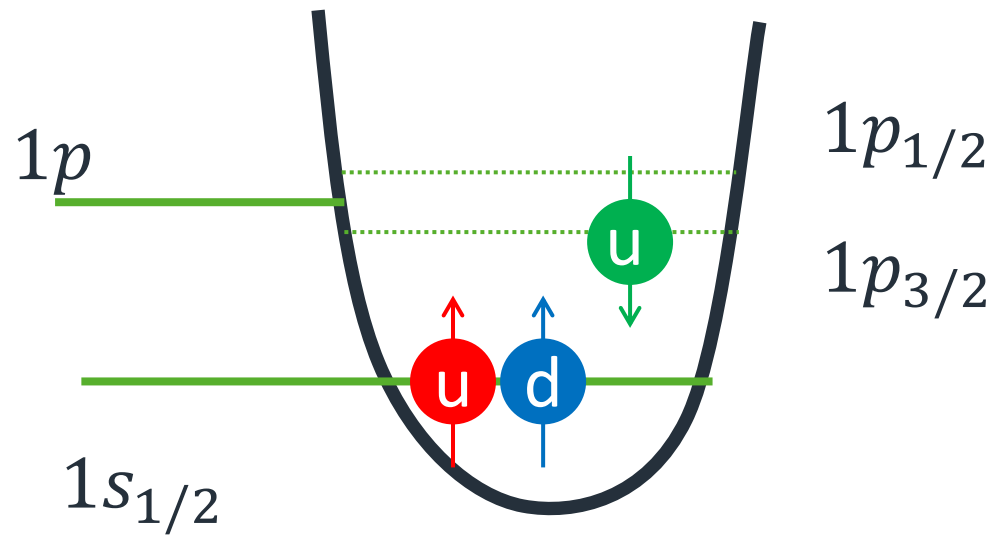
1 s-quark

$\Lambda(1405)$: $N - K$ molecule: $|uud + s\bar{d}\rangle$

— $\Lambda(1405), J^P = \frac{1}{2}^-$

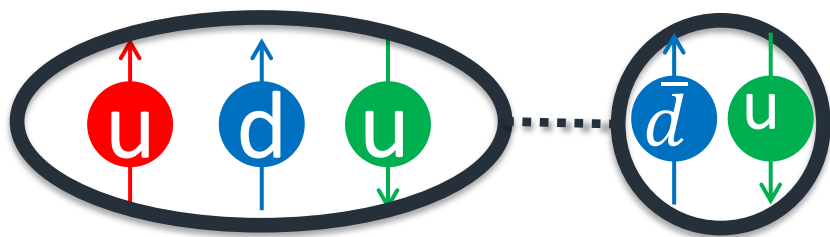


Excited states



Single quark excitations are expensive
(in terms of Energy ~ 700 MeV)

Low energy spectrum is dominated by molecular states!



Adding extra particle is cheap (140 MeV)

Baryon summary table, PDG

p	$1/2^+$	****	$\Delta(1232)$	$3/2^+$	****	Σ^+	$1/2^+$	****	Ξ^0	$1/2^+$	****	Λ_c^+	$1/2^+$	****
n	$1/2^+$	****	$\Delta(1600)$	$3/2^+$	***	Σ^0	$1/2^+$	****	Ξ^-	$1/2^+$	****	$\Lambda_c(2595)^+$	$1/2^-$	***
$N(1440)$	$1/2^+$	****	$\Delta(1620)$	$1/2^-$	****	Σ^-	$1/2^+$	****	$\Xi(1530)$	$3/2^+$	****	$\Lambda_c(2625)^+$	$3/2^-$	***
$N(1520)$	$3/2^-$	****	$\Delta(1700)$	$3/2^-$	****	$\Sigma(1385)$	$3/2^+$	****	$\Xi(1620)$	*		$\Lambda_c(2765)^+$	*	
$N(1535)$	$1/2^-$	****	$\Delta(1750)$	$1/2^+$	*	$\Sigma(1480)$	*		$\Xi(1690)$	***		$\Lambda_c(2880)^+$	$5/2^+$	***
$N(1650)$	$1/2^-$	****	$\Delta(1900)$	$1/2^-$	**	$\Sigma(1560)$	**		$\Xi(1820)$	$3/2^-$	***	$\Lambda_c(2940)^+$	***	
$N(1675)$	$5/2^-$	****	$\Delta(1905)$	$5/2^+$	****	$\Sigma(1580)$	$3/2^-$	*	$\Xi(1950)$	***		$\Sigma_c(2455)$	$1/2^+$	****
$N(1680)$	$5/2^+$	****	$\Delta(1910)$	$1/2^+$	****	$\Sigma(1620)$	$1/2^-$	*	$\Xi(2030)$	$\geq \frac{5}{2}?$	***	$\Sigma_c(2520)$	$3/2^+$	***
$N(1685)$	*		$\Delta(1920)$	$3/2^+$	***	$\Sigma(1660)$	$1/2^+$	***	$\Xi(2120)$	*		$\Sigma_c(2800)$	***	
$N(1700)$	$3/2^-$	***	$\Delta(1930)$	$5/2^-$	***	$\Sigma(1670)$	$3/2^-$	****	$\Xi(2250)$	**		Ξ_c^+	$1/2^+$	***
$N(1710)$	$1/2^+$	***	$\Delta(1940)$	$3/2^-$	**	$\Sigma(1690)$	**		$\Xi(2370)$	**		Ξ_c^0	$1/2^+$	***
$N(1720)$	$3/2^+$	****	$\Delta(1950)$	$7/2^+$	****	$\Sigma(1730)$	$3/2^+$	*	$\Xi(2500)$	*		$\Xi_c^{'+}$	$1/2^+$	***
$N(1860)$	$5/2^+$	**	$\Delta(2000)$	$5/2^+$	**	$\Sigma(1750)$	$1/2^-$	***				$\Xi_c^{'0}$	$1/2^+$	***
$N(1875)$	$3/2^-$	***	$\Delta(2150)$	$1/2^-$	*	$\Sigma(1770)$	$1/2^+$	*	Ω^-	$3/2^+$	****	$\Xi_c^{'0}$	$1/2^+$	***
$N(1880)$	$1/2^+$	**	$\Delta(2200)$	$7/2^-$	*	$\Sigma(1775)$	$5/2^-$	****	$\Omega(2250)^-$	***		$\Xi_c(2645)$	$3/2^+$	***
$N(1895)$	$1/2^-$	**	$\Delta(2300)$	$9/2^+$	**	$\Sigma(1840)$	$3/2^+$	*	$\Omega(2380)^-$	**		$\Xi_c(2790)$	$1/2^-$	***
$N(1900)$	$3/2^+$	***	$\Delta(2350)$	$5/2^-$	*	$\Sigma(1880)$	$1/2^+$	**	$\Omega(2470)^-$	**		$\Xi_c(2815)$	$3/2^-$	***
$N(1990)$	$7/2^+$	**	$\Delta(2390)$	$7/2^+$	*	$\Sigma(1900)$	$1/2^-$	*				$\Xi_c(2930)$	*	
$N(2000)$	$5/2^+$	**	$\Delta(2400)$	$9/2^-$	**	$\Sigma(1915)$	$5/2^+$	****				$\Xi_c(2980)$	***	
$N(2040)$	$3/2^+$	*	$\Delta(2420)$	$11/2^+$	****	$\Sigma(1940)$	$3/2^+$	*				$\Xi_c(3055)$	**	
$N(2060)$	$5/2^-$	**	$\Delta(2750)$	$13/2^-$	**	$\Sigma(1940)$	$3/2^-$	***				$\Xi_c(3080)$	***	
$N(2100)$	$1/2^+$	*	$\Delta(2950)$	$15/2^+$	**	$\Sigma(2000)$	$1/2^-$	*				$\Xi_c(3123)$	*	
$N(2120)$	$3/2^-$	**				$\Sigma(2030)$	$7/2^+$	****				Ω_c^0	$1/2^+$	***
$N(2190)$	$7/2^-$	****	Λ	$1/2^+$	****	$\Sigma(2070)$	$5/2^+$	*				$\Omega_c(2770)^0$	$3/2^+$	***
$N(2220)$	$9/2^+$	****	$\Lambda(1405)$	$1/2^-$	****	$\Sigma(2080)$	$3/2^+$	**				Ξ_{cc}^+	*	
$N(2250)$	$9/2^-$	****	$\Lambda(1520)$	$3/2^-$	****	$\Sigma(2100)$	$7/2^-$	*				Λ_b^0	$1/2^+$	***
$N(2300)$	$1/2^+$	**	$\Lambda(1600)$	$1/2^+$	***	$\Sigma(2250)$		***				$\Lambda_b(5912)^0$	$1/2^-$	***
$N(2570)$	$5/2^-$	**	$\Lambda(1670)$	$1/2^-$	****	$\Sigma(2455)$		**				$\Lambda_b(5920)^0$	$3/2^-$	***
$N(2600)$	$11/2^-$	***	$\Lambda(1690)$	$3/2^-$	****	$\Sigma(2620)$		**				Σ_b	$1/2^+$	***
$N(2700)$	$13/2^+$	**	$\Lambda(1710)$	$1/2^+$	*	$\Sigma(3000)$		*				Σ_b^*	$3/2^+$	***
			$\Lambda(1800)$	$1/2^-$	***	$\Sigma(3170)$		*				Ξ_b^0, Ξ_b^-	$1/2^+$	***
			$\Lambda(1810)$	$1/2^+$	***							$\Xi_b(5945)^0$	$3/2^+$	***
			$\Lambda(1820)$	$5/2^+$	****							Ω_b^-	$1/2^+$	***
			$\Lambda(1830)$	$5/2^-$	****									
			$\Lambda(1890)$	$3/2^+$	****									
			$\Lambda(2000)$	*										
			$\Lambda(2020)$	$7/2^+$	*									
			$\Lambda(2050)$	$3/2^-$	*									
			$\Lambda(2100)$	$7/2^-$	****									
			$\Lambda(2110)$	$5/2^+$	***									
			$\Lambda(2325)$	$3/2^-$	*									
			$\Lambda(2350)$	$9/2^+$	***									
			$\Lambda(2585)$	**										

Number of 3- and 4-star Resonances

Baryon	2004	2020
N^*	15	21
Δ	10	12
Λ	14	14
Σ	10	9*
Ξ	6	6
Ω	2	2

* $\Sigma(2250)$ was downgraded



Conclusion

- 3q states – a lot of progress
 - Large splitting
 - Dominated by molecules
 - mixing
- Molecules
 - Some thresholds have states
 - Some thresholds do not.
 - Shapes (production/decay channels)
- Hybrid baryons?
- Pentaquarks vs meson-baryon molecules?
- Precise, high stats experiments are the key

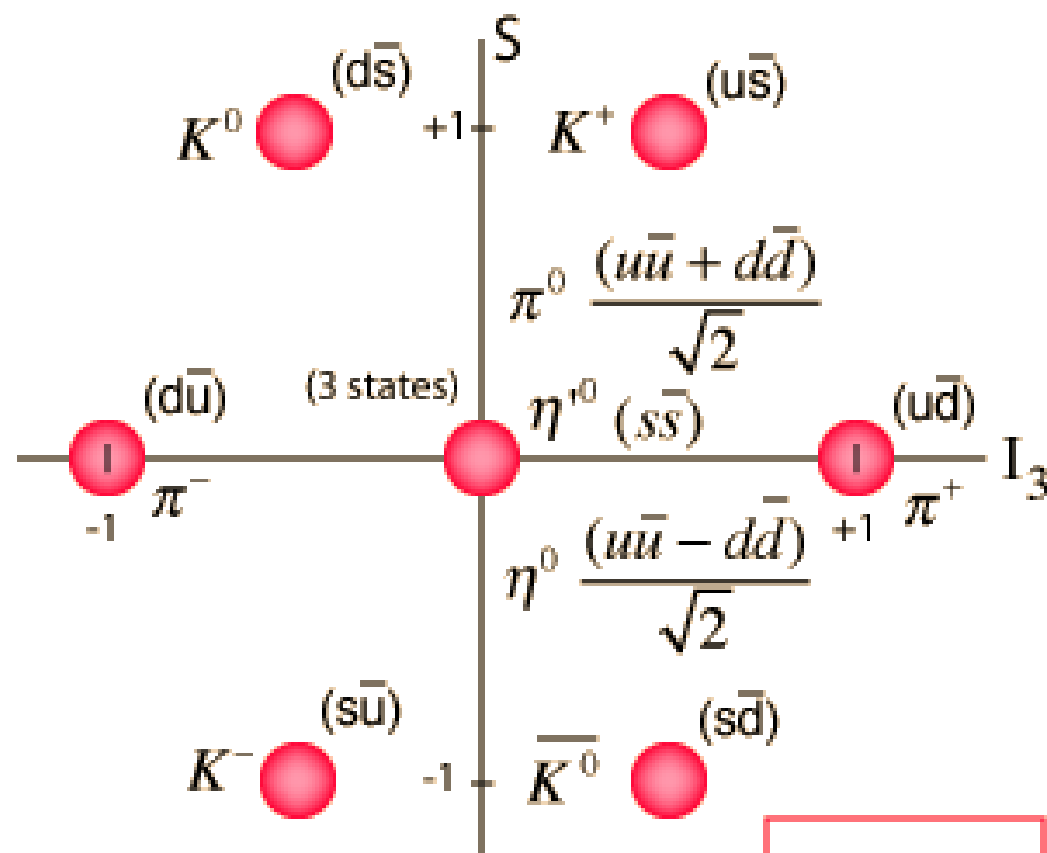
Questions

- Problem tasks:
- 1. The Roper resonance, $N^*(1440)$, has a quantum numbers $J^P = \frac{1}{2}^+$ and a pole position $M = 1395 \text{ MeV}$. Deduce what could be its SU(3) multiplet companions in single and double-strange sector and what could be their masses (might not be discovered yet)? . Hint: you can consider that Roper resonance is an interplay between $N\sigma$ and $\Delta\pi$ components
- 2. Perform similar research for the $N^*(1535)$
- 3. For the light N^* spectrum calculate possible meson-baryon thresholds which might be relevant and confront them with known states
- 4. For the meson baryon molecular states, calculate the quantum numbers of possible generated resonances (use two lowest lying baryon multiplets – octet and decuplet and two lowest meson nonets)

Mesons

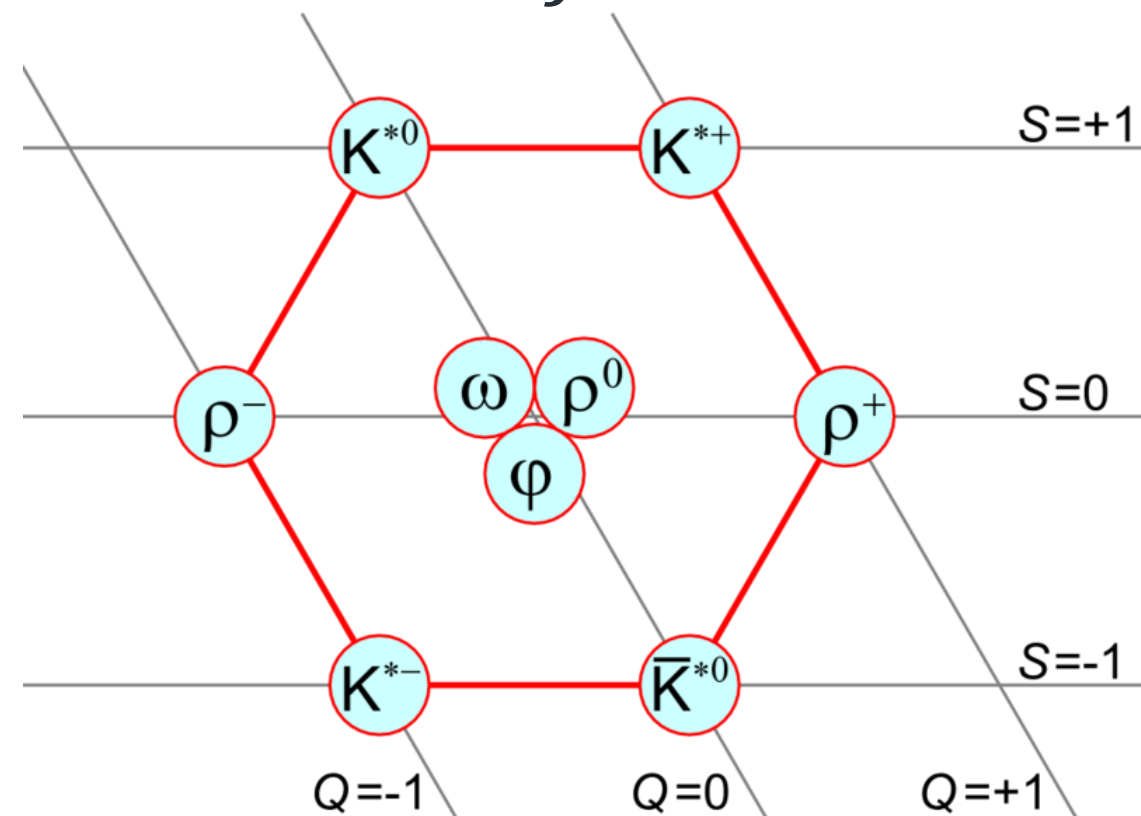
Two lightest multiplets

Pseudoscalar: $\downarrow\uparrow \quad J^P = 0^-$



$$J^P = 0^-$$

Vector: $\uparrow\uparrow \quad J^P = 1^-$



$$\rho = \frac{1}{\sqrt{2}} (u\bar{u} + d\bar{d})$$

$$\omega = \frac{1}{\sqrt{2}} (u\bar{u} - d\bar{d})$$

$$\phi = s\bar{s}$$

Pion multiplet

Particle	Quarks	S	Isospin I, I_3	J^{PC}	Mass [MeV]
K^+	$u\bar{s}$	+1	1/2, +1/2	$0^- +$	494
K^0	$d\bar{s}$	+1	1/2, -1/2	$0^- +$	498
π^+	$u\bar{d}$	0	1,+1	$0^- +$	140
π^0	$\frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})$	0	1,0	$0^- +$	135
π^-	$d\bar{u}$	0	1,-1	$0^- +$	140
η	$\frac{1}{\sqrt{2}}(u\bar{u} - d\bar{d})$	0	0,0	$0^- +$	548
η'	$s\bar{s}$	0	0,0	$0^- +$	958
$\overline{K^0}$	$s\bar{d}$	-1	1/2, +1/2	$0^- +$	498
K^-	$s\bar{u}$	-1	1/2, -1/2	$0^- +$	494

Rho multiplet

Particle	Quarks	S	Isospin I, I_3	J^{PC}	Mass [MeV]
K^{*+}	$u\bar{s}$	+1	1/2, +1/2	1^{--}	892
K^{*0}	$d\bar{s}$	+1	1/2, -1/2	1^{--}	892
ρ^+	$u\bar{d}$	0	1,+1	1^{--}	770
ρ^0	$\frac{1}{\sqrt{2}}(u\bar{u} + d\bar{d})$	0	1,0	1^{--}	770
ρ^-	$d\bar{u}$	0	1,-1	1^{--}	770
ω	$\frac{1}{\sqrt{2}}(u\bar{u} - d\bar{d})$	0	0,0	1^{--}	782
ϕ	$s\bar{s}$	0	0,0	1^{--}	1020
$\overline{K^{*0}}$	$s\bar{d}$	-1	1/2, +1/2	1^{--}	892
K^{*-}	$s\bar{u}$	-1	1/2, -1/2	1^{--}	892

Clebsch-Gordan coefficients

Note: A square-root sign is to be understood over *every* coefficient, e.g., for $-8/15$ read $-\sqrt{8/15}$.

Notation:

J	J	...
M	M	...
m_1	m_2	
m_1	m_2	Coefficients
$\vdots$	$\vdots$	
$\vdots$	$\vdots$	

$1/2 \times 1/2$

1		
+1	1	0
+1/2 + 1/2	1	0
+1/2 - 1/2	1/2	1/2
-1/2 + 1/2	1/2	-1/2
-1/2 - 1/2	1	

$$Y_1^0 = \sqrt{\frac{3}{4\pi}} \cos \theta$$

$$Y_1^1 = -\sqrt{\frac{3}{8\pi}} \sin \theta e^{i\phi}$$

$$Y_2^0 = \sqrt{\frac{5}{4\pi}} \left(\frac{3}{2} \cos^2 \theta - \frac{1}{2} \right)$$

$$Y_2^1 = -\sqrt{\frac{15}{8\pi}} \sin \theta \cos \theta e^{i\phi}$$

$$Y_2^2 = \frac{1}{4} \sqrt{\frac{15}{2\pi}} \sin^2 \theta e^{2i\phi}$$

$2 \times 1/2$

5/2	5/2	3/2
+5/2	1	+3/2 + 3/2
+2 + 1/2	1	+3/2 + 3/2
+2 - 1/2	1/5	4/5
+1 + 1/2	4/5 - 1/5	+1/2 + 1/2

$3/2 \times 1/2$

2	2	1
+2	1	+1
+3/2 + 1/2	1	+1
+3/2 - 1/2	1/4	3/4
+1/2 + 1/2	3/4 - 1/4	0

$1 \times 1/2$

3/2	3/2	1/2
+3/2	1	+1/2 + 1/2
+1 + 1/2	1	+1/2 + 1/2
+1 - 1/2	1/3	2/3
0 + 1/2	2/3 - 1/3	-1/2 - 1/2

2×1

3	3	2
+3	2	+2
+2 + 1	1	+2
+2 0	1/3	2/3
+1 + 1	2/3 - 1/3	3

$3/2 \times 1$

5/2	5/2	3/2
+5/2	1	+3/2 + 3/2
+3/2 + 1	1	+3/2 + 3/2
+3/2 0	2/5	3/5
+1/2 + 1	3/5 - 2/5	+1/2 + 1/2

1×1

2	2	1
+2	1	+1
+1 + 1	1	+1
+1 0	1/2	1/2
0 + 1	1/2 - 1/2	2

$3/2 \times 1$

5/2	5/2	3/2
+5/2	1	+3/2 + 3/2
+3/2 + 1	1	+3/2 + 3/2
+3/2 0	2/5	3/5
+1/2 + 1	3/5 - 2/5	+1/2 + 1/2

1×1

2	2	1
+2	1	+1
+1 + 1	1	+1
+1 0	1/2	1/2
0 + 1	1/2 - 1/2	2

$$d_{m,0}^\ell = \sqrt{\frac{4\pi}{2\ell+1}} Y_\ell^m e^{-im\phi}$$

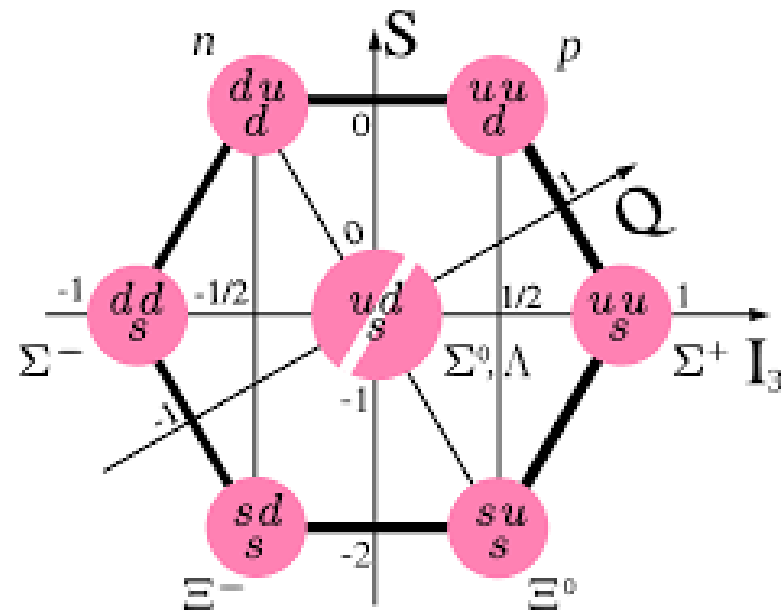
$$\langle j_1 j_2 m_1 m_2 | j_1 j_2 J M \rangle = (-1)^{J-j_1-j_2} \langle j_2 j_1 m_2 m_1 | j_2 j_1 J M \rangle$$

From PDG (particle data group)

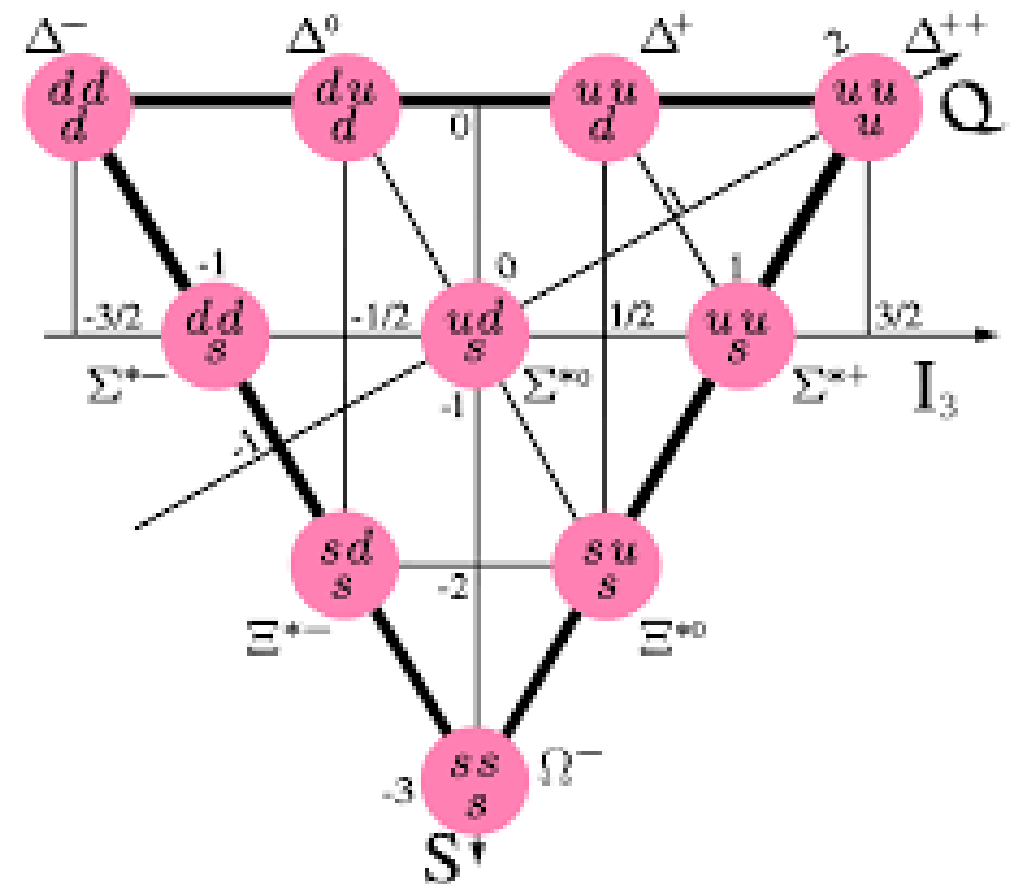
Baryons

Two lightest multiplets

Octet: $\uparrow\downarrow\uparrow$ $J^P = \frac{1}{2}^+$



Decuplet: $\uparrow\uparrow\uparrow$ $J^P = \frac{3}{2}^+$



Nucleon octet

Particle	Quarks	S	Isospin I, I_3	J^{PC}	Mass [MeV]
p	uud	0	$1/2, +1/2$	$1/2^+$	938
n	udd	0	$1/2, -1/2$	$1/2^+$	939
Σ^+	uus	-1	$1, +1$	$1/2^+$	1189
Σ^0	uds	-1	$1, 0$	$1/2^+$	1193
Σ^-	dds	-1	$1, -1$	$1/2^+$	1197
Λ	uds	-1	$0, 0$	$1/2^+$	1116
Ξ^0	uss	-2	$1/2, +1/2$	$1/2^+$	1315
Ξ^-	dss	-2	$1/2, -1/2$	$1/2^+$	1322

Delta decuplet

Particle	Quarks	S	Isospin I, I_3	J^{PC}	Mass [MeV]
Δ^{++}	uuu	0	$3/2, +3/2$	$3/2^+$	1232
Δ^+	uud	0	$3/2, +1/2$	$3/2^+$	1232
Δ^0	udd	0	$3/2, -1/2$	$3/2^+$	1232
Δ^-	ddd	0	$3/2, -3/2$	$3/2^+$	1232
Σ^+	uus	-1	$1, +1$	$3/2^+$	1385
Σ^0	uds	-1	$1, 0$	$3/2^+$	1385
Σ^-	dds	-1	$1, -1$	$3/2^+$	1385
Ξ^0	uss	-2	$0, 0$	$3/2^+$	1530
Ξ^-	dss	-2	$0, 0$	$3/2^+$	1530
Ω	sss	-3	$1/2, +1/2$	$3/2^+$	1672