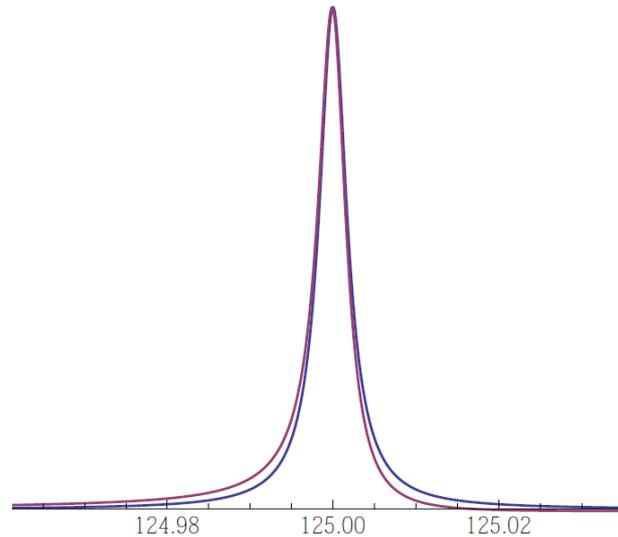


Higgs Interferometry



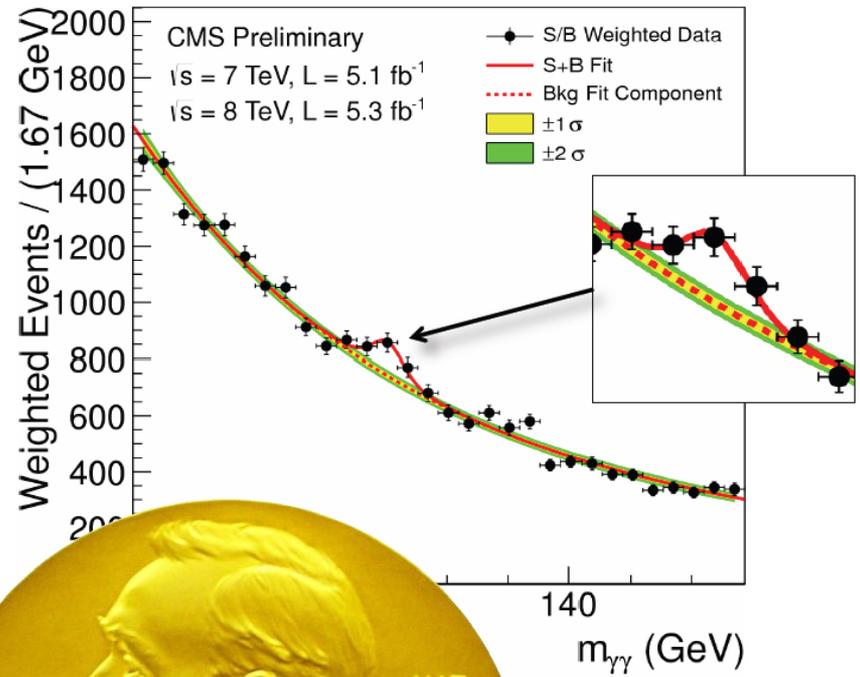
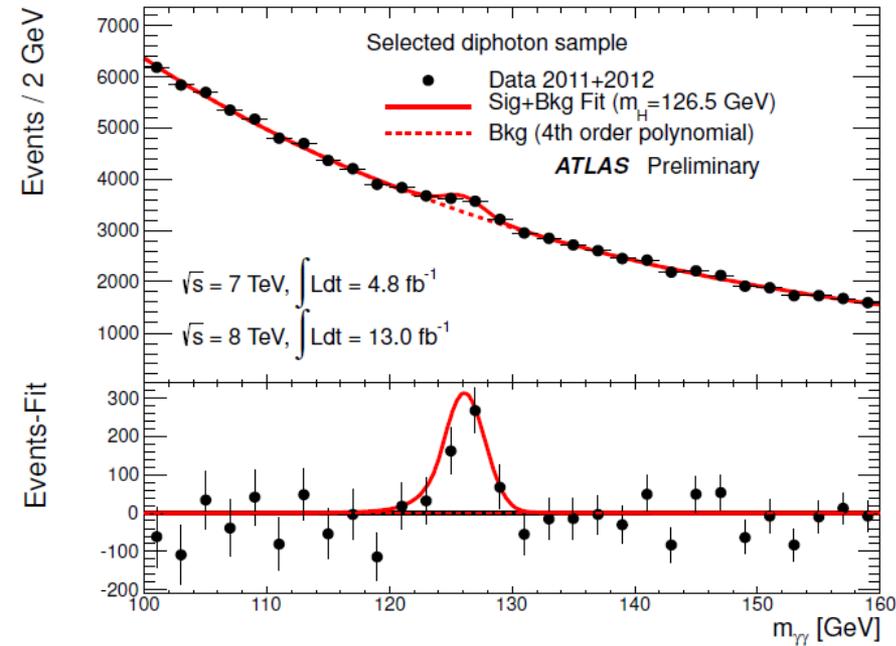
Lance Dixon (SLAC)

with Ye Li [1305.3854] and Stefan H \ddot{o} che

New Directions in Theoretical Physics

U. Edinburgh, Jan. 8, 2014

A new particle!



L. Dixon Higgs interferometry

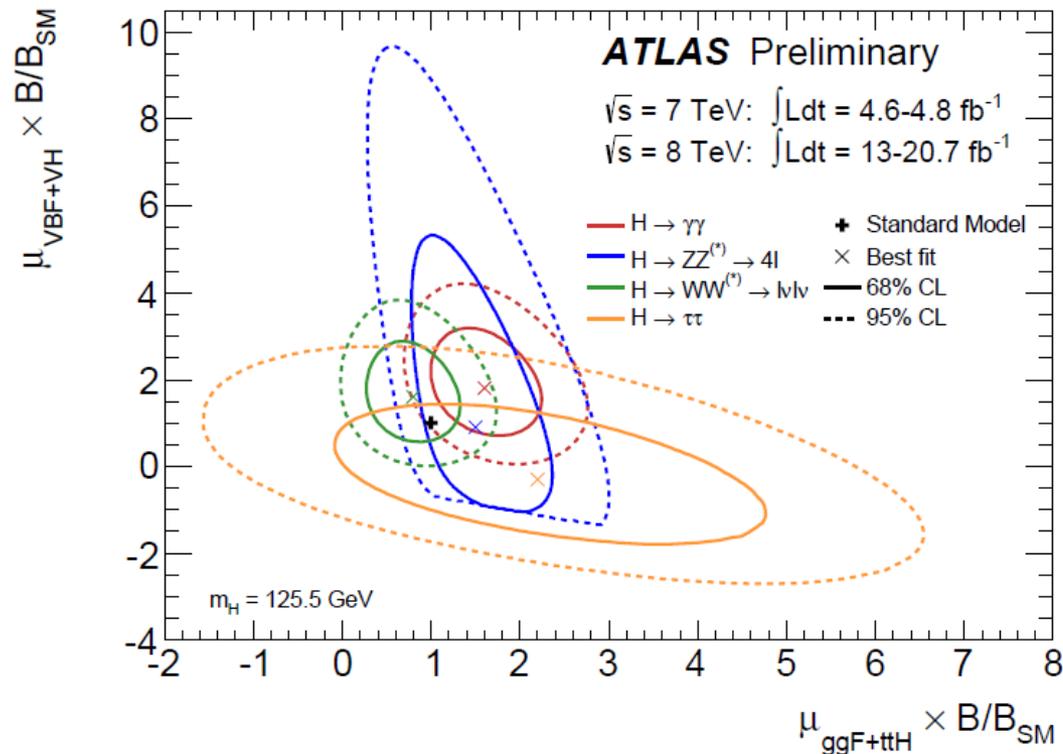


Edinburgh Jan. 8, 2014

“The Higgs boson changes everything. We’re obligated to understand it using all tools.”

- Chip Brock at “Snowmass on the Mississippi

We know a lot about it already



- These are all measurements of $\sigma_{\text{prod}} \times \text{Br}(H \rightarrow f)$.
- Besides adding more data and channels, what other types of measurements might add more information?

What about its lifetime?

- Most fundamental property of a particle, after its mass and spin.

- In the Standard Model,

$$\tau = 0.16 \times 10^{-21} \text{ s} = 1/6 \text{ zs}$$

$$c\tau = 5 \times 10^{-5} \text{ nm} \quad (\text{no displaced vertices})$$

- Width: $1/\tau = \Gamma = 4 \text{ MeV}$

Γ much smaller than typical experimental resolution on decay products, $\sim 1 \text{ GeV}$ or more.

- Direct lifetime or width measurements are not feasible at colliders (except possibly a muon collider).

Can we use event yields?

- Higgs signal strength in decay channel f :

$$\begin{aligned}\sigma_{\text{prod}}(i \rightarrow H) \cdot \text{Br}(H \rightarrow f) &= |M(i \rightarrow H)|^2 \cdot |M(H \rightarrow f)|^2 / \Gamma \\ &= [\sigma \cdot \text{Br}]_{\text{SM}} \cdot c_i^2 \cdot c_f^2 / \Gamma\end{aligned}$$

if we scale SM couplings of initial and final states i and f to H by factors of $c_{i,f}$

- **Invariant** under scaling all $c_{i,f}$ uniformly,

$$\begin{aligned}c_{i,f} &\rightarrow \xi c_{i,f} \\ \Gamma &\rightarrow \xi^4 \Gamma\end{aligned}$$

Flat direction (unless one can observe H independently of decay mode)

Stopping the flat direction

- Often said that LHC cannot directly measure the width of the Higgs boson.
- However, using interference with the continuum background for $gg \rightarrow \gamma\gamma$, future LHC data can put [LD, Y. Li 1305.3854] a fairly direct upper limit on the Higgs width, much better than ~ 1 -6.9 GeV possible directly. CMS
- It may eventually be possible to get close to the Standard Model width of 4 MeV.
- Similar idea works for $gg \rightarrow ZZ$, far from Higgs resonance Kauer, Passarino, 1206.4803; Caola, Melnikov, 1307.4935; Campbell, Ellis, Williams, 1311.3589

“Higgs Interferometry”

How to use quantum superposition

$$|\text{Higgs}\rangle + |q\bar{q}\rangle$$



to learn something new about the Higgs
(its lifetime)

Google Search

I'm Feeling Lucky

Interference in $gg \rightarrow H \rightarrow \gamma\gamma$

c_g

c_γ

$$\mathcal{A}_{gg \rightarrow \gamma\gamma} = \frac{-\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma}}{\hat{s} - m_H^2 + im_H \Gamma_H} + \mathcal{A}_{\text{cont}}$$

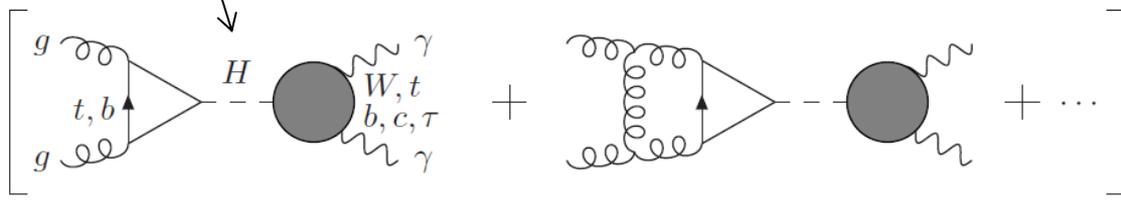
shifts peak position
(apparent mass)

$$\rightarrow \delta\hat{\sigma}_{gg \rightarrow H \rightarrow \gamma\gamma} = -2(\hat{s} - m_H^2) \frac{\text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma} \mathcal{A}_{\text{cont}}^*)}{(\hat{s} - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

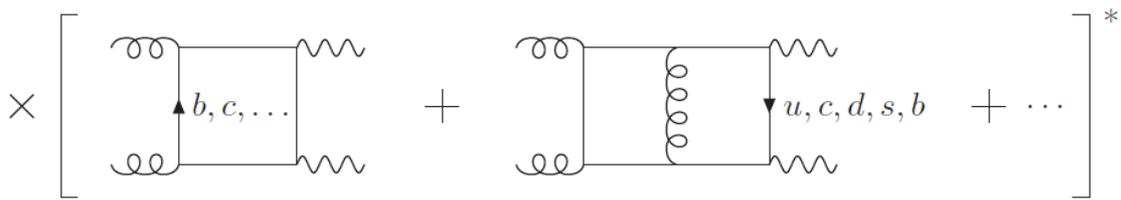
$$-2m_H \Gamma_H \frac{\text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma} \mathcal{A}_{\text{cont}}^*)}{(\hat{s} - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

shifts peak height
(event yield)

or spin 2 "G"



(assume)
dominantly real



Interference effects and Γ

LD, Y. Li 1305.3854

- All non-interference measurements at LHC give signal strength proportional to $c_i^2 \cdot c_f^2 / \Gamma$
- **Invariant** under scaling all $c_{i,f}$ uniformly,

$$c_{i,f} \rightarrow \xi c_{i,f}$$

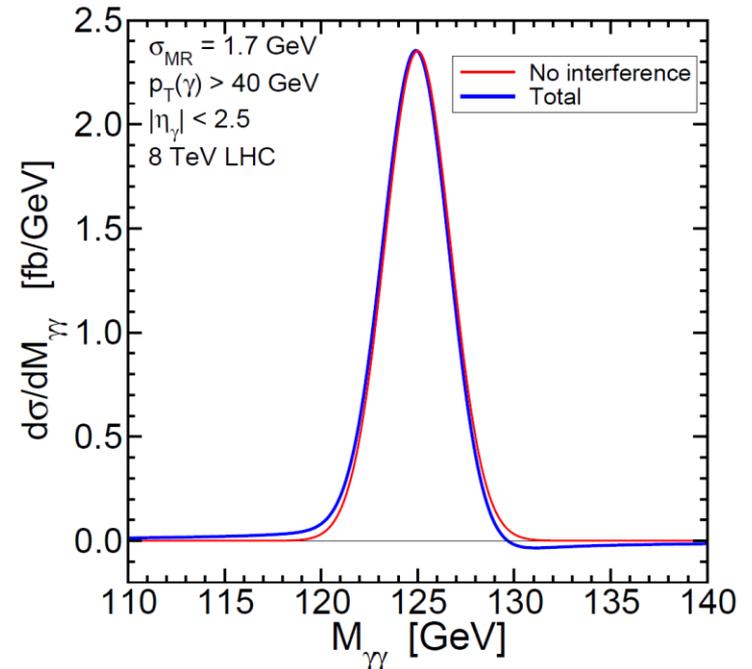
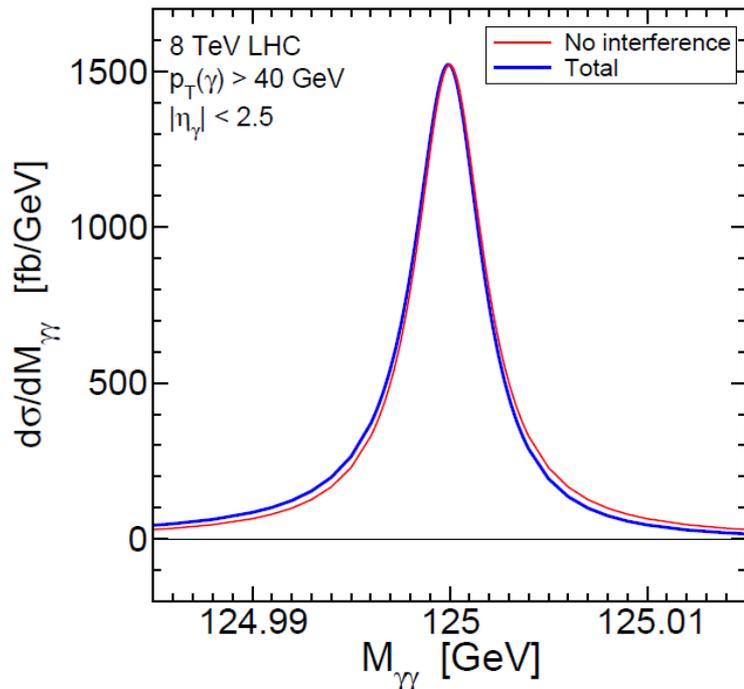
$$\Gamma \rightarrow \xi^4 \Gamma$$

- Allow for non-SM, undetectable modes in Γ
- Interference effects go like $c_i \cdot c_f$,
break this degeneracy
- **Allow one to measure or bound Higgs width**

Mass shift from real part

S. Martin, 1208.1533, 1303.3342; D. de Florian et al, 1303.1397

Smear lineshape with Gaussian with width $\sigma = 1.7$ GeV

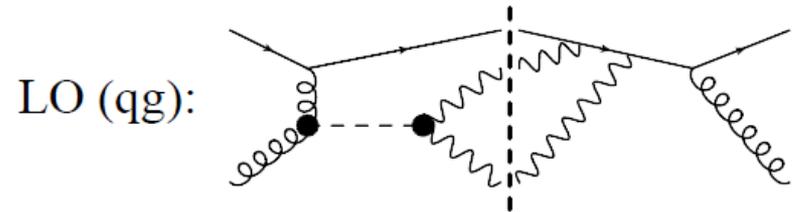
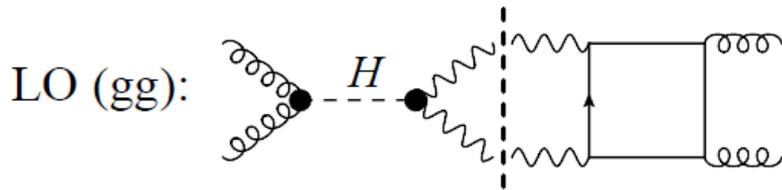


Perform least squares fit to Gaussian at mass $M + \delta M$

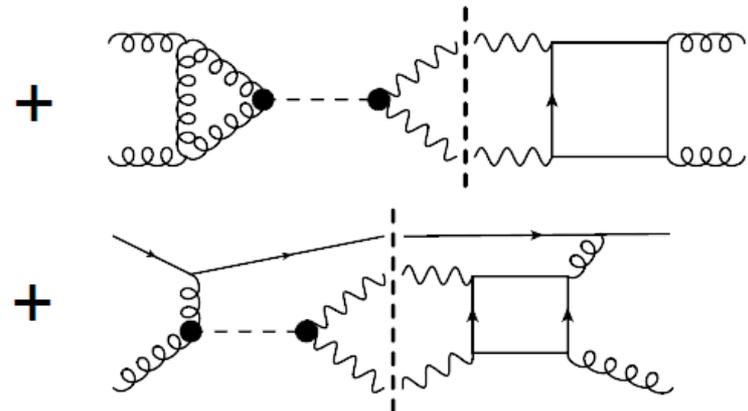
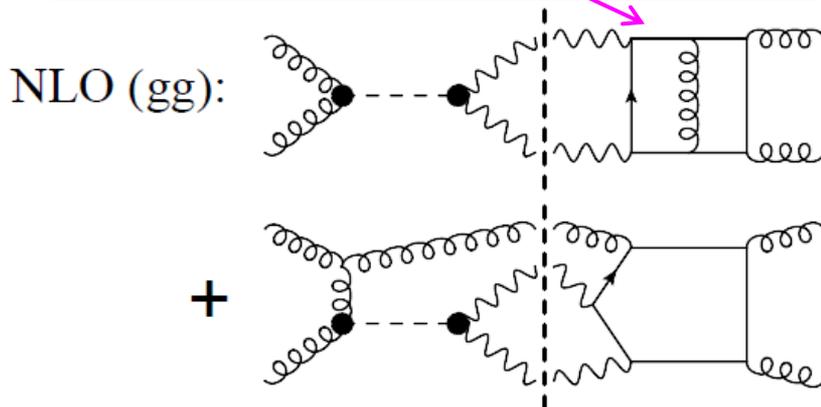
→ $\delta M \sim 100$ MeV in SM at LO

Diagrams for NLO mass shift

LD, Y. Li, 1305.3854



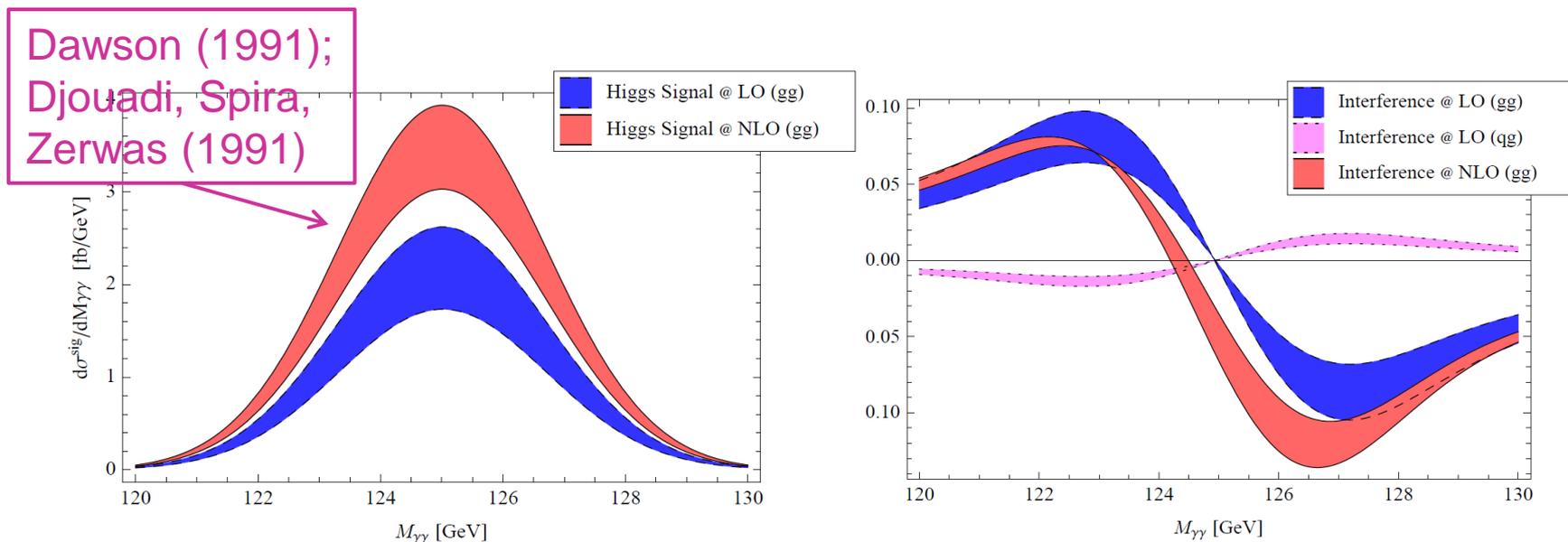
Bern, de Freitas, LD, hep-ph/0109078



Mass shift at NLO

- Reduced by 40% from LO

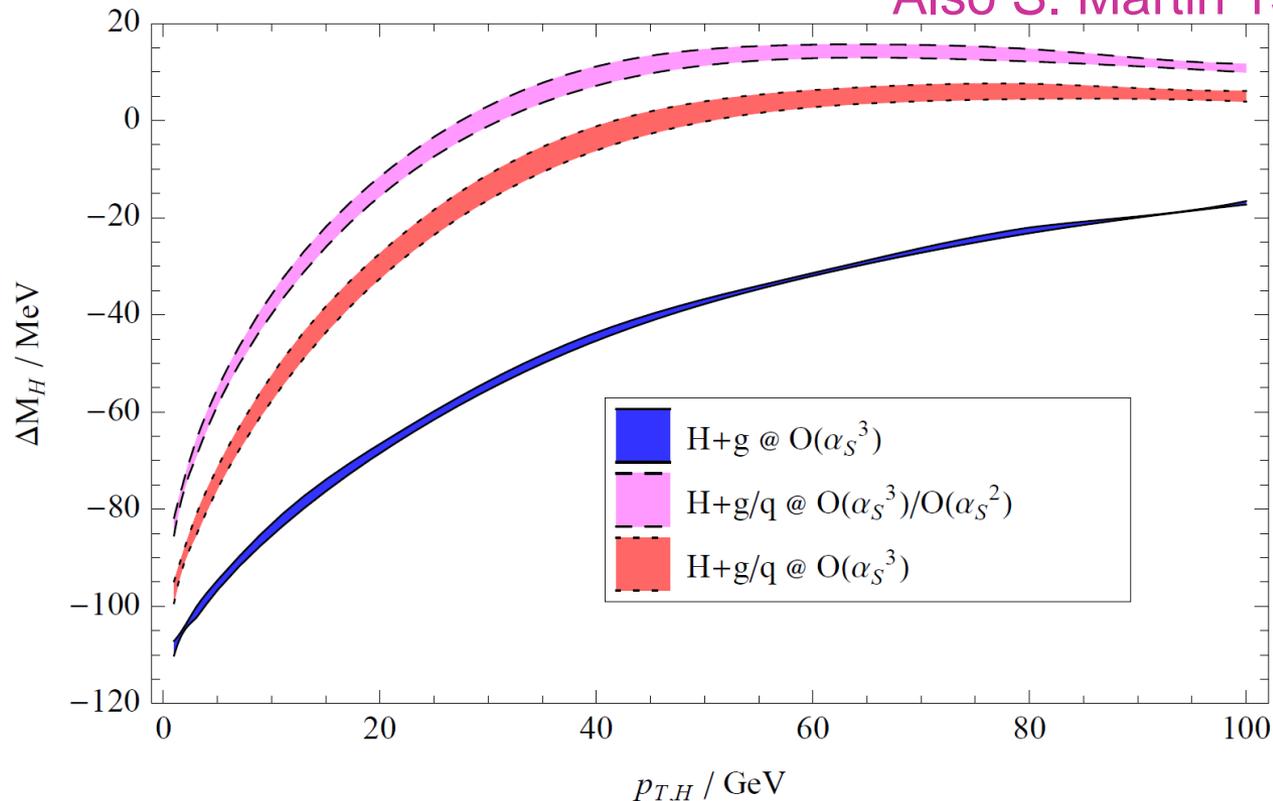
LD, Y. Li, 1305.3854



- Interference increases, but **signal increases more**

NLO mass shift vs. lower cut on Higgs p_T

Also S. Martin 1303.3342



- Big cancellation between gg and qg channel at large p_T
- Allows use of $p_T > 30$ or 40 GeV sample as “control” mass

“Control Mass” Critical

- We have no a priori knowledge of the Higgs boson mass at the 1 GeV level
- The Higgs boson mass must be measured in two high statistics, high precision samples that are affected **differently** by interference effects
- Only realistic channels are $\gamma\gamma$ and $ZZ^* \rightarrow l^+ l^- l^+ l^-$
- Low p_T versus high p_T $\gamma\gamma$ is one possibility

Two other possible control masses

1. $ZZ^* \rightarrow 4$ leptons

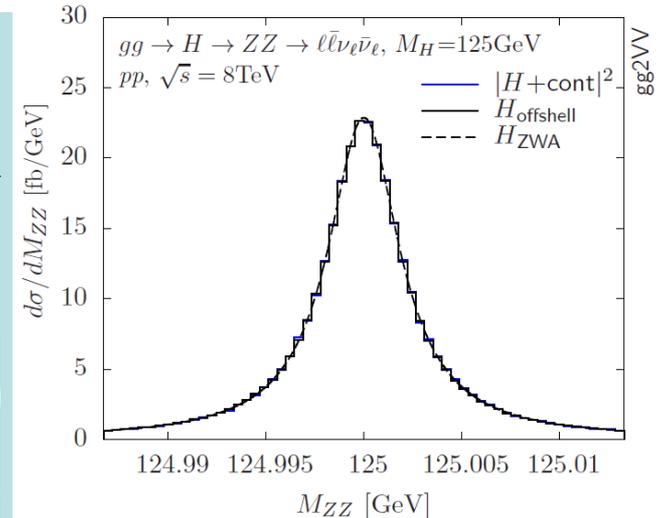
Great theoretically ($\delta M_{ZZ} \ll \delta M_{\gamma\gamma}$) \rightarrow
But experiments differ

$$\begin{aligned} m_H^{\gamma\gamma} - m_H^{ZZ} &= +2.3_{-0.7}^{+0.6} \pm 0.6 \text{ GeV (ATLAS)} \\ &= -0.4 \pm 0.7 \pm 0.6 \text{ GeV (CMS),} \end{aligned}$$

2. Mass in $\gamma\gamma$ in VBF enhanced sample

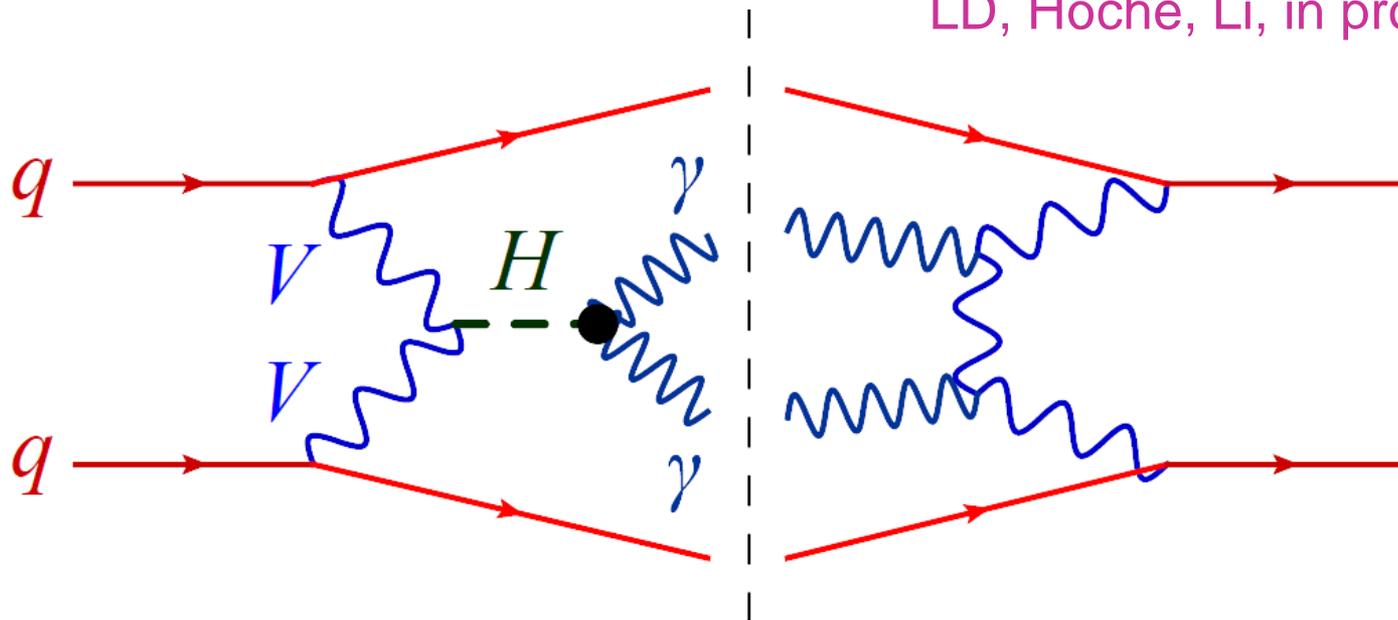
In general, comparing two $\gamma\gamma$ masses might
reduce systematic uncertainties associated with
 $e \rightarrow \gamma$ energy calibration

Kauer, Passarino, 1206.4803



Mass shift in VBF

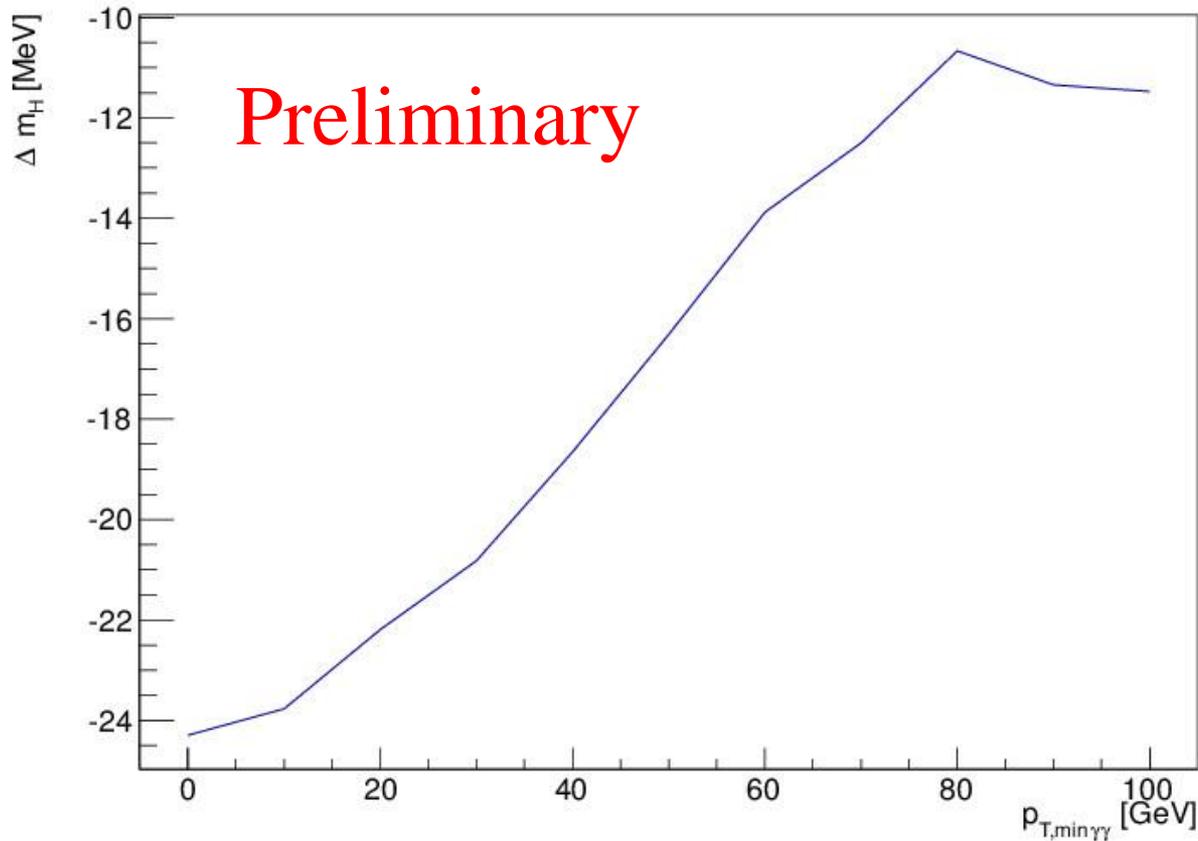
LD, Höche, Li, in progress



$V = W \text{ or } Z.$

W channel should dominate mass shift because background photons can be more central when radiated off of charged W line in t channel

Mass shift in VBF (cont.)



$$\rho_T(\gamma_{1,2}) > 20 \text{ GeV}$$
$$|\eta(\gamma_{1,2})| < 2.5$$

$$\rho_T(j_{1,2}) > 20 \text{ GeV}$$
$$M_{jj} > 800 \text{ GeV}$$
$$|\Delta\eta(jj)| > 4$$

- About 1/3 of effect in gluon fusion, and same sign
- Also declines as cut on minimum Higgs p_T is raised

Mass shift increases with Γ

- Non-interference measurements at LHC give signal proportional to $c_i^2 \cdot c_f^2 / \Gamma$
- Hold this fixed.
- Interference effects go like $c_i \cdot c_f \sim \sqrt{\Gamma}$

Coupling vs. width

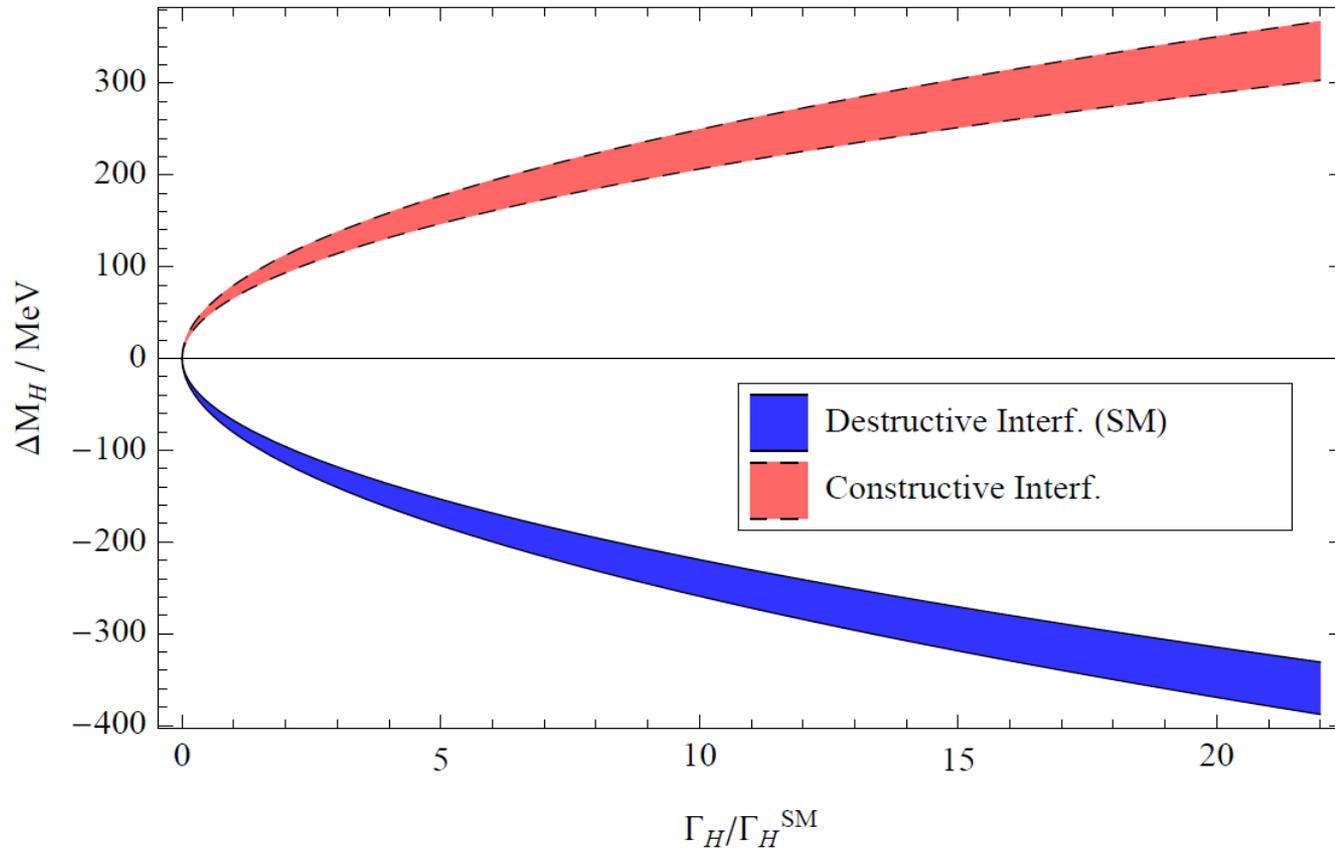
$$\mathcal{L} = - \left[\frac{\alpha_s}{8\pi} c_g b_g G_{a,\mu\nu} G_a^{\mu\nu} + \frac{\alpha}{8\pi} c_\gamma b_\gamma F_{\mu\nu} F^{\mu\nu} \right] \frac{h}{v}$$

- Coupling product $c_g \cdot c_\gamma = c_{g\gamma}$ determined by requiring that event yield is unaffected:

$$\frac{c_{g\gamma}^2 S}{m_H \Gamma_H} + c_{g\gamma} I = \left(\frac{S}{m_H \Gamma_H^{SM}} + I \right) \mu_{\gamma\gamma} :$$

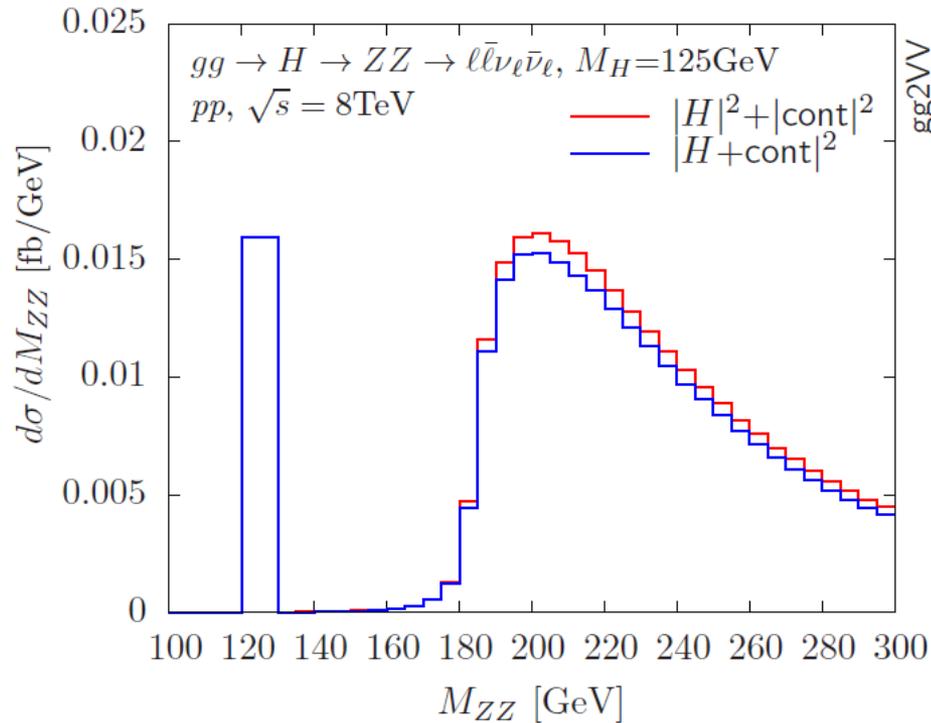
- Ignoring I ,
$$c_{g\gamma} = \sqrt{\mu_{\gamma\gamma} \Gamma_H / \Gamma_H^{SM}}$$

Mass shift vs. width in $gg \rightarrow \gamma\gamma$



- Measurement of ΔM statistically limited now, ~ 800 MeV
- Systematically limited in HL-LHC era, ~ 100 - 200 MeV

Interference in $gg \rightarrow H \rightarrow ZZ$



Kauer, Passarino, 1206.4803

ZZ production
 at high mass
 dominated by $q\bar{q}$,
 not gg

Still, if interference effect is increased enough, by
 $c_g \cdot c_Z \sim \sqrt{\Gamma}$, would get too much depletion of
 observed ZZ signal

Caola, Melnikov, 1307.4935;
 Campbell, Ellis, Williams, 1311.3589

Bound on Γ from high mass ZZ

- **Caola, Melnikov** suggest $\Gamma_H < 20\text{--}40 \Gamma_{SM}$ already with present LHC data.

- **Campbell, Ellis, Williams** ~ confirm, use kinematic discriminants to “improve” limits:

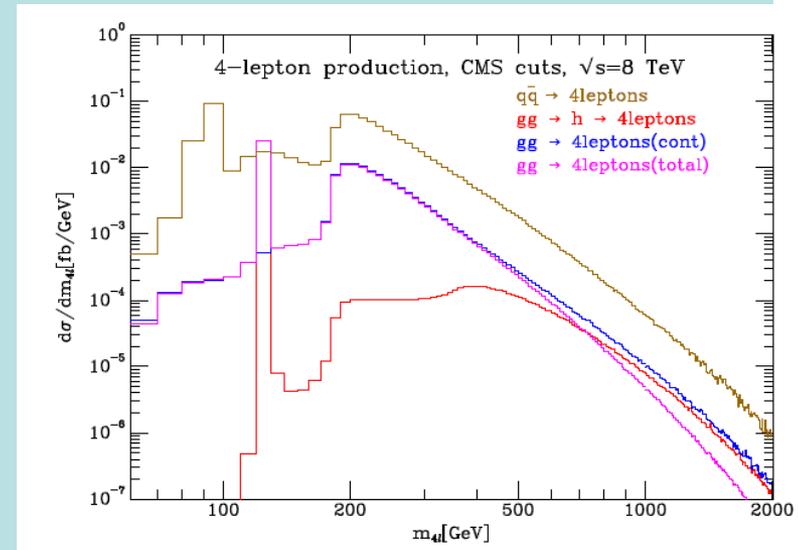
$$N_{off}^{4\ell}(m_{4\ell} > 130 \text{ GeV}) = 2.78 \left(\frac{\Gamma_H}{\Gamma_H^{SM}} \right) - 5.95 \sqrt{\frac{\Gamma_H}{\Gamma_H^{SM}}}$$

$$N_{off}^{4\ell}(m_{4\ell} > 300 \text{ GeV}) = 2.02 \left(\frac{\Gamma_H}{\Gamma_H^{SM}} \right) - 2.91 \sqrt{\frac{\Gamma_H}{\Gamma_H^{SM}}}$$

- $\Gamma_H < 43.2 \Gamma_H^{SM}$ at 95% c.l., ($m_{4\ell} > 130 \text{ GeV}$ analysis)
 $\Gamma_H < 25.2 \Gamma_H^{SM}$ at 95% c.l., ($m_{4\ell} > 300 \text{ GeV}$ analysis)

Still only LO analysis of interference, and gg component of background. Will be systematically limited at some point.

Similar recent results in WW channel: **CEW, 1312.1628**



From real part to imaginary part

$$\mathcal{A}_{gg \rightarrow \gamma\gamma} = \frac{-\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma}}{\hat{s} - m_H^2 + im_H \Gamma_H} + \mathcal{A}_{\text{cont}}$$

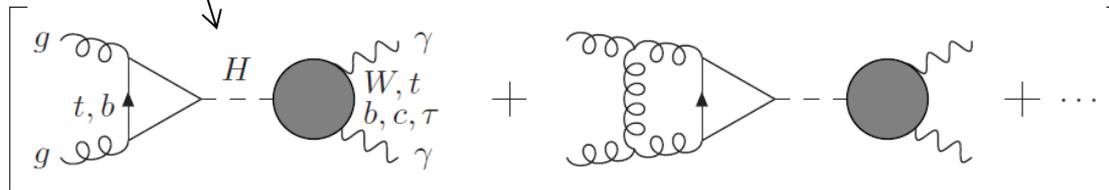
shifts peak position
(apparent mass)

$$\rightarrow \delta \hat{\sigma}_{gg \rightarrow H \rightarrow \gamma\gamma} = -2(\hat{s} - m_H^2) \frac{\text{Re}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma} \mathcal{A}_{\text{cont}}^*)}{(\hat{s} - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

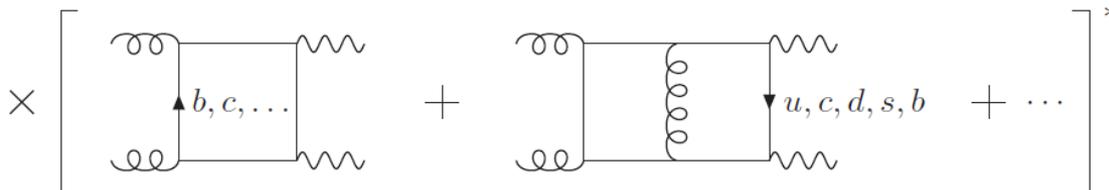
$$-2m_H \Gamma_H \frac{\text{Im}(\mathcal{A}_{gg \rightarrow H} \mathcal{A}_{H \rightarrow \gamma\gamma} \mathcal{A}_{\text{cont}}^*)}{(\hat{s} - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

shifts peak height
(event yield)

or spin 2 "G"



(assume)
dominantly real



What if it's spin 2?



What about spin 2?

LD, Höche, Li, to appear

- Rejection of spin 2 hypothesis vs. spin 0 uses distribution in $\cos\theta^*$ for $gg \rightarrow \gamma\gamma$.

[Recent ZZ analysis [CMS 1312.5353](#) prefers spin 0.]

- Without interference, distribution is unambiguous:

$$\sim 1 \quad \text{spin 0}$$

$$\sim 1 + 6 \cos^2\theta^* + \cos^4\theta^* \quad 2_m^+$$

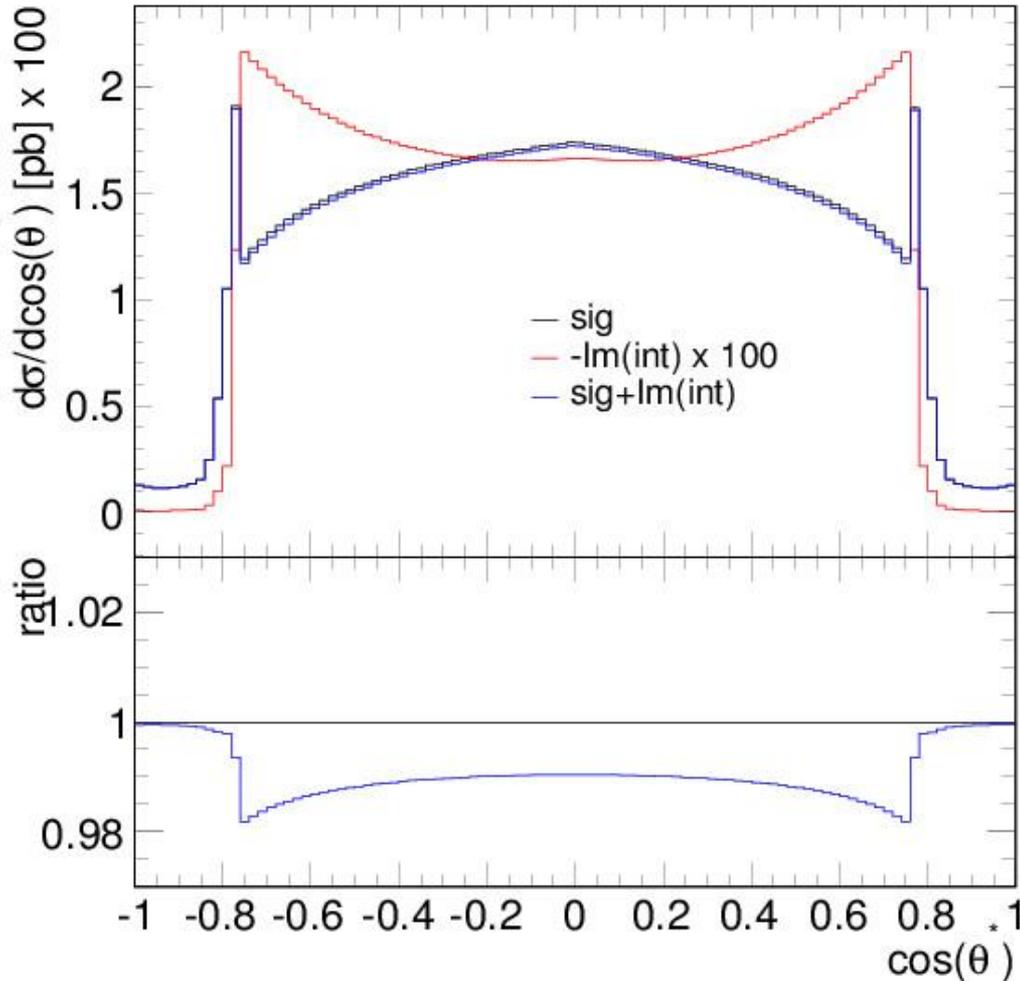
- How much distortion from interference effects [Im part]?

- SM Higgs: < few %

[LD, Siu, hep-ph/0302233](#)

Spin 0 (SM) $\cos\theta^*$ distortion

Including typical acceptance cuts



LD, Siu, hep-ph/0302233 ;
LD, Höche, Li, to appear

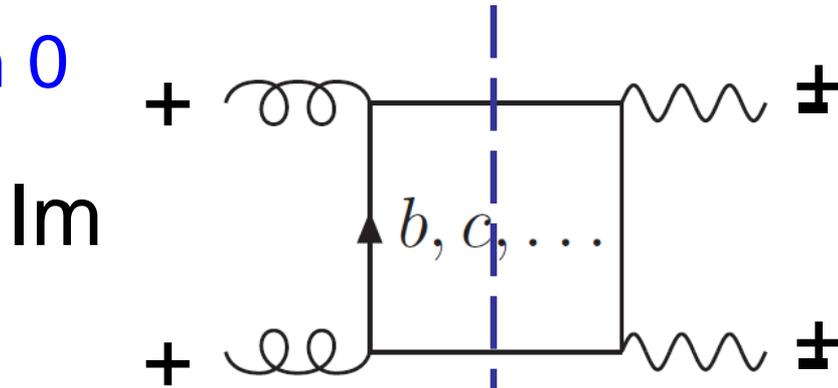
Spin 2 distortion
could be much bigger,
because:

- Im part anomalously small in spin 0 channel.
- Spin 2 width unknown

in Collins-Soper frame

Strong helicity dependence of Im part of background 1-loop amplitude

Spin 0

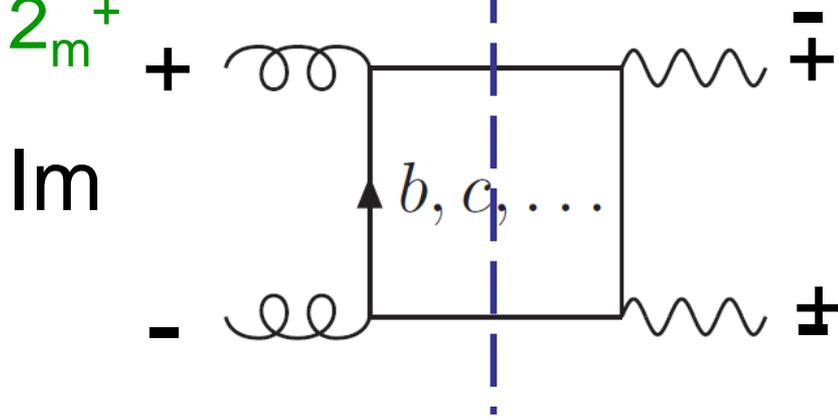


Im

$$= O(m_q^2/m_H^2) \sim 0$$

Dicus, Willenbrock (1988)

Spin 2_m^+

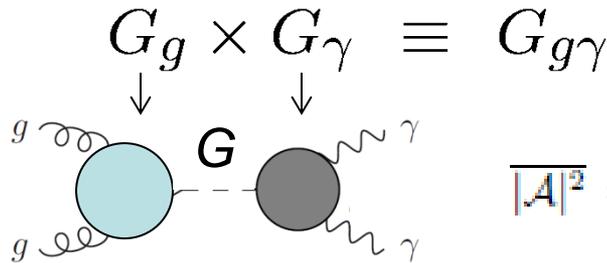


Im

$$= O(1)$$

Non-minimal spin 2 can interfere with other helicity amplitudes, but only this helicity config. has Im part

(spin 2) - 1-loop interference simple



$$\begin{aligned}
 |\overline{\mathcal{A}}|^2 = & \left[\frac{G_{g\gamma}^2}{256} f_0(c) + \pi \xi M \Gamma f_i(c) \right] \frac{1}{(\hat{s} - M^2)^2 + M^2 \Gamma^2} \\
 & + \xi f_r(c) \frac{\hat{s} - M^2}{(\hat{s} - M^2)^2 + M^2 \Gamma^2},
 \end{aligned}$$

where

$$c = \cos \theta$$

$$f_0(c) = 1 + 6c^2 + c^4,$$

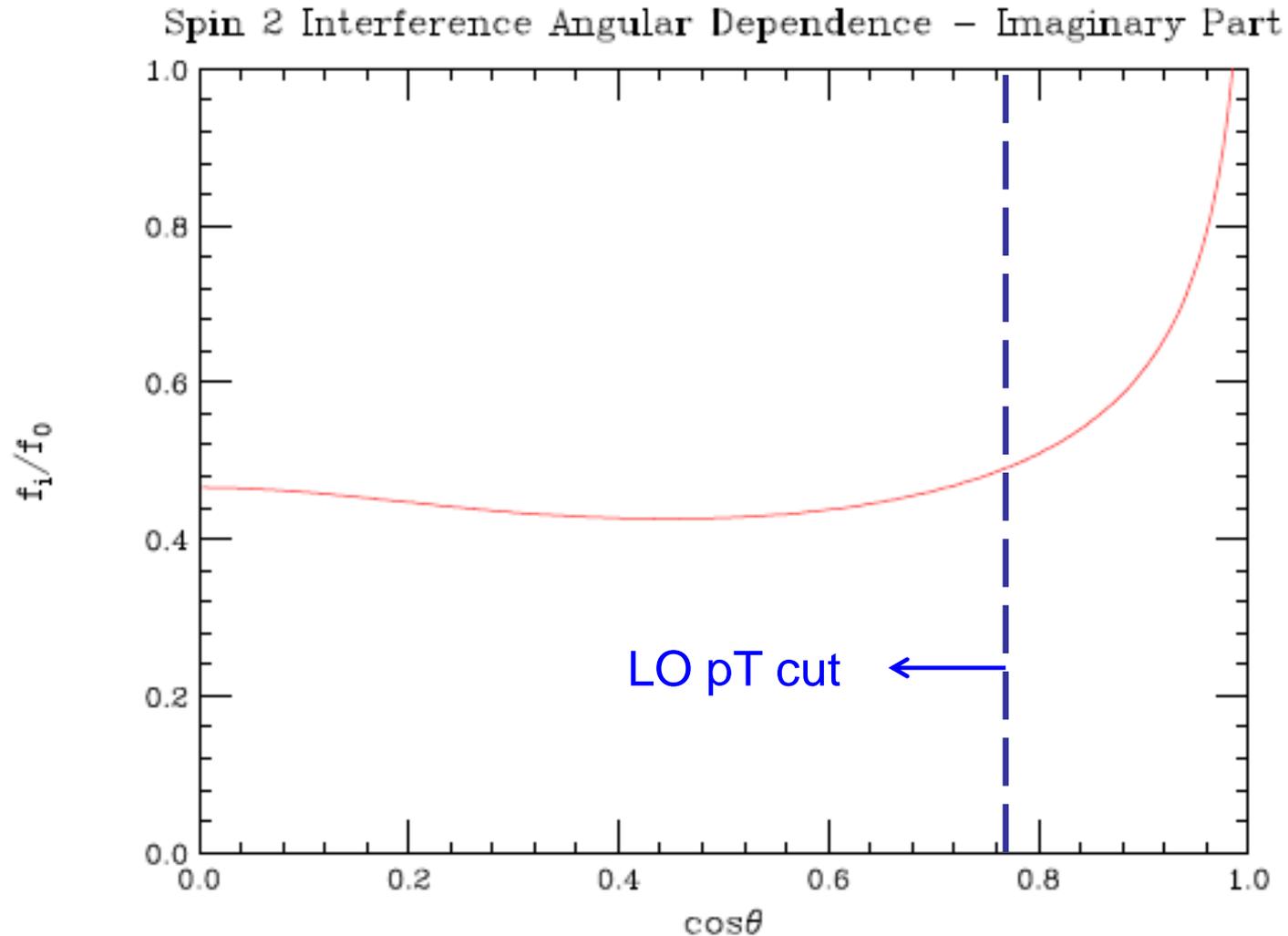
$$f_i(c) = 2 \left[\left(1 + \frac{(1-c)^2}{4} \right) \ln \left(\frac{2}{1-c} \right) + \left(1 + \frac{(1+c)^2}{4} \right) \ln \left(\frac{2}{1+c} \right) \right] - 3 + c^2,$$

$$\begin{aligned}
 f_r(c) = & \left(1 + \frac{(1-c)^2}{4} \right) \ln^2 \left(\frac{2}{1-c} \right) - \frac{(1+c)(3-c)}{2} \ln \left(\frac{2}{1-c} \right) \\
 & + \left(1 + \frac{(1+c)^2}{4} \right) \ln^2 \left(\frac{2}{1+c} \right) - \frac{(1-c)(3+c)}{2} \ln \left(\frac{2}{1+c} \right) + 1 + c^2,
 \end{aligned}$$

and

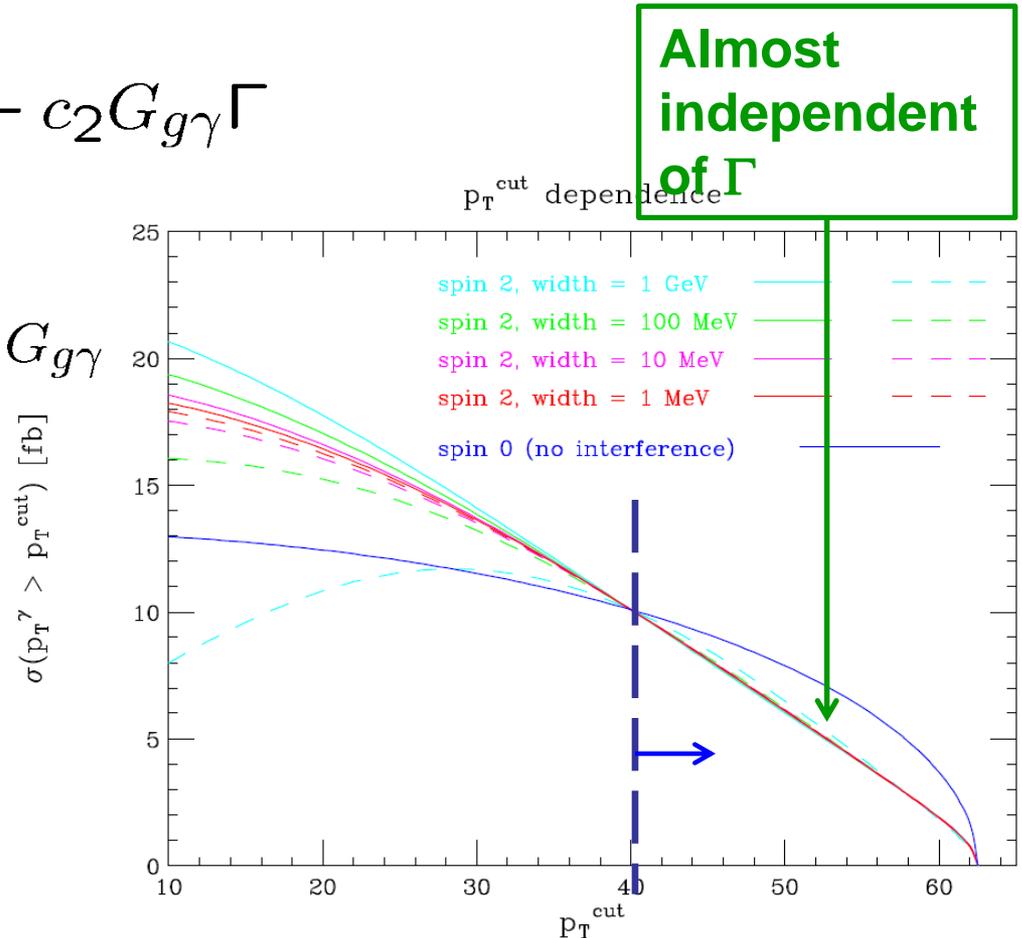
$$\xi = \frac{11}{72} G_{g\gamma} \alpha \alpha_s.$$

Im part remarkably flat in $\cos\theta$

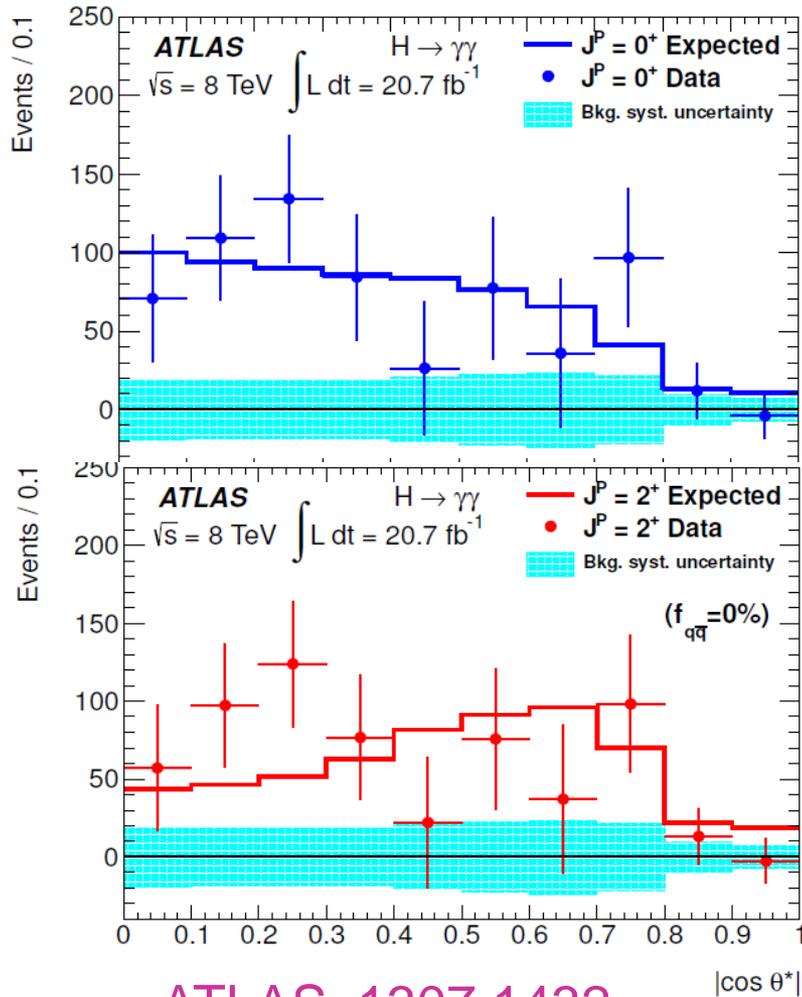


Size of interference as function of width Γ

- Event yield $\sim c_1 G_{g\gamma}^2 + c_2 G_{g\gamma} \Gamma$
- Normalize to SM Higgs at photon $p_T^{\text{cut}} = 40$ GeV.
- Quadratic equation for $G_{g\gamma}$
- Constructive, destructive solutions
- Completely model independent with respect to coupling **strengths**, other channels.

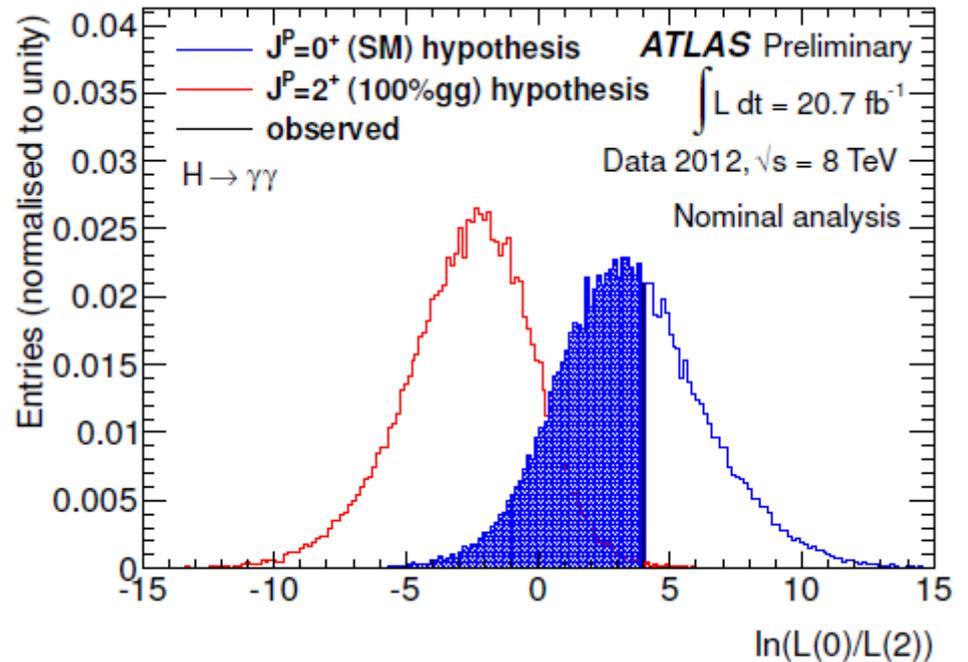


ATLAS likes spin 0



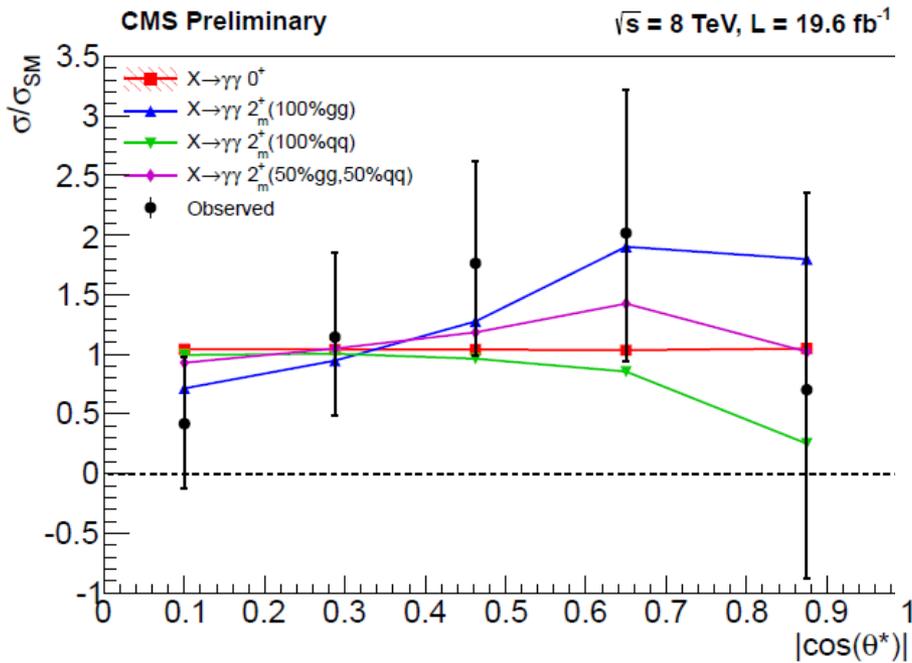
ATLAS, 1307.1432

99% exclusion of $gg \rightarrow \text{spin } 2 \rightarrow \gamma\gamma$

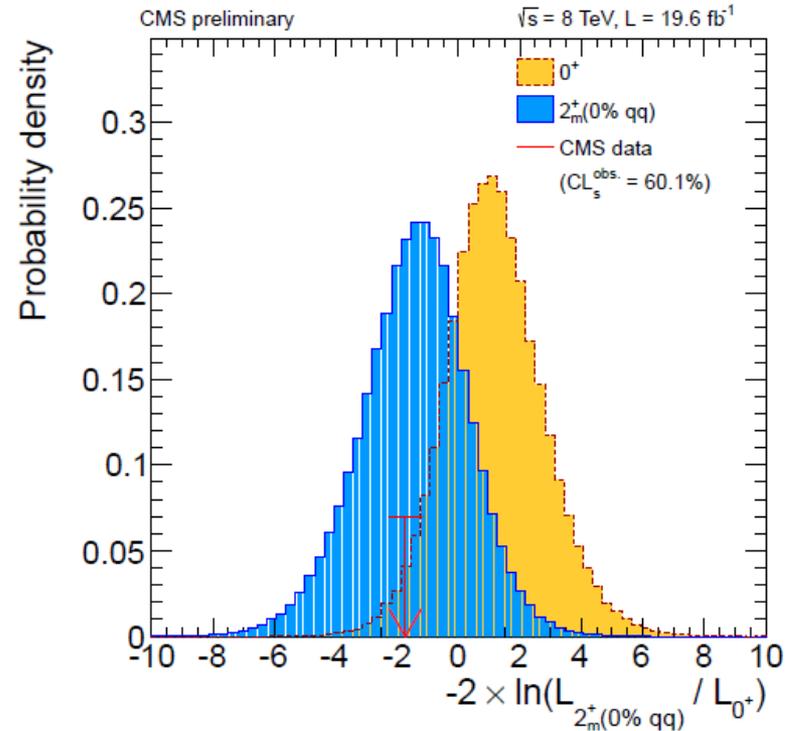


ATLAS-CONF-2013-029

CMS actually likes spin 2 (in $\gamma\gamma$)

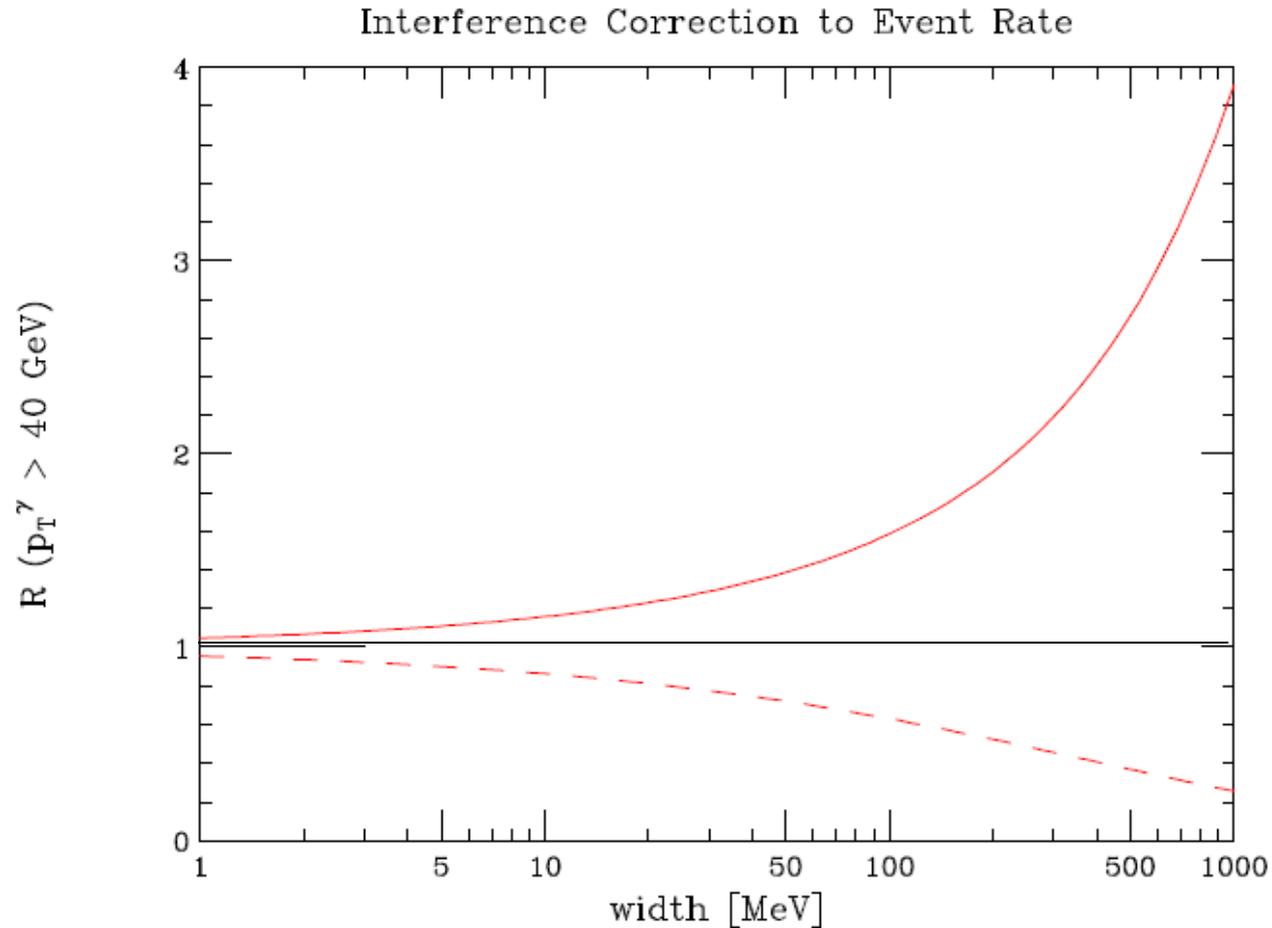


CMS-PAS-HiG-13-016



Compatibility	
Source	$\chi^2 p$ -value
Data vs. 0^+	0.68
Data vs. $2_m^+ (100\% gg)$	0.91
Data vs. $2_m^+ (100\% q\bar{q})$	0.51
Data vs. $2_m^+ (50\% gg, 50\% qq)$	0.81

Spin 2 yield might be strongly affected – even if $\cos\theta^*$ distribution is not

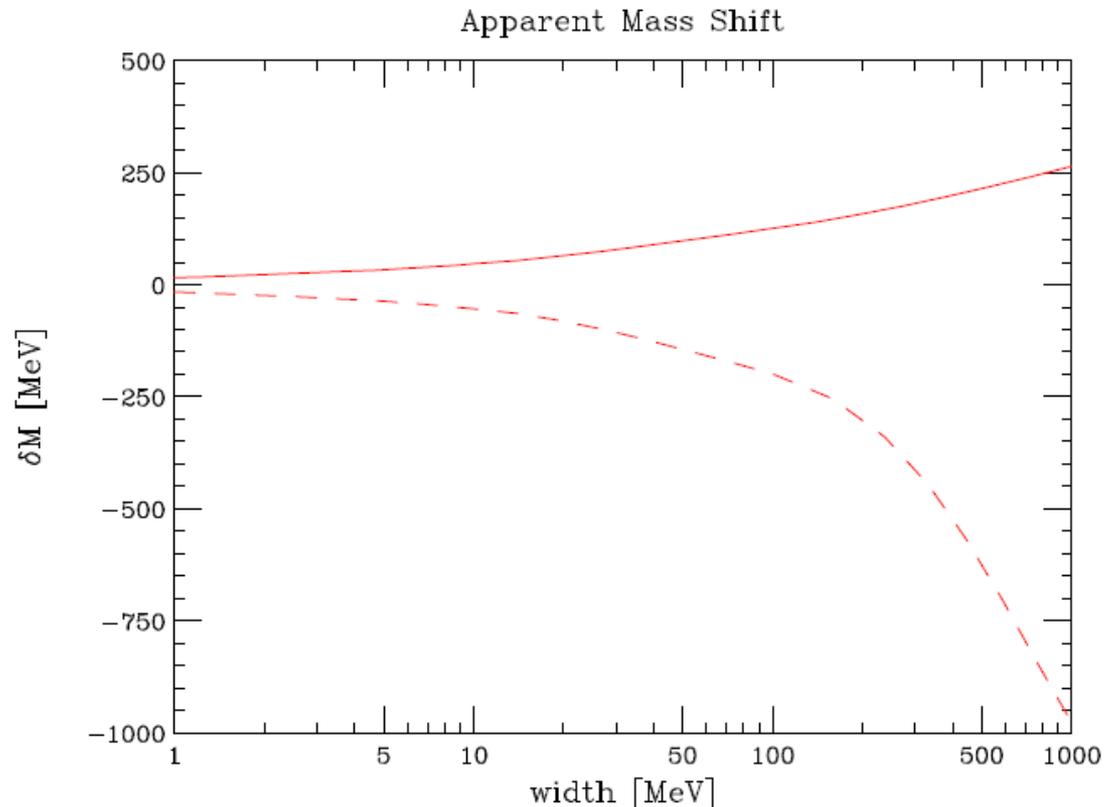


Conclusions

- Interference effects, in particular the mass shift in $\gamma\gamma$, should allow bounding the Higgs width to well under the direct experimental resolution, maybe eventually approaching the SM width. Now under study experimentally.
- At least 3 possible control masses.
- In principle, interference effects also important for testing non-SM hypotheses – e.g. spin 2 in $\gamma\gamma$. In practice, distortion of the $\cos\theta^*$ distribution is very small – where it is measurable.

Spin-2 mass shift from real part

Smear lineshape with Gaussian with width $\sigma = 1.7$ GeV.
Do least squares fit to Gaussian at mass $M + \delta M$.



NLO mass shift vs. jet veto p_T

